## Reflections implementation For ${\bf D3D9Client}$

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## Fresnel reflection

Fresnel reflection will occur when a ray of light will hit into an "optical" material that has a refractive index n. Good examples of such materials are glass, water and most plastics. Fresnel reflection is highly depended from a viewing angle. In the D3D9Client we use so called Schlick's approximation of fresnel reflection.

$$R = R_0 + (1 - R_0)(1 - \cos \theta)^p \tag{1}$$

Where the "Offset"  $R_0$  is given by

$$R_0 = \left\lceil \frac{1-n}{1+n} \right\rceil^2 \tag{2}$$

To gain some additional properties for our function we have replaced the term  $(1 - R_0)$  with a multiplier m resulting an equation

$$R = R_0 + m(1 - \cos\theta)^p \tag{3}$$

Here are two plots of the equation using different values of p. Red curve is using value 2.0 and blue 4.0. The parameter p will only effect in the view angle dependency of the fresnel reflection. The multiplier m is most often set to a value  $1 - R_0$  and in that case the maximum reflection intensity is 1.0.

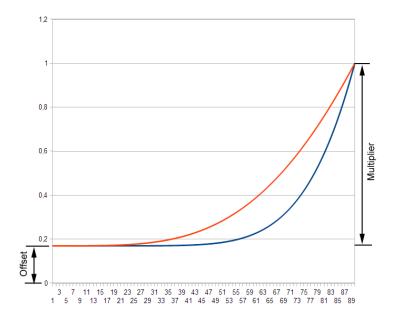


Figure 1: Plot

## Reflection Model

Here is an image about the reflection model used in D3D9Client

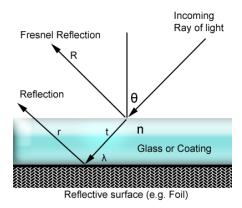


Figure 2: Model

The model consists from a fresnel reflection R and a metallic reflection r. The lambda  $\vec{\lambda}$  is a reflectivity color of the material. t is a fraction of the incoming ray that is not reflected away from the interface. Value of t is simply t = 1 - R.

The intensity of "metallic" reflection alone is independent from a viewing angle. However, when combined with a fresnel reflection it is given by

$$\vec{r} = \vec{\lambda}(1 - R) \tag{4}$$

The total reflected light is of course r + R. I suppose the fresnel reflection could take a specular color  $\vec{s}$  but currently it is considered to be white  $\vec{s} = [1, 1, 1]$ 

$$\vec{R_{tot}} = \vec{\lambda}(1 - R) + \vec{s}R \tag{5}$$

The color intensity of the diffuse surface is attenuated by the reflection intensity factor  $1 - |\vec{\lambda}|$ . Resulting pixel color  $\vec{c}$  is given by following equation where  $\vec{d}$  it the color of the diffuse surface or a texture.

$$\vec{c} = \vec{d}(1 - |\vec{\lambda}|) + \vec{\lambda}(1 - R) + \vec{s}R \tag{6}$$

In the D3D9Client we simplify the computations and we do not apply fresnel equations to incoming sunlight. A diffuse surface under a reflective coating is considered to be fully lit by the sunlight and other light sources. If we would take it in to account then the equation would become

$$\vec{c} = \vec{d}(1 - |\vec{\lambda}|)[1 - R_0 - m(1 - \cos \sigma)^p] + \vec{\lambda}(1 - R) + \vec{s}R \tag{7}$$

Where  $\sigma$  is the normal/sun angle.