

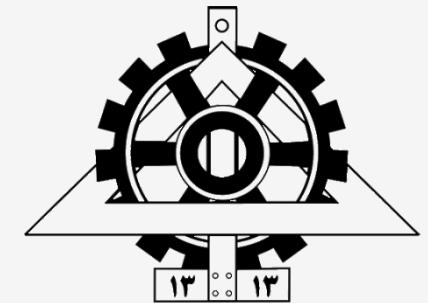


*Hyperspectral Remote Sensing*

*Spectral  
Unmixing &  
Target Detection*



**University of Tehran**  
**College of Engineering**  
**Faculty of Surveying and Geospatial engineering**  
**Remote Sensing**



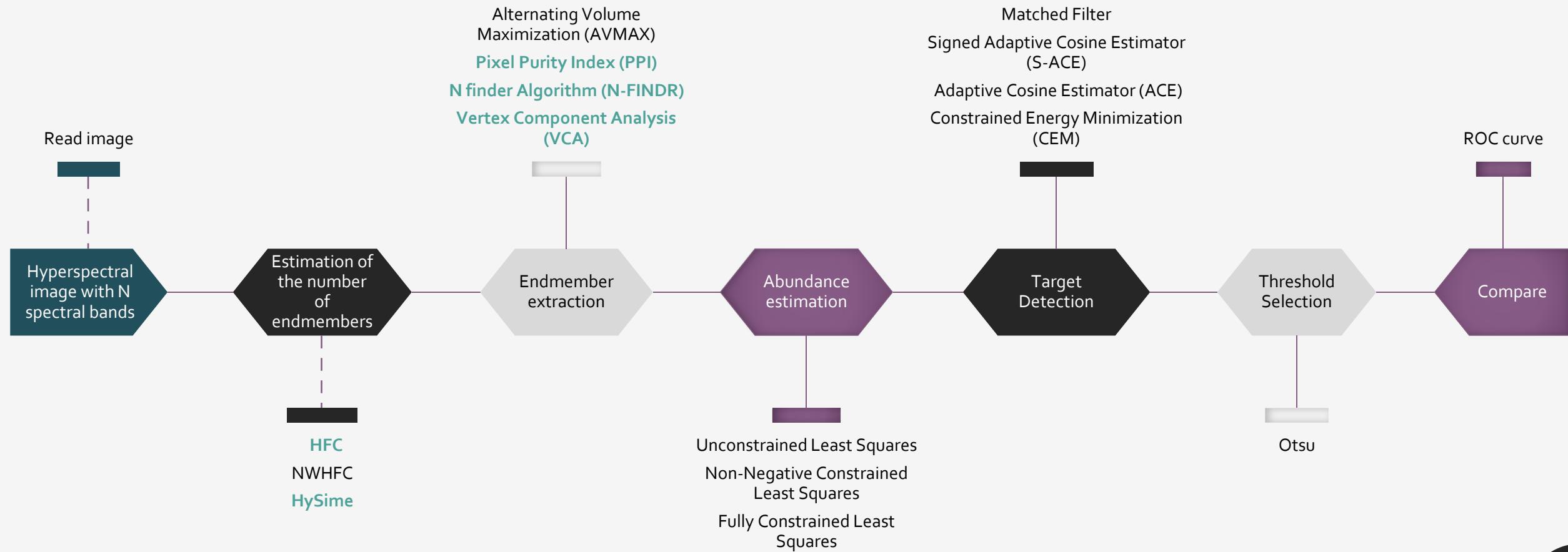
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**810399040**

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# Method



- General scheme of Spectral Unmixing And Target Detection

# *Data*

Data that I used in this project.



The Cooke City Dataset

(280\*800) \*126

# *Endmembers Estimation*

*Classic methods for subspace estimation is Virtual dimensionality HFC & NWHFC & Hyperspectral subspace identification minimum error (HySime)*



# *Endmember extraction*

Classic methods for endmember extraction



Vertex Component  
Analysis  
(VCA)



Pixel Purity Index  
(PPI)



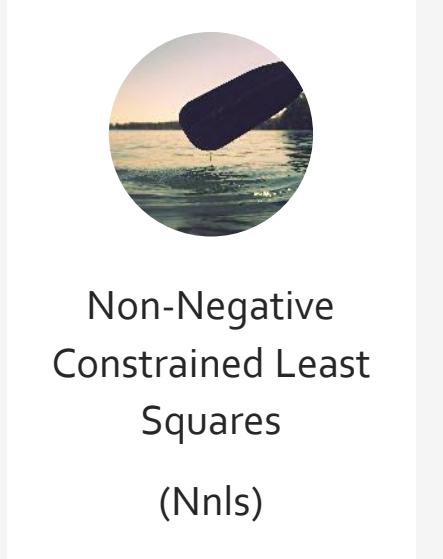
N finder Algorithm  
(N-FINDR)

# *Abundance estimation*

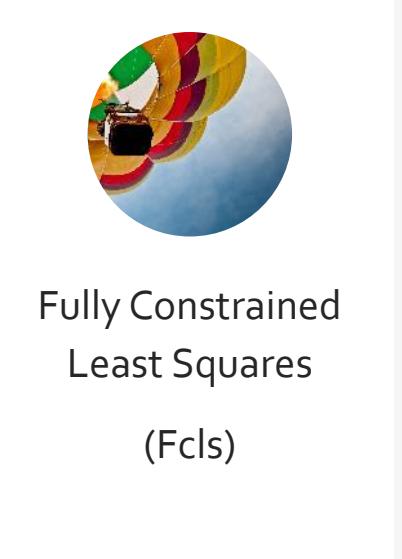
Classic methods for abundance estimation:



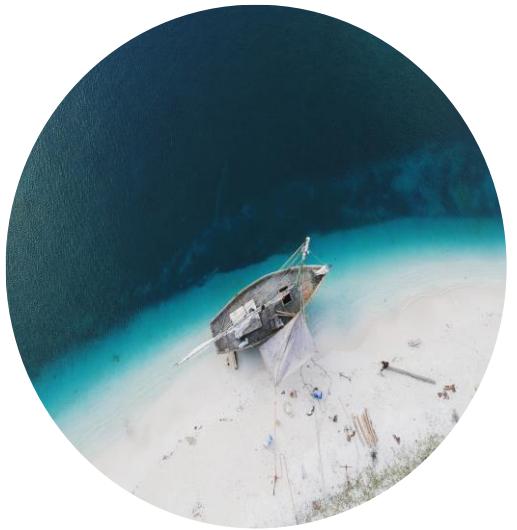
Unconstrained Least  
Squares  
(Ucls)



Non-Negative  
Constrained Least  
Squares  
(Nnls)



Fully Constrained  
Least Squares  
(Fccls)



# HFC

## Endmembers Estimation

### *Harsanyi-Farrand-Chang(HFC)*

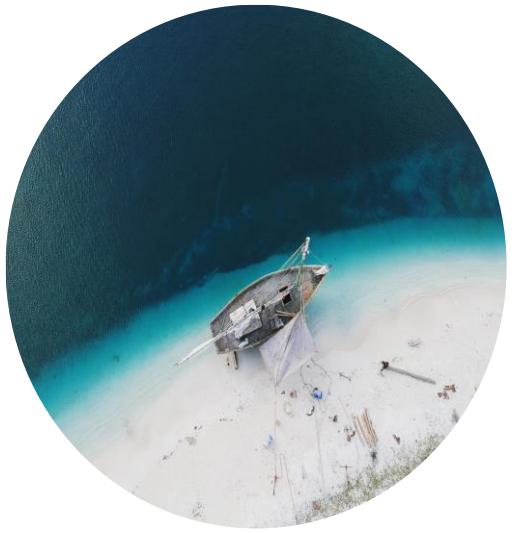
$$\mathbf{R}_{L \times L} = \sum_{i=1}^N \mathbf{r}_i \mathbf{r}_i^T \quad \{\hat{\lambda}_1 \geq \hat{\lambda}_2 \geq \dots \geq \hat{\lambda}_L\}$$

$$\mathbf{K}_{L \times L} = \sum_{i=1}^N (\mathbf{r}_i - \boldsymbol{\mu})(\mathbf{r}_i - \boldsymbol{\mu})^T \quad \{\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_L\}$$

$$\hat{\lambda}_l > \lambda_l \text{ for } l = 1, \dots, \text{VD}$$

$$\hat{\lambda}_l = \lambda_l \text{ for } l = \text{VD} + 1, \dots, L$$

The HFC method was first envisioned in Harsanyi et al. (1994a) to detect spectral signatures present in AVIRIS data. It was then used to find the now-popular terminology, VD which is defined as the number of spectral distinct signatures and later published in Chang and Du (2004). It calculates the difference between eigenvalues in sample correlation matrix and sample covariance matrix and makes use of Neyman–Pearson detector to determine the value of VD.



# *HySime*

## *Hyperspectral subspace identification minimum error*

The idea of HySime is to find the first  $k$  eigenvectors that contain the most of data information, i.e. , to find the  $k$  such that the mean square error (MSE) between the original data and its projection on to the eigenvector subspace is minimum.

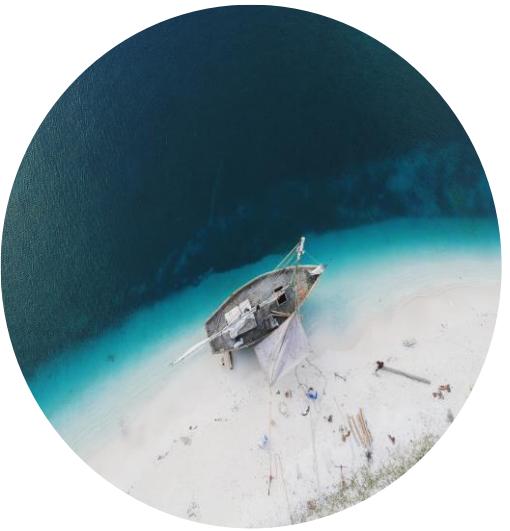
Subspace  $k$  is ranked in terms of data variance ,but noise variance is not unitary indifferent directions and the contribution from signals maybe smaller than from noise.

HySime addresses this issue using subspace projection techniques, thus bringing an additional feature with regards to VD :the modelling of noise before the estimation.

# *Result of Endmember Estimation*

Method	Noise	The Cooke City Dataset
HFC	$P_f = 10^{-8}$	33
NWHFC	$P_f = 10^{-8}$	37
HySime	$P_f = 10^{-8}$	19

we know HySime is better than NWHFC and NWHFC is better than HFC , so that I used result of increase HySime for next step.



## *Pixel Purity Index*

It is developed based on the concept of the convex geometry and the criterion of orthogonal projection.

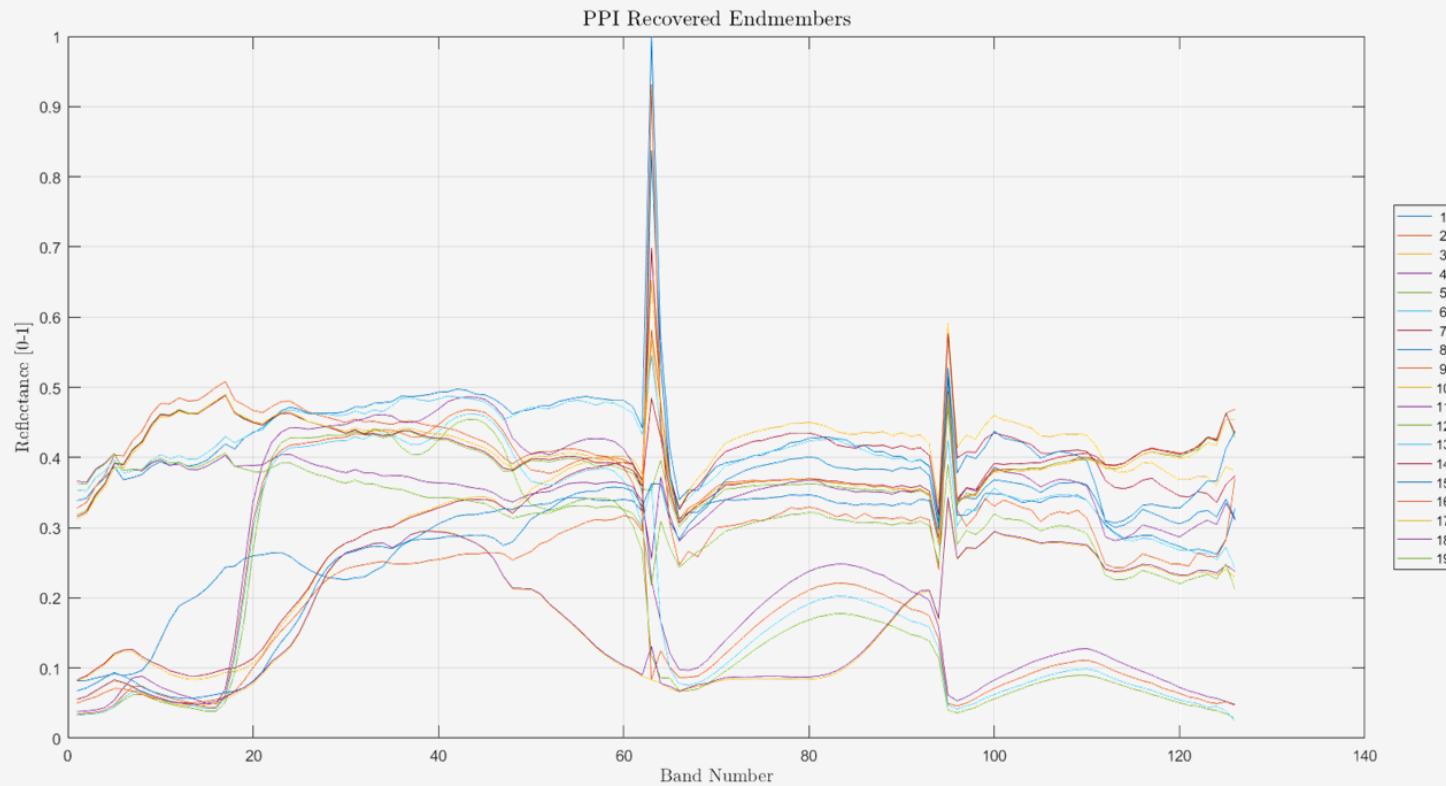
It first generates a set of  $K$  random unit vectors, called skewers, to cover all possible projection directors and then orthogonally projects all data sample vectors on these skewers to find the maximal and minimal orthogonal projections of each skewer.

For each data sample vector, it counts the number of skewers on which its orthogonal projections yield either maximal or minimal projections. This count is referred to as the PPI count, which will be used to determine whether or not a particular data sample vector is an endmember.

# *PPI*

# *Result of* **PPI**

HYPERPPI Performs the pixel purity index (PPI) algorithm  
Performs the pixel purity index algorithm for endmember finding.  
Usage  
`[U] = hyperPpi(M, q, numSkewers)`  
Inputs  
M - 2d matrix of HSI data ( $p \times N$ ) ..... **Cooke City (126\*224000)**  
q - Number of endmembers to find ..... **19**  
numSkewers - Number of "skewer" vectors to project data onto ..... **1000**  
Outputs  
U - Recovered endmembers ( $p \times q$ ) ..... **(126 \* 19)**



# *Result of* *N-Finder*

HYPERNFINDR Performs the N-FINDR (endmember extraction) algorithm

Performs the N-FINDR algorithm to find q endmembers  
and then reduce dimensionality to (q-1).

Usage

[U] = hyperNfinder(M, q)

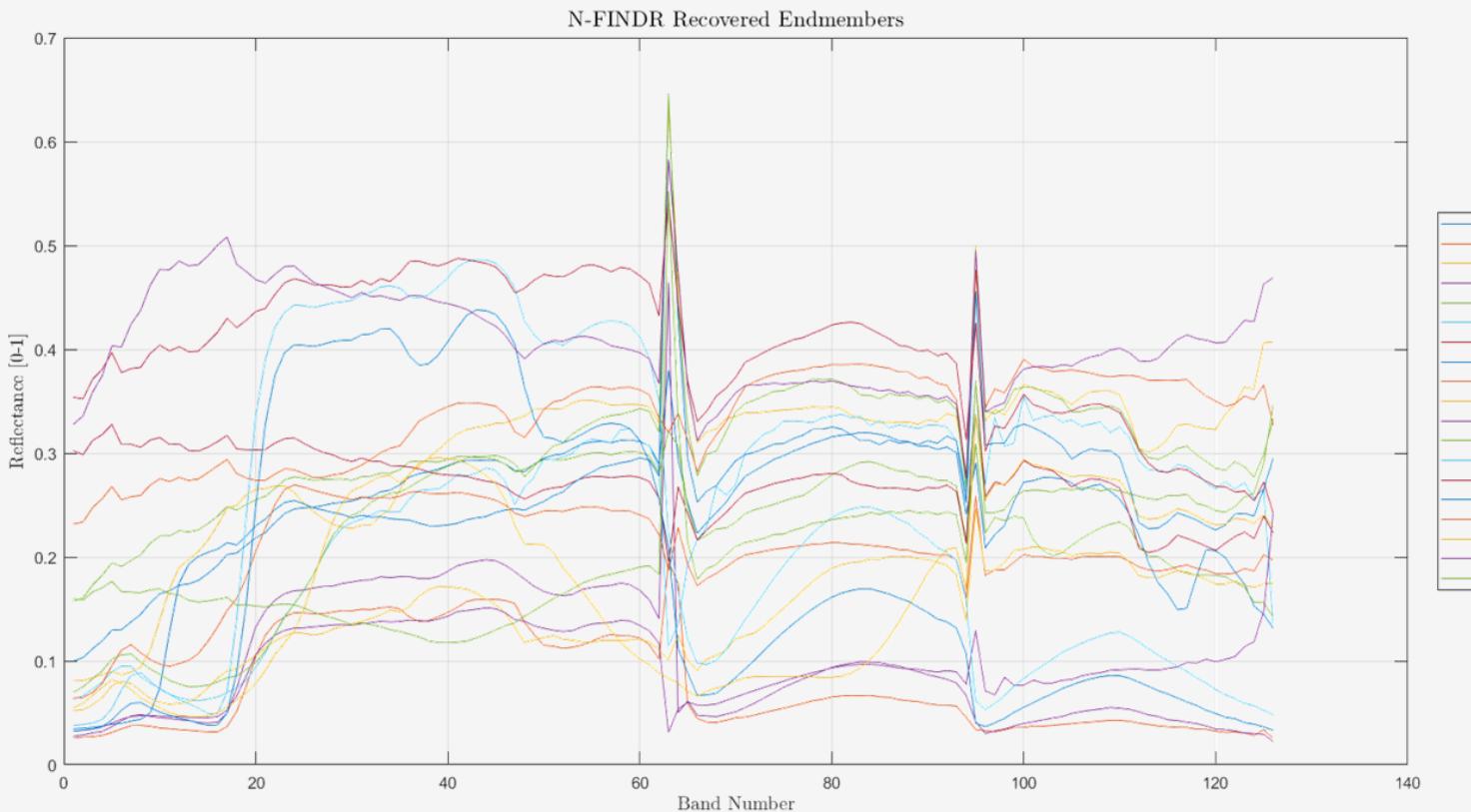
Inputs

M - 2d matrix of HSI data (p x N) ..... **Cooke City (126\*224000)**

q - Number of endmembers to find ..... **19**

Outputs

U - Recovered endmembers (p x q) ..... **(126\*19)**



# *Result of* VCA

HYPERVCA Vertex Component Analysis algorithm

hyperVca performs the vertex component analysis algorithm to find pure pixels in an HSI scene

Usage

```
[ U, indices, snrEstimate ] = hyperVca( M, q )
```

Inputs

M - HSI data as 2D matrix (p x N) ..... **Cooke City (126\*224000)**

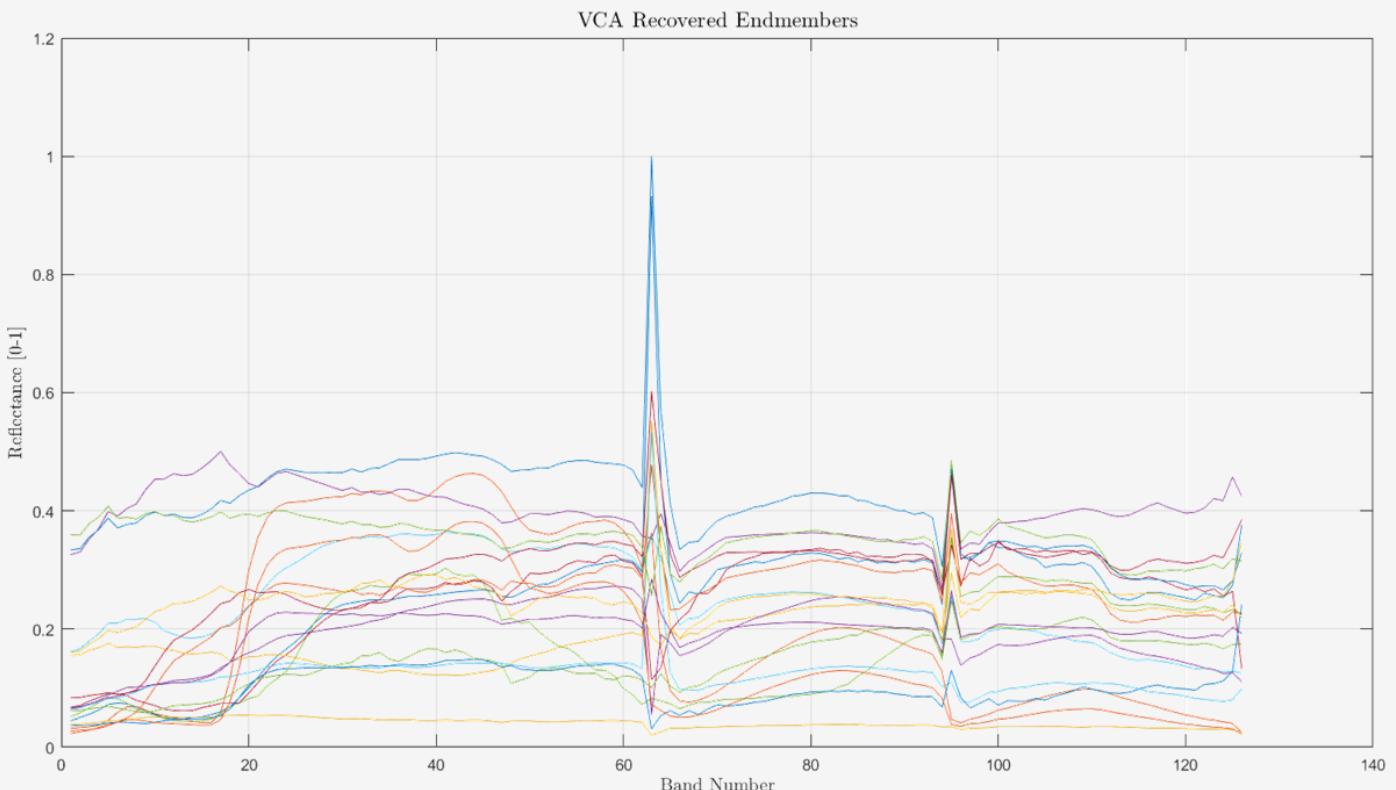
q - Number of endmembers to find ..... **19**

Outputs

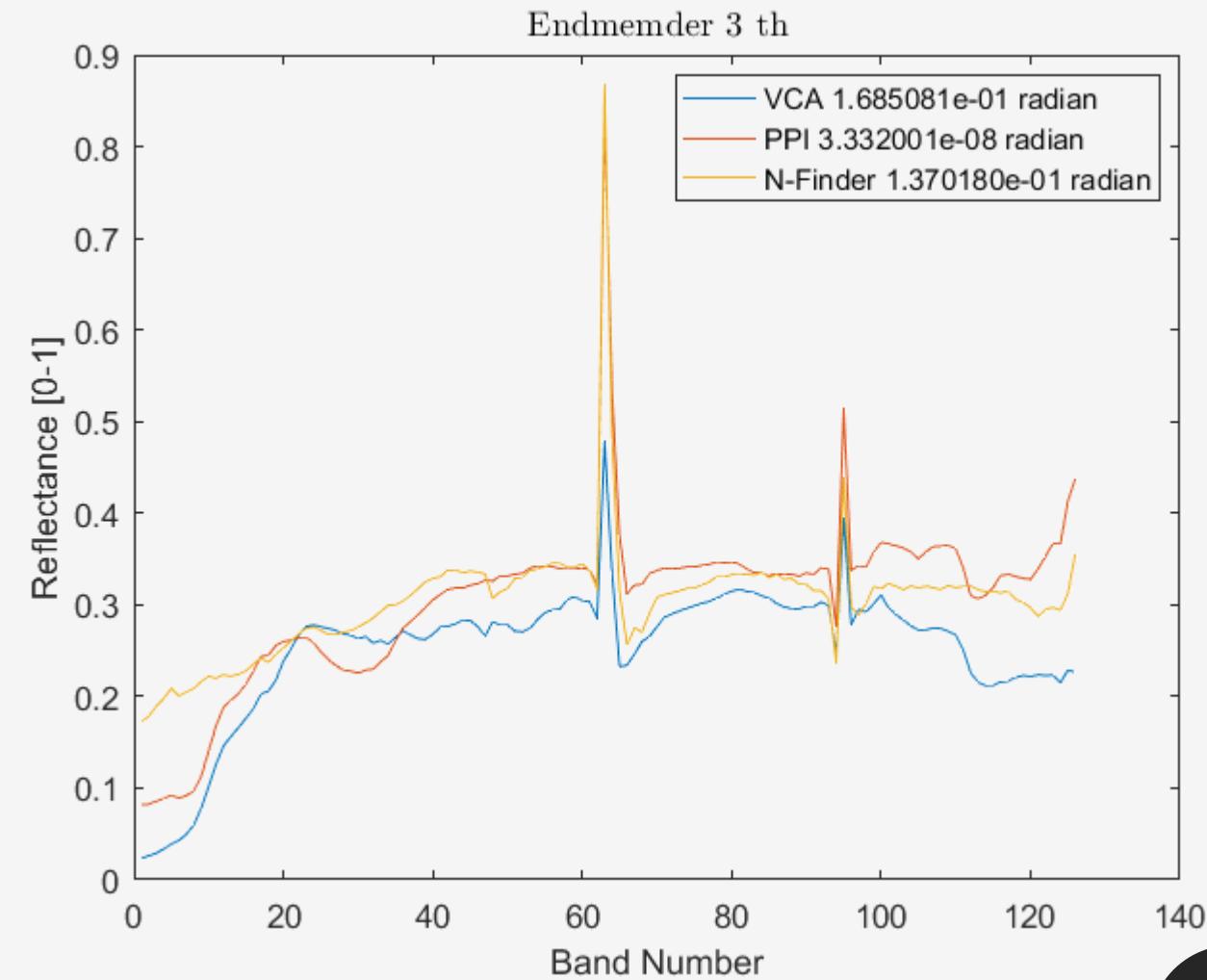
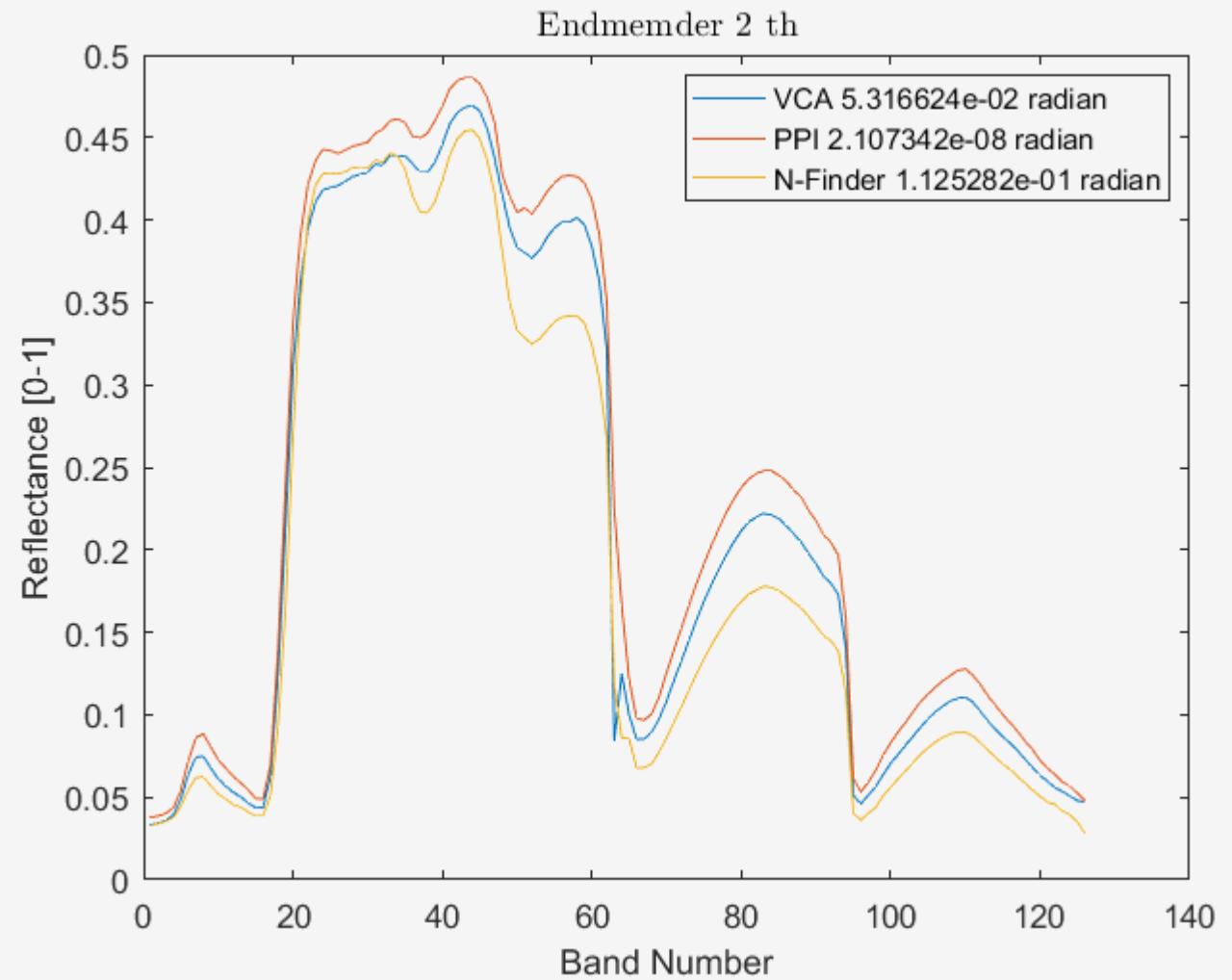
U - Matrix of endmembers (p x q)..... **(126 \* 19 )**

indices - Indices of pure pixels in U ..... **(1 \* 19 )**

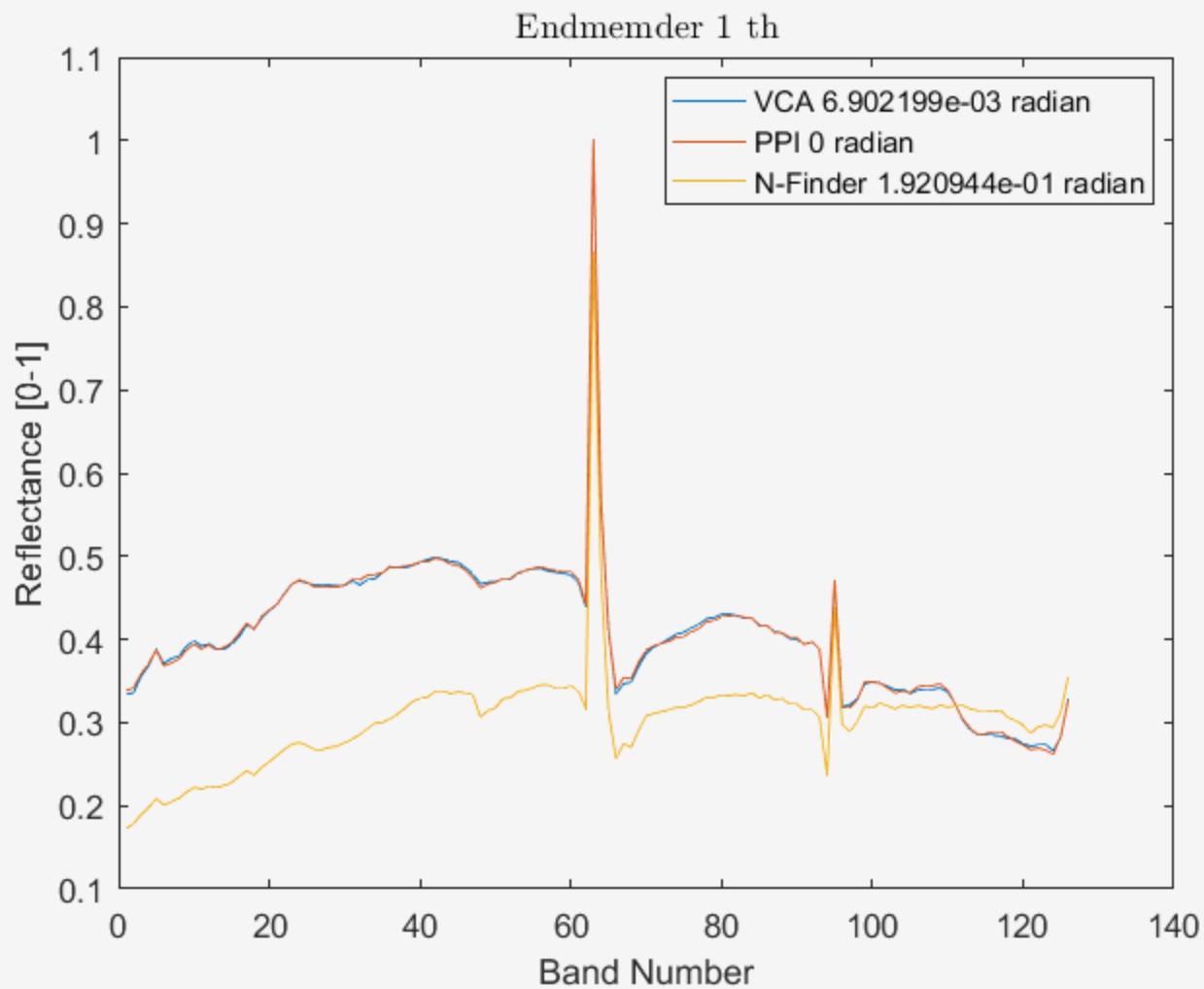
snrEstimate - SNR estimate of data [dB] ..... **46.8222**



# *Comparison signature of endmembers using SAM for Cook City dataset*

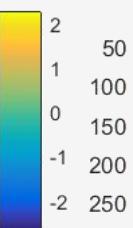
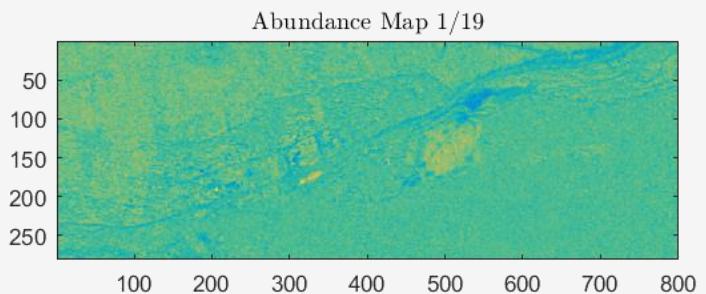


# *Comparison signature of endmembers using SAM for Cook City dataset*

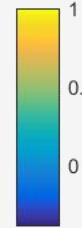
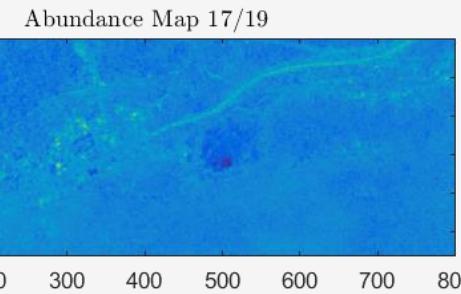


# Abundance estimation

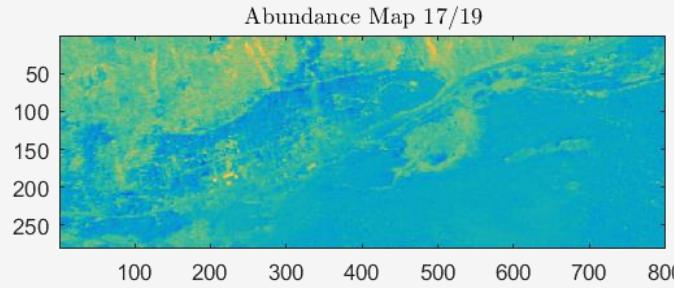
PPI



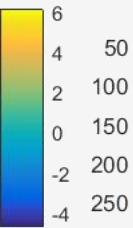
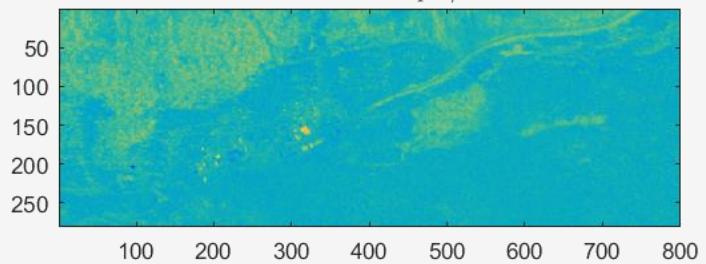
NFINDER



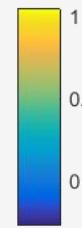
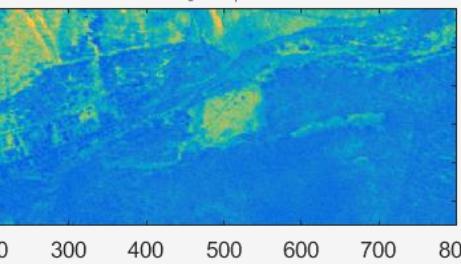
VCA



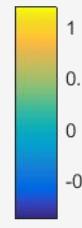
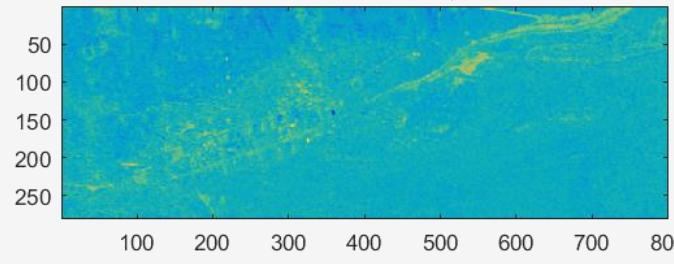
Abundance Map 2/19



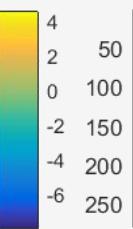
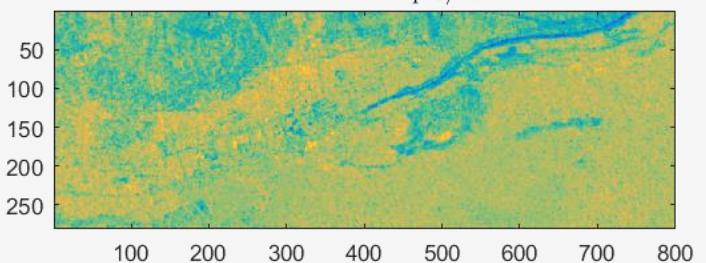
Abundance Map 18/19



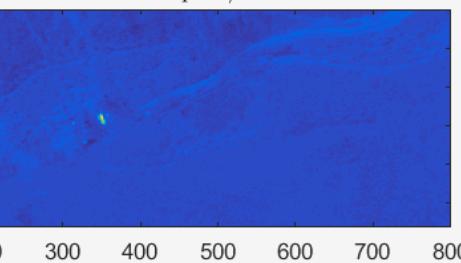
Abundance Map 18/19



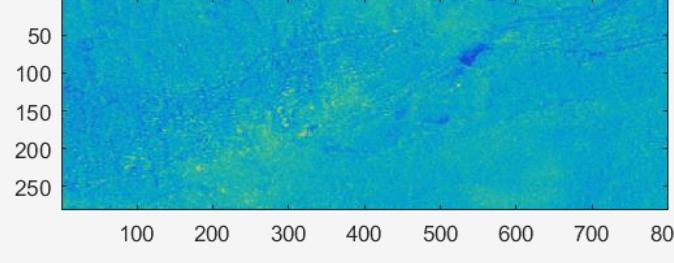
Abundance Map 3/19



Abundance Map 19/19



Abundance Map 19/19



# *Target Detection*

Structured methods for target detection



Constrained Energy  
Minimization  
(CEM)



Adaptive Cosine  
Estimator  
(ACE)



Signed Adaptive  
Cosine Estimator  
(S-ACE)



Matched Filter



Generalized Likelihood  
Ratio Test  
(GLRT)

# *Target Detection*

Unstructured methods for target detection

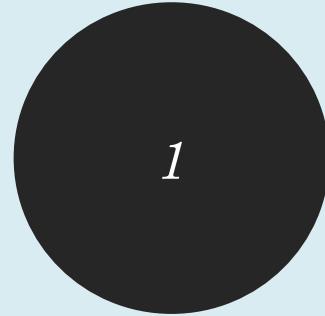


Adaptive Matched Subspace Detector (AMSD)



Orthogonal Subspace Projection (OSP)

# *Threshold Selection*



## Otsu

Otsu's method chooses a threshold that minimizes the intraclass variance of the thresholded black and white pixels.

# *CEM*

## *Constrained Energy Minimization*

- HYPERCEM Performs constrained energy minimization (CEM) algorithm
- Performs the constrained energy minimization algorithm for target detection.

### Usage

[results] = hyperCem(M, target)

### Inputs

M - 2d matrix of HSI data ( $p \times N$ ) → 126\*224000

target - target of interest ( $p \times 1$ ) → 126\*1

### Outputs

results - vector of detector output ( $N \times 1$ ) → 224000\*1

# ACE

## Adaptive Cosine Estimator

- HYPERACE Performs the adaptive cosin/coherent estimator algorithm
- Performs the adaptive cosin/coherent estimator algorithm for target detection.

### Usage

[results] = hyperAce(M, S)

### Inputs

M - 2d matrix of HSI data ( $p \times N$ ) → 126\*224000

S - 2d matrix of target endmembers ( $p \times 1$ ) → 126\*1

### Outputs

results - vector of detector output ( $N \times 1$ ) → 224000\*1

# *GLRT*

## Generalized Likelihood Ratio Test

- HYPERGLRT Performs the generalized likelihood test ratio algorithm
- Performs the generalized likelihood test ratio algorithm for target detection.

### Usage

[results] = hyperGlrt(M, U, target)

### Inputs

M - 2d matrix of HSI data ( $p \times N$ ) → 126\*224000

t - target of interest ( $p \times 1$ ) → 126\*1

### Outputs

results - vector of detector output ( $N \times 1$ ) → 224000\*1

# S-ACE

## Signed Adaptive Cosine Estimator (S-ACE)

4 of 5 Structured Method

- HYPERACE Performs the adaptive cosin/coherent estimator algorithm
- Performs the adaptive cosin/coherent estimator algorithm for target detection.

### Usage

[results] = hyperSignedAce(M, S)

### Inputs

M - 2d matrix of HSI data ( $p \times N$ ) → 126\*224000

S - target of interest ( $p \times 1$ ) → 126\*1

### Outputs

results - vector of detector output ( $N \times 1$ ) → 224000\*1

# *MF*

## Matched Filter

- HYPERACE Performs Matched Filter estimator algorithm
- Performs the estimator algorithm for target detection.

### Usage

[results] = hyperMatchedFilter(M, S)

### Inputs

M - 2d matrix of HSI data ( $p \times N$ ) → 126\*224000

S - target of interest ( $p \times 1$ ) → 126\*1

### Outputs

results - vector of detector output ( $N \times 1$ ) → 224000\*1

# OSP

## Orthogonal Subspace Projection

- HYPEROSP Performs the orthogonal subspace projection (OSP) algorithm
- Performs the orthogonal subspace projection algorithm for target detection.

### Usage

```
[results] = hyperOsp(M, U, target)
```

### Inputs

M - 2d matrix of HSI data ( $p \times N$ )

U - 2d matrix of background endmembers ( $p \times q$ )

target - target of interest ( $p \times 1$ )

### Outputs

results - vector of detector output ( $N \times 1$ )

# AMSD

## Adaptive Matched Subspace Detector

2 of 2 Unstructured Method

- HYPERAMSD Adaptive matched subspace detector (AMSD) algorithm
- Performs the adaptive matched subspace detector (AMSD) algorithm for target detection

### Usage

```
[results] = hyperAmsd(M, U, target)
```

### Inputs

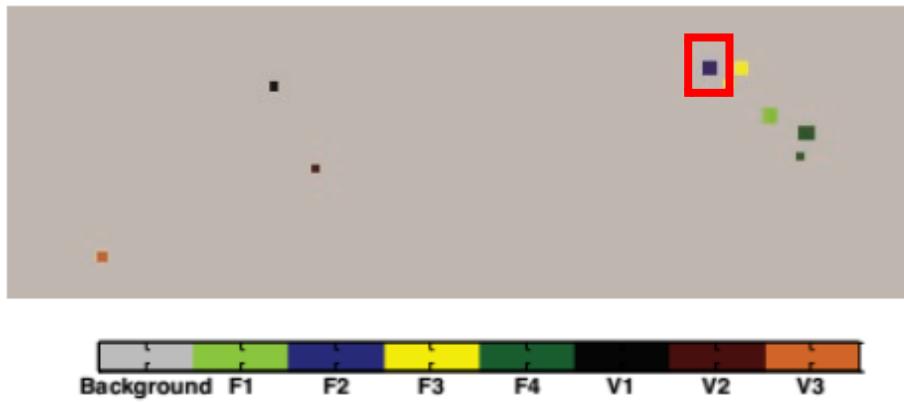
M - 2d matrix of HSI data ( $p \times N$ )

B - 2d matrix of background endmembers ( $p \times q$ )

target - target of interest ( $p \times 1$ )

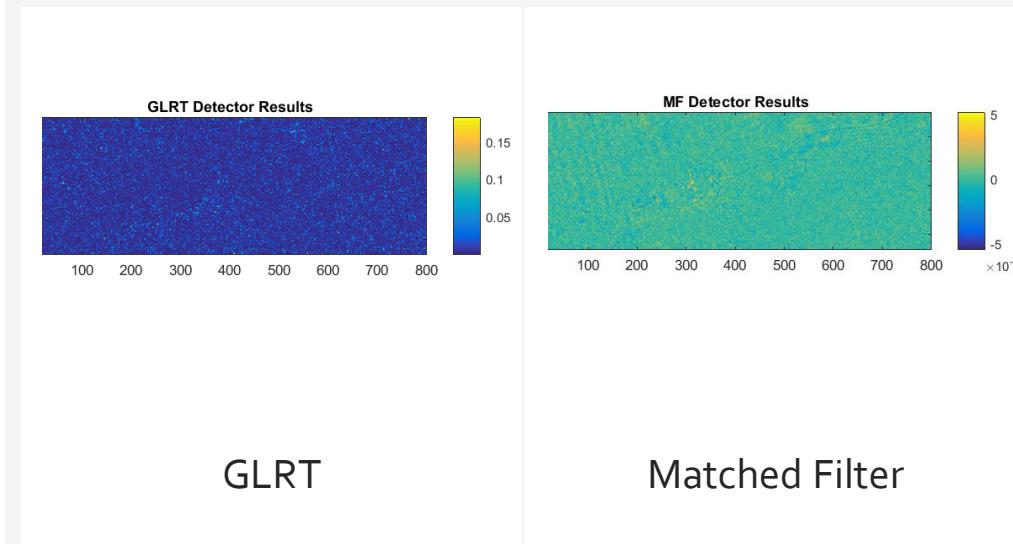
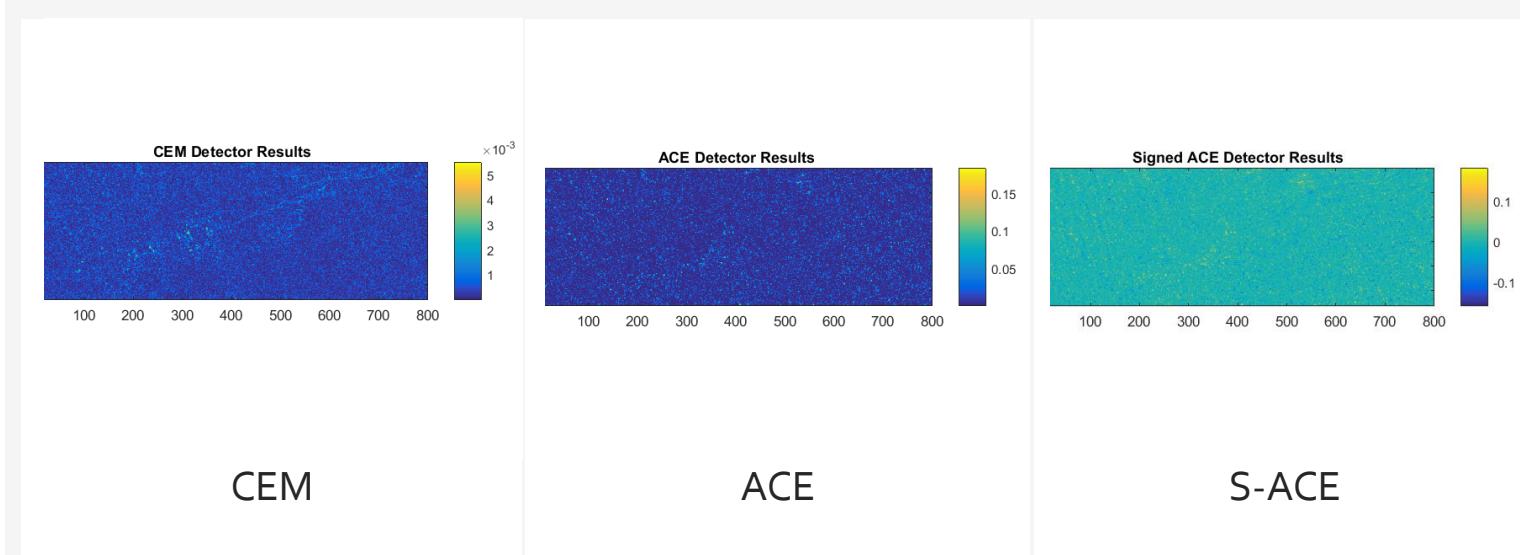
### Outputs

results - vector of detector output ( $N \times 1$ )

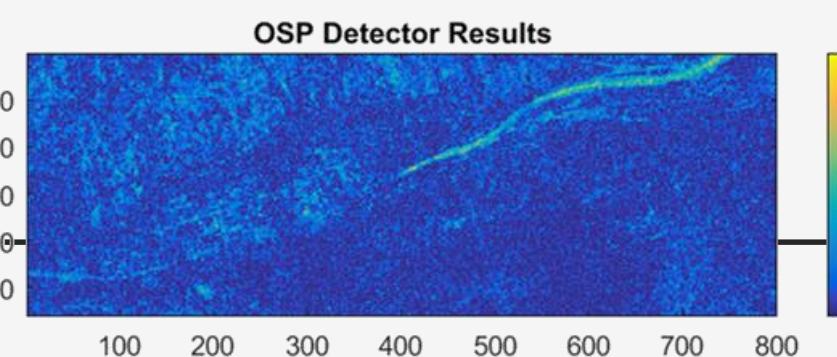
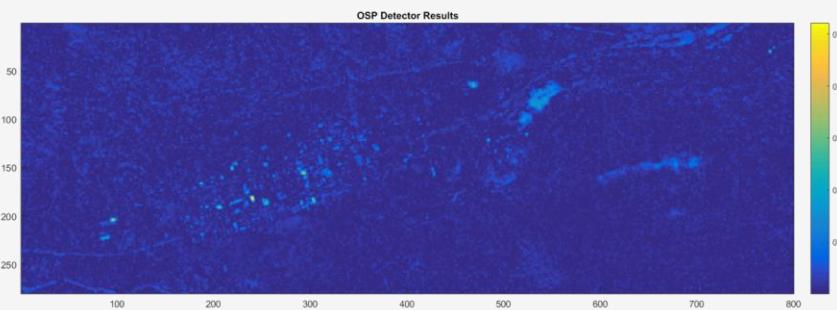
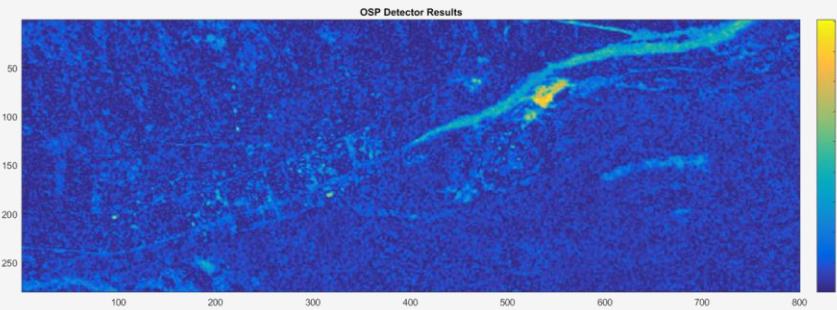
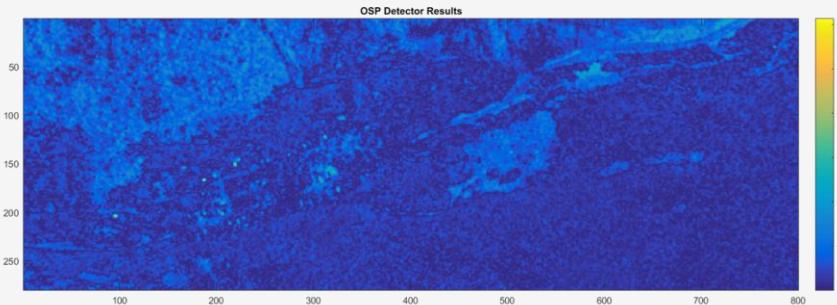


# *Fabric 2*

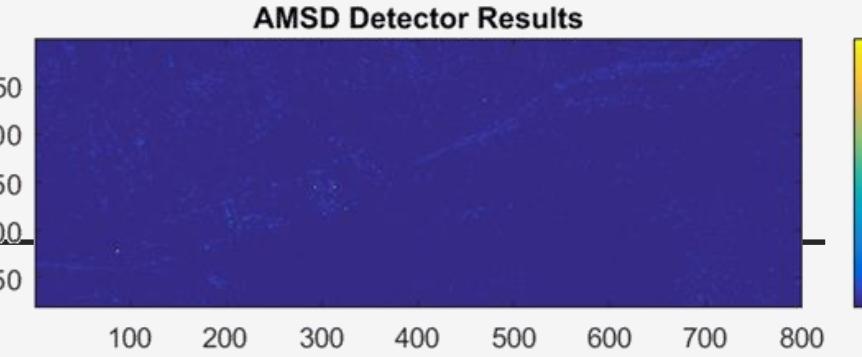
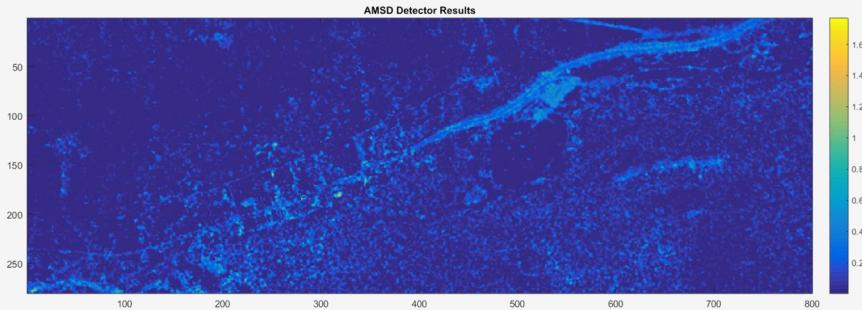
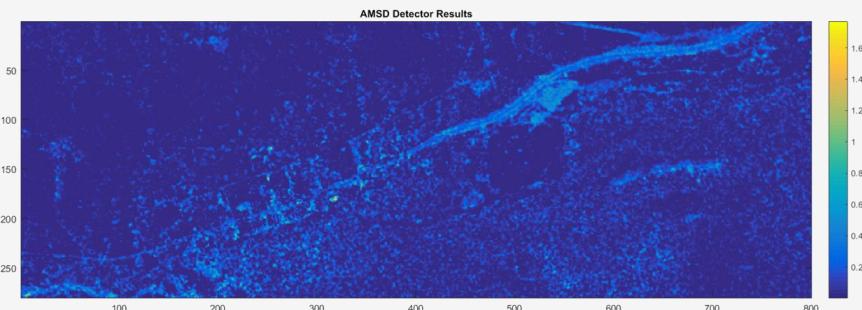
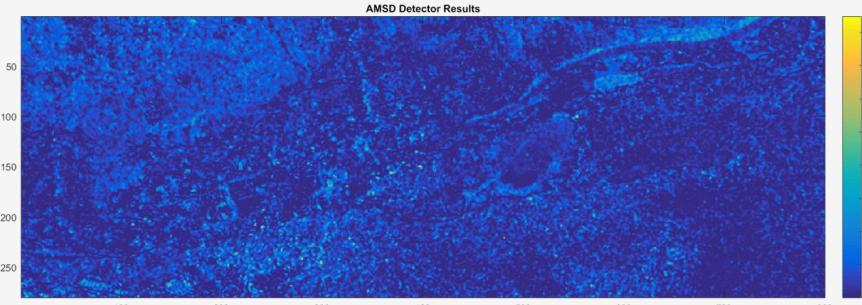
Result of Structured Method  
Detector Map



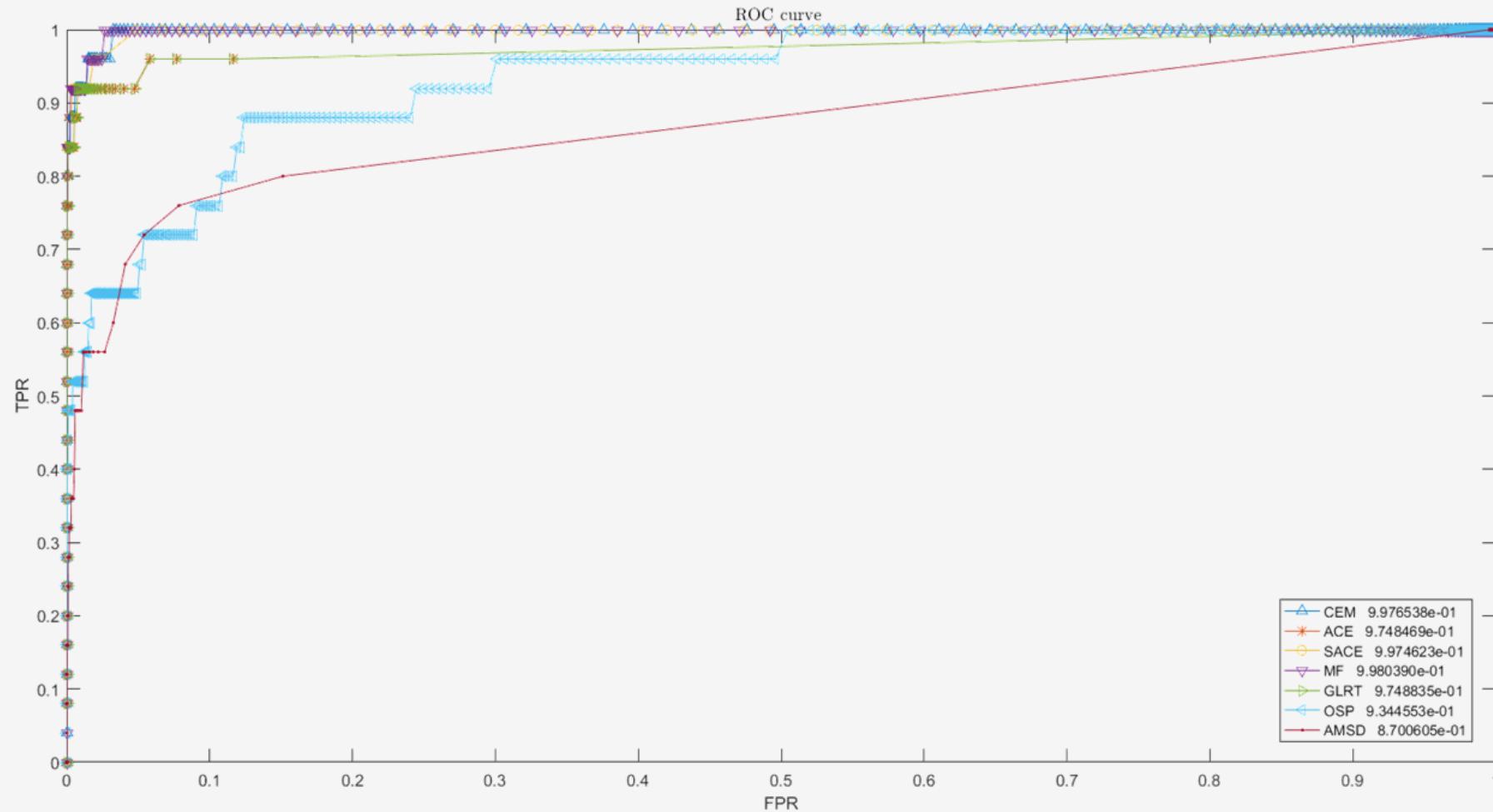
# OSP



# AMSD

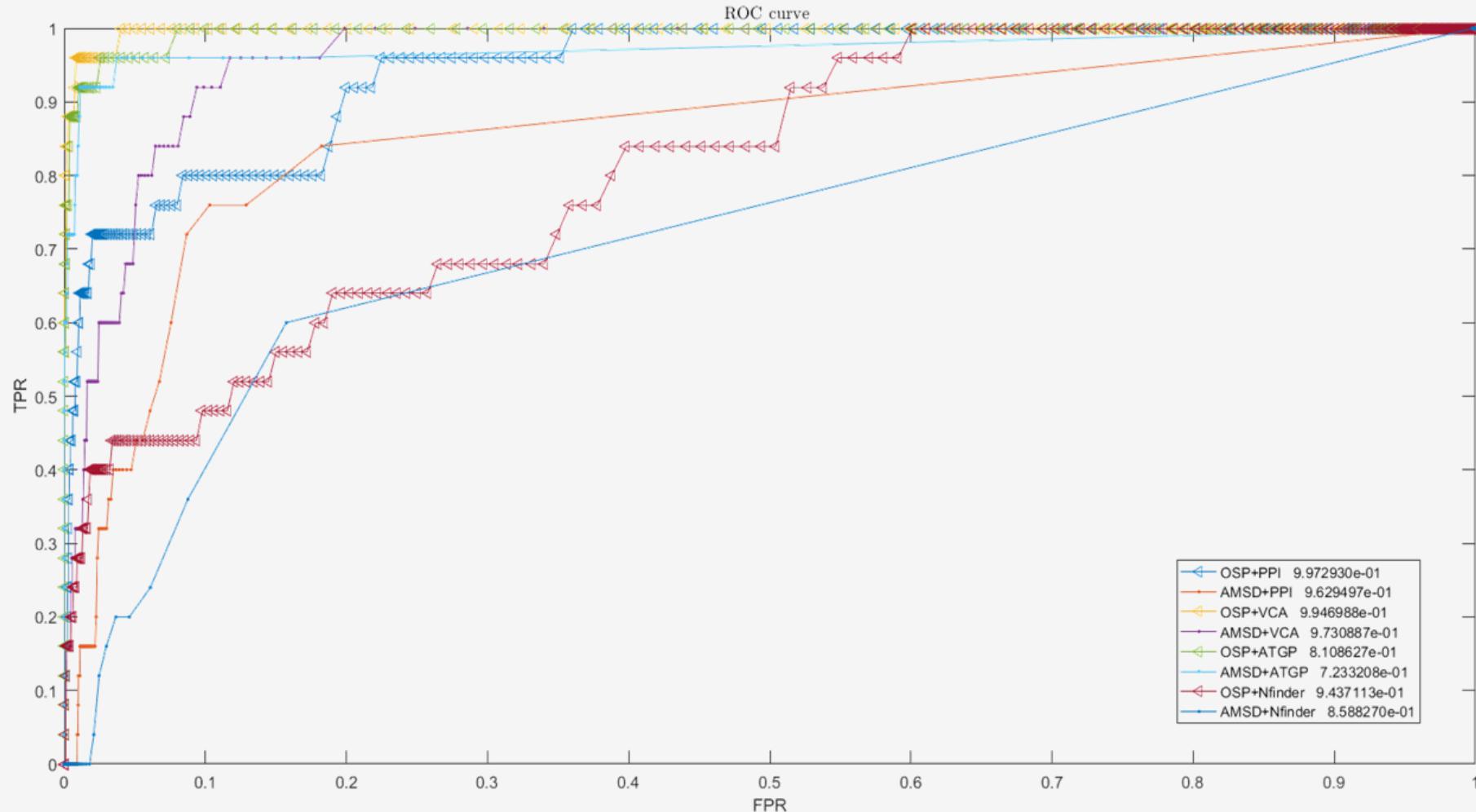


# Fabric 2



- ROC curve of Fabric 2 data for 1000 different thresholds
- For Fabric 2 data structured methods have higher AUC than unstructured methods.

# Fabric 2



- ROC curve of Fabric 2 data for 1000 different thresholds
- The AUC of each curve calculated

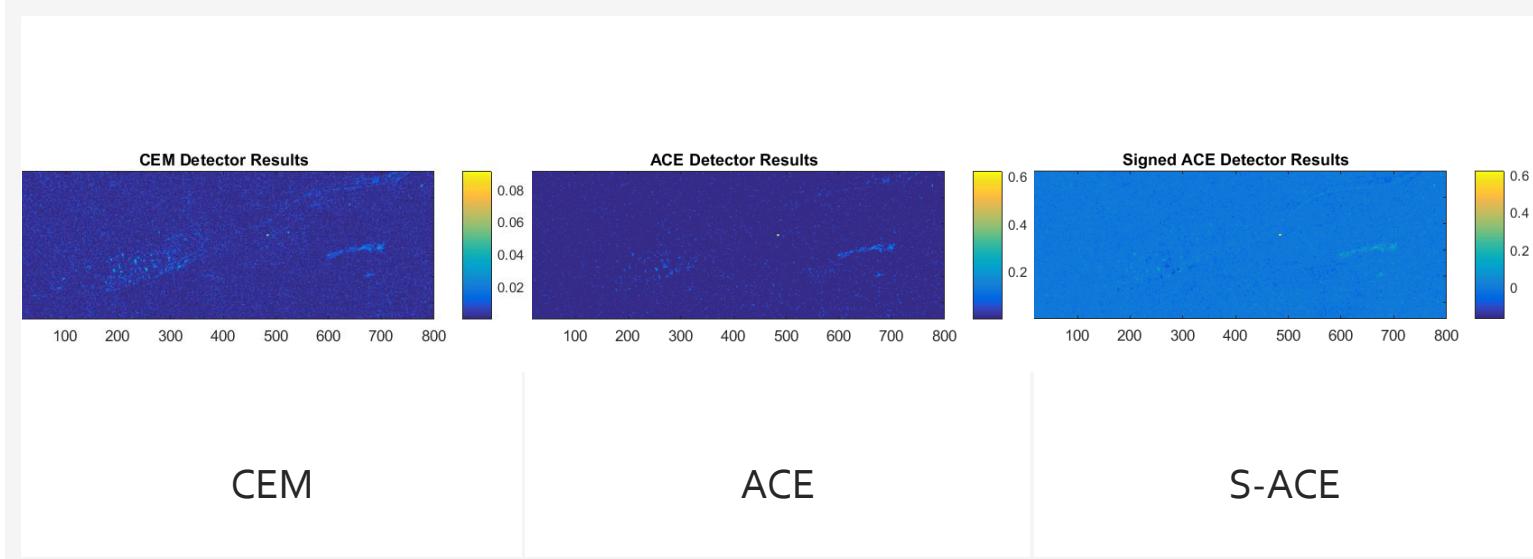
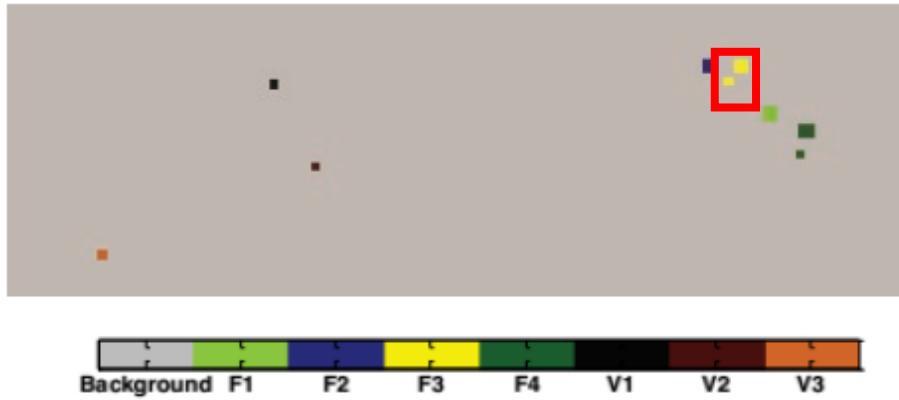
Method	AUC
OSP+PPI	0.8279
AMSD+PPI	0.8271
OSP+VCA	0.9946
AMSD+VCA	0.9730
OSP+ATGP	0.8108
AMSD+ATGP	0.7233
OSP+Nfinder	0.9228
AMSD+Nfinder	0.7937

# Fabric 2

Method	AUC	ACC	PPV* $10^{-3}$
OSP+PPI	0.8279	0.5299	0.1163
AMSD+PPI	0.8271	0.9931	0.1116
OSP+VCA	<b>0.9946</b>	0.6638	24.09
AMSD+VCA	<b>0.9730</b>	<b>0.9974</b>	<b>100</b>
OSP+ATGP	0.8108	0.6227	0.4055
AMSD+ATGP	0.7233	0.2427	0.1116
OSP+Nfinder	0.9228	0.6292	0.4630
AMSD+Nfinder	0.7937	0.9965	0.1116

Method	AUC	ACC	PPV
CEM	0.998	0.6806	1
<b>ACE</b>	<b>0.975</b>	<b>0.9982</b>	<b>1</b>
SACE	0.998	0.8197	1
MF	0.999	0.6821	1
<b>GLRT</b>	<b>0.975</b>	<b>0.9982</b>	<b>1</b>
OSP	0.935	0.6227	0.4055
AMSD	0.871	0.2427	0.1116

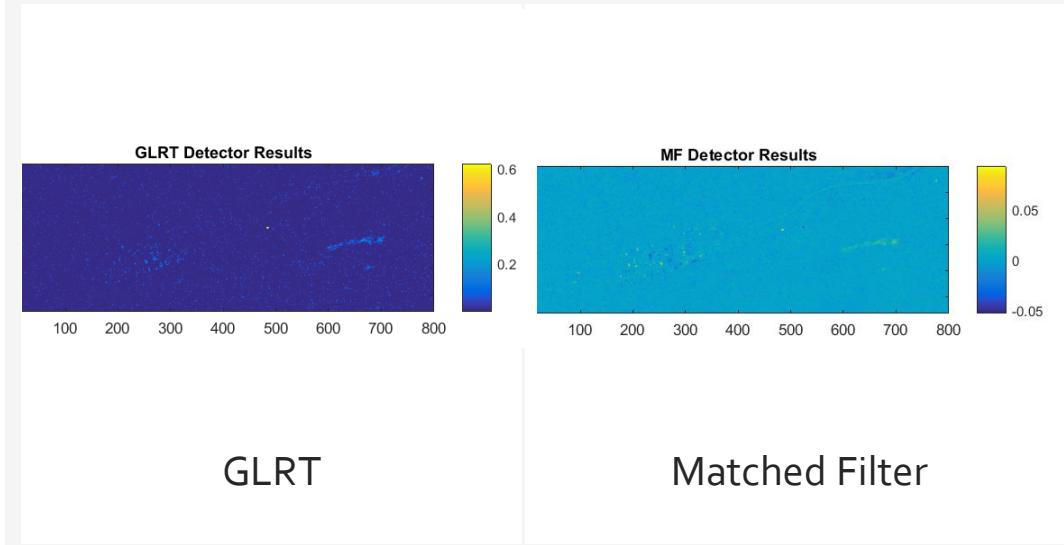
- For FABRIC<sub>3</sub> data, it is observed that the AUC parameter for the OSP method was the highest when the VCA approach was used. In general, the area under the ROC curve for the OSP method is higher, However the overall accuracy of the AMSD method is higher, and therefore the third parameter, PPV, represents the optimal method, the OSP + VCA method.
- In second table, In Unstructured method, first of all estimate number of endmembers with HFC , that is 33 , then calculate matrix of background endmembers with ATGP and finally use AMSD and OSP to target detection.



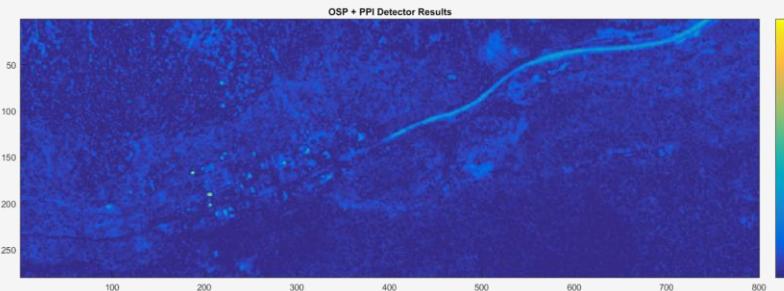
# *Fabric 3*

# Result of Structured Method

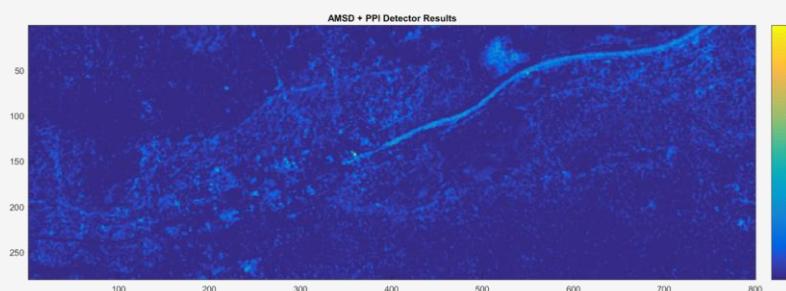
## Detector Map



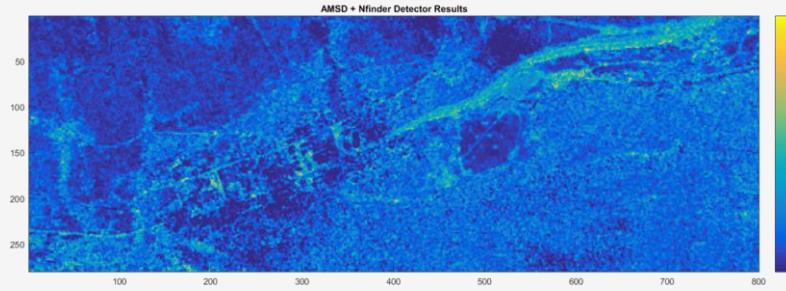
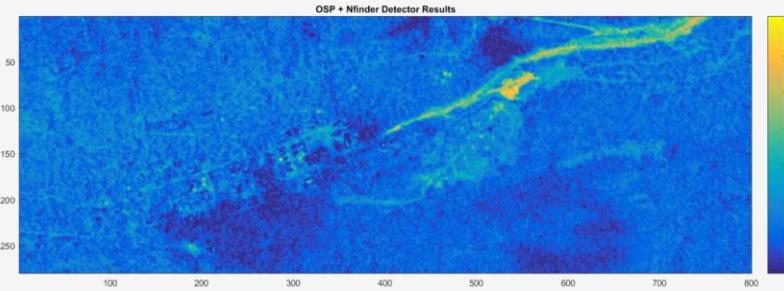
OSP



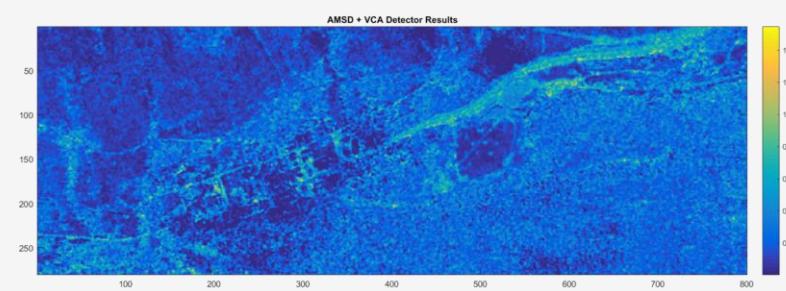
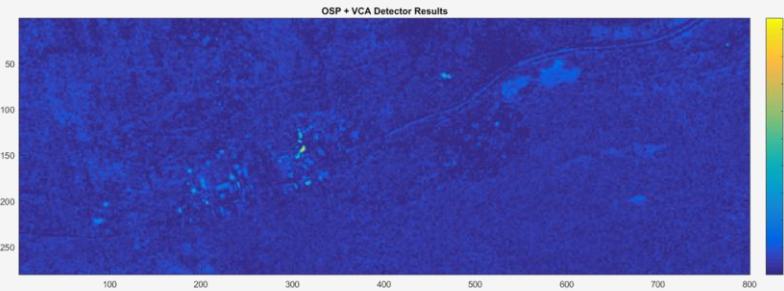
AMSD



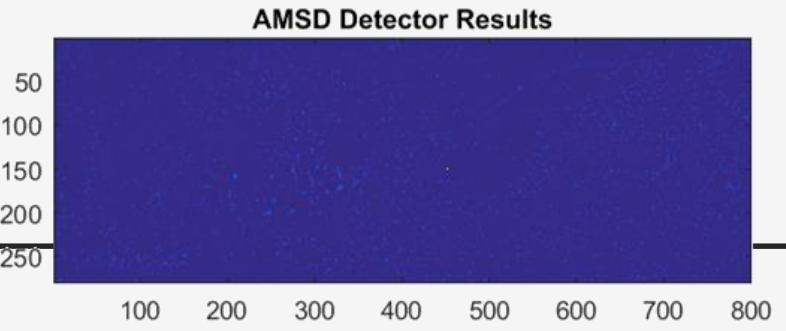
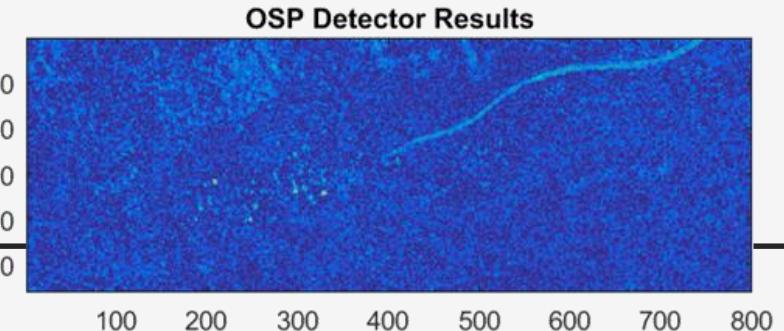
NFINDER



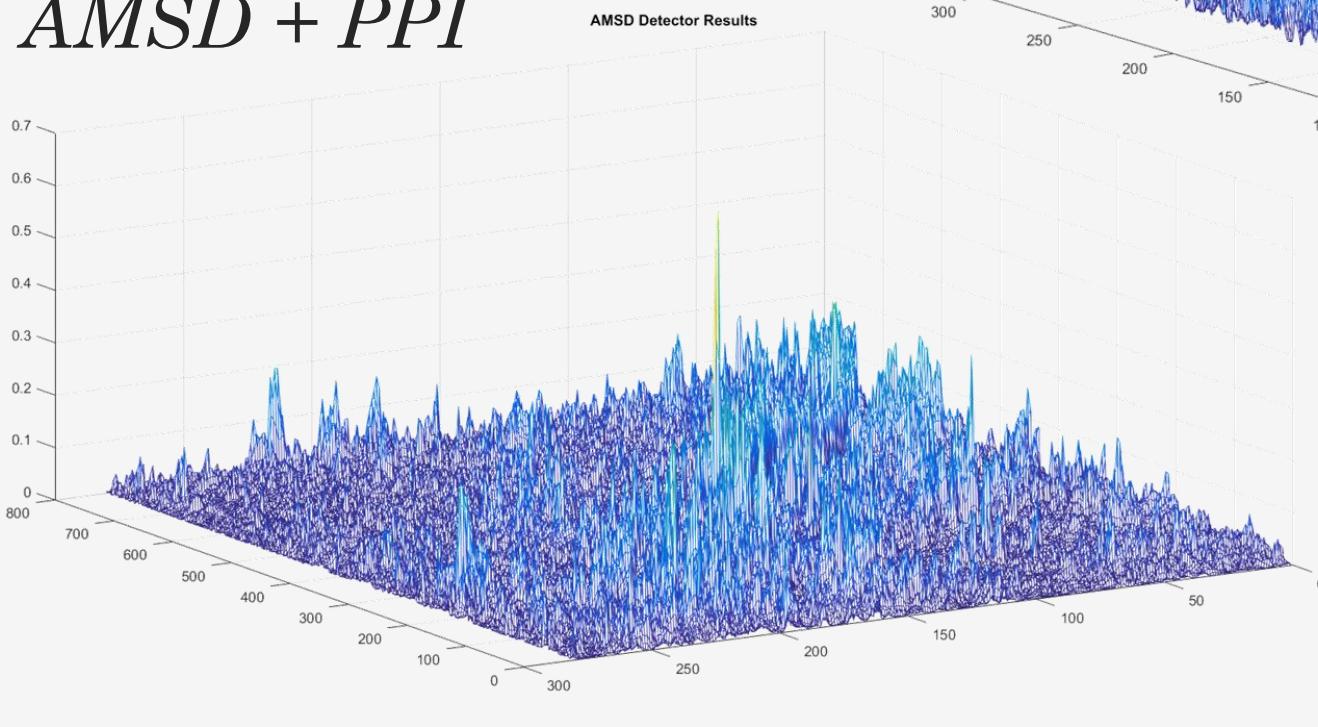
VCA



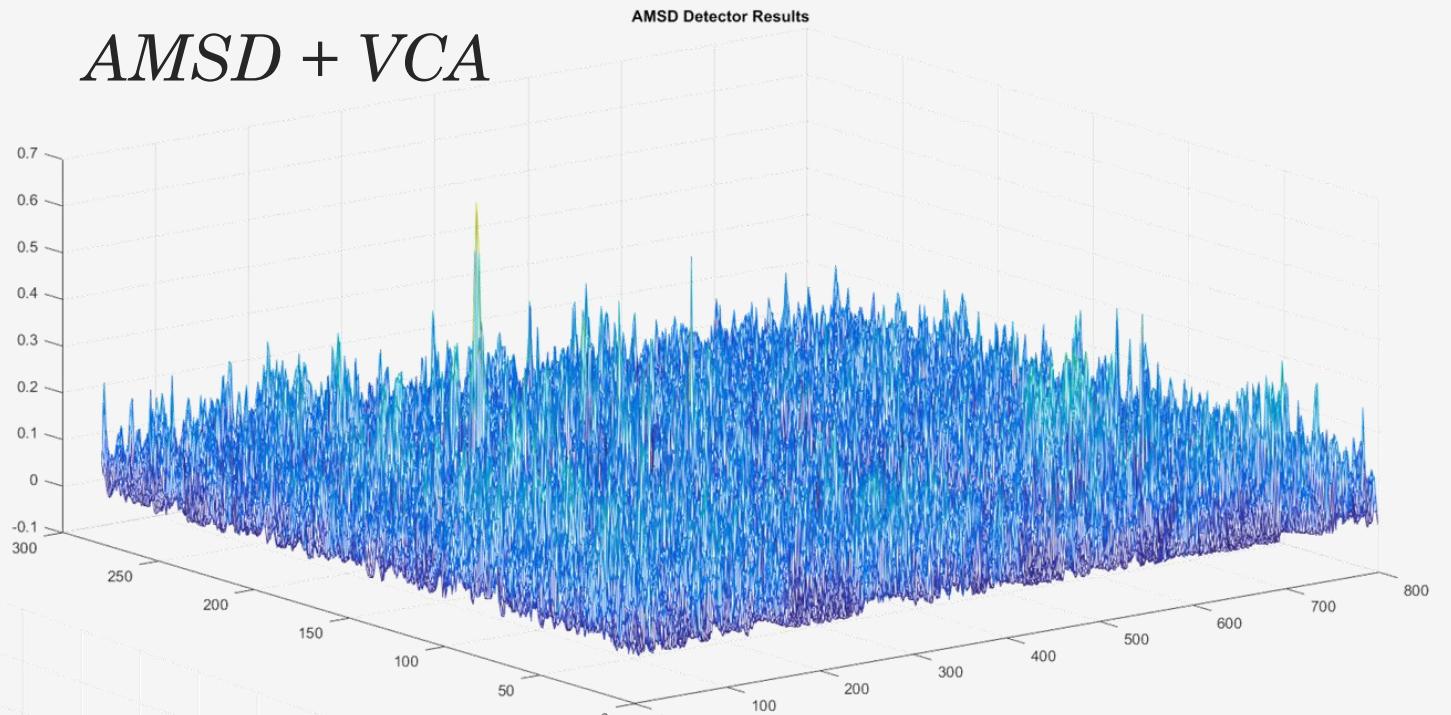
ATGP



## *AMSD + PPI*

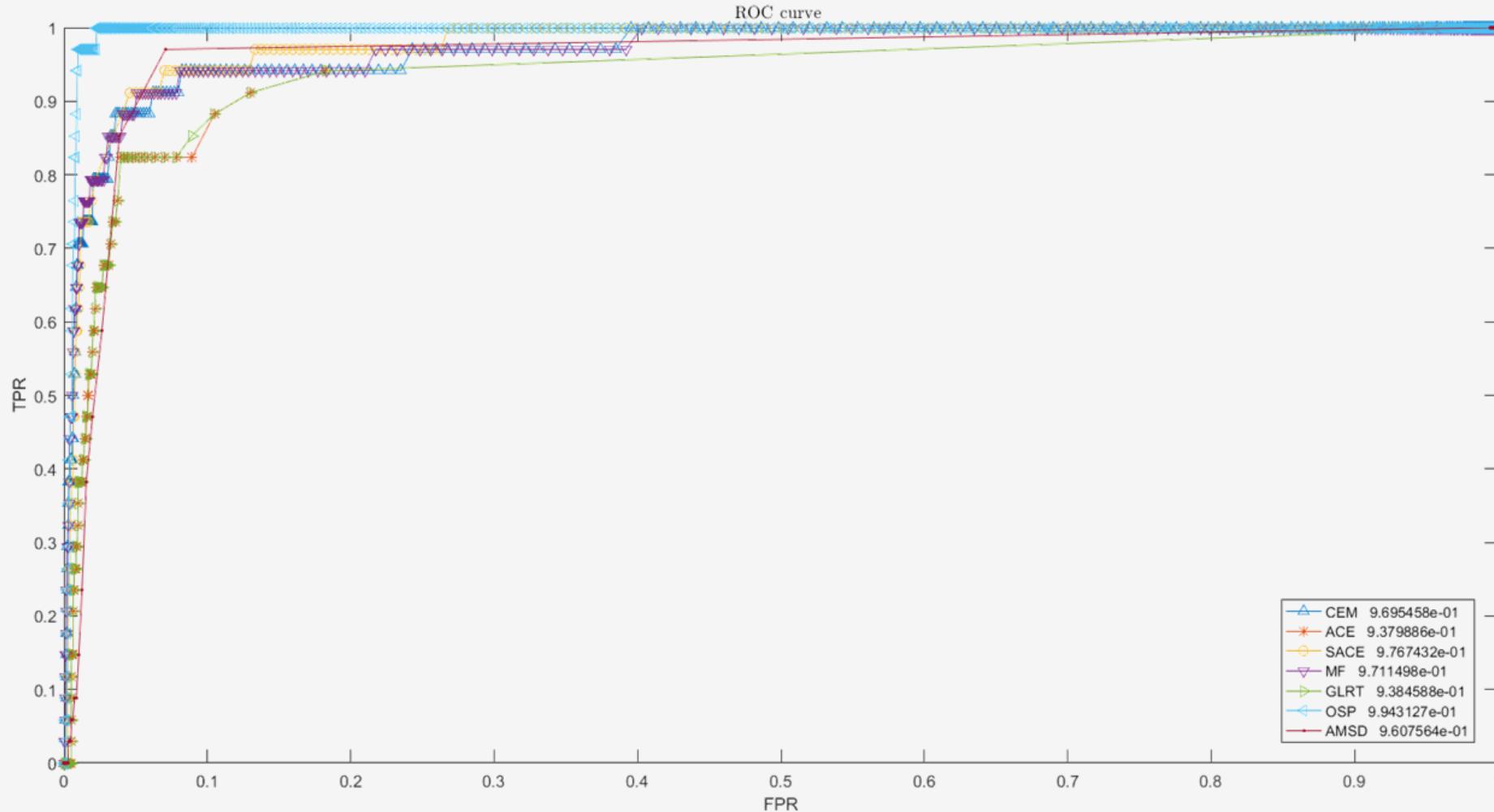


## *AMSD + VCA*



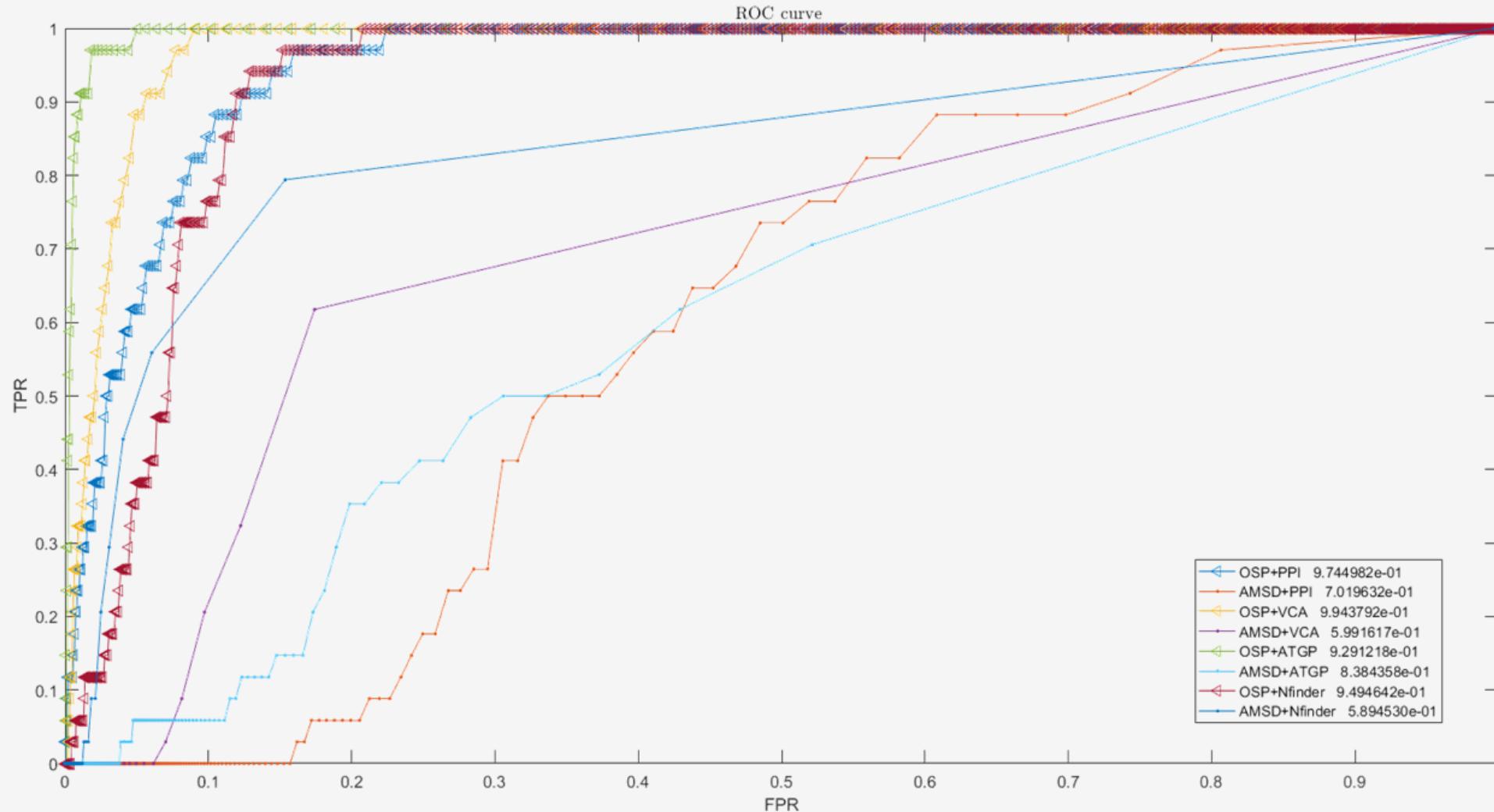
- Result of Unstructured Method
- Detector Map

# Fabric 3



- ROC curve of Fabric 3 data for 1000 different thresholds
- The AUC of each curve calculated

# Fabric 3



- ROC curve of Fabric 3 data for 1000 different thresholds
- AUC for OSP is higher than AMSD method

# Fabric 3

Method	AUC	ACC	PPV* $10^{-3}$
OSP+PPI	<u>0.9744</u>	0.7278	0.2217
AMSD+PPI	0.7019	<u>0.9973</u>	0.1517
OSP+VCA	<b>0.9943</b>	<b>0.7307</b>	<b>0.9185</b>
AMSD+VCA	0.5991	<u>0.9890</u>	0.1517
OSP+ATGP	<u>0.9291</u>	0.5822	0.1716
AMSD+ATGP	0.8384	0.2211	0.1517
OSP+Nfinder	<u>0.9494</u>	0.6369	0.2783
AMSD+Nfinder	0.5894	<u>0.9738</u>	0.1517

Method	AUC	ACC	PPV* $10^{-3}$
CEM	0.970	0.5677	0.5795
ACE	<b>0.938</b>	<b>0.9964</b>	<b>0.2292</b>
SACE	0.977	0.6325	0.4180
MF	0.972	0.5763	0.6742
GLRT	<b>0.939</b>	<b>0.9964</b>	<b>0.2298</b>
OSP	<b>0.995</b>	0.5822	0.1716
AMSD	0.961	0.2211	0.1517

- For FABRIC3 data, it is observed that the AUC parameter for the OSP method was the highest when the VCA approach was used. In general, the area under the ROC curve for the OSP method is higher, However the overall accuracy of the AMSD method is higher, and therefore the third parameter, PPV, represents the optimal method, the OSP + VCA method.and as you on detector maps OSP+Nfinder has good results.

# *Result of OTSU Threshold Selection*

Method	Fabric 2	Fabric 3	Vehicle 1
CEM	0.0028	0.0035	0.0032
ACE	0.0182	0.0183	0.0150
S-ACE	0.0166	0.0155	0.0122
MF	0.0027	0.0035	0.0032
GLRT	0.0180	0.0181	0.0149
OSP	0.0064	0.0011	0.0068
AMSD	0.0783	0.0648	0.0903
OSP+PPI	0.0103	0.0019	0.0078
AMSD+PPI	0.1611	0.0404	0.0565
OSP+Nfinder	0.0329	0.0029	0.0260
AMSD+Nfinder	0.1561	0.2872	0.1648
OSP+VCA	0.0086	0.0085	0.0312
AMSD+VCA	0.1258	0.0720	0.1628

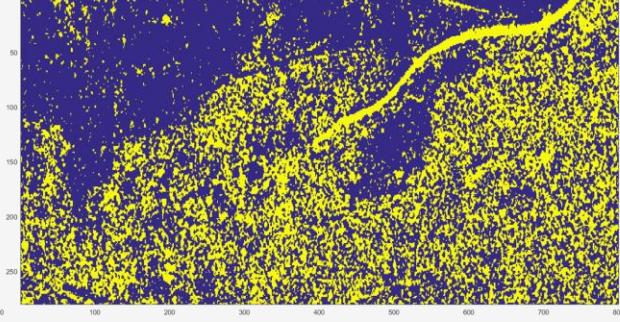
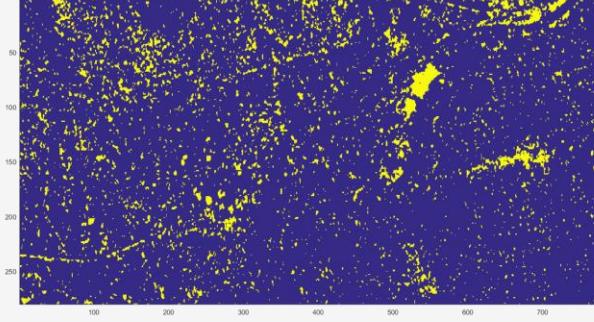
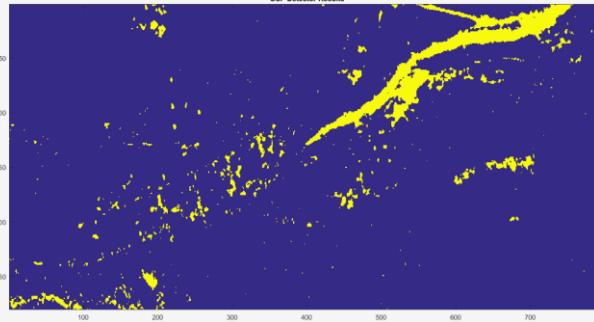
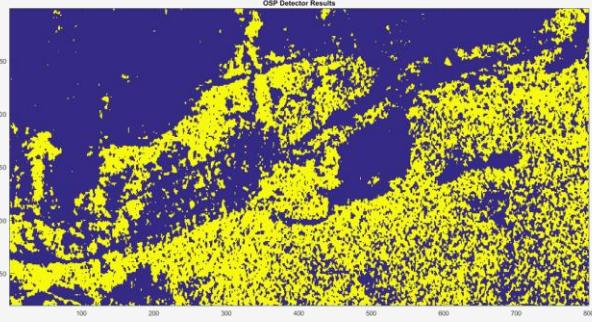
PPI

NFINDER

VCA

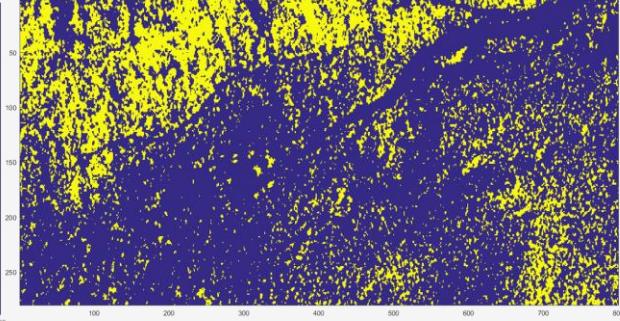
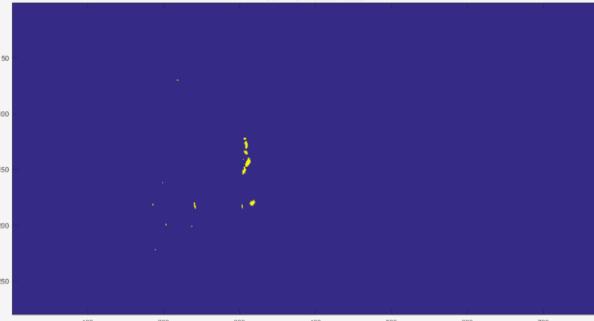
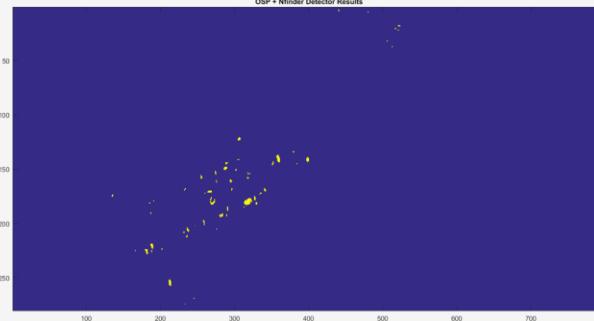
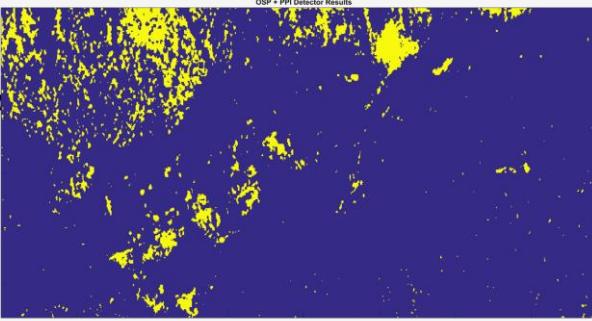
ATGP

Fabric 2



$$T = 0.0064$$

Fabric 3



$$T = 0.0011$$

## *Threshold Selection Result on OSP Method*

- This algorithm seems to work optimistically or because the amount of target data is small, this algorithm has low accuracy

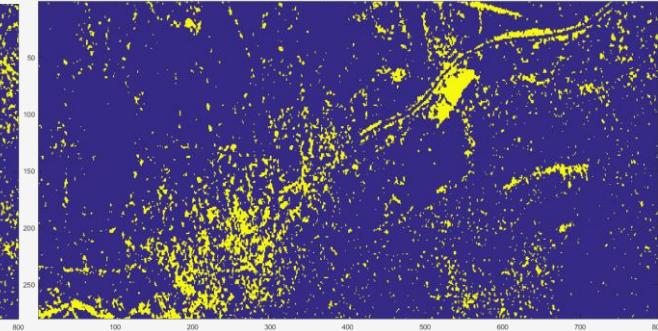
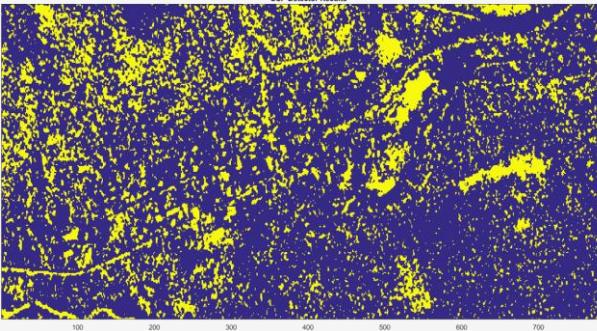
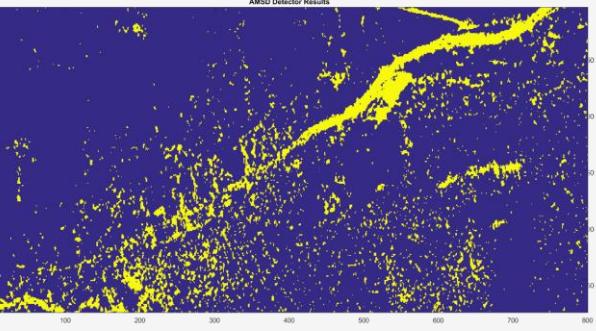
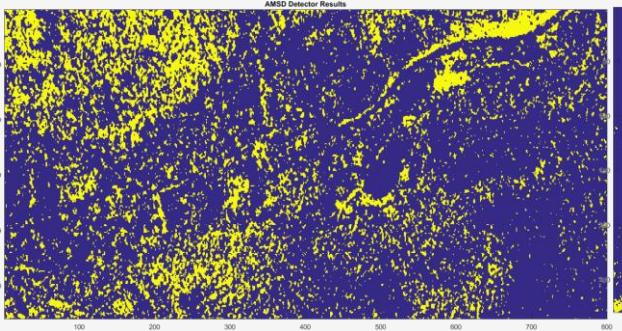
PPI

NFINDER

VCA

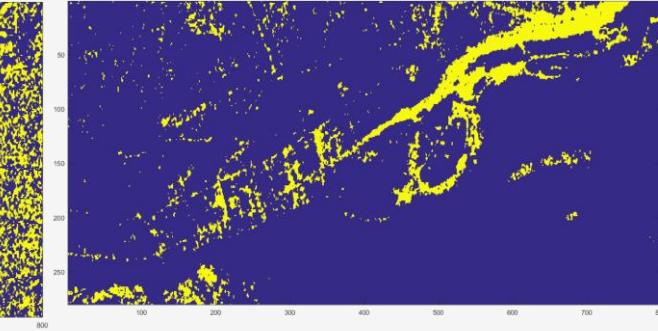
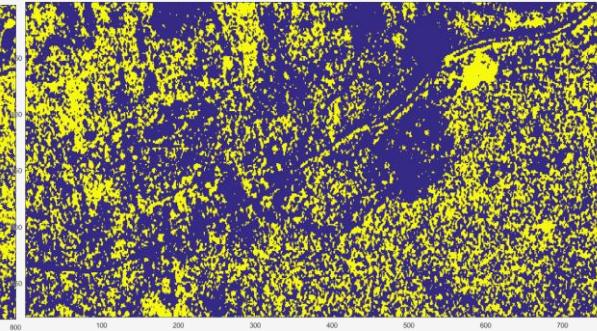
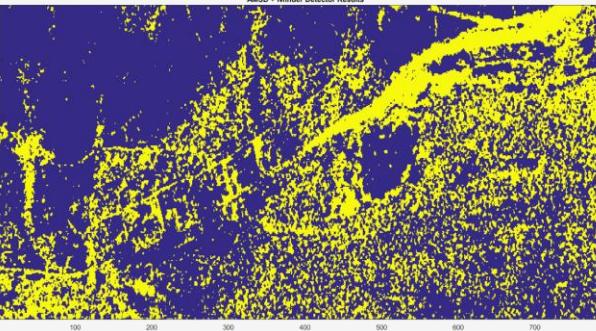
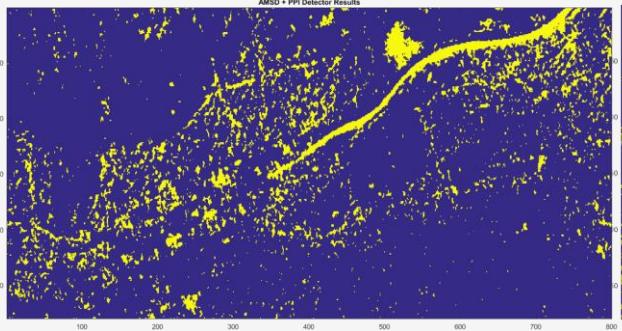
ATGP

Fabric 2



$$T = 0.0064$$

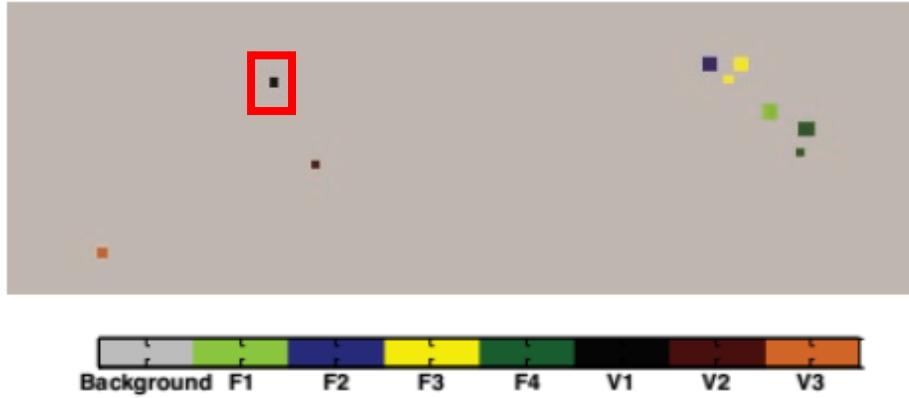
Fabric 3



$$T = 0.0011$$

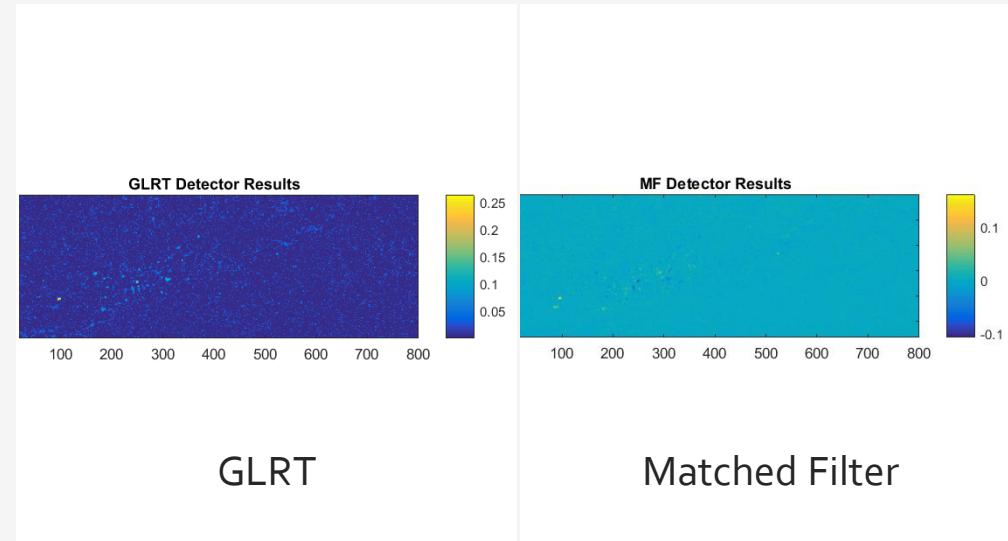
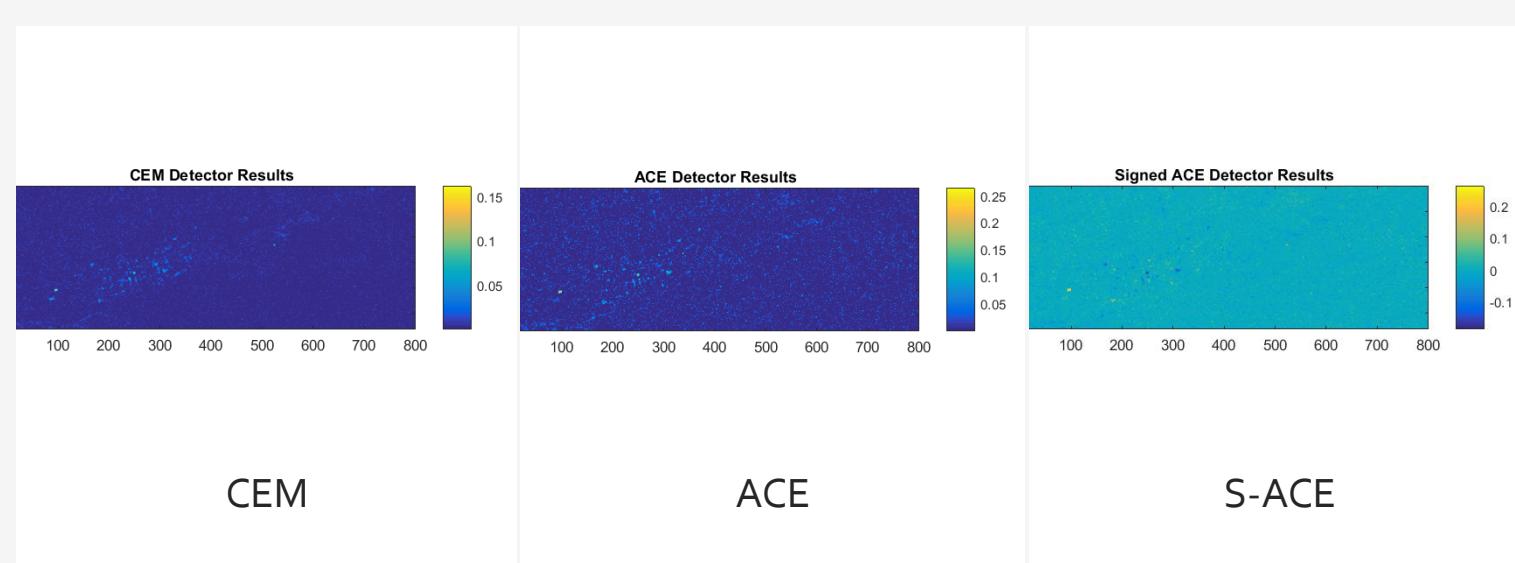
## Threshold Selection Result on AMSD Method

- This algorithm seems to work optimistically or because the amount of target data is small, this algorithm has low accuracy

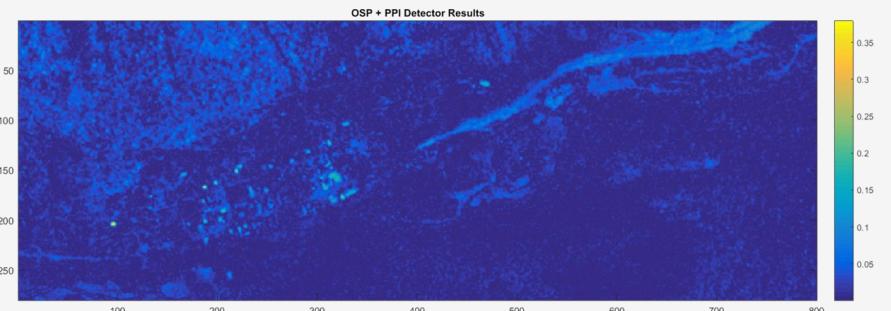


# *Vehicle 1*

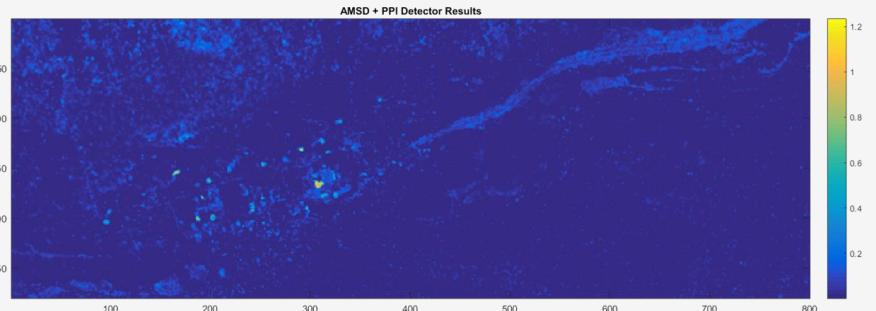
Result of Structured Method  
Detector Map



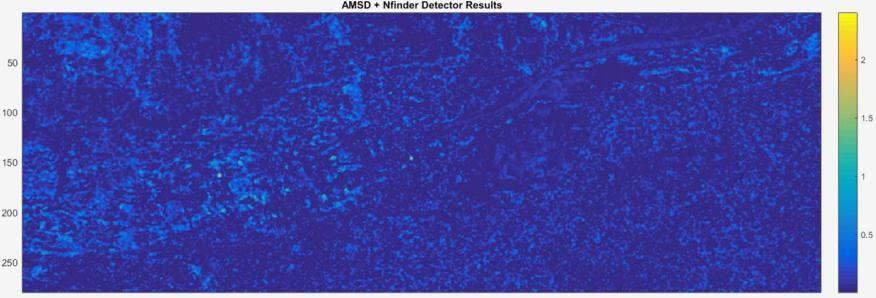
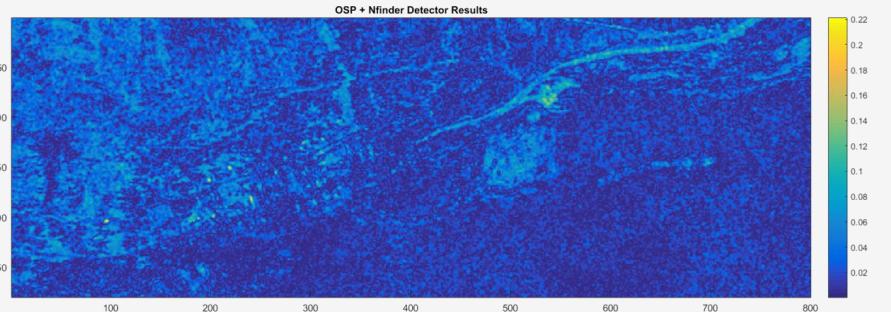
OSP



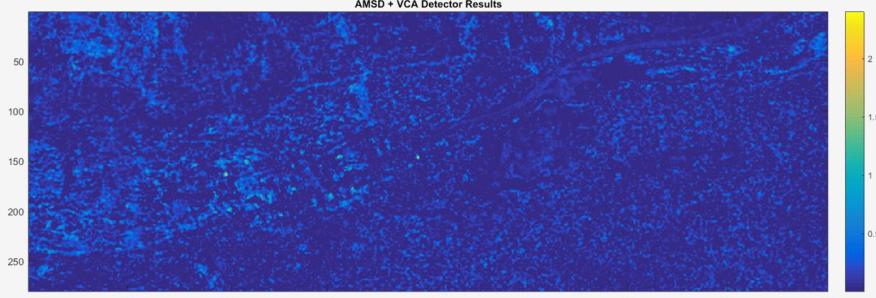
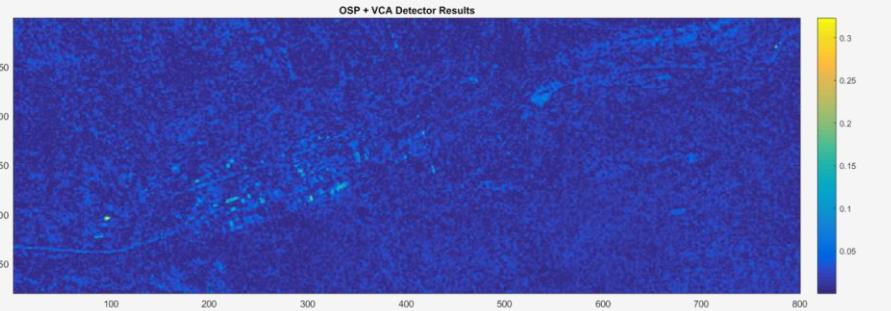
AMSD



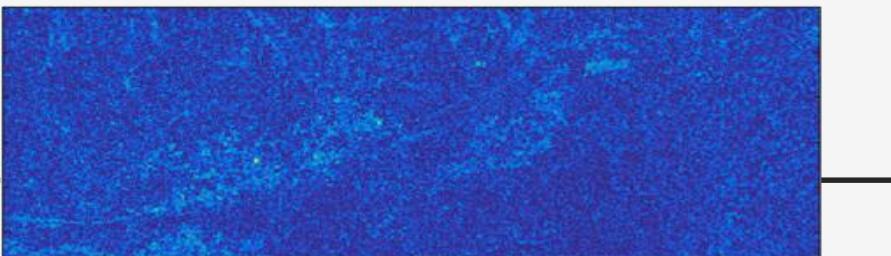
NFINDER



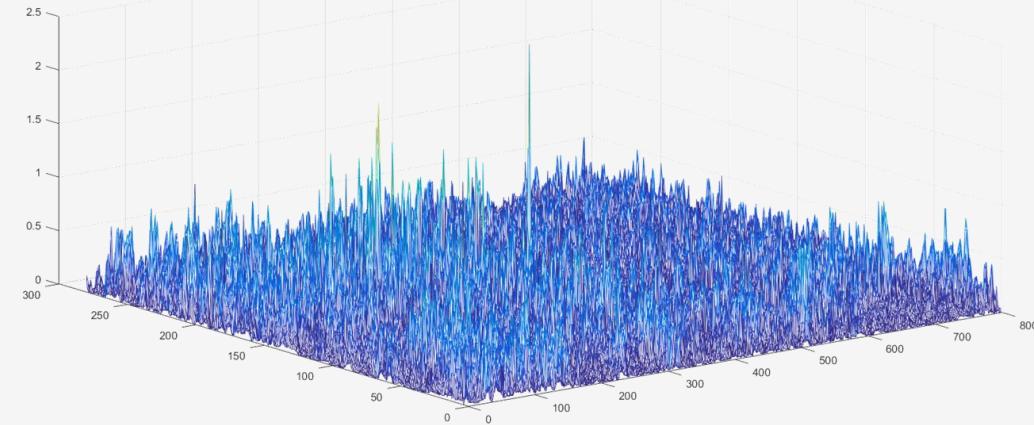
VCA



ATGP

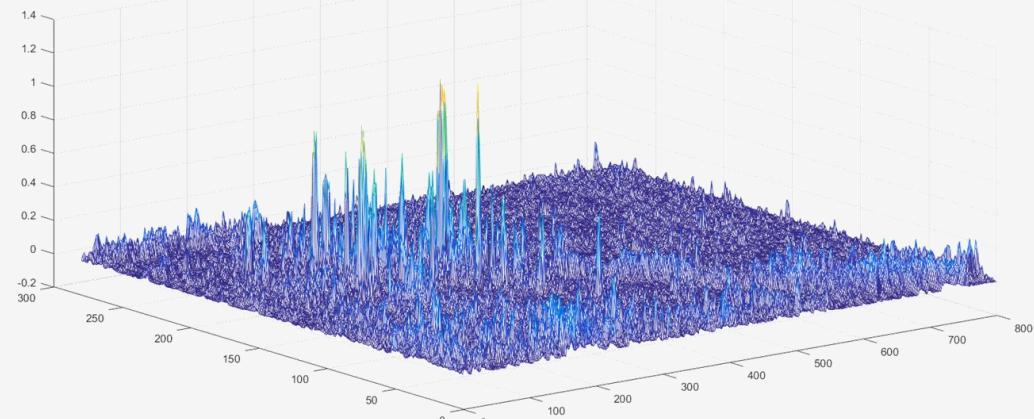


AMSD Detector Results



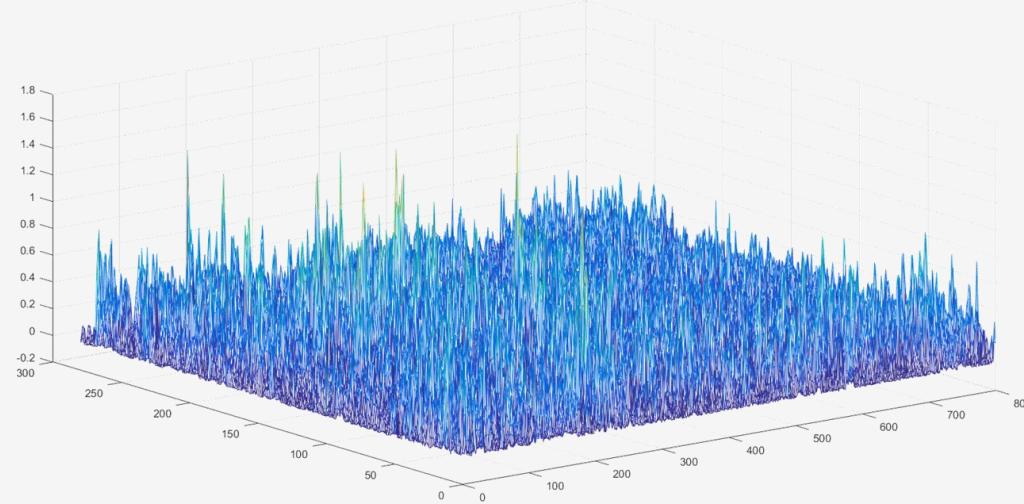
*AMSD + Nfinder*

AMSD Detector Results



*AMSD + PPI*

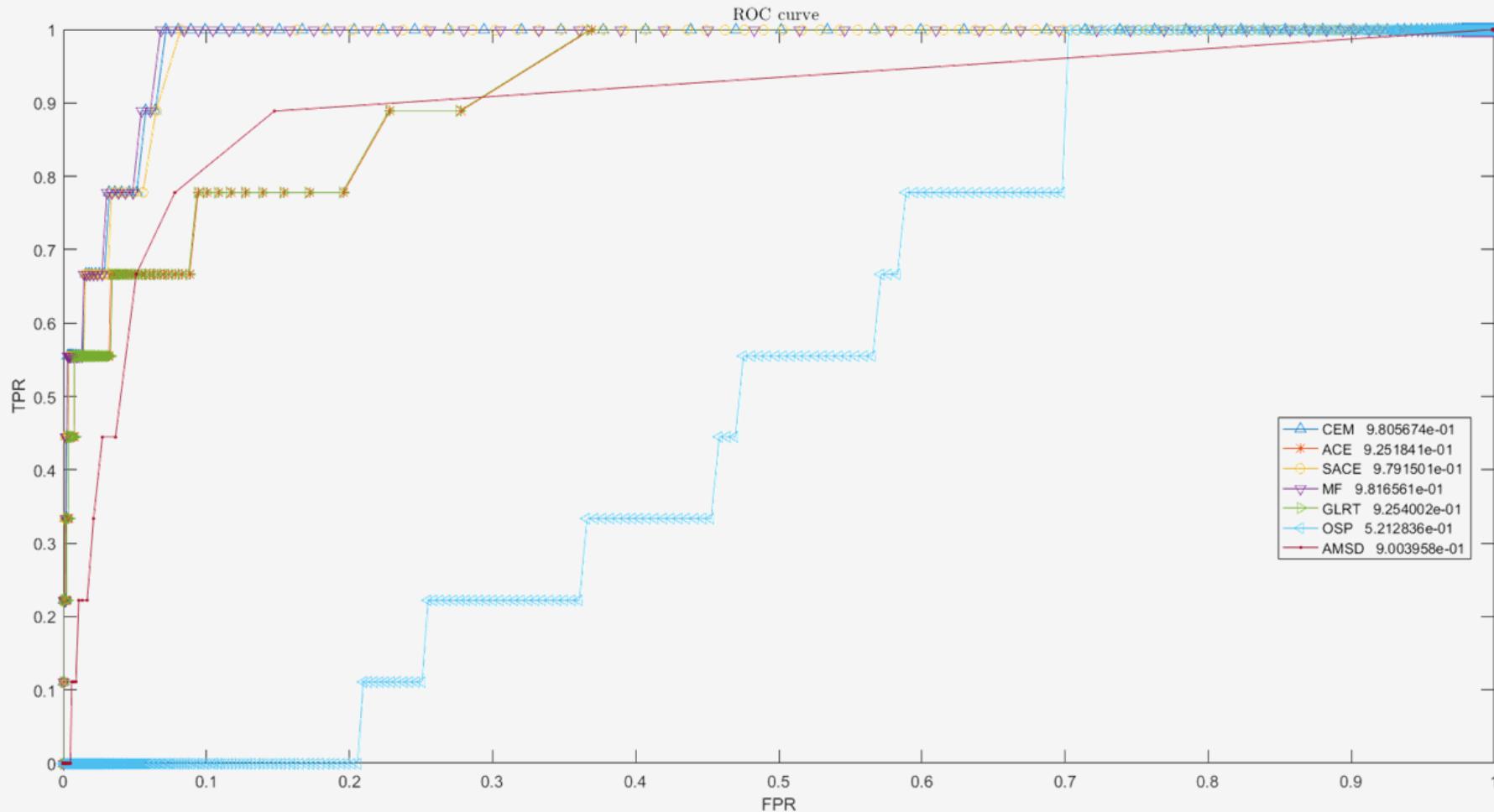
AMSD Detector Results



*AMSD + VCA*

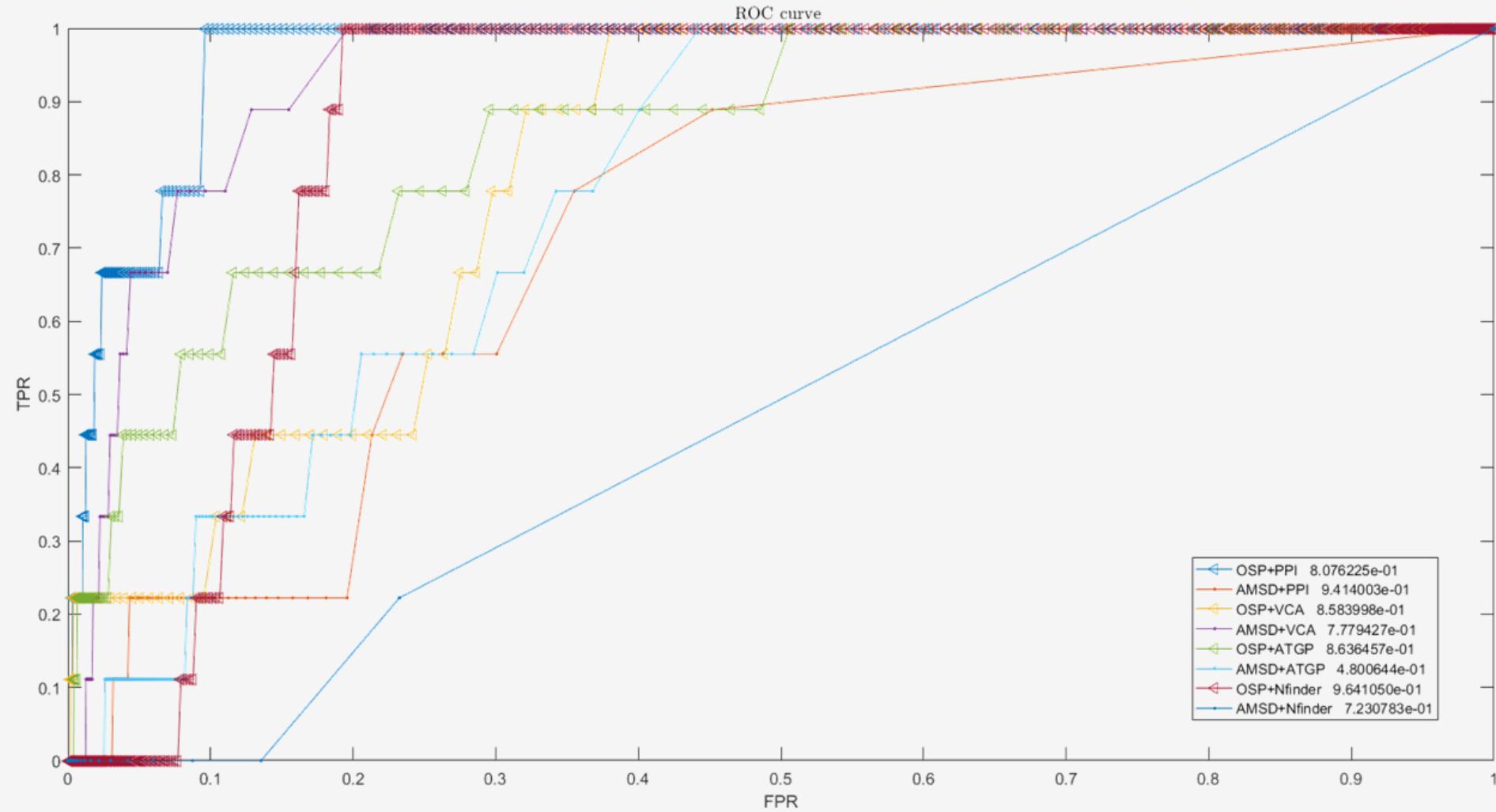
- Result of Unstructured Method
- Detector Map

# *Vehicle 1*



- ROC curve of Vehicle 1 data for 1000 different thresholds
- The AUC of each curve calculated

# Vehicle 1



- ROC curve of Vehicle 1 data for 1000 different thresholds
- The AUC of each curve calculated

# Vehicle 1

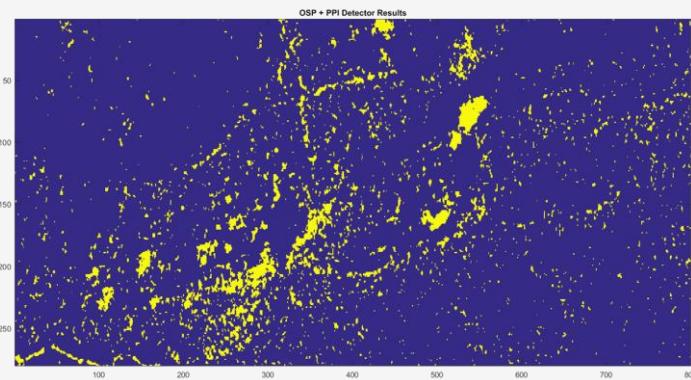
Method	AUC	ACC	PPV* $10^{-3}$
OSP+PPI	0.8076	0.5635	0.3261
AMSD+PPI	0.9414	0.9964	0.0919
OSP+VCA	0.8583	0.6557	0.160
AMSD+VCA	0.7779	0.9856	0.0458
OSP+ATGP	0.8636	0.6558	0.0589
AMSD+ATGP	0.4800	0.8323	0.0401
OSP+Nfinder	0.9641	0.5750	0.3695
AMSD+Nfinder	0.7230	0.9921	0.0405

Method	AUC	ACC	PPV* $10^{-3}$
CEM	0.981	0.6205	5.63
ACE	0.926	0.9945	31.77
SACE	0.980	0.6210	55.55
MF	0.982	0.6211	5.84
GLRT	0.926	0.9946	31.74
OSP	0.522	0.6558	0.0589
AMSD	0.901	0.8323	0.0401

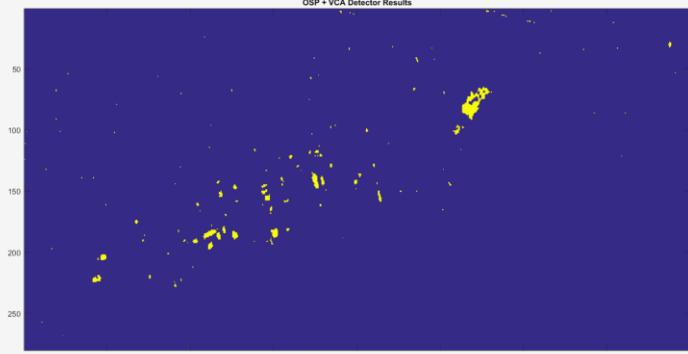
# *Result of OTSU Threshold Selection*

Method	Fabric 2	Fabric 3	Vehicle 1
CEM	0.0028	0.0035	0.0032
ACE	0.0182	0.0183	0.0150
S-ACE	0.0166	0.0155	0.0122
MF	0.0027	0.0035	0.0032
GLRT	0.0180	0.0181	0.0149
OSP	0.0064	0.0011	0.0068
AMSD	0.0783	0.0648	0.0903
OSP+PPI	0.0103	0.0019	0.0078
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OSP+VCA	0.0086	0.0085	0.0312
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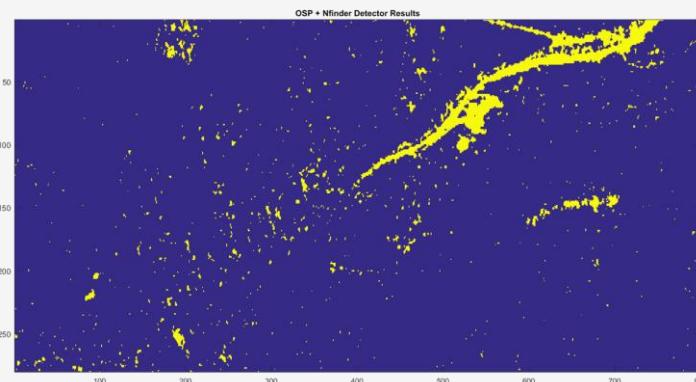
PPI



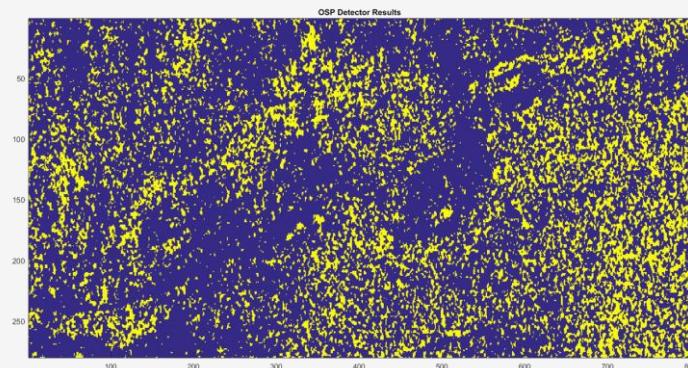
VCA



NFINDER



ATGP

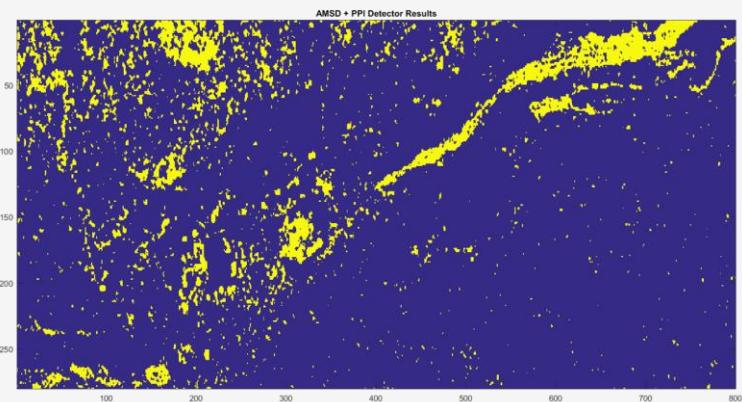


## *Threshold Selection Result on OSP Method*

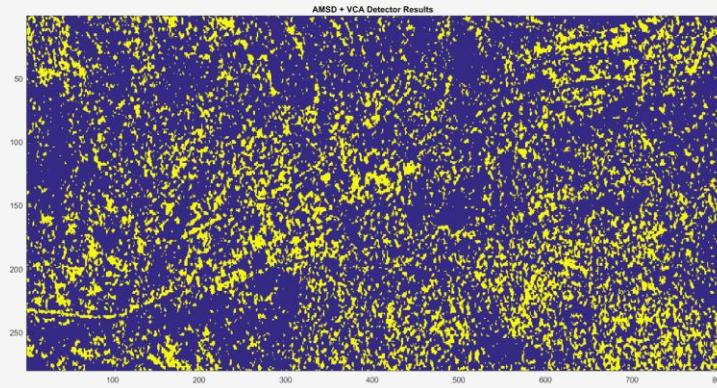
- This algorithm seems to work optimistically or because the amount of target data is small, this algorithm has low accuracy

## Vehicle 1

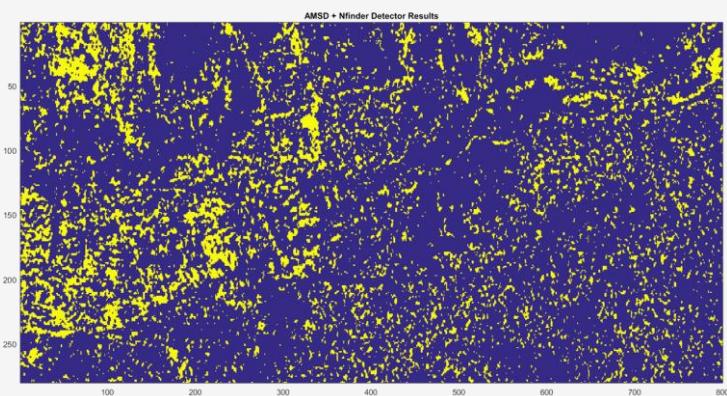
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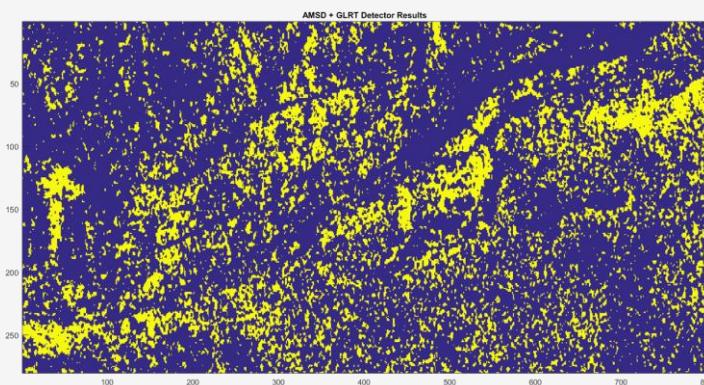
VCA



NFINDER



ATGP



## *Threshold Selection Result on AMSD Method*

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- This algorithm seems to work optimistically or because the amount of target data is small, this algorithm has low accuracy

# *Thank You*

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 09224015584

# *The End*

References for code ,data and results:

<https://github.com/FaezehZamiri/Hyperspectralremotesensing/>