

TPL4

HOJA N°

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FECIA

$$1) \text{ si } \alpha_{\max} = 1 \text{ dB} \rightarrow \xi^2 = 10^{\frac{\alpha_{\max} \text{ dB}}{10}} - 1 \rightarrow \boxed{\xi^2 = 0,259}$$

Tomando la Transferencia normalizada del TPL3, $\Omega_z = R_3$ y $\Omega_w = \omega_0$

$$T(s)_{\text{norma}} = \frac{(-1) \cdot K}{s^2 + s \cdot \frac{1}{Q} + 1} \rightarrow \boxed{n=2}$$

$$\text{si } T(\omega) = \frac{1}{1 + \xi^2 \cdot \omega^{2n}} \rightarrow |T(s)|^2_{\omega = \frac{s}{j}} = \frac{1}{1 + \xi^2 \cdot (-j)^{2n} \cdot s^{2n}}$$

$$\text{si } n=2 \rightarrow \therefore |T(s)|^2 = \frac{\frac{1}{\xi^2}}{s^4 + \frac{1}{\xi^2}} \quad (1)$$

$$T(s) \cdot T(-s) = \frac{(-1) \cdot K}{(s^2 + s \cdot \frac{1}{Q} + 1)} \cdot \frac{(-1) \cdot K}{(s^2 - s \cdot \frac{1}{Q} + 1)}$$

$$|T(s)|^2 = \frac{K^2}{s^4 - \cancel{s^3 \cdot \frac{1}{Q}} + s^2 + \cancel{s \cdot \frac{1}{Q}} - s^2 \cdot \frac{1}{Q^2} + \cancel{s \cdot \frac{1}{Q}} + s^2 - \cancel{s \cdot \frac{1}{Q}} + 1}$$

$$\boxed{|T(s)|^2 = \frac{K^2}{s^4 + s^2 \cdot (2 - \frac{1}{Q^2}) + 1}} \quad (2)$$

igualdo ① y ②

$$\frac{\frac{1}{\xi^2}}{s^4 + \frac{1}{\xi^2}} = \frac{K^2}{s^4 + s^2 \cdot (2 - \frac{1}{\xi^2}) + 1}$$

$$K^2 = \frac{1}{\xi^2} \rightarrow K = \frac{1}{\sqrt{\xi^2}} \rightarrow K = 1,965$$

$$2 - \frac{1}{\xi^2} = 0 \rightarrow 2 = \frac{1}{\xi^2} \rightarrow \xi = \frac{1}{\sqrt{2}} = 0,707$$

$$\therefore T(s) = \frac{(-1) \cdot (1,965)}{s^2 + s \cdot \frac{1}{0,707} + 1} \rightarrow \text{para un } \alpha_{\max} = 1\text{dB}$$

2) si $s = j\omega \rightarrow T(j\omega) = \frac{(-1) \cdot (1,965)}{-\omega^2 + j\omega \cdot \frac{1}{0,707} + 1} = \frac{(-1) \cdot (1,965)}{(1 - \omega^2) + j(\frac{\omega}{0,707})}$

$$T(\omega) = \frac{1,965}{\sqrt{(1 - \omega^2)^2 + (\frac{\omega}{0,707})^2}} \cdot \frac{e^{j\pi}}{e^{j \arctan(\frac{\omega/0,707}{1 - \omega^2})}}$$

$$|T(0)| = 1,965$$

$$|T(\infty)| = 0$$

esta normalizada en $\omega_0 \rightarrow \omega_0' = 1$

$$|T(\omega_0')| = 1,389$$

$$\angle T(0) = \pi$$

$$\angle T(\infty) = 0$$

$$\angle T(\omega_0') = \frac{\pi}{2}$$

