

Test 8

1) $x - 4 \neq 0 \Leftrightarrow x \neq 4 \Leftrightarrow x > 4$

$$D_f = \{x \in \mathbb{R} \mid x > 4\}$$

2) $\lim_{x \rightarrow 3^+} \frac{x^2 - 9}{x - 3} = \cancel{x-3} \cdot \frac{2x}{1} = 2x = 2(3) = 6$

b) $\lim_{x \rightarrow +\infty} \frac{2x^3 + x}{x^3 - 1} = 2 \lim_{x \rightarrow +\infty} \frac{x^3 + \cancel{x}}{x^3 - \cancel{1}} = 2 \lim_{x \rightarrow +\infty} = -2$

$$2 \times (-1) = -2$$

3) $f(x) = \frac{x^2 - 4}{x - 2} = \frac{(x-2)(x+2)}{x-2} = x+2 = 2+2 = 4$

4) $f(0) = 0^3 - 3 \cdot 0 + 1 = 0^3 - 3(0) + 1 = 0 - 0 + 1 = 1$

$$f(1) = 1^3 - 3 \cdot 1 + 1 = 1^3 - 3(1) + 1 = 1 - 3 + 1 = -1$$

$$f(0) = 1 > 0$$

$$f(1) = -1 < 0$$

exists zero entre $[0, 1]$.

5) $x - 1 \neq 0 \Leftrightarrow x \neq 1$

$$f(1^+) = \frac{x^2 + 2x}{x - 1} = \frac{(1^+)^2 + 2(1^+)}{1^+ - 1} = \frac{1^+ + 2^+}{0^+} = \frac{3}{0^+} = +\infty$$

$$f(1^-) = \frac{x^2 + 2x}{x - 1} = \frac{(1^-)^2 + 2(1^-)}{1^- - 1} = \frac{1^- + 2^-}{0^-} = \frac{3}{0^-} = -\infty$$

$$m = \frac{x^2 + 2x}{x(x-1)} = \frac{x(x+2)}{x(x-1)} = \frac{x(x+2)}{x(x-1)} = \frac{x+2}{x-1} = \frac{2}{1}$$

$$m = +\infty \quad 1$$

$$b = \lim_{x \rightarrow +\infty} \left[\frac{x^2 + 2x}{x-1} - (-2)x \right] = \left[\frac{x^2 + 2x + 2x}{x-1} \right] =$$

$$b = \lim_{x \rightarrow +\infty} \left[\frac{x^2 + 2x - 2x}{x-1} \right] = \lim_{x \rightarrow +\infty} \left[\frac{x^2}{x-1} \right] = \lim_{x \rightarrow +\infty} \frac{(x+3)(x-1)}{x-1} = \lim_{x \rightarrow +\infty} (x+3) = +\infty$$

$$D = \lim_{x \rightarrow +\infty} \left[\frac{x^2 + 2x}{x-1} + \frac{2x}{x-1} \right] = \left[\frac{1}{x-1} + \frac{2x}{1} \right]$$

$$b = \lim_{x \rightarrow +\infty} \left[\frac{x^2 + 2x}{x-1} + \frac{2x(x-1)}{x-1} \right] = \frac{x^2 + 2x + 2x^2 - 2x}{x-1}$$

$$b = \lim_{x \rightarrow +\infty} \left[\frac{x^2 + 2x}{x-1} - 1 \cdot x \right] = \left[\frac{x^2 + 2x - x}{x-1} \right]$$

$$b = \lim_{x \rightarrow +\infty} \left[\frac{x^2 + 2x - x(x-1)}{x-1} \right] = \frac{x^2 + 2x - (x^2 - x)}{x-1}$$

$$b = \lim_{x \rightarrow +\infty} \left[\frac{x^2 + 2x - x^2 + x}{x-1} \right] = \frac{3x}{x-1} = \frac{3}{1-\frac{1}{x}} = \frac{3}{1-0} = 3$$

$$b = 3$$

$$y = x + 3$$

Asintota vertical = 1

Asintota obliqua = $x + 3$

6)

a)

b)

7)

$$\text{a) } \int 4x^3 - 3x + 2 \, dx = \frac{4x^4}{4} - \frac{3x^2}{2} + 2x + C, C \in \mathbb{R}$$

~~$$\int \frac{4x}{x^2 + 1} \, dx = \int \frac{4x}{x^2 + 1} \, dx = \text{Integration by substitution } u = x^2 + 1, du = 2x \, dx$$~~

$$\text{b) } \frac{4x}{x^2 + 1} = 4x \cdot \frac{\text{antideriv}}{\cancel{x^2 + 1}}(x) + C, C \in \mathbb{R}$$

$$\text{8) } \int x \cdot e^x \, dx = x \cdot e^x - \int e^x = x \cdot e^x - e^x + C, C \in \mathbb{R}$$

$$\text{9) } \int_1^2 2x + 1 \, dx = \left[\frac{2x^2}{2} + x \right]_1^2 = \left(\frac{2(1)^2}{2} + 1 \right) + \left(\frac{2(2)^2}{2} + 2 \right) \\ = \left(\frac{2}{2} + 2 \right) + \left(\frac{8}{2} + 2 \right) = 3 + 6 = 9$$

$$\text{10) } A = \int_0^1 x^2 - x \, dx = \left[\frac{x^3}{3} - \frac{x^2}{2} \right]_0^1 = \left[\frac{0^3}{3} + \frac{0^2}{2} \right] - \left[\frac{1^3}{3} + \frac{1^2}{2} \right]$$

$$= 0 - \left[\frac{1}{6} + \frac{1}{2} \right] = 0 - \frac{5}{6} = -\frac{5}{6}$$