

10

$$1) a) x^2 - 9 \neq 0 \Leftrightarrow x^2 \neq 9 \Leftrightarrow x \neq 3 \vee x \neq -3$$

$$D_f = ]-\infty, -3[ \cup ]3, +\infty[$$

$$b) x^2 - 1 \neq 0 \Leftrightarrow x \neq 1 \vee x \neq -1$$

$$D_g = ]-\infty, -1[ \cup ]1, +\infty[$$

$$2) a) \lim_{x \rightarrow 3} \frac{x^2 - 9}{x - 3} = \frac{(x-3)(x+3)}{x-3} = x+3 = 3+3 = 6$$

$$b) \lim_{x \rightarrow +\infty} \frac{2x^3 - x - 4}{5x^3 + 3x^2} = \frac{2 - \frac{1}{x} + \frac{4}{x^2}}{5 + \frac{3}{x}} = \frac{2 - 0 + 0}{5 + 0} = \frac{2}{5}$$

$$3) f(x) = \frac{x^2 - 4}{x - 2} = \frac{(x-2)(x+2)}{x-2} = x+2 = 2+2 = 4$$

$$4) f(0) = x^3 - 3x + 1 = (0)^3 - 3(0) + 1 = 0 - 0 + 1 = 1$$

$$f(1) = x^3 - 3x + 1 = (1)^3 - 3(1) + 1 = 1 - 3 + 1 = -1$$

$$f(0) = 1 > 0$$

$$f(1) = -1 < 0$$

$$5) x - 2 \neq 0 \Leftrightarrow x \neq 2$$

$$f(2^+) = \frac{2x^2 - x + 1}{x - 2} = \frac{2(2^+)^2 - 2^+ + 1}{2 - 2} = \frac{8 - 2 + 1}{0^+} = \frac{7}{0^+} = +\infty$$

$$f(2^-) = \frac{2x^2 - x + 1}{x - 2} = \frac{2(2^-)^2 - 2^- + 1}{2^- - 2} = \frac{7}{0^-} = -\infty$$



~~max 2/3~~

$$m = \frac{2x^2 - x + 1}{x(x-1)} = \frac{2x^2 - x + 1}{x^2 - x} = 2 \cdot \frac{x^2 - x + 1}{x^2 - x} \quad 2 \times 1 = 2$$

$$b = \lim_{x \rightarrow 100} \left[ \frac{2x^2 - x + 1}{x - 1} - 2x \right]$$

$$6) \quad f(2) = 2^3 - 3 \cdot 2^2 - 9 \cdot 2 + 5 = (2)^3 - 3(2)^2 - 9(2) + 5 = 8 - 12 - 18 + 5 = -17$$

$$f'(2) = 3x^2 - 6x - 9 = 3(2)^2 - 6(2) - 9 = 12 - 12 - 9 = -9$$

$$y = -9x + (-17 - (-9(2))) = -9x + 1$$

$$7) a) \quad \int 4x^3 - 2x + 5 \, dx = \frac{4x^4}{4} - \frac{2x^2}{2} + 5x + C, C \in \mathbb{R}$$

$$b) \quad \int \frac{6x^2}{x^3+1} = \int 2 \frac{3x^2}{1+x^3} = 2 \arctan(x^3) + C, C \in \mathbb{R}$$

$$c) \quad \int x \cdot \cos(x) \, dx = x \cdot \sin(x) - \int \cos(x) = x \cdot \sin(x) + \sin(x)$$

$$x \cdot \sin(x) + \sin(x) + C, C \in \mathbb{R}$$

$$8) a) \quad \int_1^3 2x - 1 \, dx = \left[ \frac{2x^2}{2} \right]_1^3 = \frac{2(3)^2}{2} - \frac{2(1)^2}{2} = \frac{18}{2} - \frac{2}{2} = 9 - 1 = 8$$

$$b) \quad \int_0^1 x \cdot e^x \, dx = \left[ x \cdot e^x \right]_0^1 - \int_0^1 e^x = \left[ x \cdot e^x - e^x \right]_0^1 =$$

$$\left[ (1 \cdot e^1 - e^1) - (0 \cdot e^0 - e^0) \right] = 0 - (-1) = 0 + 1 = 1$$