

# GMOR error propagation

$m$  - fermion mass /  $\Sigma$  - chiral condensate /  $M$  - pion mass

$$F_\pi = \frac{\sqrt{2m\Sigma}}{M}$$

```
In [1]: var('m', 'Σ', 'M')
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```
Out[1]: (m, Σ, M)
```

```
In [2]: Fpi = sqrt(2 * m * Σ) / M
```

```
In [3]: derivative(Fpi, Σ)^2
```

```
Out[3]: 1/2*m/(M^2*Σ)
```

```
In [4]: show(_)
```

$$\frac{m}{2 M^2 \Sigma}$$

```
In [5]: derivative(Fpi, M)^2
```

```
Out[5]: 2*m*Σ/M^4
```

```
In [6]: show(_)
```

$$\frac{2 m \Sigma}{M^4}$$

$$\sigma_F = \sqrt{\frac{m}{2\Sigma M^2} \sigma_\Sigma^2 + \frac{2m\Sigma}{M^4} \sigma_M^2} = \frac{1}{M} \sqrt{\frac{m}{2\Sigma} \sigma_\Sigma^2 + \frac{2m\Sigma}{M^2} \sigma_M^2}$$

Hip, 2022-04-20