## DAR/IDAR Coursework 1

#### 1. Statistical learning methods

(12%)

For each of parts (a) through (d), indicate whether we would generally expect the performance of a flexible statistical learning method to be better or worse than an inflexible method. Justify your answer.

(a) The number of predictors p is extremely large, and the number of observations n is small.

An inflexible method is better because an overly complex model with many parameters compared to the number of observations can overfit and therefore not generalise. The variance of an inflexible model on with a large p and small s will be large.

(b) The sample size n is extremely large, and the number of predictors p is small.

A flexible model is better. The large sample size reduces risk of overfitting and the bias is reduced.

(c) The relationship between the predictors and response is highly non-linear.

A flexible model is better otherwise the non-linearity will not be modeled. An inflexible model will oversimplify and not detect the complicated relationship between the predictors and response.

(d) The standard deviation of the error terms, i.e.  $\sigma = \operatorname{sd}(\varepsilon)$ , is extremely high.

An inflexible model is better. A flexible model will overfit, and try to model the noise of the high variance of the errors.

# 2. Bayes' rule (12%) Given a

dataset including 20 observations (S\_1, ..., S\_20) about the temperature (i.e. hot or cool) for playing golf (i.e. yes or no), you are required to use the Bayes' rule to calculate by hand the probability of playing golf according to the temperature, i.e. P(Play Golf | Temperature).

	S_1	S_2	S_3	S_4	S_5	S_6	S_7	S_8	S_9	S_10
Temperature	cool	hot	hot	hot	cool	cool	hot	cool	hot	hot
Play Golf	yes	no	yes	no	yes	yes	no	yes	no	yes

	S_11	S_12	S_13	S_14	S_15	S_16	S_17	S_18	S_19	S_20
Temperature	hot	hot	hot	cool	hot	hot	cool	cool	cool	hot
Play Golf	no	no	yes	no	no	no	yes	no	no	no

We can calculate the following probabilities from the dataset:

$$P(Play Golf = yes) = 8/20 = 0.4$$

$$P(Play Golf = no) = 12/20 = 0.6$$

$$P(Temperature = hot) = 12/20 = 0.6$$

$$P(Temperature = cool) = 8/20 = 0.4$$

$$P(Temperature = hot \mid Play Golf = yes) = 3/8 = 0.375$$

$$P(Temperature = cool \mid Play Golf = yes) = 5/8 = 0.625$$

$$P(Temperature = hot | Play Golf = no) = 9/12 = 0.75$$

$$P(Temperature = cool \mid Play Golf = no) = 3/12 = 0.25$$

Now, using Bayes' rule, we can calculate:

P(Play Golf = yes | Temperature = hot) = 
$$(0.375 * 0.4) / 0.6 = 0.25$$

P(Play Golf = yes | Temperature = cool) = 
$$(0.625 * 0.4) / 0.4 = 0.625$$

$$P(Play Golf = no \mid Temperature = hot) = (0.75 * 0.6) / 0.6 = 0.75$$

#### 3. Descriptive analysis

(22%)

This question involves the Auto dataset included in the "ISLR" package.

(a) Which of the predictors are quantitative, and which are qualitative?

##		mpg	cylinders	displacement	horsepower	weight	acceleration	year	origin
##	1	18	8	307	130	3504	12.0	70	1
##	2	15	8	350	165	3693	11.5	70	1
##	3	18	8	318	150	3436	11.0	70	1
##	4	16	8	304	150	3433	12.0	70	1
##	5	17	8	302	140	3449	10.5	70	1
##	6	15	8	429	198	4341	10.0	70	1
##		name							
##	1	chevrolet chevelle malibu							
##	2		buick skylark 320						
##	3		plymouth satellite						
##	4		amc rebel sst						
##	5		ford torino						
##	6		ford galaxie 500						

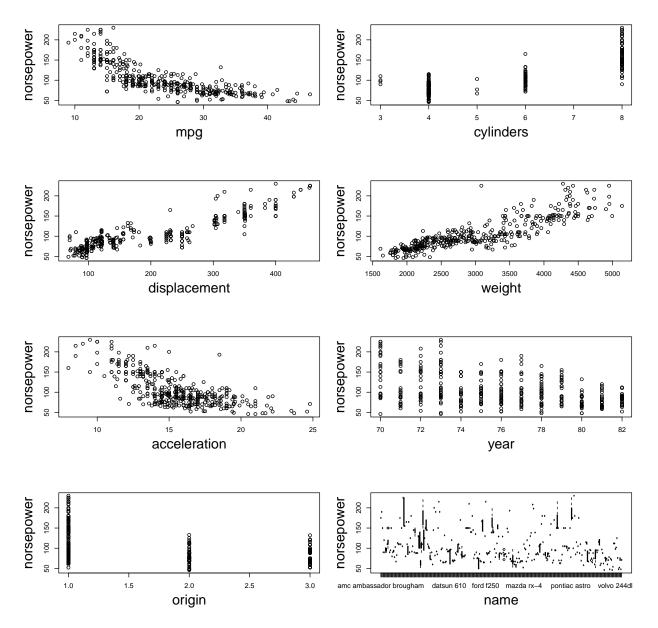
Quantitative: mpg, cylinders, displacement, horsepower, weight, acceleration, year

Qualitative: origin, name

(b) What are the range, median and variance of each quantitative predictor?

##	:	range	median	variance
##	mpg	37.60	22.75	60.92
##	cylinders	5.00	4.00	2.91
##	displacement	387.00	151.00	10950.37
##	horsepower	184.00	93.50	1481.57
##	weight	3527.00	2803.50	721484.71
##	acceleration	16.80	15.50	7.61
##	year	12.00	76.00	13.57

(c) Using the full data set, investigate the relationship between individual predictors with the target response engine horsepower (horsepower) graphically. Comment on your findings.



### horsepower vs. mpg

Negative relationship. As mpg increases, horspower approaches 0 (possibly exponential decrease)

#### horsepower vs. cylinders

No clear relationship. More cylinders does not necessarily mean more horsepower. However, the median horsepower of cars with 8 cylinders is larger than 3 to 6.

## horsepower vs. displacment

Positive, linear looking relationship. As displacement increases, horsepower also increases.

#### horsepower vs. weight

Positive overall relationship. However the variance in horsepower does increase with weight.

## horsepower vs. acceleration

Negative relationship. Horsepower shows a decreasing trend with increasing acceleration, which tends to low values at large accelerations.

#### horsepower vs. year

The variance in horsepower appears to be reduced in later rather earlier years. The mean horsepower may also have a negative trend with years.

#### horsepower vs. origin

Cars come from location 1 more than any other. Location 1 also has the largest variance in horsepower. The other two locations are quite similar.

#### horsepower vs. name

Other analysis required

(d) Suppose that we wish to predict horsepower on the basis of the other variables. Do your plots suggest that any of the other variables might be useful in predicting horsepower? Justify your answer.

Yes: mpg, displacement, weight and acceleration seem to be the most useful attributes for predicting horsepower. From (c), these predictors showed a clear correlation with horsepower. Therefore, they might be useful in predicting horsepower.

This question involves the use of simple linear regression on the Auto dataset.

(a) Use the lm() function to perform a simple linear regression with acceleration as the response and horsepower as the predictor. Use the summary() function to print the results. Comment on the output. For example:

```
##
## Call:
## lm(formula = acceleration ~ horsepower, data = Auto)
##
## Residuals:
##
               1Q Median
                                3Q
                                       Max
  -4.9947 -1.2913 -0.1748 1.1229
                                   7.6053
##
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 20.70193
                          0.29274
                                     70.72
                                             <2e-16 ***
                                   -18.78
## horsepower -0.04940
                          0.00263
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.002 on 390 degrees of freedom
## Multiple R-squared: 0.475, Adjusted R-squared: 0.4736
## F-statistic: 352.8 on 1 and 390 DF, p-value: < 2.2e-16
```

i. Is there a relationship between the predictor and the response?

The magnitude of the t-value is large (18.78) and the p-value is small (< 2.2e-16). We can therefore reject the null hypothesis. There is a relationship between the predictor and the response.

ii. How strong is the relationship between the predictor and the response?

The adjusted R-squared is 0.4736. This implies that only about 47.36% of the sample variation in fire horsepower is explained by acceleration.

iii. Is the relationship between the predictor and the response positive or negative?

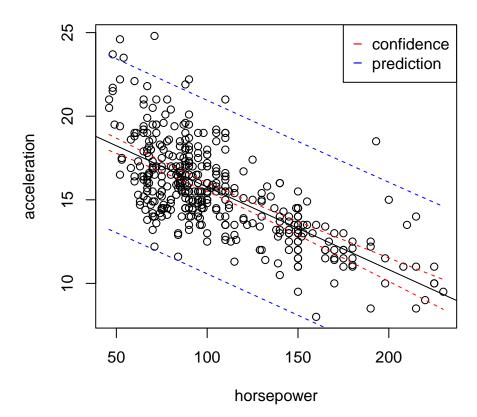
The relationship is negative with slope -9.6155 (0.5119).

iv. What is the predicted acceleration associated with a horsepower of 93.5? What are the associated 99% confidence and prediction intervals?

```
## fit lwr upr
## Confidence 16.08320 15.81107 16.35532
## Prediction 16.08320 10.89501 21.27138
```

The predicted acceleration is 16.0832s. The associated 99% confidence interval is between 15.81107 and 16.35532. The associated 99% prediction interval is between 10.89501 and 21.27138.

- (b) Plot the response and the predictor. Use the abline() function to display the least squares regression line
- (c) Plot the 99% confidence interval and prediction interval in the same plot as (b) using different colours and legends.



#### 5. Logistic regression and cross validation

(30%)

A recent study has shown that the accurate prediction of the office room occupancy leads to potential energy savings of 30%. In this question, you are required to build logistic regression models by using different environmental measurements as predictors (features), such as temperature, humidity, light,  $CO_2$  and humidity ratio, to predict the office room occupancy. The provided training dataset consists of 1,000 observations, whilst the testing dataset consists of 300 observations.

(a) Load the training and testing datasets from corresponding files, and display the statistics about different predictors in the training dataset.

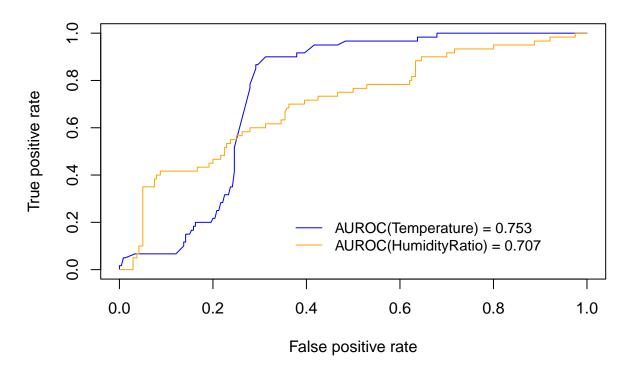
```
##
     Temperature
                        Humidity
                                           Light
                                                           C02
                             :22.84
##
    Min.
            :20.79
                     Min.
                                      Min.
                                              :
                                                 0
                                                     Min.
                                                             : 428.0
    1st Qu.:21.00
##
                     1st Qu.:24.89
                                       1st Qu.:
                                                      1st Qu.: 447.4
                                                 0
    Median :21.50
                     Median :25.86
                                                     Median: 498.0
##
                                      Median:
                                                 0
            :21.67
                                                             : 643.9
##
    Mean
                     Mean
                             :25.75
                                                     Mean
                                      Mean
                                              :141
##
    3rd Qu.:22.29
                     3rd Qu.:26.95
                                      3rd Qu.:438
                                                      3rd Qu.: 841.0
##
    Max.
            :23.18
                     Max.
                             :28.50
                                      Max.
                                              :744
                                                     Max.
                                                             :1139.0
##
    HumidityRatio
                          Occupancy
                                :0.000
##
   Min.
            :0.003462
                        Min.
    1st Qu.:0.003824
##
                        1st Qu.:0.000
##
    Median :0.004104
                        Median : 0.000
##
    Mean
            :0.004134
                        Mean
                                :0.242
##
    3rd Qu.:0.004472
                        3rd Qu.:0.000
##
    Max.
            :0.004793
                                :1.000
                        Max.
```

(b) Conduct a 5-fold cross validation to compare the predictive performance of two different predictors, i.e. Humidity and HumidityRatio by using logistic regression method. Report the average accuracies and AUROC values obtained over the 5-fold cross validation. Set the value of random seed as "100" when generating fold indices. Consider the predictive label equals to 1, if the predictive probability is greater than 0.5.

```
## Loading required package: ggplot2
## Loading required package: lattice
## [1] 0.73
## [1] 0.8319416
## [1] 0.784
## [1] 0.8873837
```

HumidityRatio is the best predictor since it gives higher average accuracy and AUROC values from the 5-fold CV.

(c) Predict the class labels of the testing observations by using two different logistic regression models, i.e. one model is trained by using the best predictor obtained in Step (b), whilst the other model is trained by using the Temperature predictor. Compare the performance of those two models by drawing ROC curves and calculating corresponding AUROC values. Discuss the results.



The AUROC value for Temperature is greater than for HumidityRatio. Therefore, the model using Temperature as a predictor is more accurate and better at classifying the Occupancy with a lower error rate.