

$$1a) \frac{4 \pm \sqrt{(-4)^2 - 4 \times 1 \times 3}}{2 \times 1} = \frac{4 \pm \sqrt{16 - 12}}{2} = \frac{4 \pm \sqrt{4}}{2}$$

$$\frac{4+2}{2} = \frac{6}{2} = 3$$

$$\frac{4-2}{2} = \frac{2}{2} = 1$$

$$D_f =]1, 3[$$

$$b) x^2 - 9 > 0 \Leftrightarrow x^2 > 9 \Leftrightarrow x > 3$$

$$D_g =]-\infty, -3[\cup]3, +\infty[$$

$$c) x - 1 \neq 0 \Leftrightarrow x \neq 1$$

$$x - 2 \geq 0 \Leftrightarrow x \geq 2$$

$$D_h = [-2, 1[\cup]1, +\infty[$$

2)

$$a) \lim_{x \rightarrow 2} \frac{x^2 - 4}{x^2 - 5x + 6} = \frac{(\cancel{x-2})(x+2)}{(\cancel{x-2})(x-3)} = \frac{x+2}{x-3} = \frac{2+2}{2-3} =$$

$$\frac{4}{-1} = -4$$

$$b) \lim_{x \rightarrow +\infty} \frac{(1)x^3 - 2x + 1}{2x^3 + x^2 - 3} = \frac{4 - \frac{2}{x^2} + \frac{1}{x^3}}{2 + \frac{1}{x} - \frac{3}{x^3}} = \frac{4}{2} = 2$$

$$c) \frac{\sqrt{1+2x} - 1}{x} = \frac{\sqrt{1+2x} - 1}{x} \times \frac{\sqrt{1+2x} + 1}{\sqrt{1+2x} + 1} = \frac{(1+2x) - 1}{x(\sqrt{1+2x} + 1)}$$

$$\underline{2x}$$

$$3) f(1) = \frac{x^2 - 1}{x - 1} = \frac{(x-1)(x+1)}{x-1} = x+1 = 1+1 = 2$$

$$K = 2$$

$$4) g(0) = x^3 - 3x + 1 = (0)^3 - 3(0) + 1 = 1$$

$$g(1) = x^3 - 3x + 1 = 1^3 - 3(1) + 1 = -1$$

$$g(0) = 1 > 0$$

$$g(1) = -1 < 0$$

$$5) f(-2^+) = \frac{3x-1}{x+2} = \frac{3(-2)-1}{-2+2} = \frac{-7}{0^+} = +\infty$$

$$\lim_{x \rightarrow +\infty} \frac{3x-1}{x+2} = \frac{3 - \frac{1}{x}}{1 + \frac{2}{x}} = 3$$

$$AV = -2$$

$$AH = 3$$

6)

$$a) 5x^4 - 12x^2 + 2$$

$$b) 4(3x^2 + 1)^3 \cdot 6x$$

c)

$$d) (e^{2x} \cdot x) \cdot \frac{1}{x}$$

$$7) f(1) = x^3 - 2x = 1^3 - 2(1) = -1$$

$$f'(1) = 3x^2 - 2 = 3(1)^2 - 2 = 1$$

$$P_{\text{onto}} = (1, -1)$$

$$NT = -1$$

$$8) \quad a) \int 6x^2 - 4x + 3 \, dx = 2x^3 - 2x^2 + 3x + C, C \in \mathbb{R}$$

$$b) \int \frac{4x}{x^2 + 3} \, dx = \ln(x^2 + 3) + C, C \in \mathbb{R}$$

$$c) \int x \cdot \cos(x) \, dx = x \cdot \sin(x) - \int \sin(x) \cdot 1 = x \cdot \sin(x) - \cos(x) + C, C \in \mathbb{R}$$

$$d) \int x^2 \cdot e^x \, dx = x^2 \cdot e^x - \int 2x \cdot e^x \, dx = x^2 \cdot e^x - 2x \cdot e^x - \int 2e^x \, dx = \\ x^2 \cdot e^x - 2x \cdot e^x - 2e^x - \int e^x \, dx = \\ x^2 \cdot e^x - 2x \cdot e^x - 2e^x - e^x + C, C \in \mathbb{R}$$

$$9) \quad \int_1^3 2x^2 - x + 1 \, dx = \left[\frac{2x^3}{3} - \frac{x^2}{2} + x \right]_1^3 = \\ \left(\frac{2(3)^3}{3} - \frac{3^2}{2} + 3 \right) - \left(\frac{2(1)^3}{3} - \frac{1^2}{2} + 1 \right) = \left(\frac{54}{3} - \frac{27}{2} + 3 \right) - \left(\frac{2}{3} - \frac{1}{2} + 1 \right) = \\ = (18 - 9 - 3) - \left(\frac{12}{6} - \frac{3}{6} - 1 \right) = 6 - \left(\frac{9}{6} - 1 \right) = 6 - \left(\frac{3}{2} - \frac{1}{1} \right) = 6 - \frac{3}{2} - \frac{1}{2} = \\ = \frac{6}{1} - \frac{1}{2} = \frac{12}{2} - \frac{1}{2} = \frac{11}{2}$$

$$10) \quad F(x) = 2 \ln(x) + 2x^2 + C = 3, C = 1$$

$$11) \quad 6 - x^2 = 6 - 4 = -2$$

$$\int_{-2}^2 2 - 6 - x^2 \, dx = \left[2x - 6x - \frac{x^3}{3} \right]_{-2}^2 = \left(2(2) - 6(2) - \frac{2^3}{3} \right) - \left(2(-2) - 6(-2) - \frac{(-2)^3}{3} \right) \\ = \left(4 - 12 - \frac{8}{3} \right) + \left(4 + 12 - \frac{-8}{3} \right) = \left(-\frac{8}{1} - \frac{8}{3} \right) + \left(\frac{16}{1} - \frac{-8}{3} \right) = \\ = \left(-\frac{24}{3} + \frac{8}{3} \right) + \left(\frac{48}{3} - \frac{-8}{3} \right) = \frac{-16}{3} + \frac{56}{3} = \frac{40}{3}$$