

### **Exercise 13-1 (c=1):**

(1) Create an example where the optimal solution is always obtained by the greedy algorithm independent of the selection order of the shortest paths. (2) Create another example where  $|I^*| \geq \sqrt{m} |I|$  always holds independent of the selection order of the shortest paths. (3) Create another example where  $|I^*| > \sqrt{m} |I|$  holds depending on the selection order of the shortest paths.

### **Exercise 13-2 (c = 2):**

(1) Create an example where the optimal solution is always obtained by the greedy algorithm (independent of the choice of the shortest paths: independent of a tie-breaking method).

(2) Create another example where the greedy algorithm solution  $|I|$  is close to  $|I^*| / (4m^{1/3} + 1)$  depending on the choice of the shortest paths (i.e., depending on a tie-breaking method).