## Optimal fit of $m_{\pi}$ vs. $(m_{peac}^2 g)^{1/3}$ .

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Several experiments were made in order to determine the most proper way to fit the data of  $m_{\pi}$  vs.  $(m_{pcac}^2g)^{1/3}$ . Functions of the form  $\sqrt{a+bx^3}$ ,  $\sqrt{a+bx^2}$ ,  $\sqrt{a+bx^4}$ ,  $\sqrt{a+bx^c}$ ,  $a+bx^2$ ,  $a+bx^c$ , where  $x=(m_{pcac}^2g)^{1/3}$  and a,b and c are fit parameters were used. The best results were obtained with functions of the form

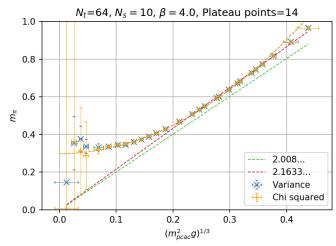
$$y = a + bx^{c},$$
  

$$y = \sqrt{a + bx^{c}},$$
  

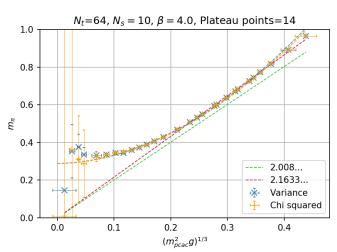
$$y = \sqrt{a + bx^{3}}.$$

Results of the pion decay constant  $F_{\pi}$  are shown as well. Everything was done for  $\beta = 4.0$ 

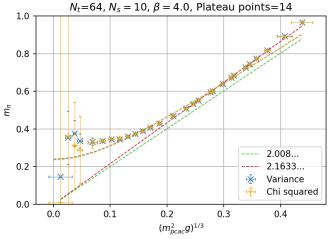
## **Experiments** 1



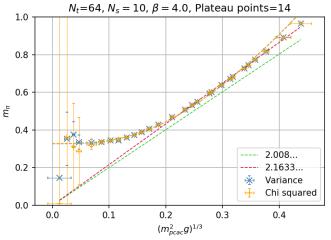
(a)  $y = a + bx^c$  was fitted,  $m_{pcac} > 0$ .  $a = 0.298 \pm 0.0018$ ,  $b = 3.7842 \pm 0.0304$ , c = 2.0,  $m_{\pi} = 0.2980(18)$  for variance and  $a = 0.2984 \pm 0.0017$ ,  $b = 3.7777 \pm 0.028$ , c = 2.0,  $m_{\pi} = 0.2984(17)$  for chi squared.



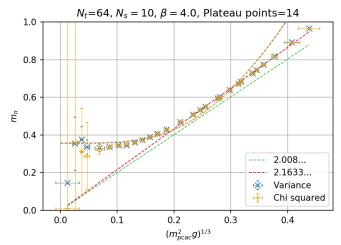
(b)  $y = a + bx^c$  was fitted,  $m_{pcac} > 0$ .  $a = 0.2892 \pm 0.0047$ ,  $b = 3.4319 \pm 0.1535, c = 1.8969 \pm 0.0475, m_{\pi} = 0.2892(47)$  for variance and  $a = 0.2878 \pm 0.0044$ ,  $b = 3.3815 \pm 0.1315$ ,  $c = 1.8969 \pm 0.0475$ ,  $m_{\pi} = 0.2878(44)$  for chi squared.



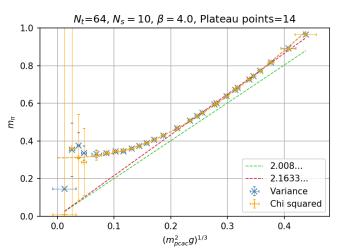
(c)  $y = \sqrt{a + bx^c}$  was fitted,  $m_{pcac} > 0$ .  $a = 0.0578 \pm 0.0045$ ,  $b = 3.9498 \pm 0.082$ ,  $c = 2.0 \ m_{\pi} = 0.2404(94)$  for variance and for chi squared



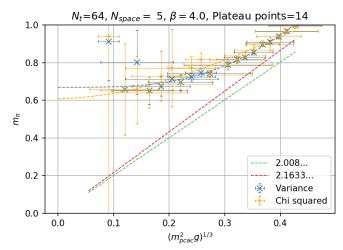
(d)  $y = \sqrt{a + bx^c}$  was fitted,  $m_{pcac} > 0$ .  $a = 0.1068 \pm 0.0013$ ,  $b = 11.238 \pm 0.1228, c = 3.0 \ m_{\pi} = 0.3269(21)$  for variance and  $a = 0.0559 \pm 0.0046, \ b = 3.9763 \pm 0.0799, \ c = 2.0, \ m_{\pi} = 0.2364(97) \quad a = 0.1077 \pm 0.0014, \ b = 11.1881 \pm 0.1152, \ c = 3.0, \ m_{\pi} = 0.3281(21)$ for chi squared



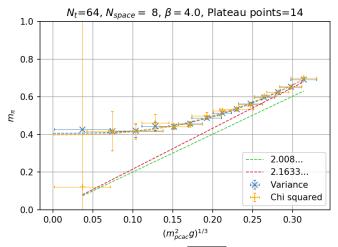
(e)  $y = \sqrt{a + bx^c}$  was fitted,  $m_{pcac} > 0$ .  $a = 0.1265 \pm 0.0032$ ,  $b = 35.3606 \pm 1.4906$ ,  $c = 4.0 \ m_{\pi} = 0.3557(46)$  for variance and for chi squared



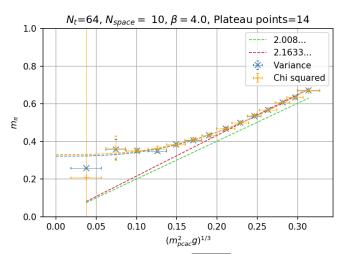
(f)  $y = \sqrt{a + bx^c}$  was fitted,  $m_{pcac} > 0$ .  $a = 0.0964 \pm 0.0014$ ,  $b = 7.9435 \pm 0.275, c = 2.6832 \pm 0.0319 \ m_{\pi} = 0.3105(23)$  for variance  $a = 0.1286 \pm 0.0035, b = 34.8539 \pm 1.4156, c = 4.0, m_{\pi} = 0.3586(49)$  and  $a = 0.0965 \pm 0.0012, b = 7.9065 \pm 0.2137, c = 2.6832 \pm 0.0319$  $m_{\pi} = 0.3106(19)$  for chi squared



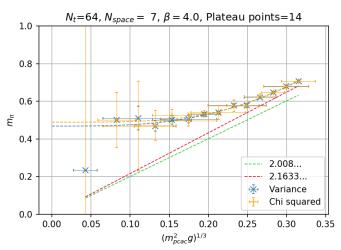
(g) A function of the form  $y = \sqrt{a + bx^c}$  was fitted.  $m_{pcac} > 0$ .  $c = 3.4651 \pm 0.7174$ ,  $m_{\pi} = 0.6689 \pm 0.0232$  for variance and  $c = 1.9228 \pm 0.7116$ ,  $m_{\pi} = 0.6097 \pm 0.0854$  for chi squared.



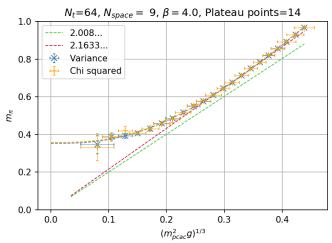
(i) A function of the form  $y = \sqrt{a + bx^c}$  was fitted.  $m_{pcac} > 0$ .  $c = 3.0663 \pm 0.2013, m_{\pi} = 0.4065 \pm 0.0075$  for variance and  $c = 2.783 \pm 0.3346, m_{\pi} = 0.3979 \pm 0.017$  for chi squared.



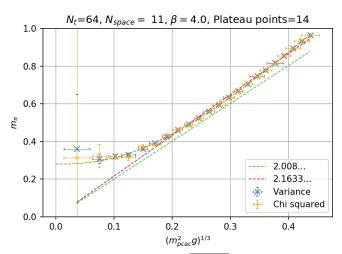
(k) A function of the form  $y = \sqrt{a + bx^c}$  was fitted.  $m_{pcac} > 0$ .  $c = 2.8691 \pm 0.1585, \, m_{\pi} = 0.322 \pm 0.0074$  for variance and  $c = 2.9509 \pm 0.1014, \, m_{\pi} = 0.3305 \pm 0.0045$  for chi squared.



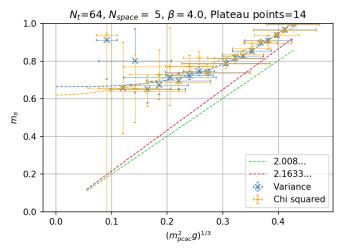
(h) A function of the form  $y = \sqrt{a + bx^c}$  was fitted.  $m_{pcac} > 0$ .  $c = 3.2848 \pm 0.4176, m_{\pi} = 0.4684 \pm 0.0111$  for variance and  $c = 3.8378 \pm 0.6821, m_{\pi} = 0.4892 \pm 0.0143$  for chi squared



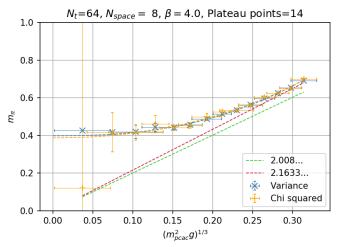
(j) A function of the form  $y = \sqrt{a + bx^c}$  was fitted.  $m_{pcac} > 0$ .  $c = 2.7049 \pm 0.0456, m_{\pi} = 0.3525 \pm 0.0038$  for variance and  $c = 2.7325 \pm 0.0753, m_{\pi} = 0.3575 \pm 0.0067$  for chi squared.



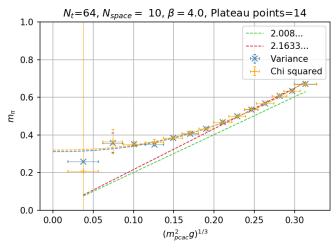
(l) A function of the form  $y = \sqrt{a + bx^c}$  was fitted.  $m_{pcac} > 0$ .  $c = 2.5818 \pm 0.0323$ ,  $m_{\pi} = 0.2798 \pm 0.0036$  for variance and  $c = 2.5528 \pm 0.0539$ ,  $m_{\pi} = 0.2807 \pm 0.0066$  for chi squared.



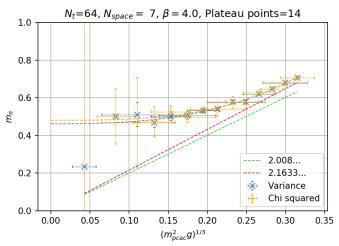
(m) A function of the form  $y = a + bx^c$  was fitted.  $m_{pcac} > 0$ .  $c = 3.0182 \pm 0.7033$ ,  $m_{\pi} = 0.664 \pm 0.0259$  for variance and  $c = 1.7735 \pm 0.7512$ ,  $m_{\pi} = 0.6196 \pm 0.0806$  for chi squared.



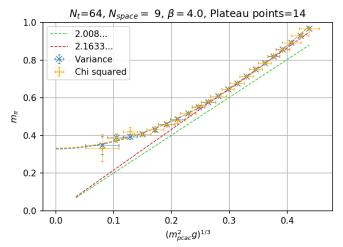
(o) A function of the form  $y = a + bx^c$  was fitted.  $m_{pcac} > 0$ .  $c = 2.4945 \pm 0.2091$ ,  $m_{\pi} = 0.3984 \pm 0.0095$  for variance and  $c = 2.2133 \pm 0.3326$ ,  $m_{\pi} = 0.3874 \pm 0.0206$  for chi squared.



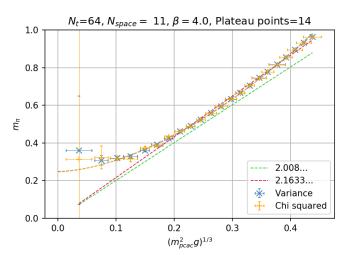
(q) A function of the form  $y=a+bx^c$  was fitted.  $m_{pcac}>0$ .  $c=2.2171\pm0.169,\ m_{\pi}=0.3114\pm0.01$  for variance and  $c=2.2766\pm0.1222,\ m_{\pi}=0.3197\pm0.007$  for chi squared.



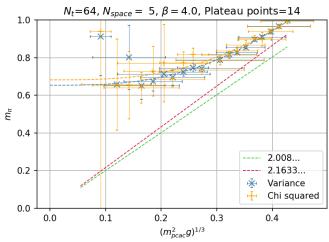
(n) A function of the form  $y = a + bx^c$  was fitted.  $m_{pcac} > 0$ .  $c = 2.7568 \pm 0.4221, m_{\pi} = 0.4622 \pm 0.0136$  for variance and  $c = 3.132 \pm 0.6695, m_{\pi} = 0.4806 \pm 0.0183$  for chi squared.

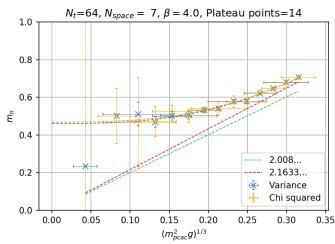


(p) A function of the form  $y = a + bx^c$  was fitted.  $m_{pcac} > 0$ .  $c = 1.9056 \pm 0.0561$ ,  $m_{\pi} = 0.3284 \pm 0.0065$  for variance and  $c = 1.9209 \pm 0.0809$ ,  $m_{\pi} = 0.3325 \pm 0.0098$  for chi squared.

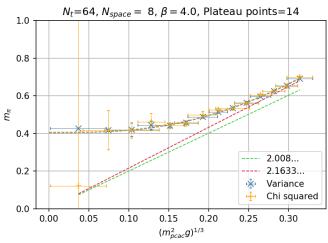


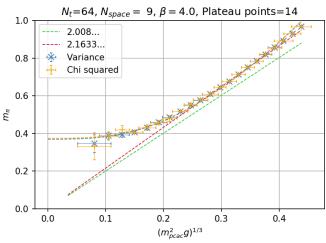
(r) A function of the form  $y=a+bx^c$  was fitted.  $m_{pcac}>0$ .  $c=1.7062\pm0.047,\ m_{\pi}=0.2489\pm0.0073$  for variance and  $c=1.6732\pm0.0557,\ m_{\pi}=0.2469\pm0.0093$  for chi squared.



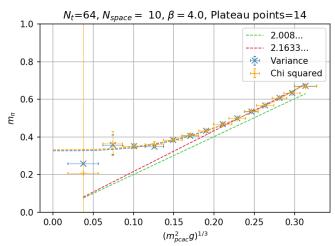


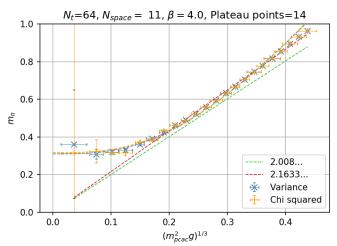
(s) A function of the form  $y=\sqrt{a+bx^3}$  was fitted.  $m_{pcac}>0$ . (t) A function of the form  $y=\sqrt{a+bx^3}$  was fitted.  $m_{pcac}>0$ .  $m_{\pi}=0.65356\pm0.01149$  for variance and  $m_{\pi}=0.6821\pm0.01744$  for  $m_{\pi}=0.46083\pm0.00521$  for variance and  $m_{\pi}=0.46838\pm0.00775$  for chi squared





(u) A function of the form  $y = \sqrt{a + bx^3}$  was fitted.  $m_{pcac} > 0$ . (v) A function of the form  $y = \sqrt{a + bx^3}$  was fitted.  $m_{pcac} > 0$ .  $m_{\pi} = 0.40426 \pm 0.00317$  for variance and  $m_{\pi} = 0.40679 \pm 0.00629$  for  $m_{\pi} = 0.36969 \pm 0.00309$  for variance and  $m_{\pi} = 0.37412 \pm 0.00402$  for chi squared.





(w) A function of the form  $y = \sqrt{a + bx^3}$  was fitted.  $m_{pcac} > 0$ . (x) A function of the form  $y = \sqrt{a + bx^3}$  was fitted.  $m_{pcac} > 0$ .  $m_{\pi} = 0.32665 \pm 0.00334$  for variance and  $m_{\pi} = 0.33234 \pm 0.00218$  for  $m_{\pi} = 0.3098 \pm 0.00439$  for variance and  $m_{\pi} = 0.31667 \pm 0.00538$  for chi squared.

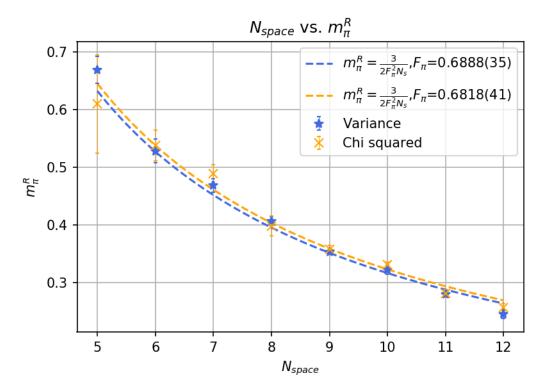


Figure 1: Result obtained by fitting  $y = \sqrt{a + bx^c}$ . For variance  $F_{\pi} = 0.6888(35)$ , while for chi squared  $F_{\pi} = 0.6818(41)$ 

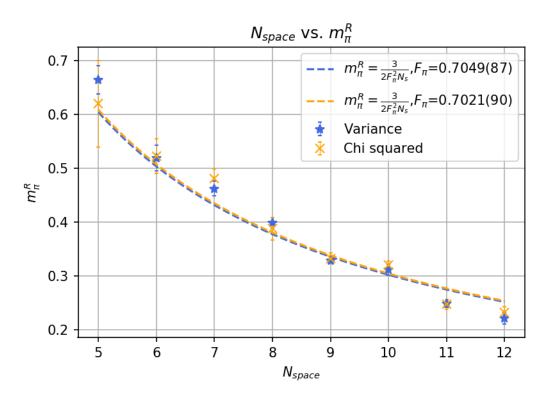


Figure 2: Result obtained by fitting  $y = a + bx^c$ . For variance  $F_{\pi} = 0.7049(87)$ , while for chi squared  $F_{\pi} = 0.7021(90)$ 

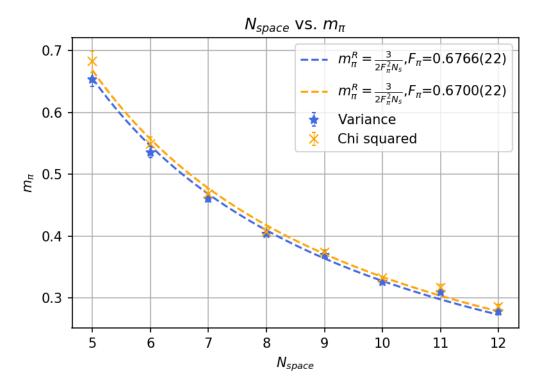


Figure 3: Result obtained by fitting  $y = a + bx^3$ . For variance  $F_{\pi} = 0.6766(22)$ , while for chi squared  $F_{\pi} = 0.6700(22)$ .