

$$1a) x^2 - 9 > 0 \Leftrightarrow x^2 > 9 \Leftrightarrow x > 3 \\ x < -3$$

$$\text{Df} =]-\infty, -3] \cup [3, +\infty[$$

$$b) 2x - 3 \neq 0 \Leftrightarrow 2x \neq 3 \Leftrightarrow x \neq \frac{3}{2}$$

$$x+1 > 0 \Leftrightarrow x > -1$$

$$\text{Dg} = \{-1, \frac{3}{2}\} \cup \left[\frac{3}{2}, +\infty \right[$$

$$2a) \frac{x^2 - 9}{x^2 - 5x + 6} = \frac{(x-3)(x+3)}{(x-2)(x-3)} = \frac{x+3}{x-2} = \frac{3+3}{3-2} = 6$$

$$b) \frac{3x^3 - 2x + 1}{6x^3 + x^2 - 1} = \frac{\frac{3}{x^2} - \frac{2}{x^2} + \frac{1}{x^2}}{6 + \frac{1}{x} - \frac{1}{x^3}} = \frac{\frac{3}{x^2}}{6} < \frac{1}{2}$$

$$c) \frac{\sqrt{1+x} - 1}{x} =$$

$$3) f(x) = \frac{x^2 - 4}{x - 2} = \frac{(x-2)(x+2)}{x-2} = x + 2 = 2 + 2 = 4$$

$$x = 4$$

$$4) h(0) = x^3 - 3x + 1 = 0^3 - 3(0) + 1 = 1$$

$$h(1) = x^3 - 3x + 1 = 1^3 - 3(1) + 1 = -1$$

$$h(0) = 1 > 0 \\ h(1) = -1 < 0$$

$$5) x+2 > 0 \Leftrightarrow x > -2 \quad \text{Df} =]-\infty, -2] \cup [-2, +\infty[$$

$$f(x) = \frac{dx^2 + x - 1}{x + 2} = \frac{2(2^2) + 2^2 - 1}{2 + 2} = \frac{8 + 2 - 1}{0^+} = \frac{9}{0^+} = +\infty$$

$$f(2) = \frac{2x^2 + x - 1}{x+2} = \frac{2(2)^2 + 2 - 1}{2+2} = \frac{8+2-1}{0} = \frac{9}{0} = -\infty$$

$$m = \lim_{n \rightarrow +\infty} \frac{2x^2 + x - 1}{x^2 + 2} = \frac{\frac{1}{n} + \frac{1}{n^2} - \frac{1}{n^2}}{\frac{1}{n^2} + \frac{2}{n^2}} = \frac{1+0-0}{0+0} = 1$$

$$b = \lim_{n \rightarrow +\infty} \frac{2x^2 + x - 1}{x+2} - 2x = \frac{2x^2 + x - 1 - 2x(n+2)}{x+2} = \frac{2x^2 + x - 1 - 2x^2 + 4x}{x+2}$$

$$= \frac{5x - 1}{n+2} = \frac{5}{n} - \frac{1}{n} = \frac{5-0}{0+0} = 5$$

$$y = 2x - 12 - 2(2) = 2x - (2 - 4) = 2x + 2$$

$$\Delta V = 2$$

$$\Delta H = \text{New term} - \frac{\text{grau 2}}{\text{grau 1}}$$

$$\Delta O = 2x + 2$$

$$6a) f'(x) = \frac{3x(x^2-2) - 2x(3x+1)}{(x^2-2)^2} = \frac{3x^3 - 6 - 5x^2 + 2}{x^4 - 4}$$

$$b) g'(x) = \ln(x^3 + 2x - 1)$$

$$c) h'(x) = -\sin(x) \cdot e^{2x} + \cos(x) \times 2e^{2x}$$

$$7a) \int 4x^3 - 6x + 5 \, dx = \frac{4x^4}{4} - \frac{6x^2}{2} + 5x + C, C \in \mathbb{R}$$

$$b) \int \frac{6x^2}{x^3 + 4} \, dx = 2 \ln(x^3 + 4) + C, C \in \mathbb{R}$$

$$c) \int x \cdot \cos(x) \, dx = x \cdot \sin(x) - \int \sin(x) \, dx = x \cdot \sin(x) - \cos(x)$$

$$x \cdot \sin(x) - \cos(x) + C, C \in \mathbb{R}$$

$$8) \int x^2 + 2x - 1 \, dx = \left[\frac{x^3}{3} + \frac{2x^2}{2} - x \right]_1^2 =$$

$$\frac{2^3}{3} + \frac{2(2)^2}{2} - 2 - \frac{(-1)^3}{3} + \frac{2(-1)^2}{2} + 1 = \frac{8}{3} - \frac{8}{2} - \frac{2}{1} - \frac{-1}{3} + \frac{1}{2} + \frac{1}{1}$$

$$\frac{16}{6} - \frac{12}{6} - \frac{12}{6} + \frac{3}{6} + \frac{6}{6} = \frac{-9}{6} = \frac{-3}{2}$$

9)

$$F(1) = \frac{6x^3}{3} - \frac{4x^2}{2} + C = 2x^3 - 2x^2 + C = 3, C \in \mathbb{R}$$

$$10) x^2 = 3^2 = 9$$

$$2x + 3 = 9$$

$$A = \int_{-1}^3 x^2 - (2x + 3) \, dx = \left[\frac{x^3}{3} - \left(\frac{2x^2}{2} + 3x \right) \right]_{-1}^3 =$$

$$A = \frac{3^3}{3} - \left(\frac{2(3)^2}{2} + 3(3) \right) - \frac{-1^3}{3} - \left(\frac{2(-1)^2}{2} + 3(-1) \right) =$$

$$A = \frac{27}{3} - \left(\frac{18}{2} + \frac{9}{1} \right) - \frac{-1}{3} - \left(\frac{2}{2} - \frac{3}{1} \right) =$$

$$A = \frac{27}{3} - \left(\frac{18}{2} + \frac{17}{2} \right) - \frac{-1}{3} - \left(\frac{2}{2} - \frac{6}{2} \right) =$$

$$A = \frac{27}{3} - \frac{36}{2} - \frac{-1}{3} + \frac{4}{2} = \\ (\times 2) \quad (\times 1) \quad (\times 2) \quad (\times 3)$$

$$A = \frac{54}{6} - \frac{108}{6} - \frac{-2}{6} + \frac{12}{6} = -\frac{40}{6}$$

$$A = -\frac{40}{6}$$