

**Reflections implementation**  
**For**  
**D3D9Client**

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## Fresnel reflection

Fresnel reflection will occur when a ray of light will hit into an "optical" material that has a refractive index  $n$ . Good examples of such materials are glass, water and most plastics. Fresnel reflection is highly depended from a viewing angle. In the D3D9Client we use so called Schlick's approximation of fresnel reflection.

$$R = R_0 + (1 - R_0)(1 - \cos \theta)^p \quad (1)$$

Where the "Offset"  $R_0$  is given by

$$R_0 = \left[ \frac{1 - n}{1 + n} \right]^2 \quad (2)$$

To gain some additional properties for our function we have replaced the term  $(1 - R_0)$  with a multiplier  $m$  resulting an equation

$$R = R_0 + m(1 - \cos \theta)^p \quad (3)$$

Here are two plots of the equation using different values of  $p$ . Red curve is using value 2.0 and blue 4.0. The parameter  $p$  will only effect in the view angle dependency of the fresnel reflection. The multiplier  $m$  is most often set to a value  $1 - R_0$  and in that case the maximum reflection intensity is 1.0.

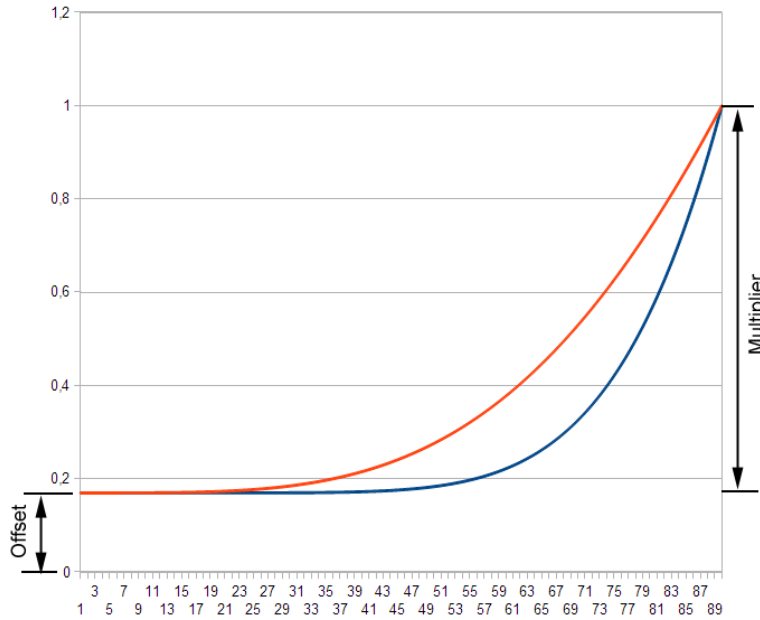


Figure 1: Reflection intensity as function of angle

## Reflection Model

Here is an image about the reflection model used in D3D9Client

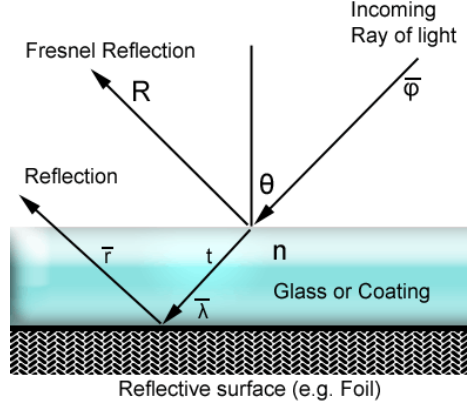


Figure 2: Reflection model

The model consists from a fresnel reflection  $R$  and a metallic reflection  $r$ . The lambda  $\vec{\lambda}$  is a reflectivity color of the material.  $t$  is a fraction of the incoming ray that is not reflected away from the interface.  $\vec{\varphi}$  is the color of incoming ray of light. The value of  $t$  is simply  $t = 1 - R$ .

The intensity of "metallic" reflection alone is independent from a viewing angle. However, when combined with a fresnel reflection it is given by

$$\vec{r} = \vec{\lambda}t\vec{\varphi} = \vec{\lambda}(1 - R)\vec{\varphi} \quad (4)$$

The total reflected light is, of course,  $\vec{R}_{tot} = r + R$ . I suppose the fresnel reflection could take a specular color  $\vec{s}$  of the material but currently it is considered to be white  $\vec{s} = [1, 1, 1]$

$$\vec{R}_{tot} = (\vec{\lambda}(1 - R) + \vec{s}R)\vec{\varphi} \quad (5)$$

The color intensity of the diffuse surface is attenuated by the reflection intensity factor  $1 - |\vec{\lambda}|$ . Resulting pixel color  $\vec{c}$  is given by following equation where  $\vec{d}$  is the color of the diffuse material or a texture.

$$c_{rgb} = d_{rgb}(1 - |\vec{\lambda}|) + \vec{R}_{tot} \quad (6)$$

Material/Texture alpha must be modified for alpha blending stage to make reflections visible on otherwise transparent surfaces like glass.

$$\vec{c}_a = \max(\vec{d}_a, |\vec{R}_{tot}|) \quad (7)$$

In the D3D9Client we simplify the computations and we do not apply fresnel equations to incoming sunlight. A diffuse surface under a reflective coating is considered to be fully lit by the sunlight and other light sources.

If we would take the sun angle  $\sigma$  in to account then the equation would become

$$c_{rgb} = d_{rgb}(1 - |\vec{\lambda}|)[1 - R_0 - m(1 - \cos \sigma)^p] + \vec{R}_{tot} \quad (8)$$