



$$1a) x^2 - 5x + 6 \neq 0$$

$$\frac{5 \pm \sqrt{-5^2 - 4 \times 1 \times 6}}{2 \times 1} = \frac{5 \pm \sqrt{25 - 24}}{2} =$$

$$\frac{5+1}{2} = \frac{6}{2} = 3$$

$$\frac{5-1}{2} = \frac{4}{2} = 2$$

$$Df = ]-\infty, 2[ \cup ]2, 3[ \cup ]3, +\infty[$$

$$b) 4 - x^2 > 0 \Leftrightarrow -x^2 > -4 \Leftrightarrow x^2 < 4 \Leftrightarrow x \in ]-2, 2[$$

$$Dg = ]-2, 2[$$

$$c) 2x - 6 > 0 \Leftrightarrow 2x > 6 \Leftrightarrow x > \frac{6}{2} \Leftrightarrow x > 3$$

$$Dh = ]3, +\infty[$$

$$2a) \lim_{x \rightarrow 3} = \frac{x^2 - 9}{x - 3} = \lim_{x \rightarrow 3} \frac{(x-3)(x+3)}{x-3} =$$

$$\lim_{x \rightarrow 3} x+3 = 3+3 = 6$$

$$b) \lim_{n \rightarrow +\infty} \frac{5x^2 - 3x + 1}{2x^2 + 7} = \lim_{n \rightarrow +\infty} \frac{\frac{5}{n^2} - \frac{3}{n} + \frac{1}{n^2}}{\frac{2}{n^2} + \frac{7}{n^2}} = \frac{5}{2}$$

$$c) \lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x} = \frac{\sqrt{1+x} - 1}{x} \times \frac{\sqrt{1+x} + 1}{\sqrt{1+x} + 1} \stackrel{?}{=} \frac{(1+x) - 1}{x(\sqrt{1+x} + 1)}$$

$$\frac{x}{x(\sqrt{1+x} + 1)} = \frac{1}{\sqrt{1+x} + 1} = \frac{1}{\sqrt{1+0} + 1} = \frac{1}{1+1} = \frac{1}{2}$$

$$3) f(x) = \frac{x^2 - 4}{x - 2} = \frac{(x-2)(x+2)}{x-2} = x+2 = 2+2 = 4$$

$$k = 4$$

$$4) g(0) = x^3 - 4x + 1 = 0^3 - 4(0) + 1 = 1$$

$$g(2) = x^3 - 4x + 1 = 2^3 - 4(2) + 1 = 8 - 8 + 1 = 1$$

Now ten zeros more  $10, 2\Sigma$

$$5) \lim_{n \rightarrow 3^+} \frac{2n+1}{n-3} = \frac{2(3)+1}{3-3} = \frac{7}{0^+} = +\infty$$

$$\lim_{n \rightarrow +\infty} \frac{2x+1}{n-3} = \frac{2 + \frac{1}{n}}{1 - \frac{3}{n}} = 2$$

$$AV = 3$$

$$AH = 2$$

$$6) a) 4x^3 - 6x + 5$$

$$b) 5(2x+1)^4 x^2$$

$$c) \frac{2x(x+3) - (x^2 - 1)}{(x+3)^2}$$

$$d) e^{x^2+1} \cdot 2x$$

$$7) f(1) = x^3 - 2x = 1^3 - 2(1) = -1$$

$$f'(1) = 3x^2 - 2 = 3(1)^2 - 2 = 1$$

$$\text{Ponto} = (1, -1)$$

$$\text{Neta} = 1$$

$$8) a) \int 4x^3 - 6x + 2 \, dx = \frac{4x^4}{4} - \frac{6x^2}{2} + 2x = \\ x^4 - 3x^2 + 2x + C, C \in \mathbb{R}$$

$$b) \int \frac{2x}{x^2 + 1} \, dx = \ln(x^2 + 1) + C, C \in \mathbb{R}$$

$$c) \int x \cdot e^x \, dx = \frac{x^2}{2} \cdot e^x - \int e^x \, dx = \\ \frac{x^2}{2} \cdot e^x - e^x + C, C \in \mathbb{R}$$

$$d) \int \ln(x) \, dx = x \cdot \ln(x) - x + C, C \in \mathbb{R}$$

$$9) \int_0^2 (3x^2 - 4x + 1) \, dx = \left[ x^3 - 2x^2 + x \right]_0^2 =$$

$$2^3 - 2(2)^2 + 2 = 8 - 8 + 2 = 2$$

$$10) f(1) = 3 \ln(1) + 1^2 + C = 5, C = 4$$

$$11) \int_{-2}^2 (4 - x^2) \, dx = \left[ 4x - \frac{x^3}{3} \right]_{-2}^2 = 4(2) - \frac{2^3}{3} - 4(-2) - \frac{(-2)^3}{3}$$

$$= \frac{8}{1} - \frac{8}{3} + \frac{8}{1} - \frac{-8}{3} = \frac{24}{3} - \frac{8}{3} + \frac{24}{3} - \frac{-8}{3} =$$

$$= \frac{16}{3} + \frac{24}{3} - \frac{8}{3} = \frac{40}{3} - \frac{8}{3} = \frac{48}{3} = 16$$