Comparing kNN and Logistic Regression algorithms for Wine classification

T-61.3050 Term Project, final report 472735 Fábio Pinheiro & 472191 João Duro

Abstract

The idea of the project and this report is to see how different kNN and Logistic Regression are. Our main problem divides itself in two sub problems of supervised classification, with one being a binary supervised classification and the other a 7-class supervised classification, and we will see how both algorithms behave in each case.

I. Introduction

The data we're given consists of a set of measures from 6000 different wines. attributes of the wines are "fixedAcidity", "volatileAcidity"," citricAcid", "residualSugar", "chlorides", freeSulfurDioxide, "totalSulfur-Dioxide", "density", "pH", "sulphates", "alcohol", "quality" and "type". Our first goal is try and predict the quality of the wine, which is classified as "White" or "Red, and later, try and predict based on the same attributes the quality of the wine which is a integer variable ranging from 1 to 7, 1 being really good, and 7 being really poor. Based on the results and our understading of how the algoithms work, we will try and see how different it is to predict to a binary class or a 7-value class.

II. Methods

Normalize data

k-nearest neighbors algorithm (kNN)

K-nearest neighbors algorithm also known as kNN is a non-parametric method used for classification and regression. In both cases the kNN algorithm starts from the principle that similar data are closed one to another.

The algorithm is just given a point Y' to find the k' points from training data where distance where is smaller that all the anthers. Then choose the class more frequent, in case of a tie, pick one at random among them.

The pseudocode for kNN can be seen in Algorithm 1 [2]

Euclidean Distance

For n dimensions Euclidean Distance is give by following formula:

$$d(p,q) = \sqrt{(p_1 - q_1)^2 + (p_2 - q_2)^2 + \dots + (p_n - q_n)^2}$$

(Dimensions in here is the number of feature/parameters of the data)

Logistic Regression

"It is assumed that we have a series of N observed data points. Each data point i consists of a set of m explanatory variables $x_{1,i}x_{2,i}...x_{m,i}$ (also called independent variables, predictor variables, input variables, features, or attributes), and an associated binary-valued outcome variable Y_i (also known as a dependent variable, response variable, output variable, outcome variable or class variable), i.e. it can assume only the two possible values "failure" or 1 "success". The goal of logistic regression is to explain the relationship between

Algorithm 1 kNN

- 1: Define the distance measure or similarity between two objects
- 2: Find k;
- 3: Compute the distance between the new object and all objects in the training set: d(xi, x0)i = 1, 2, ..., n;
- 4: Sort the distances in increasing numerical order and pick the first k elements (neighbours), let be $Vk(x0) \subseteq D$, the set of those neighbours;
- 5: Save the classifications of all neighbours;
- 6: Assign new object to the class based on majority vote of its neighbours 2, i.e.

$$\mathcal{Y}_0 = \operatorname*{arg\ max}_{C_j} \sum_{(x_i, y_i) \subset V_i(x_0)} I(y_i = C_j)$$

the explanatory variables and the outcome, so that an outcome can be predicted for a new set of explanatory variables."

III. EXPERIMENTS

The first thing we need to do is to separate our data consisting of 6000 row elements in training and validation set, and a test set, which will be used exclusevly to predict the error of our methods. We splited the data so we have 1000 elements in the test set, and the remaining data will be used to train our model or to make assesments about the data, this will not be used to predict the error of our models.

A premminilary analysis shows us the data is not normalized, so when applying different algorithms this will play a huge role, but we decided to test it as it is, and then normalize the data and see how much it improves, if it improves, as we believe it will.

The procedures we took for predict the quality and type of the wine were the same, except when predicting the quality we used the values predicted for wine type to see if would improve it somehow.

Our first task is to predict the wine type since it will be more accurate being just a binary problem. When applying the kNN we first had to predict what's the k (the number of neighbours). We did this, separating the training set (consisting of the 5000 elements) into 3750 training elements, and 1250 validation el-

ements. We run the kNN with K going from 1 to 20, recorded the errors and took conclusions from that. We then did the same for the standardized data. To apply the logistic regression we just used the whole training set as one, and didn't split it. Predicted the type with non normalized data, it was time to use a go with the normalized approach. The logistic regression was basically the same, we normalized the variables using the 6000 elements, and made a prediction. We the kNN, we first normalized the 5000 elements of the training set (without the quality and type) and tried to get the best K for the problem. After that, we joined both the training set and test set, without the quality and type variables, and normalized it, and we made the prediciton for the type.

As said before, when predicting the quality type using either algorithm, we tried using the wine type to see if the results improved in some way.

IV. RESULTS

Data:

• Number of parameters: 11

• Number of samples in training set: 5000

• #Red: 906

• #White: 4094

• #Quality1: 5

• #Quality2: 161

• #Quality3: 854

• #Quality4: 2197

• #Quality5: 1604

• #Quality6: 159

• #Quality7: 20

• Number of samples in test set: 1000

kNN:

Table 1: *Result summary for kNN*

Experiment	Accuracy
Type (k=4)	95.3%
Type (scaled & K=1)	99.4%
Quality (k=12)	42.8%
Quality (scaled & k=1)	63.4%

Table 2: Confusion matrix for type using kNN with k=1 and data scaled

Type	White	Red
White	798	6
Red	0	196

The columns have the expected results and the line we have the real values, for example: In table 2 six white wines have been predicted to be red

Table 3: Confusion matrix for quality using kNN with k=1 and data scaled

Quality	1	2	3	4	5	6	7
1	0	0	0	0	0	0	0
2	0	13	7	5	1	0	0
3	0	9	114	49	9	0	0
4	0	6	44	272	78	8	0
5	0	0	11	99	225	9	0
6	0	0	3	11	12	10	0
7	0	0	0	1	3	1	0

Logistic Regression:

Table 4: Result summary for Logistic Regression

Experiment	Accuracy
Туре	99.6%
Quality	51.3%
Quality using type	51.8%

Table 5: Confusion matrix for type using Logistic Regression

Type	White	Red
White	802	2
Red	2	194

Table 6: Confusion matrix for quality using Logistic Regression

Quality	1	2	3	4	5	6	7
1	0	0	0	0	0	0	0
2	0	0	13	13	0	0	0
3	0	0	42	129	10	0	0
4	0	0	19	312	77	0	0
5	0	0	3	177	164	0	0
6	0	0	0	12	24	0	0
7	0	0	0	2	2	1	0

V. Discussion

space and computers power espaço ocupado pelo kNN e pelo logistic regresion

The values of quality are not independent with this a mean if a wine and classify was quality 'x' with is not the correct one, but is much more probably that the right quality is x - 1 or x + 1 than be x - 2, x + 2, x - 3, x + 3

We could have used this to classify the quality of wine.

One of the motives for the result be soo low for the quality of one wine is a subjective thing, two wine enthusiasts do not necessary give the same qualification for the same wine. This way it would be interesting to compare the result our classifier with two independent groups of human wine enthusiasts for each wine. Since the quality is a subjective we would expect the error between our result and the human result should be close to the error between the two independent groups of humans.

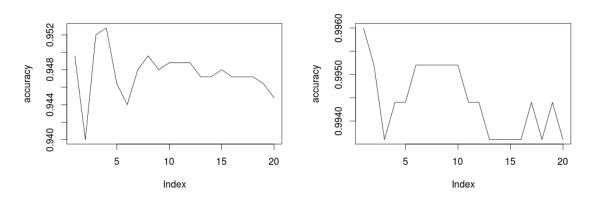
k par and k odd

REFERENCES

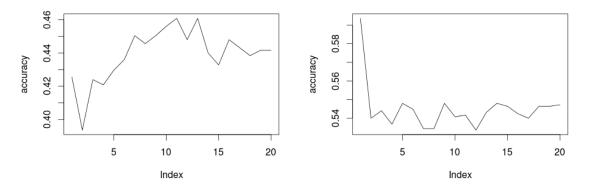
- [1] Alpaydin, Ethem Introduction to machine learning, MIT press, 2004.
- [2] Conceição, Amado Lecture Slides: Statistical Methods in Data Mining (2014). Instituto

- Superior Técnico, Portugal.
- [3] Duro, João & Pinheiro, Fábio Project code of Machine Learning Basic Principles, https://github.com/FabioPinheiro/ MachineLearningBasicPrinciples-T-61. 3050
- [4] Howe, Bill k Nearest Neighbors, https://class.coursera.org/datasci-001/lecture/161
- [5] Ng, Andrew Machine Learning. Multiclass Classifier: One-vs-All, https://class. coursera.org/ml-005/lecture/38.

Appendix A



(a) kNN - Type (With out and with the data scaled)



(b) kNN - Quality (With out and with the data scaled)

Figure 1: *Find k for the kNN*