

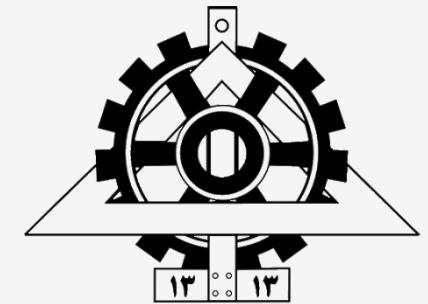


Hyperspectral Remote Sensing

*Spectral
Unmixing &
Target Detection*



University of Tehran
College of Engineering
Faculty of Surveying and Geospatial engineering
Remote Sensing



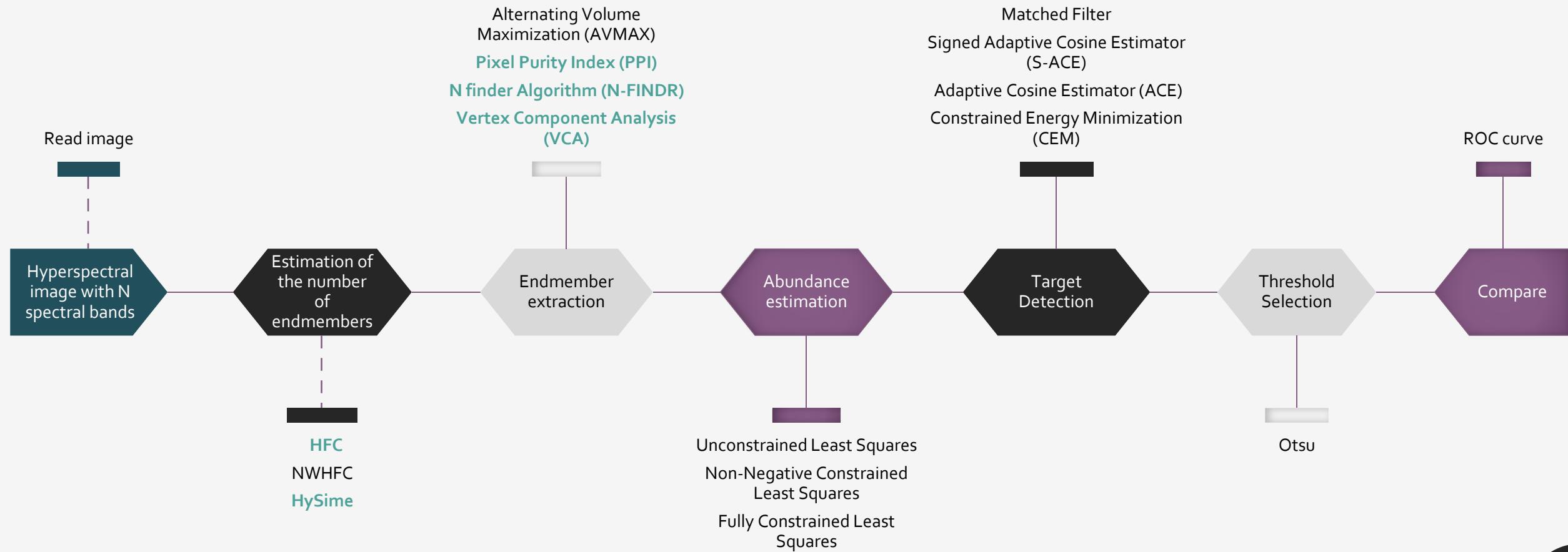
Dr. Hasanlou

Faezeh Zamiri

810399040

aghdam.zamiri.fa@ut.ac.ir

Method



- General scheme of Spectral Unmixing And Target Detection

Data

Data that I used in this project.

Link to Download dataset:

- https://rslab.ut.ac.ir/documents/8196_0329/105075217/Data.part1.rar
- https://rslab.ut.ac.ir/documents/8196_0329/105075217/Data.part2.rar
- https://rslab.ut.ac.ir/documents/8196_0329/105075217/Targets.rar



The Cooke City Dataset

(280*800) *126

Endmembers Estimation

Classic methods for subspace estimation is Virtual dimensionality HFC & NWHFC & Hyperspectral subspace identification minimum error (HySime)



Endmember extraction

Classic methods for endmember extraction



Vertex Component
Analysis
(VCA)



Pixel Purity Index
(PPI)



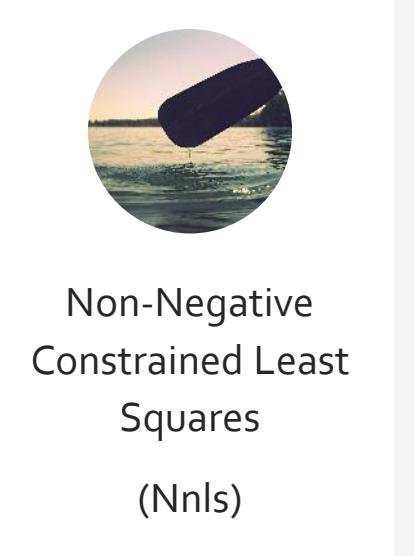
N finder Algorithm
(N-FINDR)

Abundance estimation

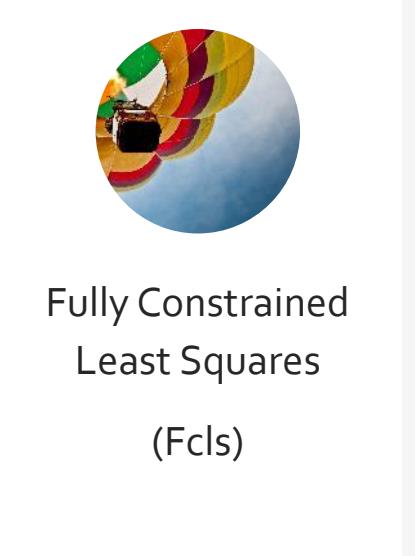
Classic methods for abundance estimation:



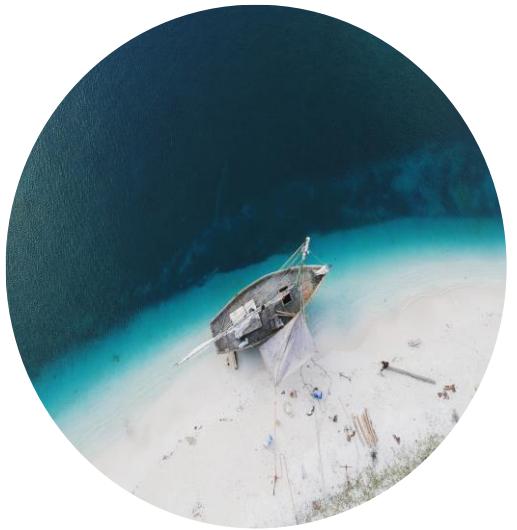
Unconstrained Least
Squares
(Ucls)



Non-Negative
Constrained Least
Squares
(Nnls)



Fully Constrained
Least Squares
(Fccls)



HFC

Endmembers Estimation

Harsanyi-Farrand-Chang(HFC)

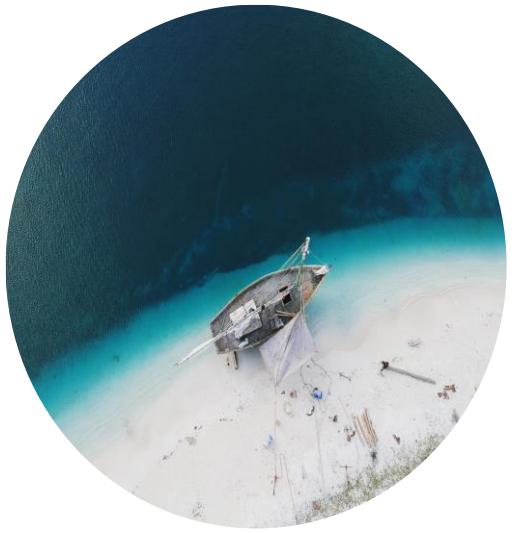
$$\mathbf{R}_{L \times L} = \sum_{i=1}^N \mathbf{r}_i \mathbf{r}_i^T \quad \{\hat{\lambda}_1 \geq \hat{\lambda}_2 \geq \dots \geq \hat{\lambda}_L\}$$

$$\mathbf{K}_{L \times L} = \sum_{i=1}^N (\mathbf{r}_i - \boldsymbol{\mu})(\mathbf{r}_i - \boldsymbol{\mu})^T \quad \{\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_L\}$$

$$\hat{\lambda}_l > \lambda_l \text{ for } l = 1, \dots, \text{VD}$$

$$\hat{\lambda}_l = \lambda_l \text{ for } l = \text{VD} + 1, \dots, L$$

The HFC method was first envisioned in Harsanyi et al. (1994a) to detect spectral signatures present in AVIRIS data. It was then used to find the now-popular terminology, VD which is defined as the number of spectral distinct signatures and later published in Chang and Du (2004). It calculates the difference between eigenvalues in sample correlation matrix and sample covariance matrix and makes use of Neyman–Pearson detector to determine the value of VD.



HySime

Hyperspectral subspace identification minimum error

The idea of HySime is to find the first k eigenvectors that contain the most of data information, i.e. , to find the k such that the mean square error (MSE) between the original data and its projection on to the eigenvector subspace is minimum.

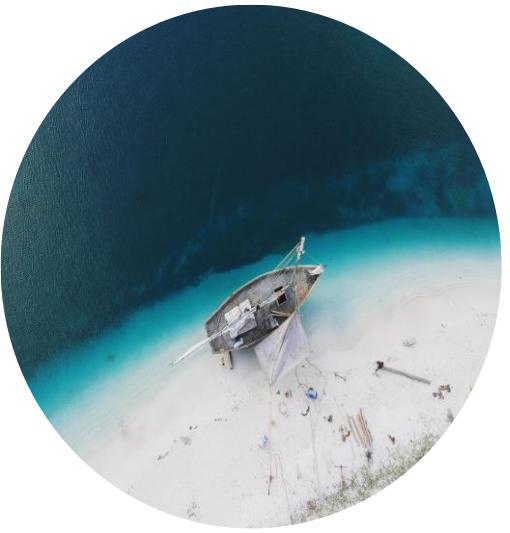
Subspace k is ranked in terms of data variance ,but noise variance is not unitary indifferent directions and the contribution from signals maybe smaller than from noise.

HySime addresses this issue using subspace projection techniques, thus bringing an additional feature with regards to VD :the modelling of noise before the estimation.

Result of Endmember Estimation

Method	Noise	The Cooke City Dataset
HFC	$P_f = 10^{-8}$	33
NWHFC	$P_f = 10^{-8}$	37
HySime	$P_f = 10^{-8}$	19

we know HySime is better than NWHFC and NWHFC is better than HFC , so that I used result of increase HySime for next step.



Pixel Purity Index

It is developed based on the concept of the convex geometry and the criterion of orthogonal projection.

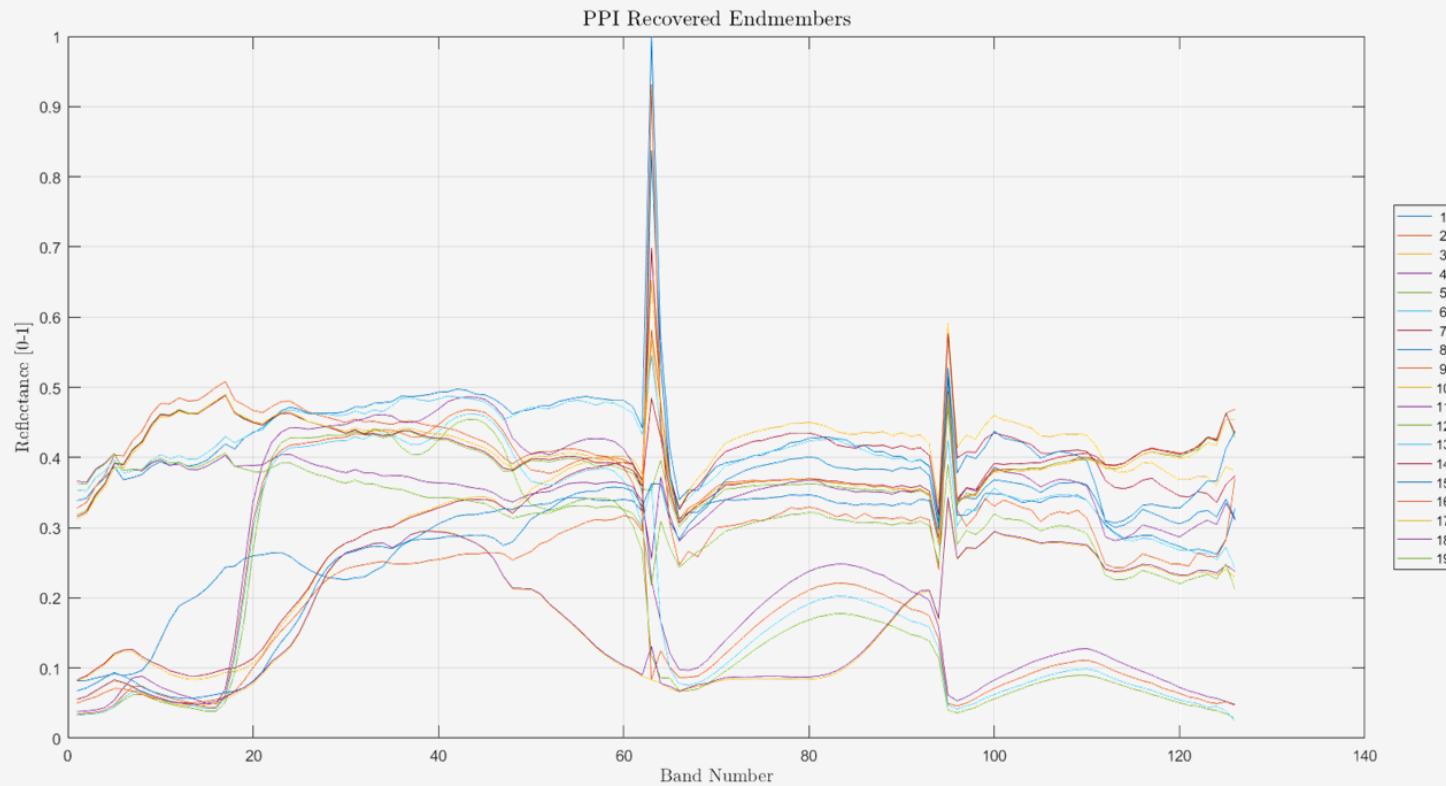
It first generates a set of K random unit vectors, called skewers, to cover all possible projection directors and then orthogonally projects all data sample vectors on these skewers to find the maximal and minimal orthogonal projections of each skewer.

For each data sample vector, it counts the number of skewers on which its orthogonal projections yield either maximal or minimal projections. This count is referred to as the PPI count, which will be used to determine whether or not a particular data sample vector is an endmember.

PPI

Result of **PPI**

HYPERPPI Performs the pixel purity index (PPI) algorithm
Performs the pixel purity index algorithm for endmember finding.
Usage
`[U] = hyperPpi(M, q, numSkewers)`
Inputs
M - 2d matrix of HSI data ($p \times N$) **Cooke City (126*224000)**
q - Number of endmembers to find **19**
numSkewers - Number of "skewer" vectors to project data onto **1000**
Outputs
U - Recovered endmembers ($p \times q$) **(126 * 19)**



Result of *N-Finder*

HYPERNFINDR Performs the N-FINDR (endmember extraction) algorithm

Performs the N-FINDR algorithm to find q endmembers
and then reduce dimensionality to (q-1).

Usage

[U] = hyperNfinder(M, q)

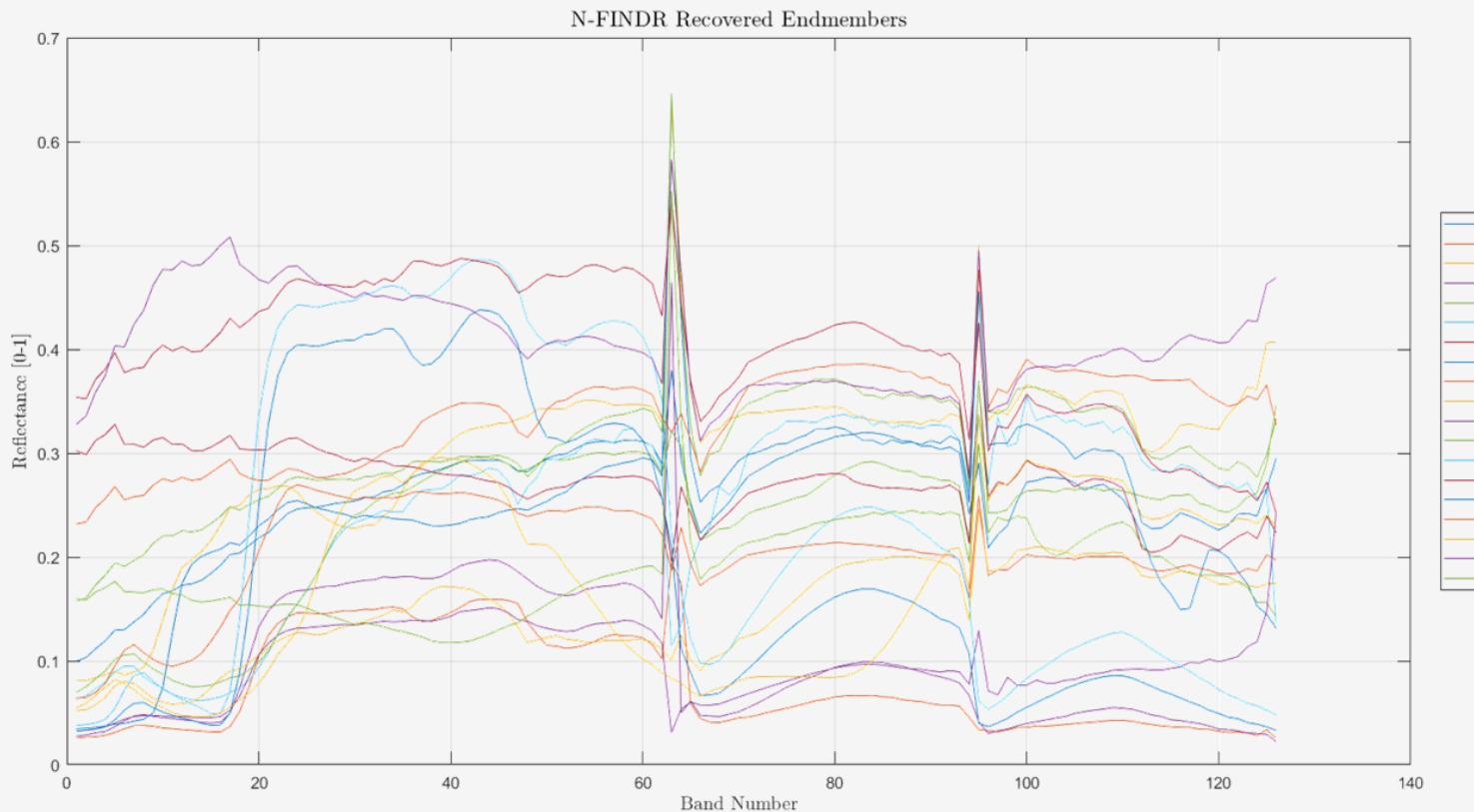
Inputs

M - 2d matrix of HSI data (p x N) **Cooke City (126*224000)**

q - Number of endmembers to find **19**

Outputs

U - Recovered endmembers (p x q) **(126*19)**



Result of VCA

HYPERVCA Vertex Component Analysis algorithm

hyperVca performs the vertex component analysis algorithm to find pure pixels in an HSI scene

Usage

```
[ U, indices, snrEstimate ] = hyperVca( M, q )
```

Inputs

M - HSI data as 2D matrix (p x N) **Cooke City (126*224000)**

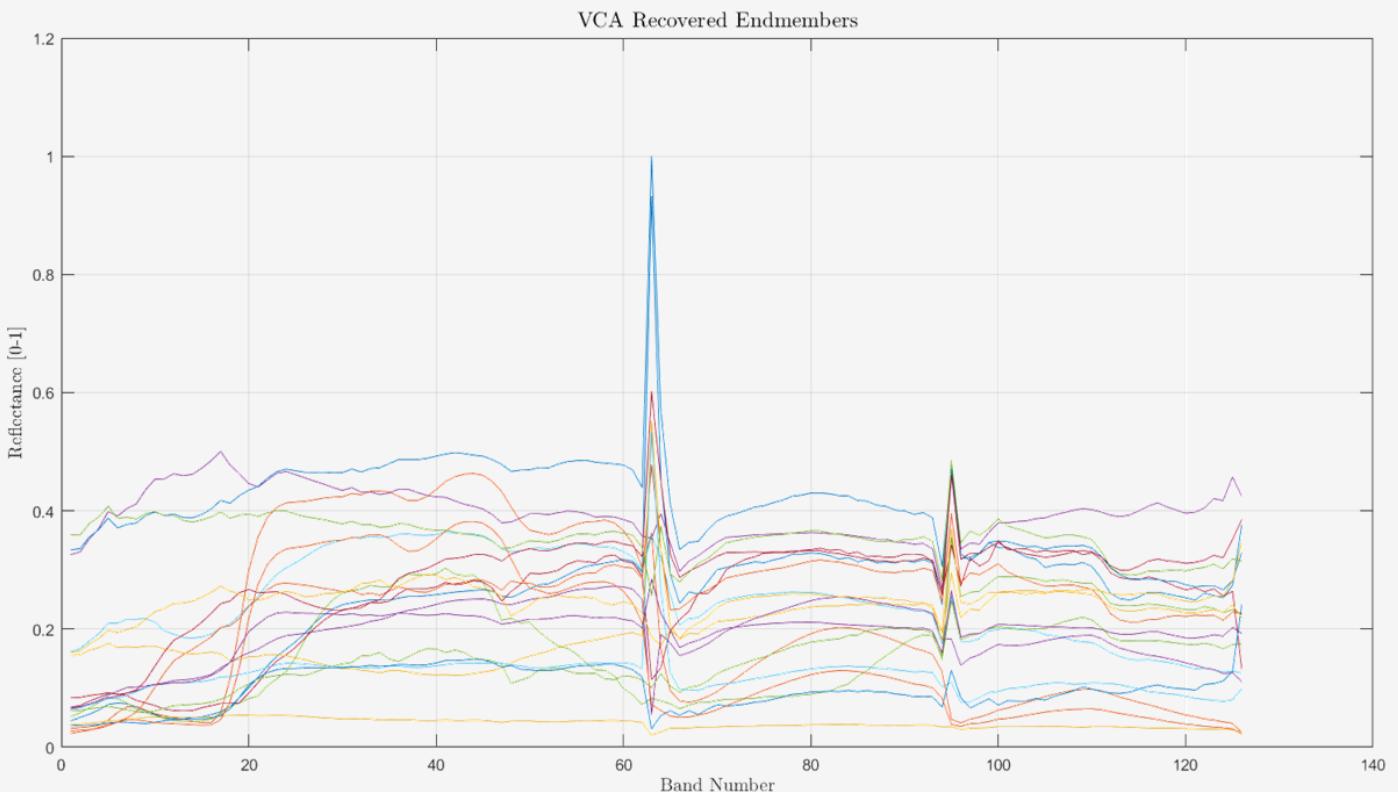
q - Number of endmembers to find **19**

Outputs

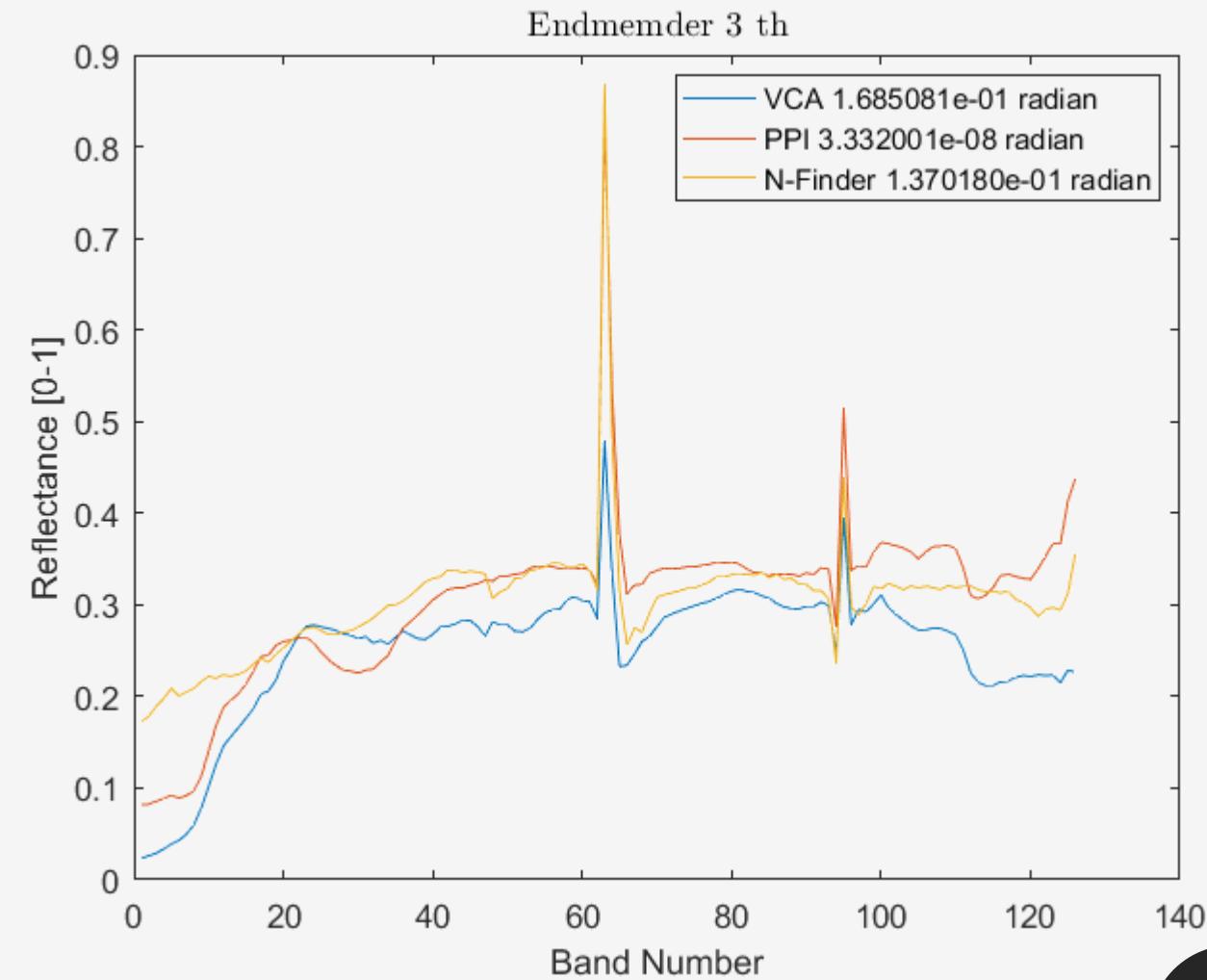
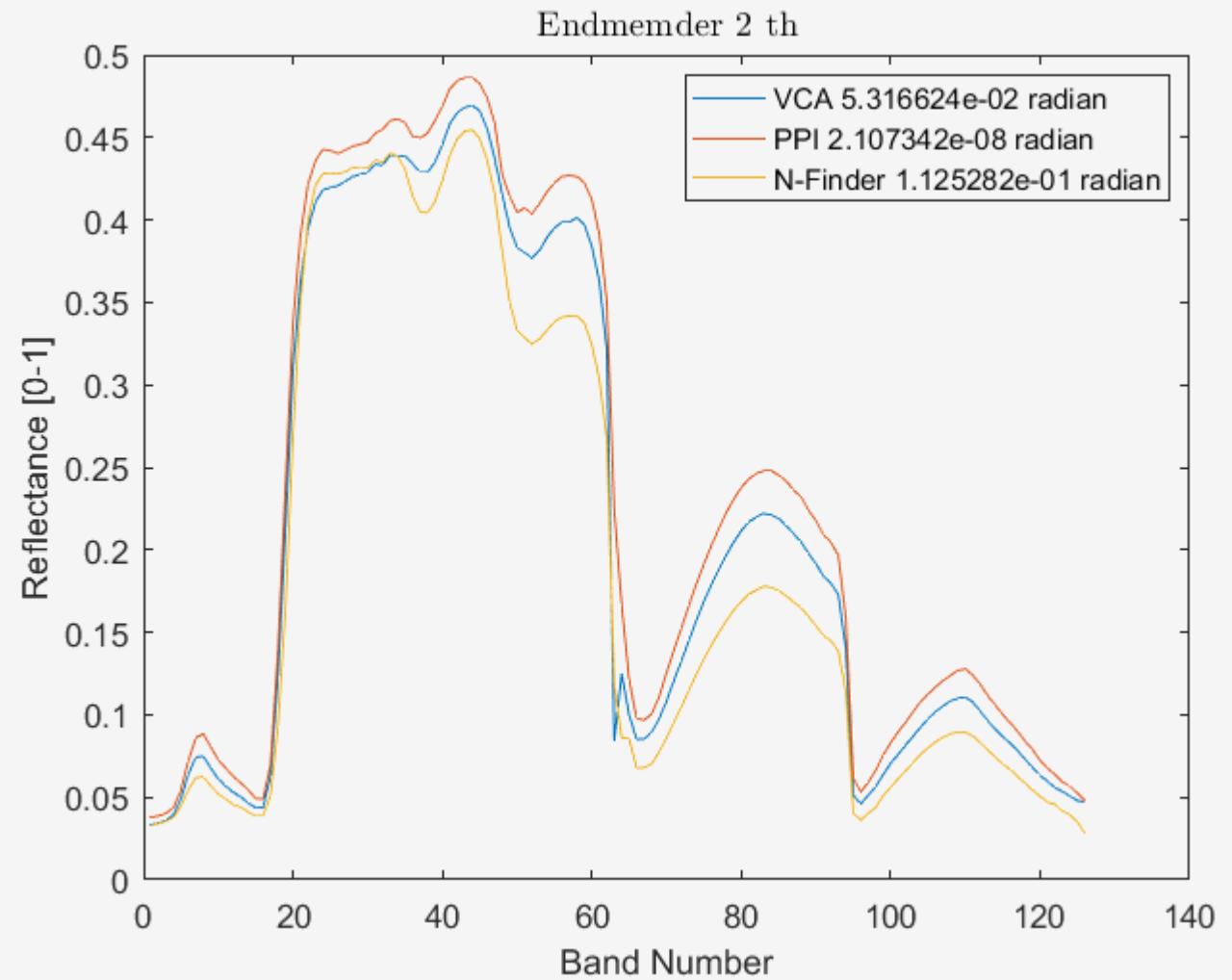
U - Matrix of endmembers (p x q)..... **(126 * 19)**

indices - Indices of pure pixels in U **(1 * 19)**

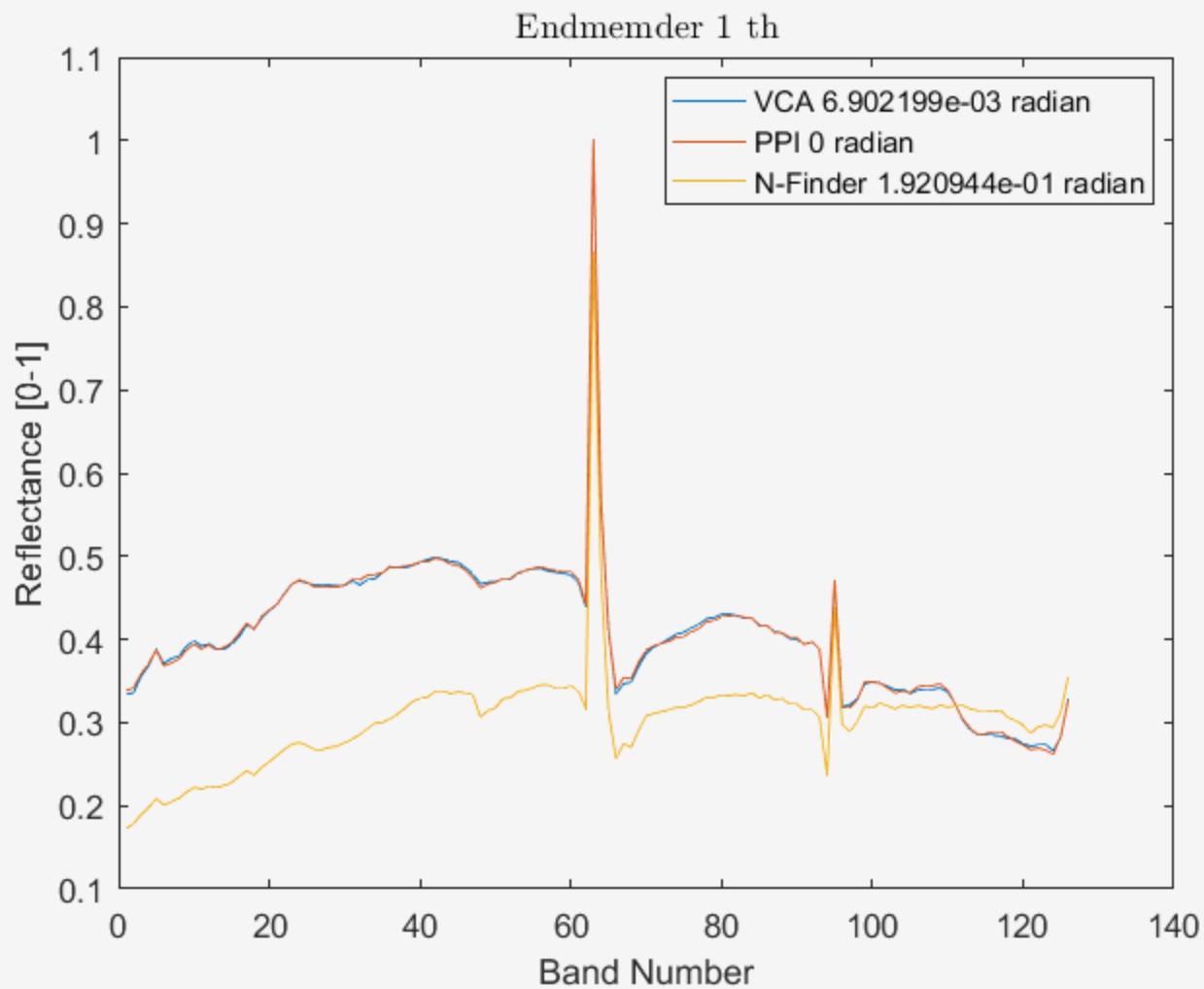
snrEstimate - SNR estimate of data [dB] **46.8222**



Comparison signature of endmembers using SAM for Cook City dataset

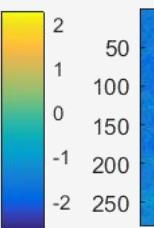
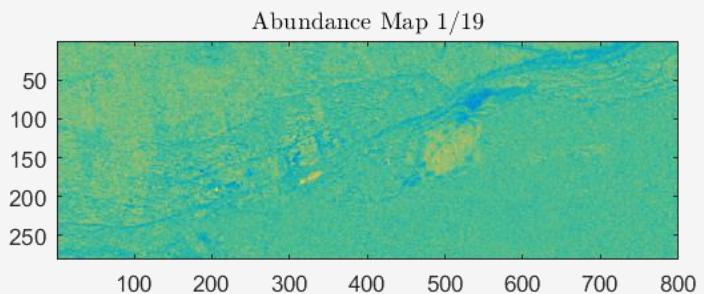


Comparison signature of endmembers using SAM for Cook City dataset

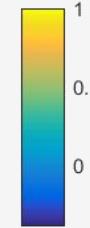
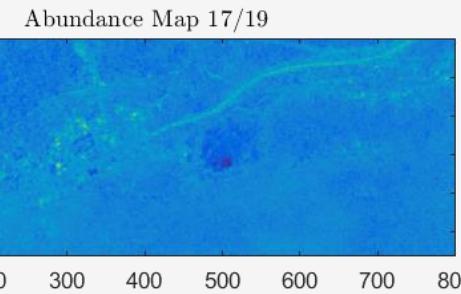


Abundance estimation

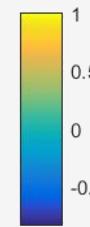
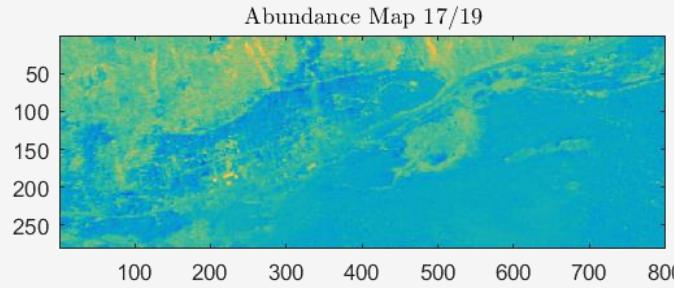
PPI



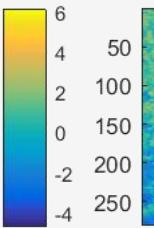
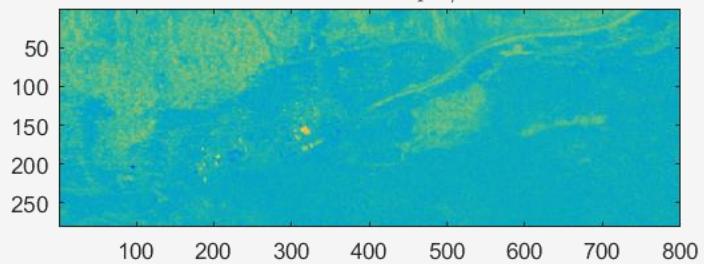
NFINDER



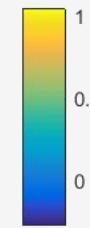
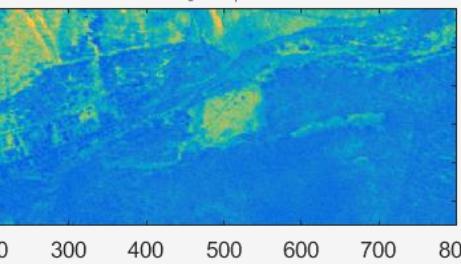
VCA



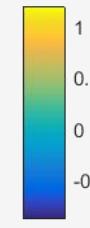
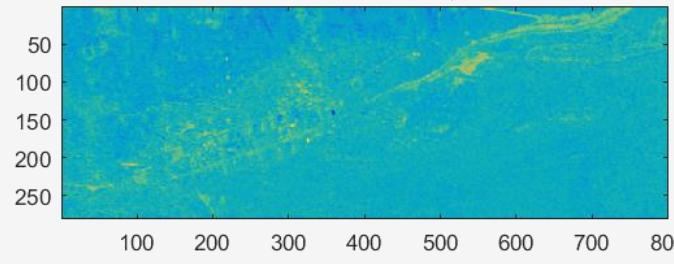
Abundance Map 2/19



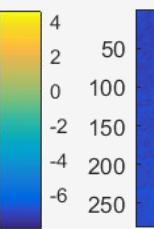
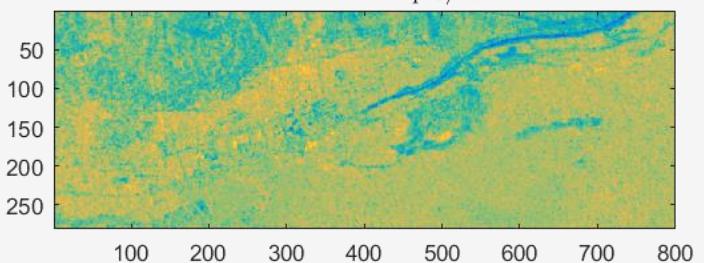
Abundance Map 18/19



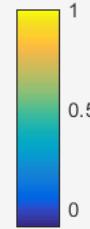
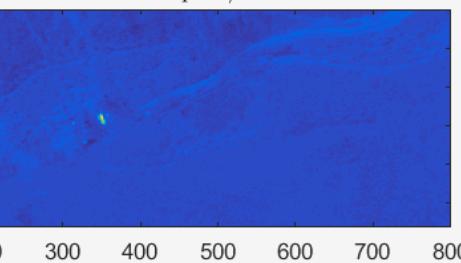
Abundance Map 18/19



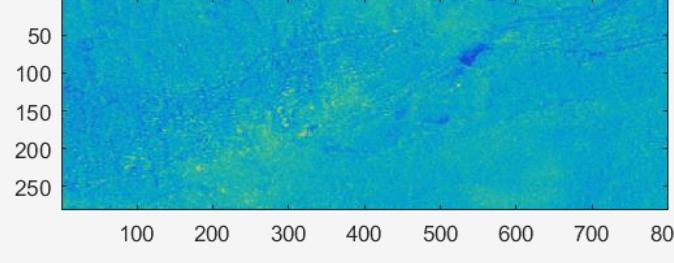
Abundance Map 3/19



Abundance Map 19/19



Abundance Map 19/19



Target Detection

Structured methods for target detection



Constrained Energy
Minimization
(CEM)



Adaptive Cosine
Estimator
(ACE)



Signed Adaptive
Cosine Estimator
(S-ACE)



Matched Filter



Generalized Likelihood
Ratio Test
(GLRT)

Target Detection

Unstructured methods for target detection

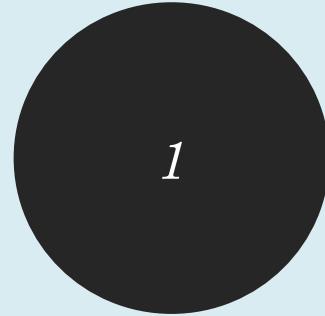


Adaptive Matched Subspace Detector (AMSD)



Orthogonal Subspace Projection (OSP)

Threshold Selection



Otsu

Otsu's method chooses a threshold that minimizes the intraclass variance of the thresholded black and white pixels.

CEM

Constrained Energy Minimization

- HYPERCEM Performs constrained energy minimization (CEM) algorithm
- Performs the constrained energy minimization algorithm for target detection.

Usage

[results] = hyperCem(M, target)

Inputs

M - 2d matrix of HSI data ($p \times N$) → 126*224000

target - target of interest ($p \times 1$) → 126*1

Outputs

results - vector of detector output ($N \times 1$) → 224000*1

ACE

Adaptive Cosine Estimator

- HYPERACE Performs the adaptive cosin/coherent estimator algorithm
- Performs the adaptive cosin/coherent estimator algorithm for target detection.

Usage

[results] = hyperAce(M, S)

Inputs

M - 2d matrix of HSI data ($p \times N$) → 126*224000

S - 2d matrix of target endmembers ($p \times 1$) → 126*1

Outputs

results - vector of detector output ($N \times 1$) → 224000*1

GLRT

Generalized Likelihood Ratio Test

- HYPERGLRT Performs the generalized likelihood test ratio algorithm
- Performs the generalized likelihood test ratio algorithm for target detection.

Usage

[results] = hyperGlrt(M, U, target)

Inputs

M - 2d matrix of HSI data ($p \times N$) → 126*224000

t - target of interest ($p \times 1$) → 126*1

Outputs

results - vector of detector output ($N \times 1$) → 224000*1

S-ACE

Signed Adaptive Cosine Estimator (S-ACE)

4 of 5 Structured Method

- HYPERACE Performs the adaptive cosin/coherent estimator algorithm
- Performs the adaptive cosin/coherent estimator algorithm for target detection.

Usage

[results] = hyperSignedAce(M, S)

Inputs

M - 2d matrix of HSI data ($p \times N$) → 126*224000

S - target of interest ($p \times 1$) → 126*1

Outputs

results - vector of detector output ($N \times 1$) → 224000*1

MF

Matched Filter

- HYPERACE Performs Matched Filter estimator algorithm
- Performs the estimator algorithm for target detection.

Usage

[results] = hyperMatchedFilter(M, S)

Inputs

M - 2d matrix of HSI data ($p \times N$) → 126*224000

S - target of interest ($p \times 1$) → 126*1

Outputs

results - vector of detector output ($N \times 1$) → 224000*1

OSP

Orthogonal Subspace Projection

- HYPEROSP Performs the orthogonal subspace projection (OSP) algorithm
- Performs the orthogonal subspace projection algorithm for target detection.

Usage

```
[results] = hyperOsp(M, U, target)
```

Inputs

M - 2d matrix of HSI data ($p \times N$)

U - 2d matrix of background endmembers ($p \times q$)

target - target of interest ($p \times 1$)

Outputs

results - vector of detector output ($N \times 1$)

AMSD

Adaptive Matched Subspace Detector

2 of 2 Unstructured Method

- HYPERAMSD Adaptive matched subspace detector (AMSD) algorithm
- Performs the adaptive matched subspace detector (AMSD) algorithm for target detection

Usage

```
[results] = hyperAmsd(M, U, target)
```

Inputs

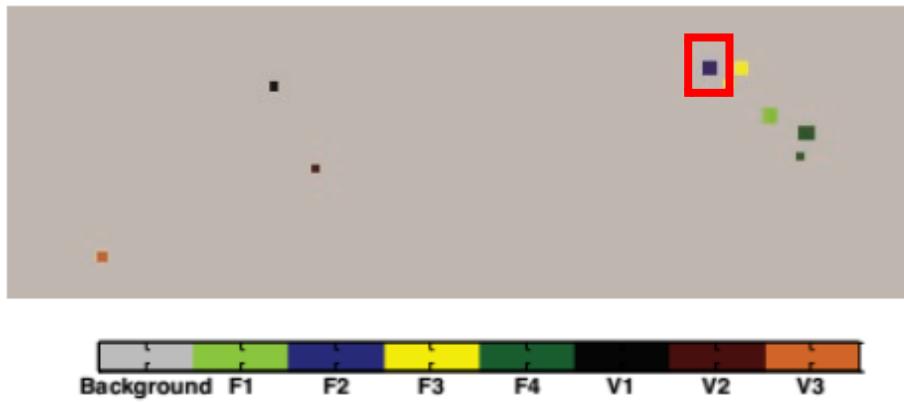
M - 2d matrix of HSI data ($p \times N$)

B - 2d matrix of background endmembers ($p \times q$)

target - target of interest ($p \times 1$)

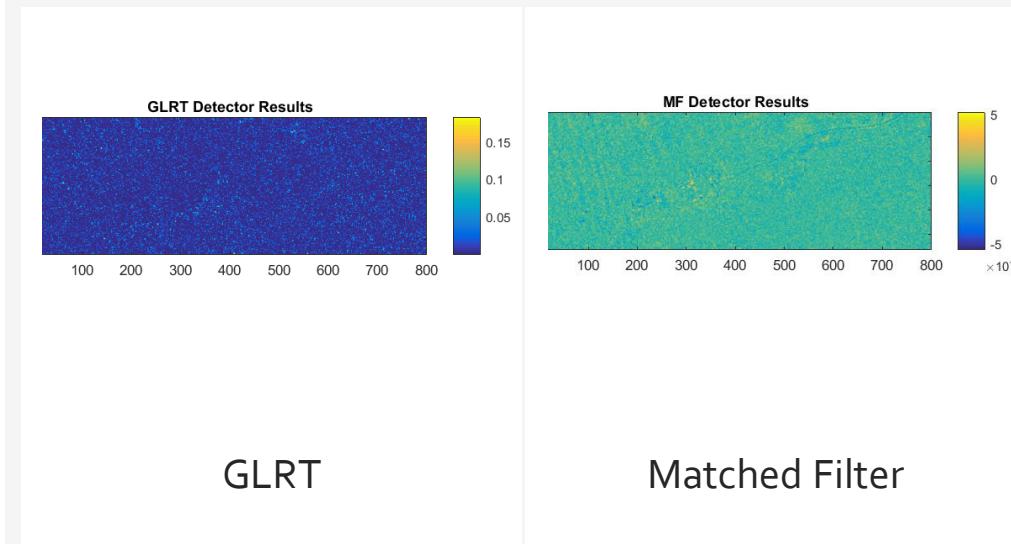
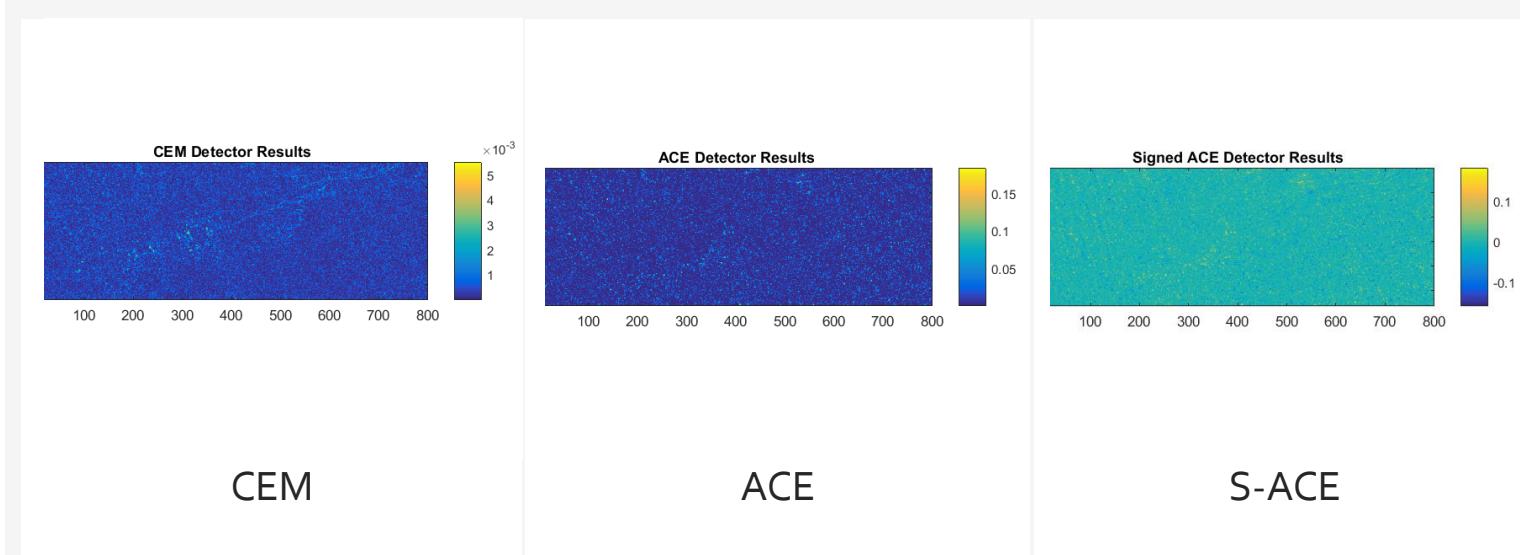
Outputs

results - vector of detector output ($N \times 1$)

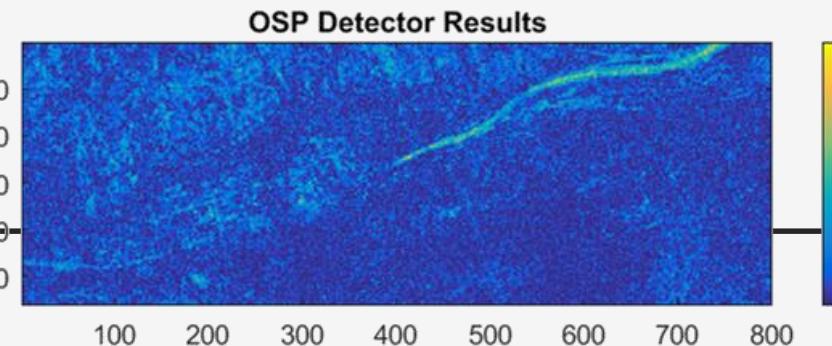
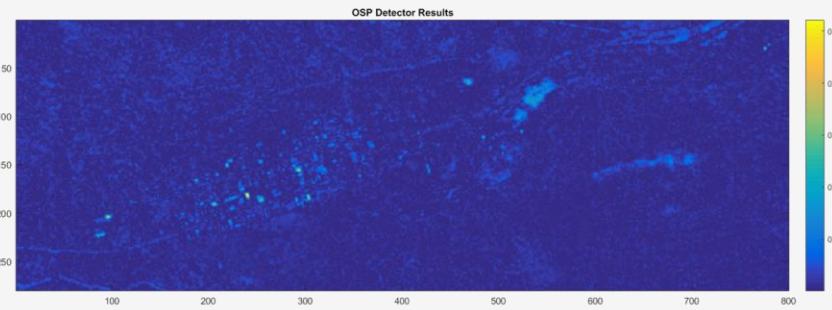
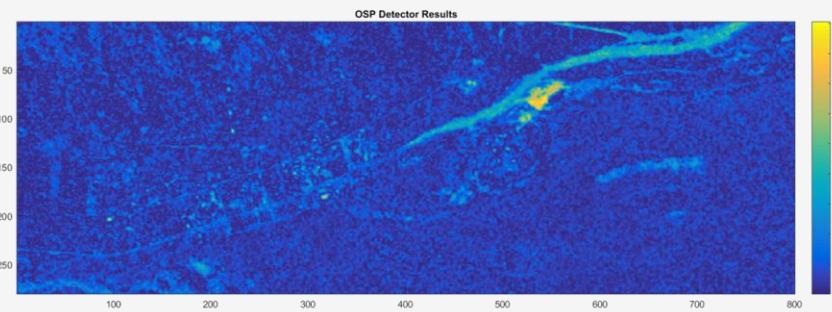
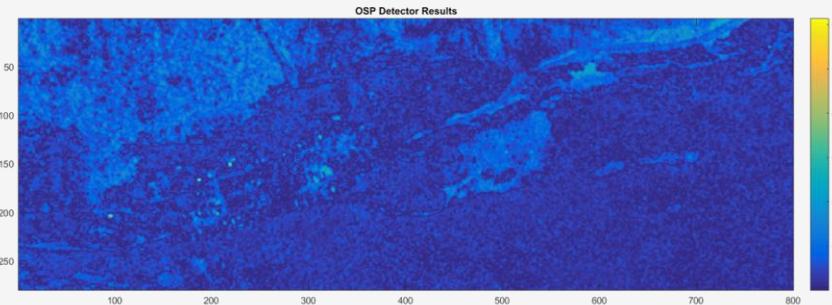


Fabric 2

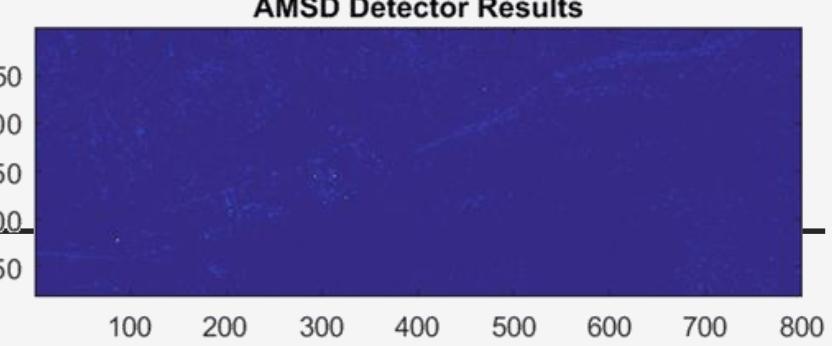
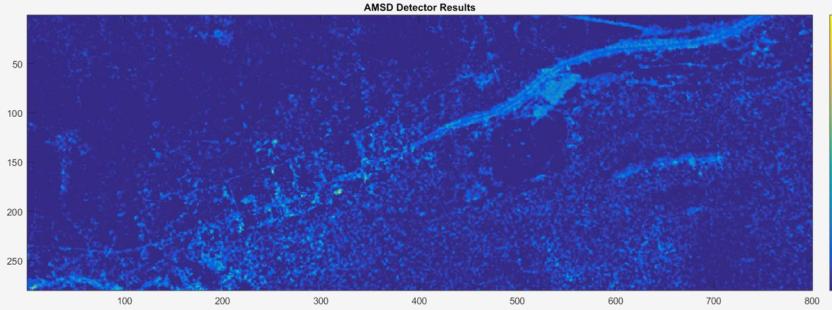
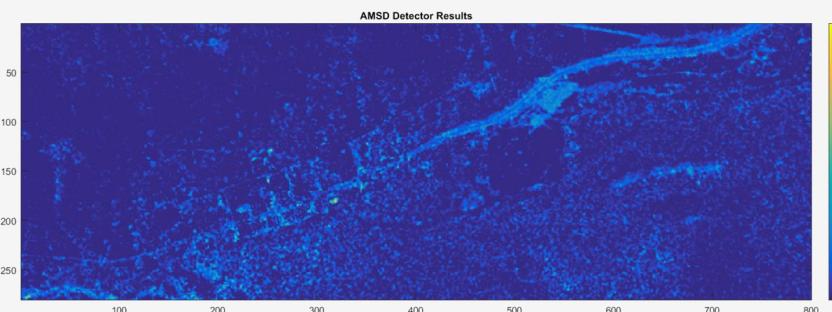
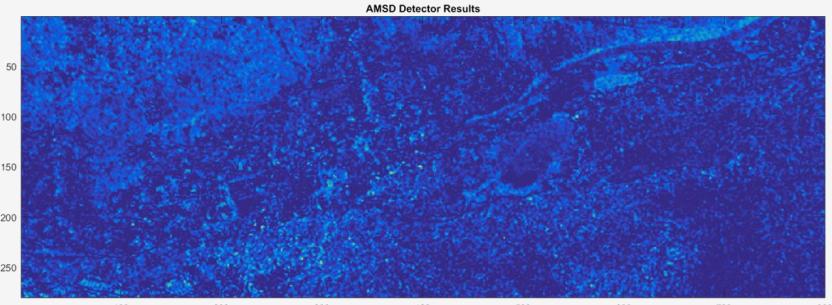
Result of Structured Method
Detector Map



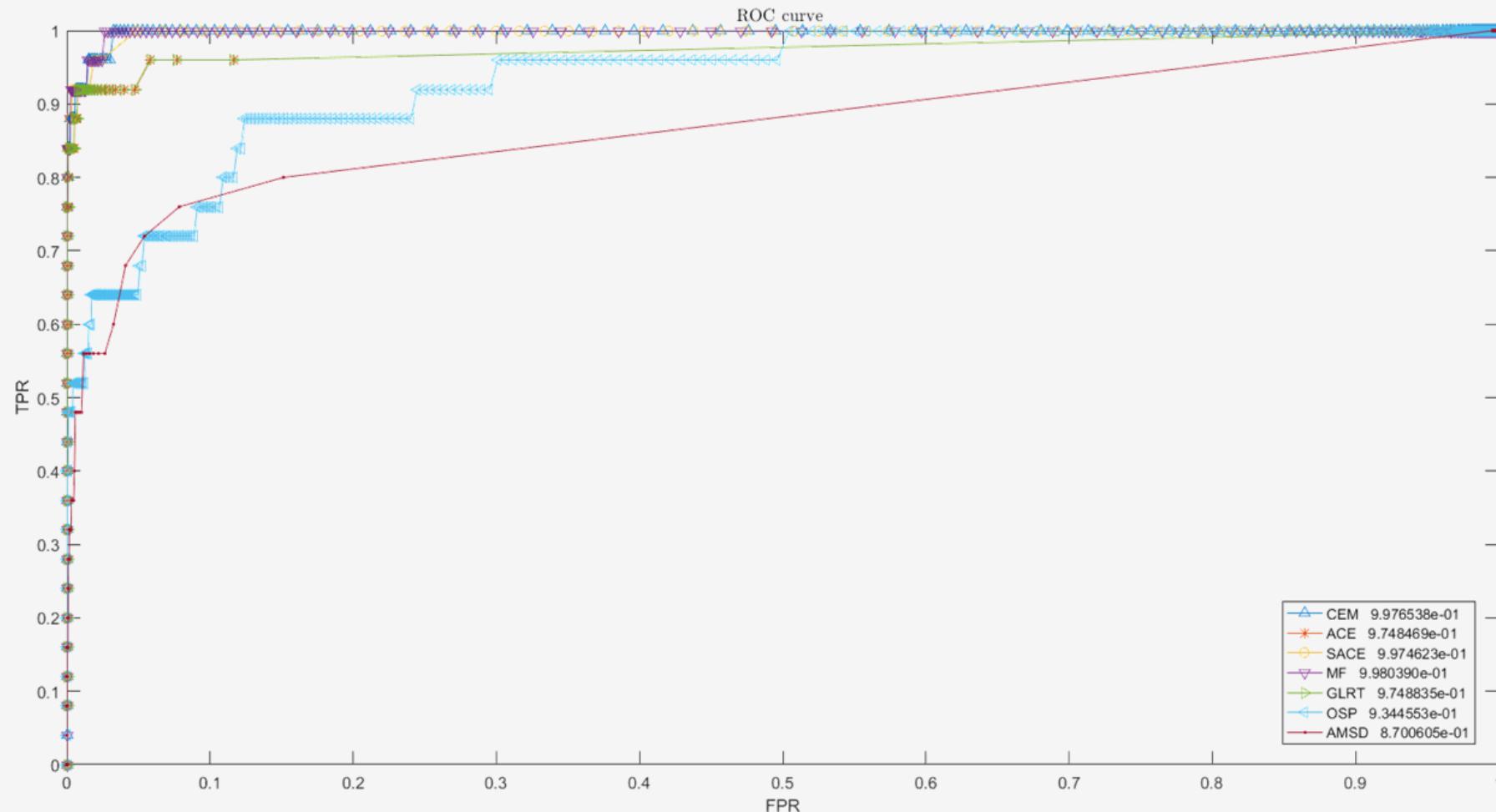
OSP



AMSD

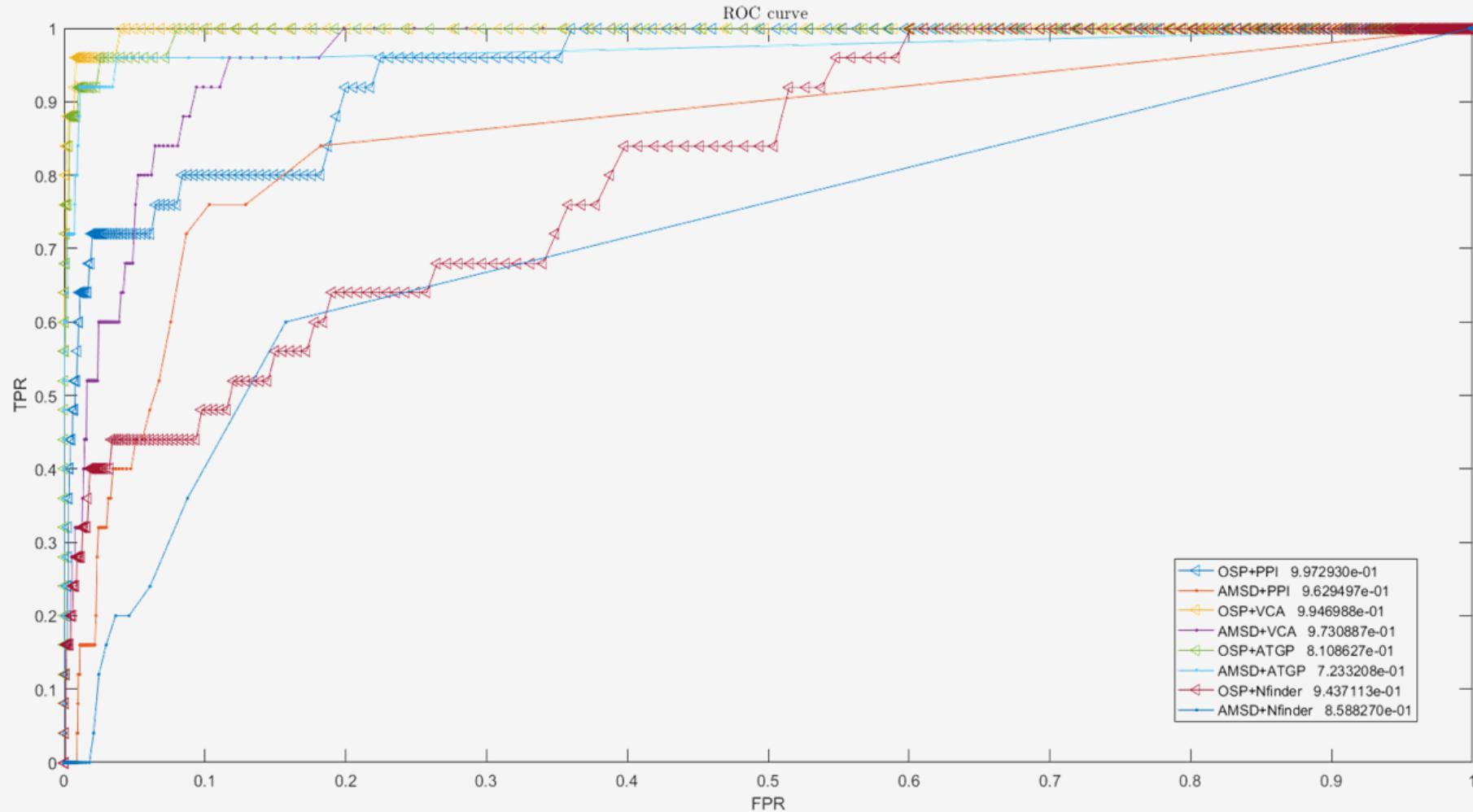


Fabric 2



- ROC curve of Fabric 2 data for 1000 different thresholds
- For Fabric 2 data structured methods have higher AUC than unstructured methods.

Fabric 2



- ROC curve of Fabric 2 data for 1000 different thresholds
- The AUC of each curve calculated

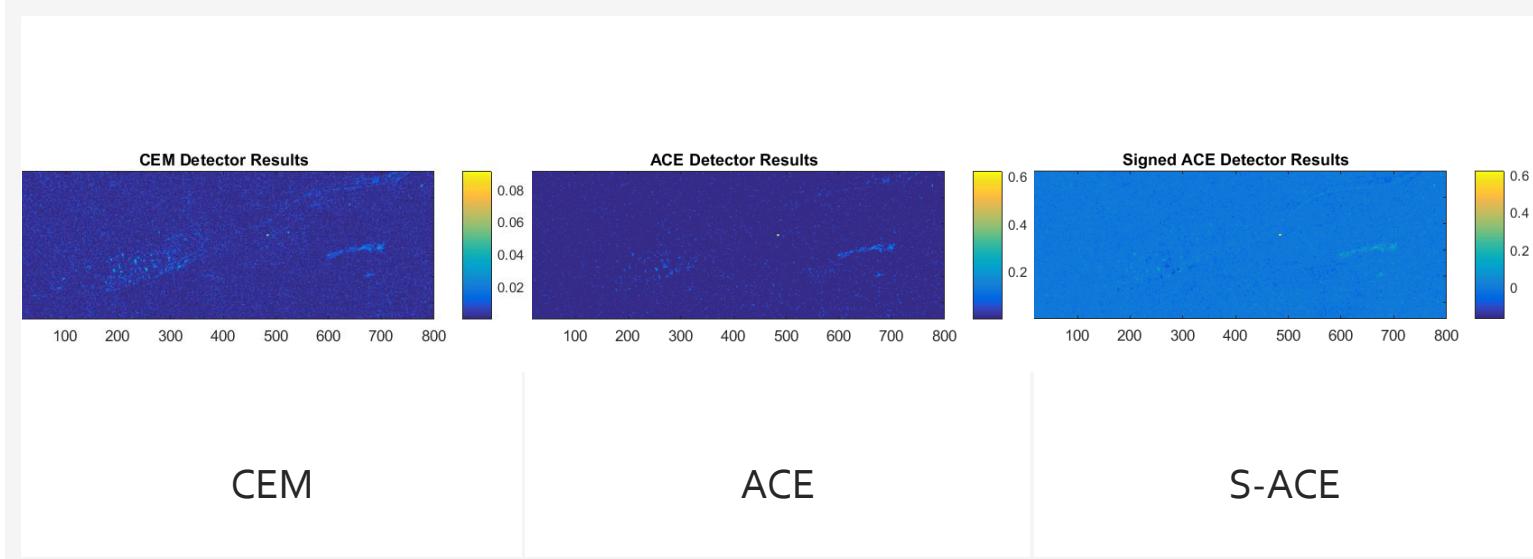
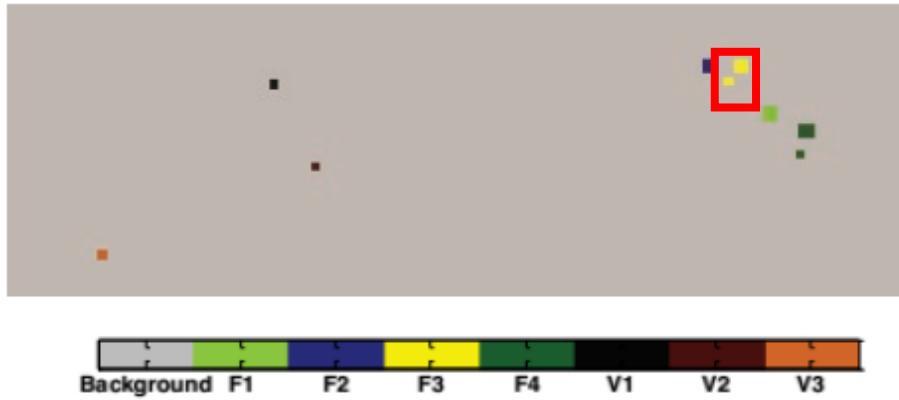
Method	AUC
OSP+PPI	0.8279
AMSD+PPI	0.8271
OSP+VCA	0.9946
AMSD+VCA	0.9730
OSP+ATGP	0.8108
AMSD+ATGP	0.7233
OSP+Nfinder	0.9228
AMSD+Nfinder	0.7937

Fabric 2

Method	AUC	ACC	PPV* 10^{-3}
OSP+PPI	0.8279	0.5299	0.1163
AMSD+PPI	0.8271	0.9931	0.1116
OSP+VCA	0.9946	0.6638	24.09
AMSD+VCA	0.9730	0.9974	100
OSP+ATGP	0.8108	0.6227	0.4055
AMSD+ATGP	0.7233	0.2427	0.1116
OSP+Nfinder	0.9228	0.6292	0.4630
AMSD+Nfinder	0.7937	0.9965	0.1116

Method	AUC	ACC	PPV
CEM	0.998	0.6806	1
ACE	0.975	0.9982	1
SACE	0.998	0.8197	1
MF	0.999	0.6821	1
GLRT	0.975	0.9982	1
OSP	0.935	0.6227	0.4055
AMSD	0.871	0.2427	0.1116

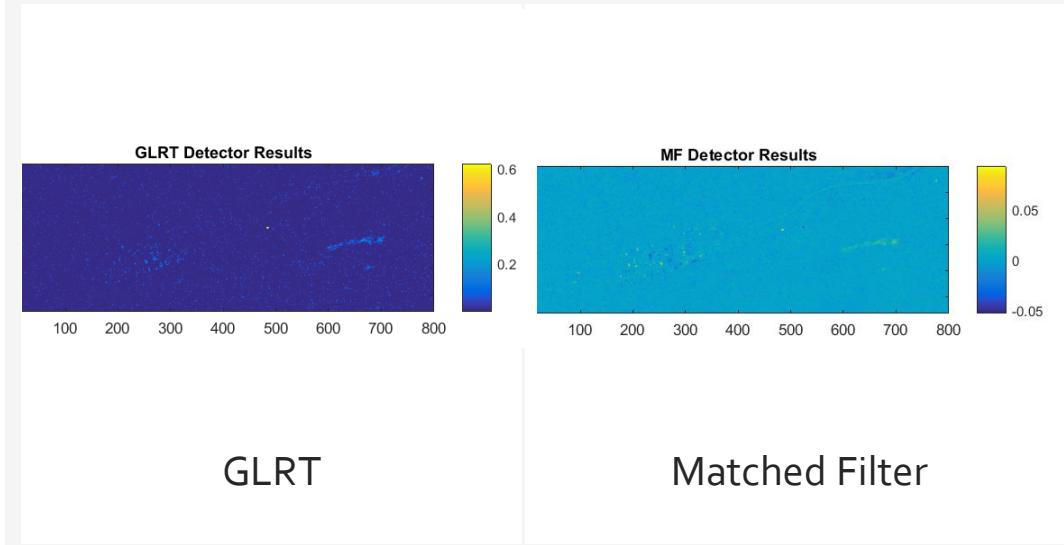
- For FABRIC₃ data, it is observed that the AUC parameter for the OSP method was the highest when the VCA approach was used. In general, the area under the ROC curve for the OSP method is higher, However the overall accuracy of the AMSD method is higher, and therefore the third parameter, PPV, represents the optimal method, the OSP + VCA method.
- In second table, In Unstructured method, first of all estimate number of endmembers with HFC , that is 33 , then calculate matrix of background endmembers with ATGP and finally use AMSD and OSP to target detection.



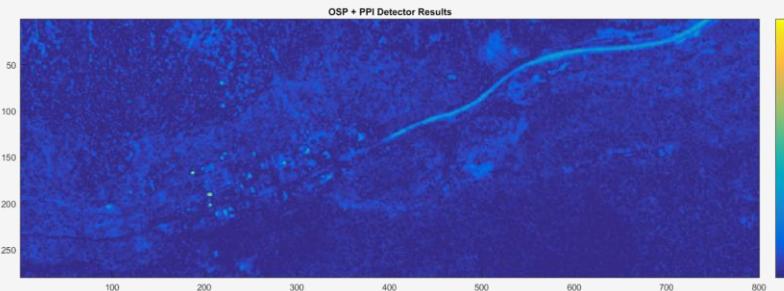
Fabric 3

Result of Structured Method

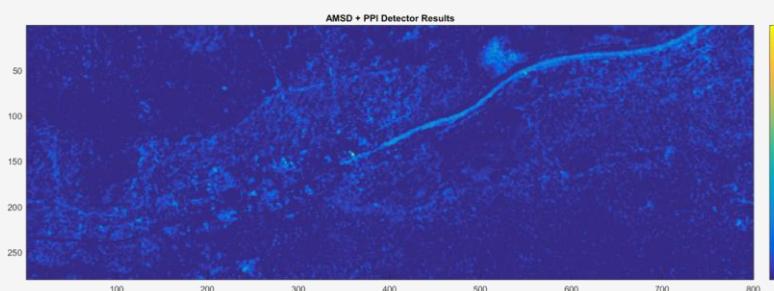
Detector Map



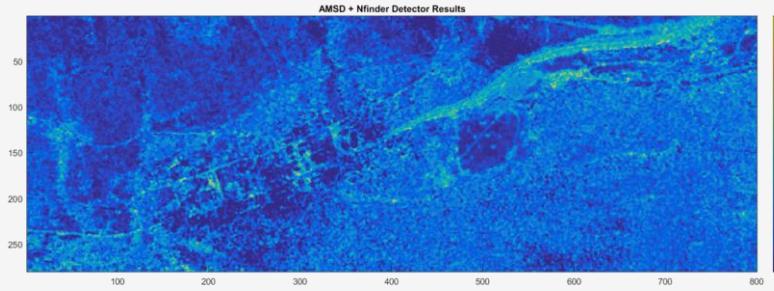
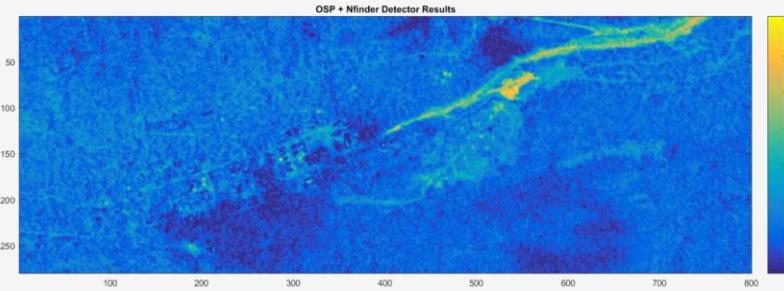
OSP



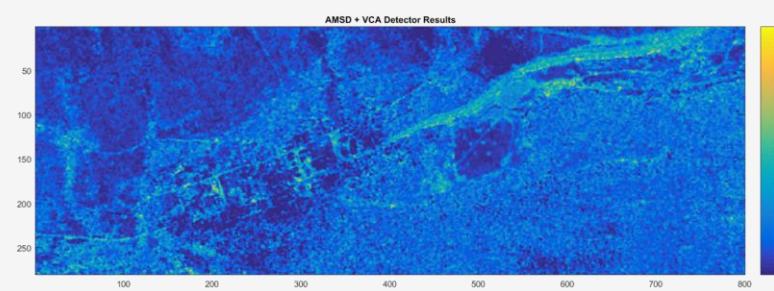
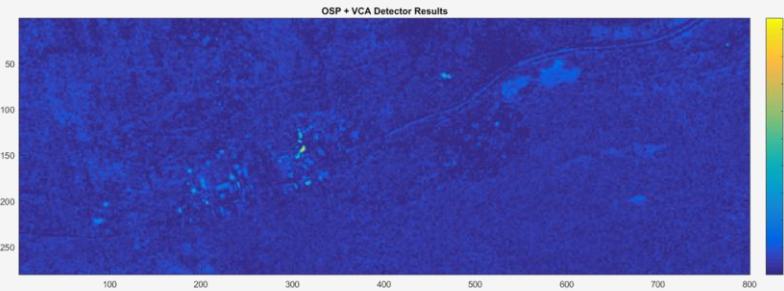
AMSD



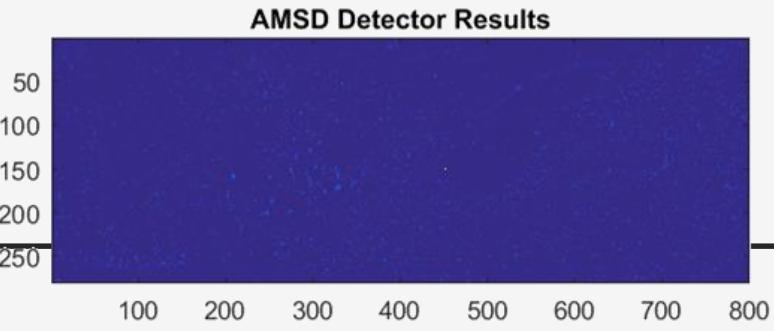
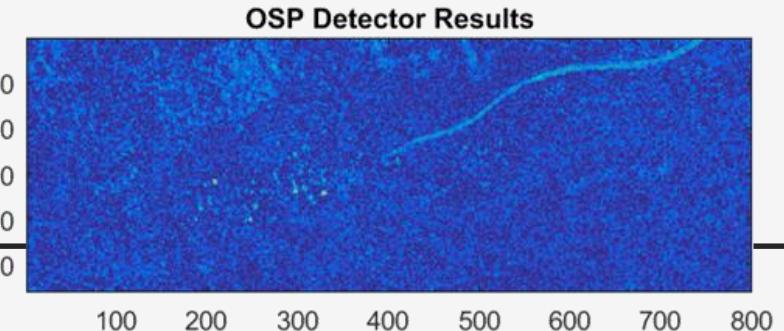
NFINDER



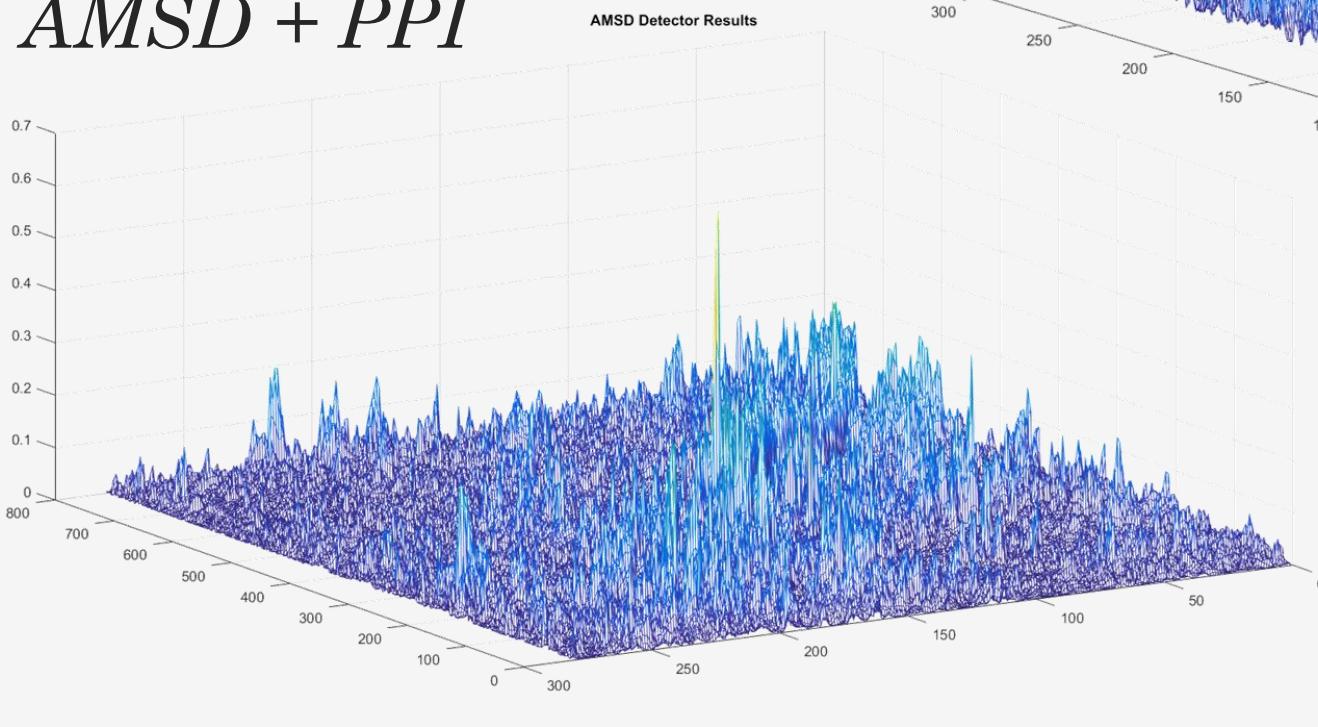
VCA



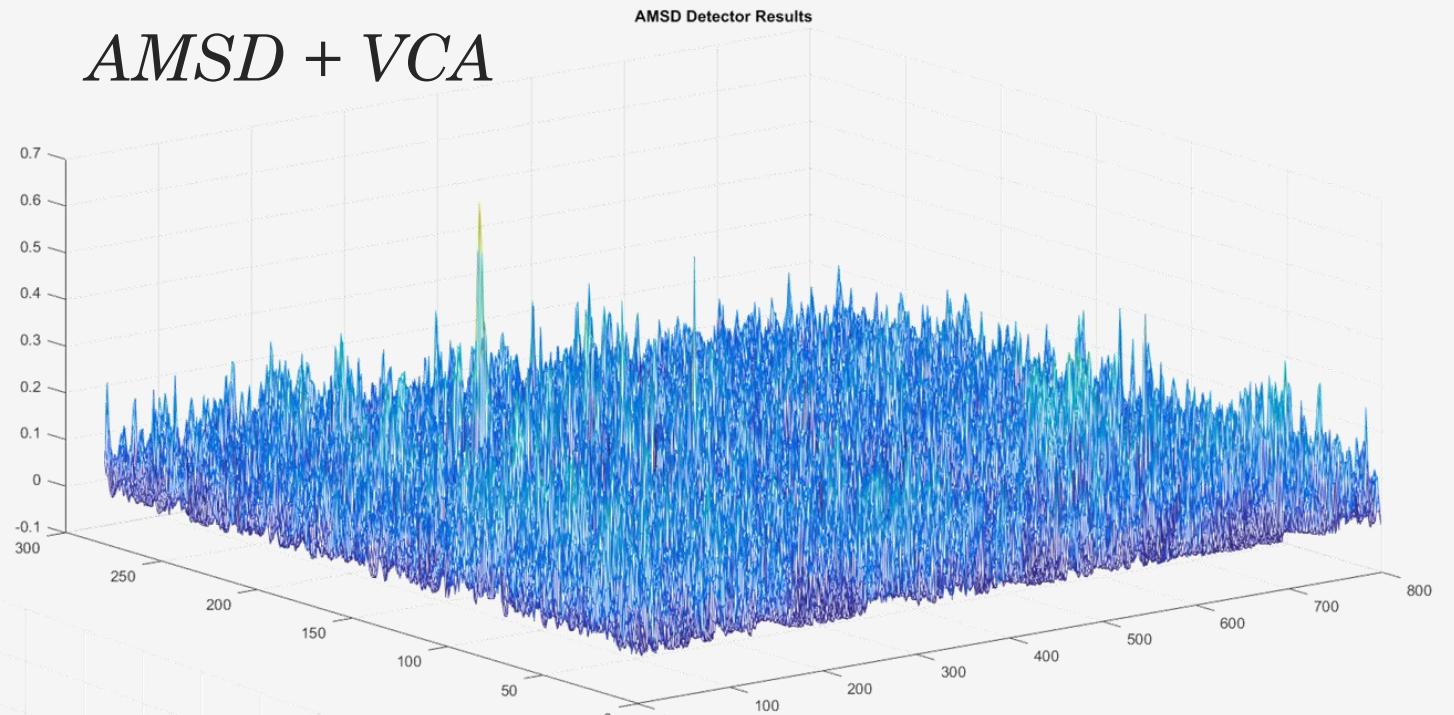
ATGP



AMSD + PPI

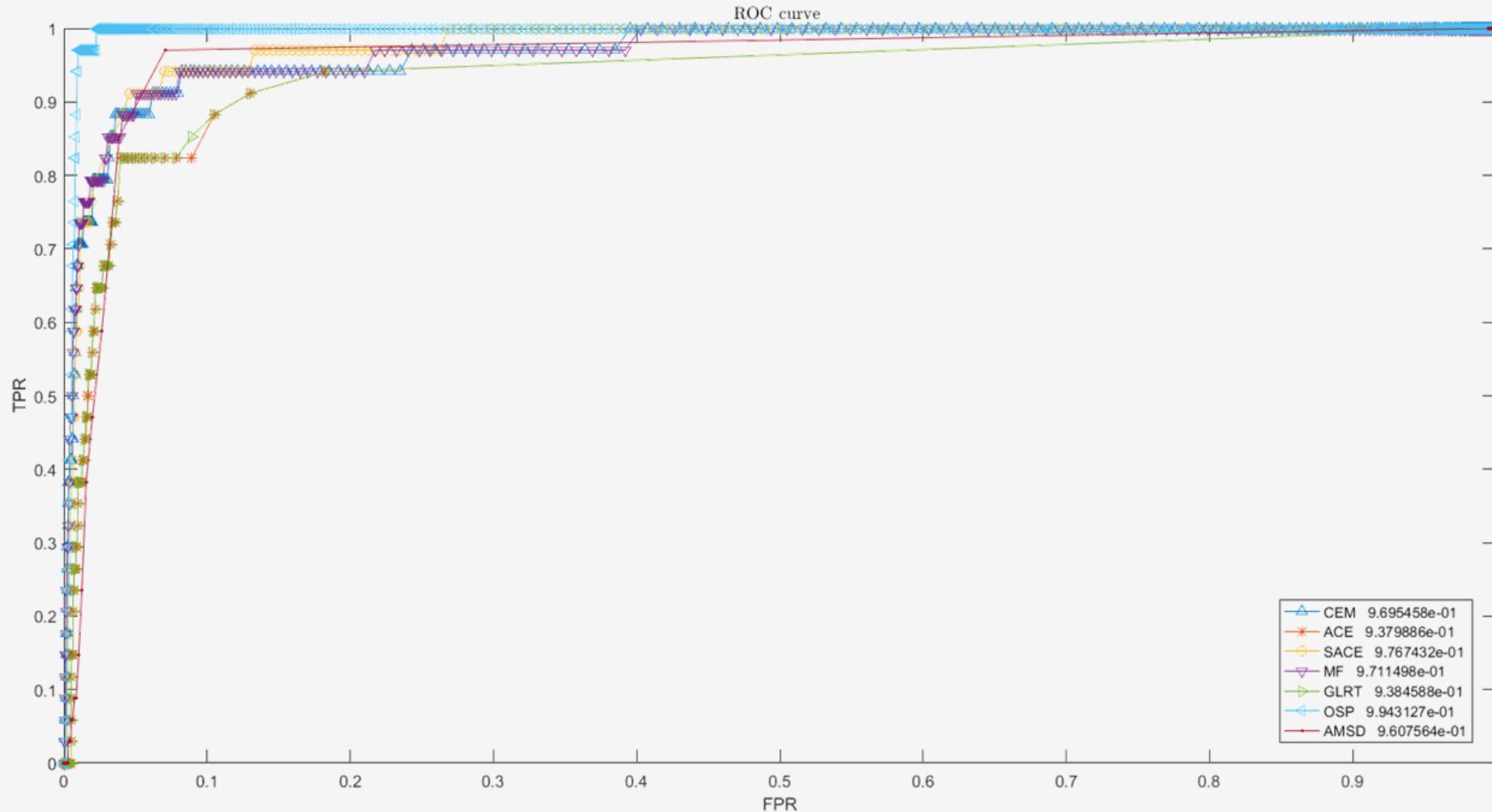


AMSD + VCA



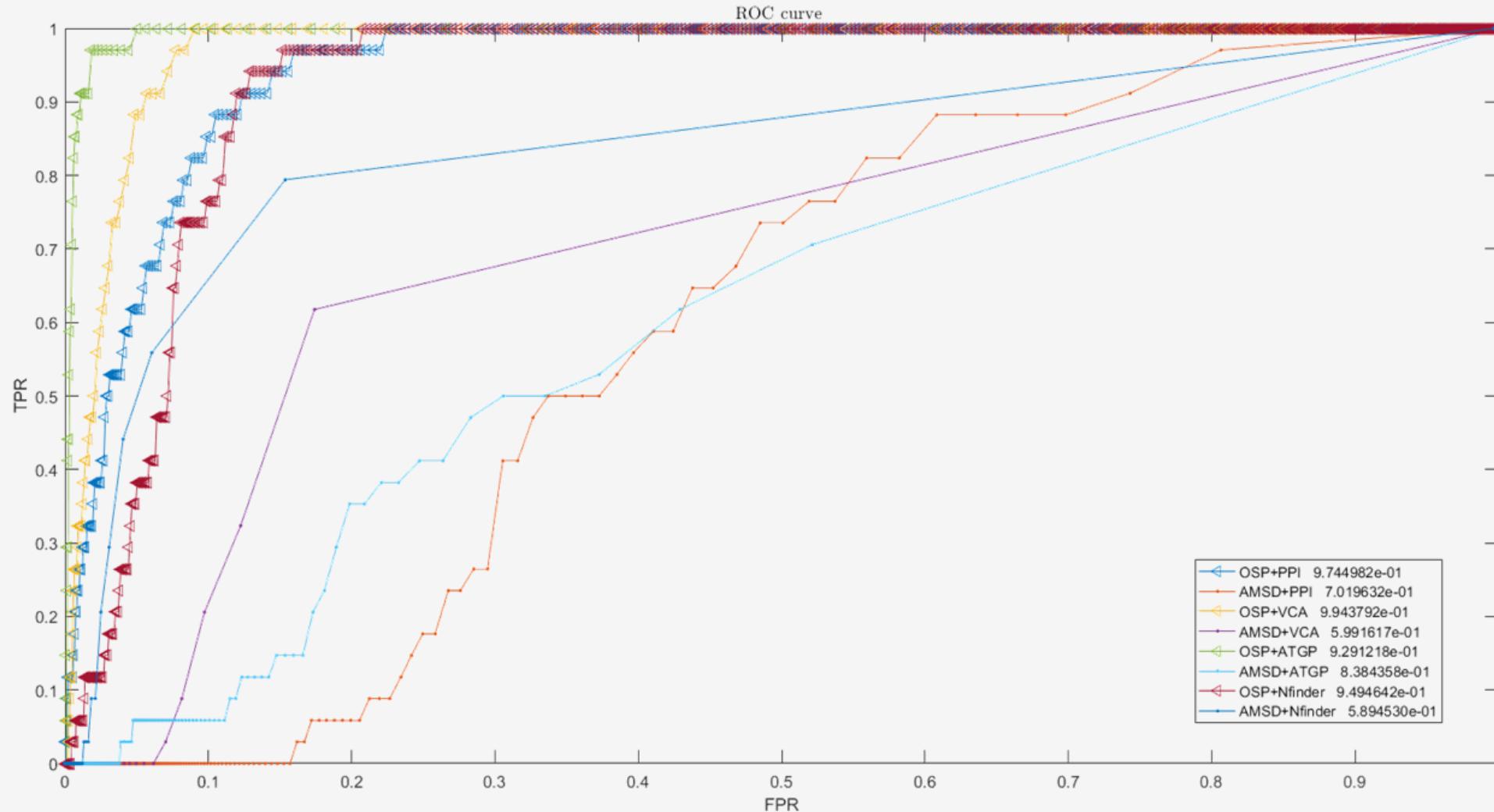
- Result of Unstructured Method
- Detector Map

Fabric 3



- ROC curve of Fabric 3 data for 1000 different thresholds
- The AUC of each curve calculated

Fabric 3



- ROC curve of Fabric 3 data for 1000 different thresholds
- AUC for OSP is higher than AMSD method

Fabric 3

Method	AUC	ACC	PPV* 10^{-3}
OSP+PPI	<u>0.9744</u>	0.7278	0.2217
AMSD+PPI	0.7019	<u>0.9973</u>	0.1517
OSP+VCA	0.9943	0.7307	0.9185
AMSD+VCA	0.5991	<u>0.9890</u>	0.1517
OSP+ATGP	<u>0.9291</u>	0.5822	0.1716
AMSD+ATGP	0.8384	0.2211	0.1517
OSP+Nfinder	<u>0.9494</u>	0.6369	0.2783
AMSD+Nfinder	0.5894	<u>0.9738</u>	0.1517

Method	AUC	ACC	PPV* 10^{-3}
CEM	0.970	0.5677	0.5795
ACE	0.938	0.9964	0.2292
SACE	0.977	0.6325	0.4180
MF	0.972	0.5763	0.6742
GLRT	0.939	0.9964	0.2298
OSP	0.995	0.5822	0.1716
AMSD	0.961	0.2211	0.1517

- For FABRIC3 data, it is observed that the AUC parameter for the OSP method was the highest when the VCA approach was used. In general, the area under the ROC curve for the OSP method is higher, However the overall accuracy of the AMSD method is higher, and therefore the third parameter, PPV, represents the optimal method, the OSP + VCA method.and as you on detector maps OSP+Nfinder has good results.

Result of OTSU Threshold Selection

Method	Fabric 2	Fabric 3	Vehicle 1
CEM	0.0028	0.0035	0.0032
ACE	0.0182	0.0183	0.0150
S-ACE	0.0166	0.0155	0.0122
MF	0.0027	0.0035	0.0032
GLRT	0.0180	0.0181	0.0149
OSP	0.0064	0.0011	0.0068
AMSD	0.0783	0.0648	0.0903
OSP+PPI	0.0103	0.0019	0.0078
AMSD+PPI	0.1611	0.0404	0.0565
OSP+Nfinder	0.0329	0.0029	0.0260
AMSD+Nfinder	0.1561	0.2872	0.1648
OSP+VCA	0.0086	0.0085	0.0312
AMSD+VCA	0.1258	0.0720	0.1628

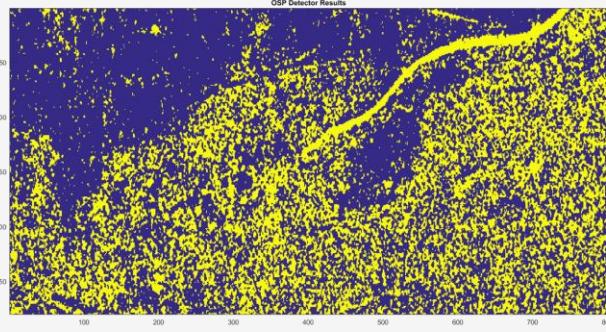
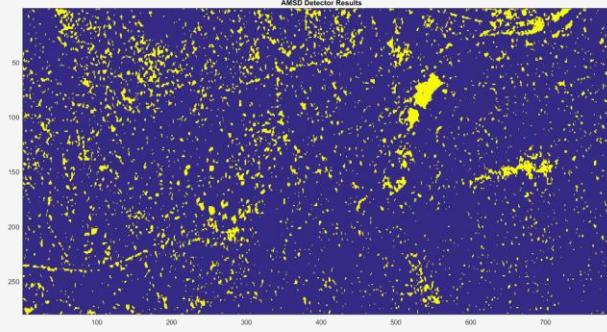
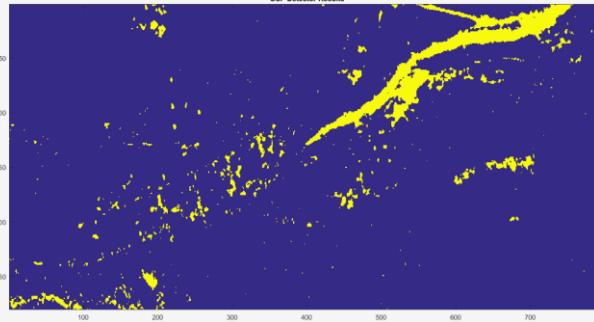
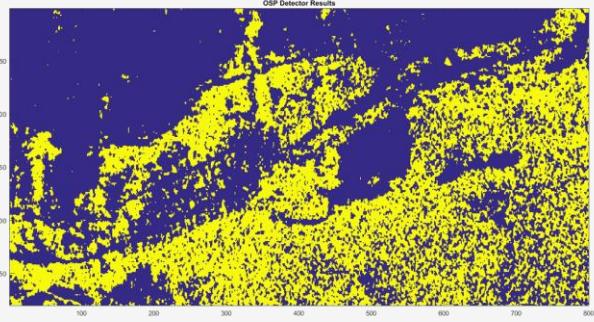
PPI

NFINDER

VCA

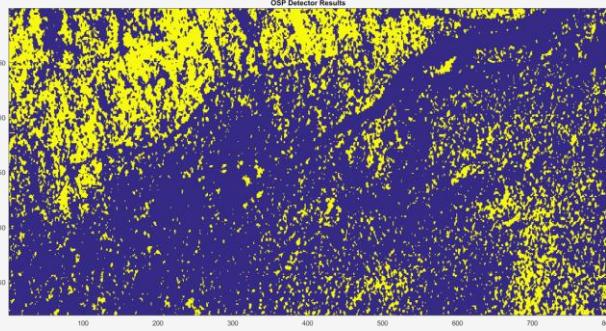
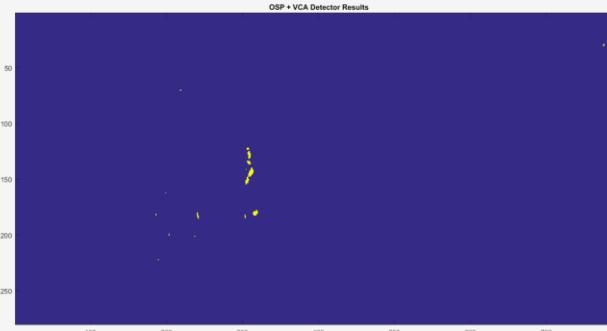
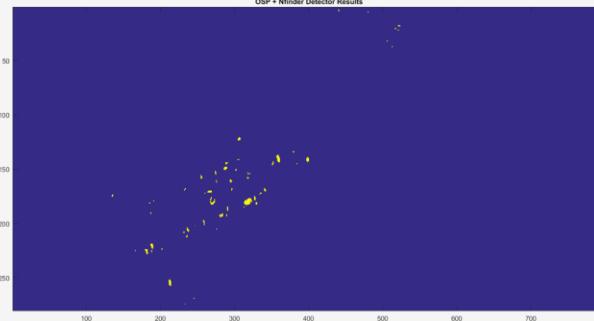
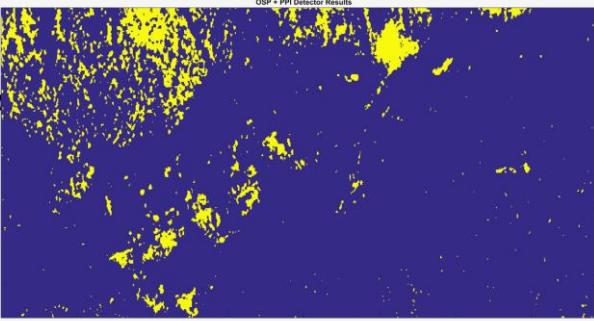
ATGP

Fabric 2



$$T = 0.0064$$

Fabric 3



$$T = 0.0011$$

Threshold Selection Result on OSP Method

- This algorithm seems to work optimistically or because the amount of target data is small, this algorithm has low accuracy

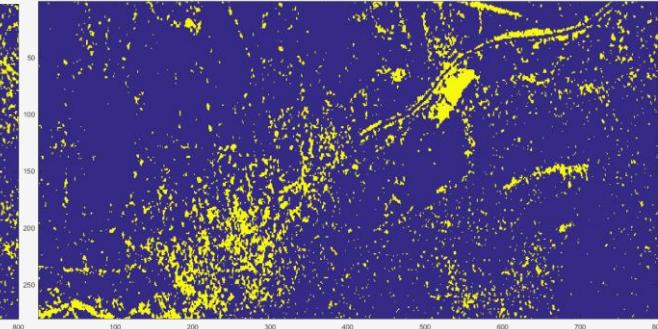
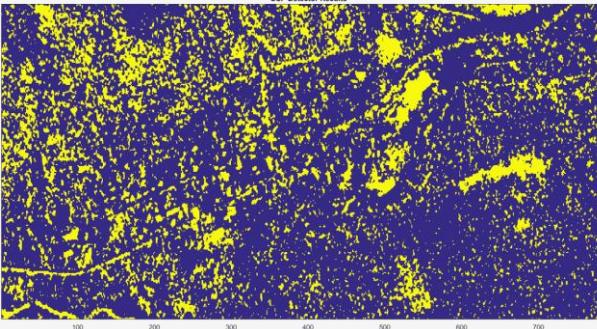
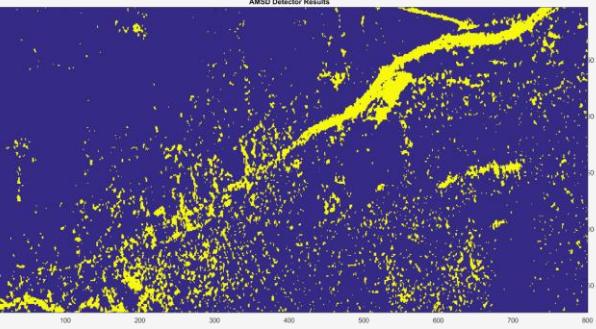
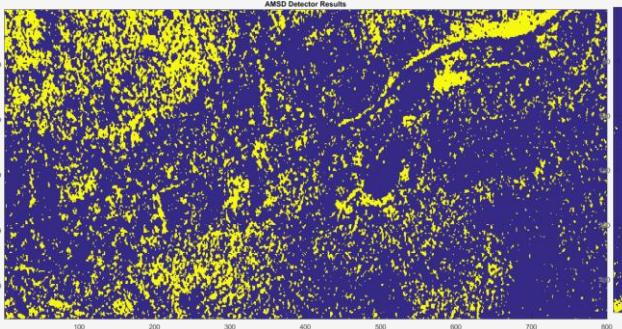
PPI

NFINDER

VCA

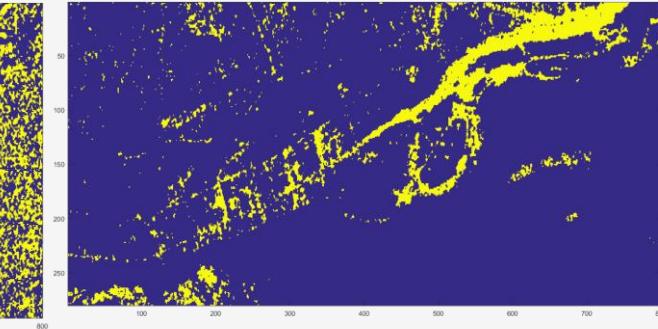
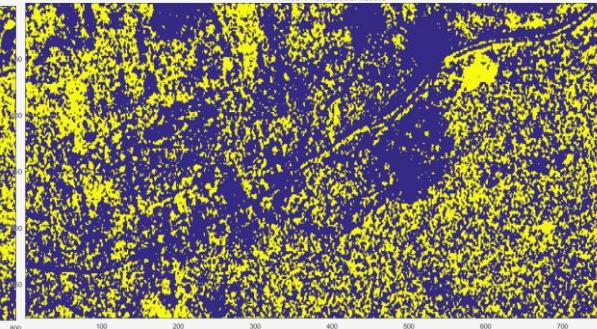
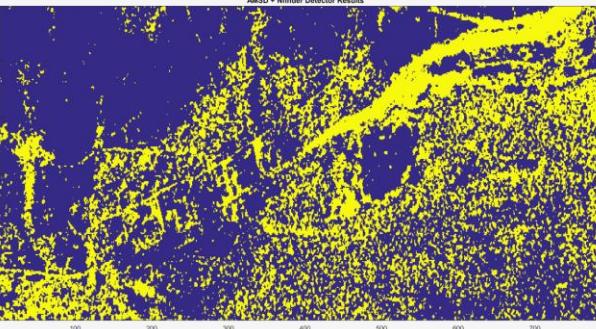
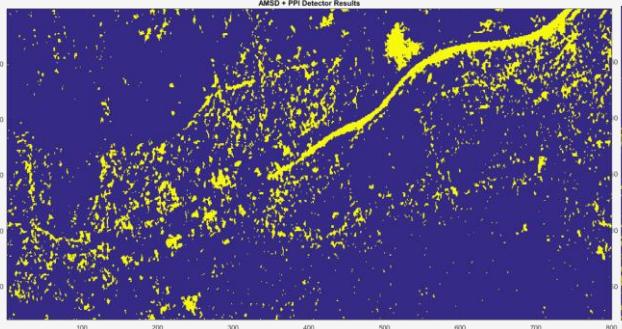
ATGP

Fabric 2



$$T = 0.0064$$

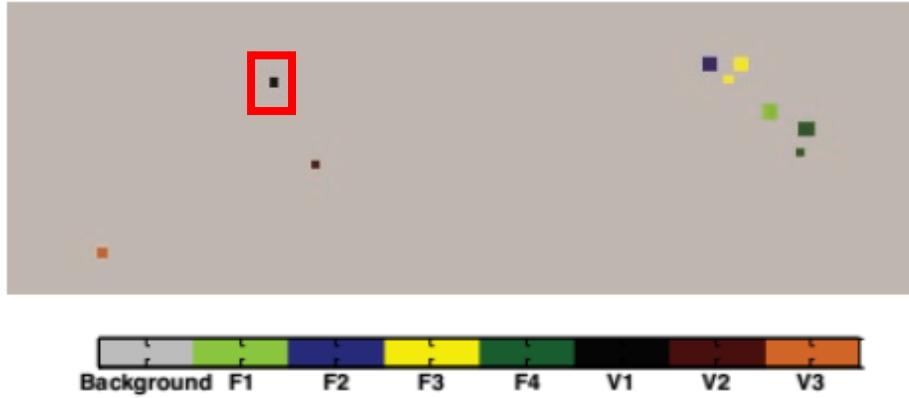
Fabric 3



$$T = 0.0011$$

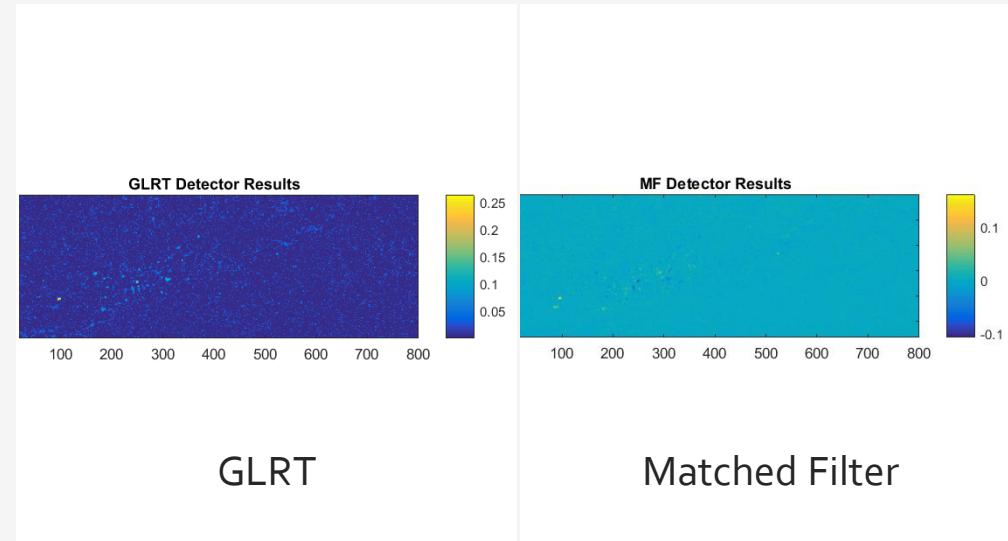
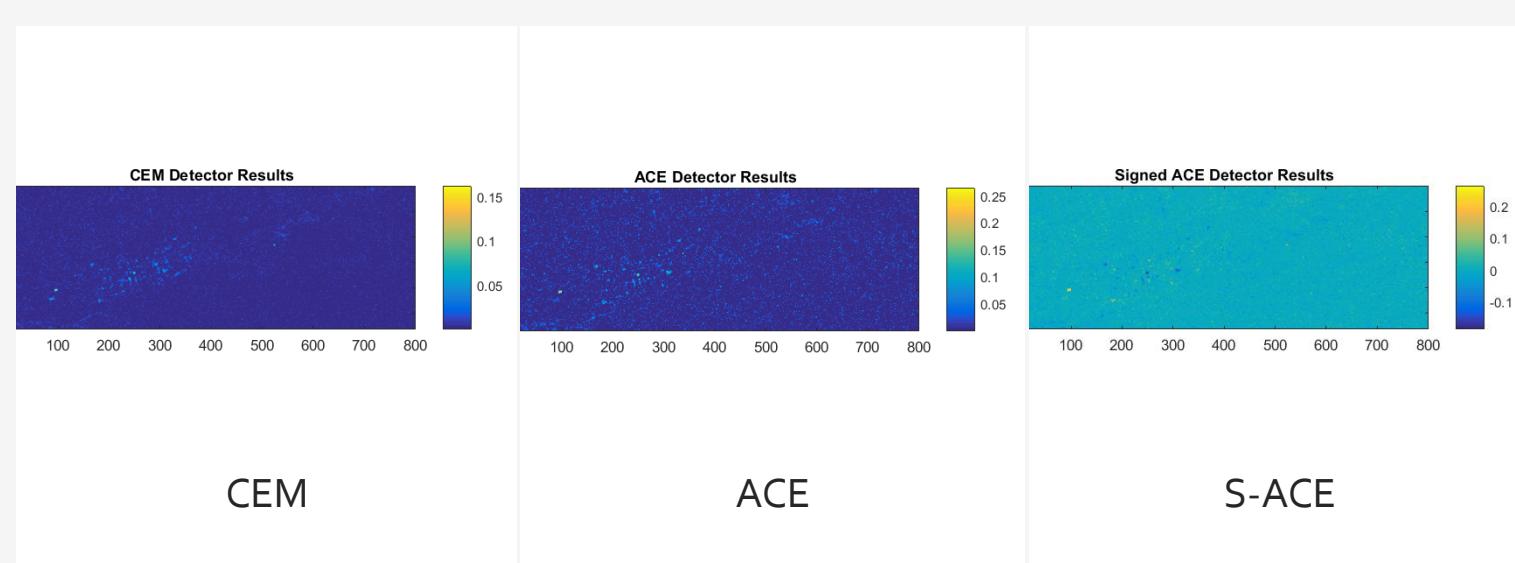
Threshold Selection Result on AMSD Method

- This algorithm seems to work optimistically or because the amount of target data is small, this algorithm has low accuracy

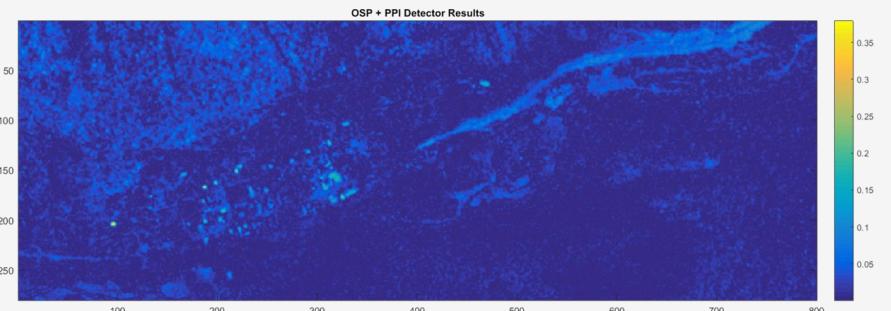


Vehicle 1

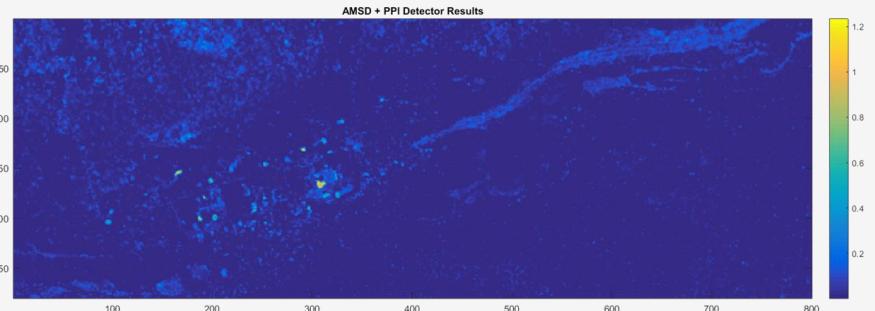
Result of Structured Method
Detector Map



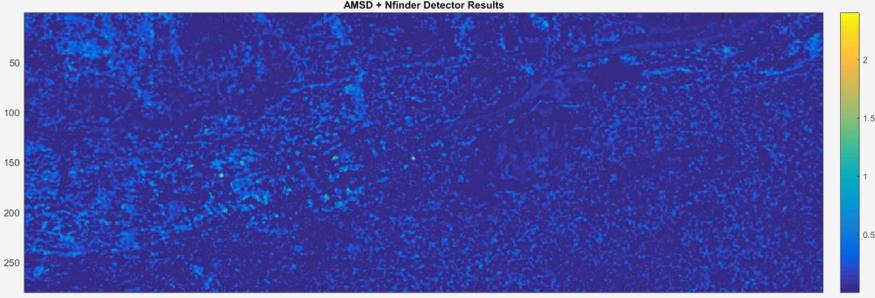
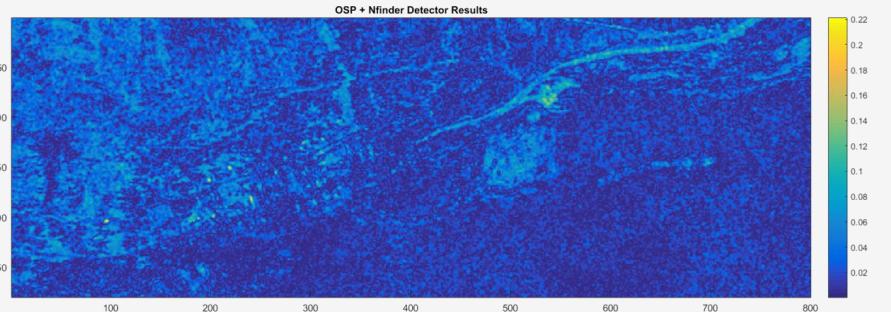
OSP



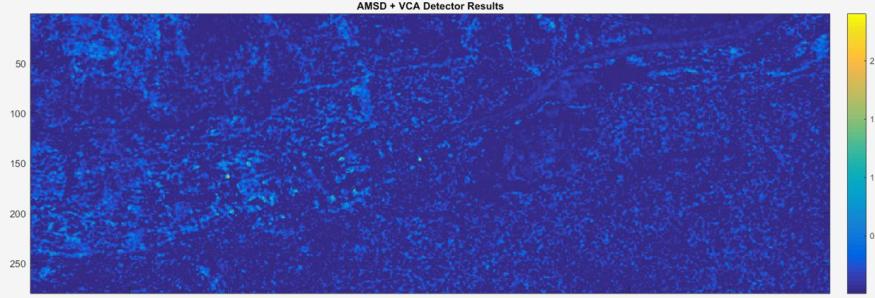
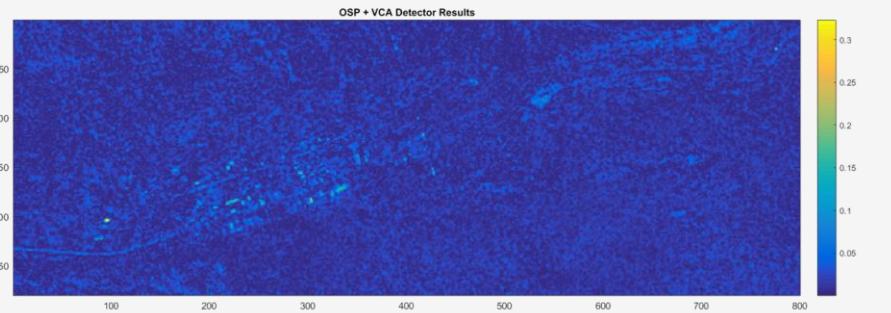
AMSD



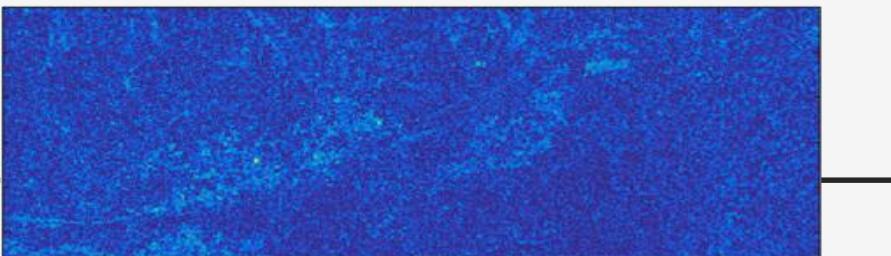
NFINDER



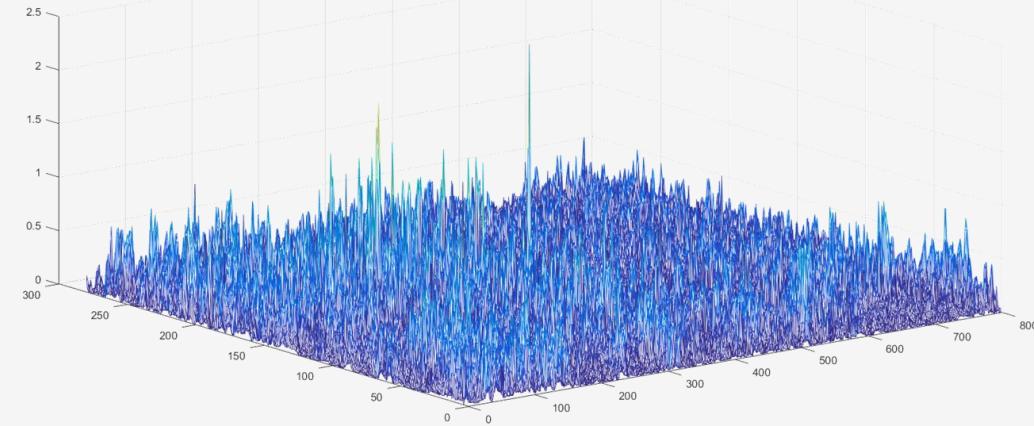
VCA



ATGP

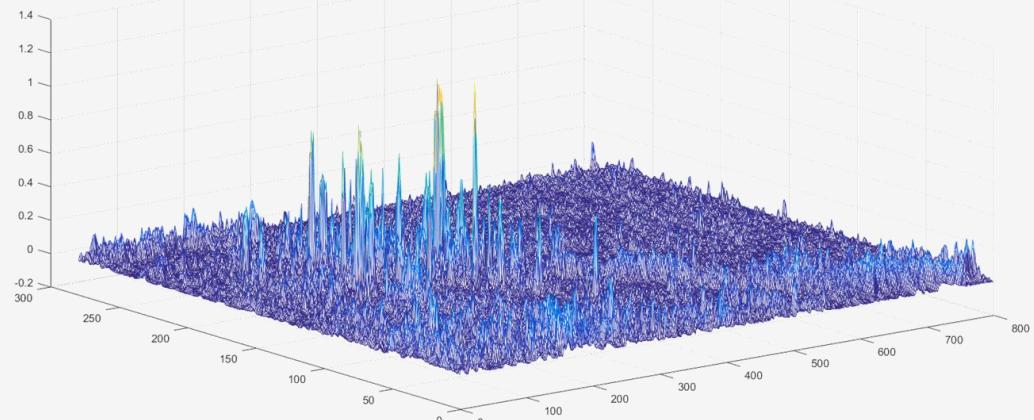


AMSD Detector Results



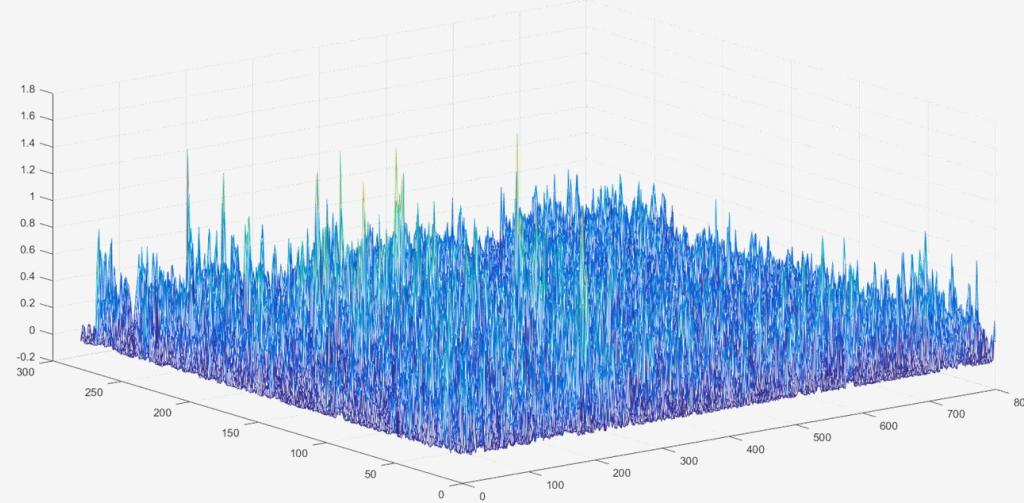
AMSD + Nfinder

AMSD Detector Results



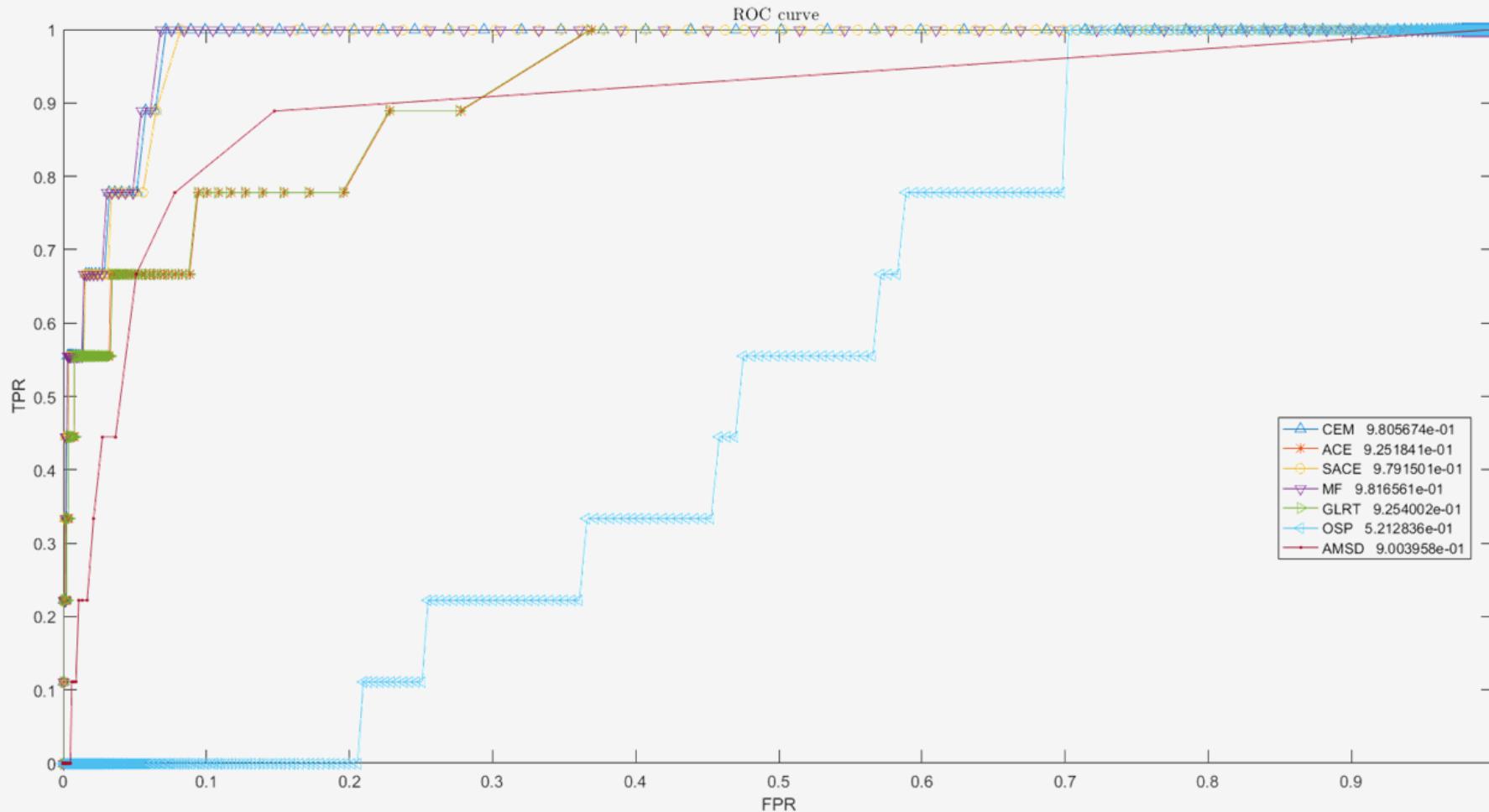
AMSD + PPI

AMSD Detector Results



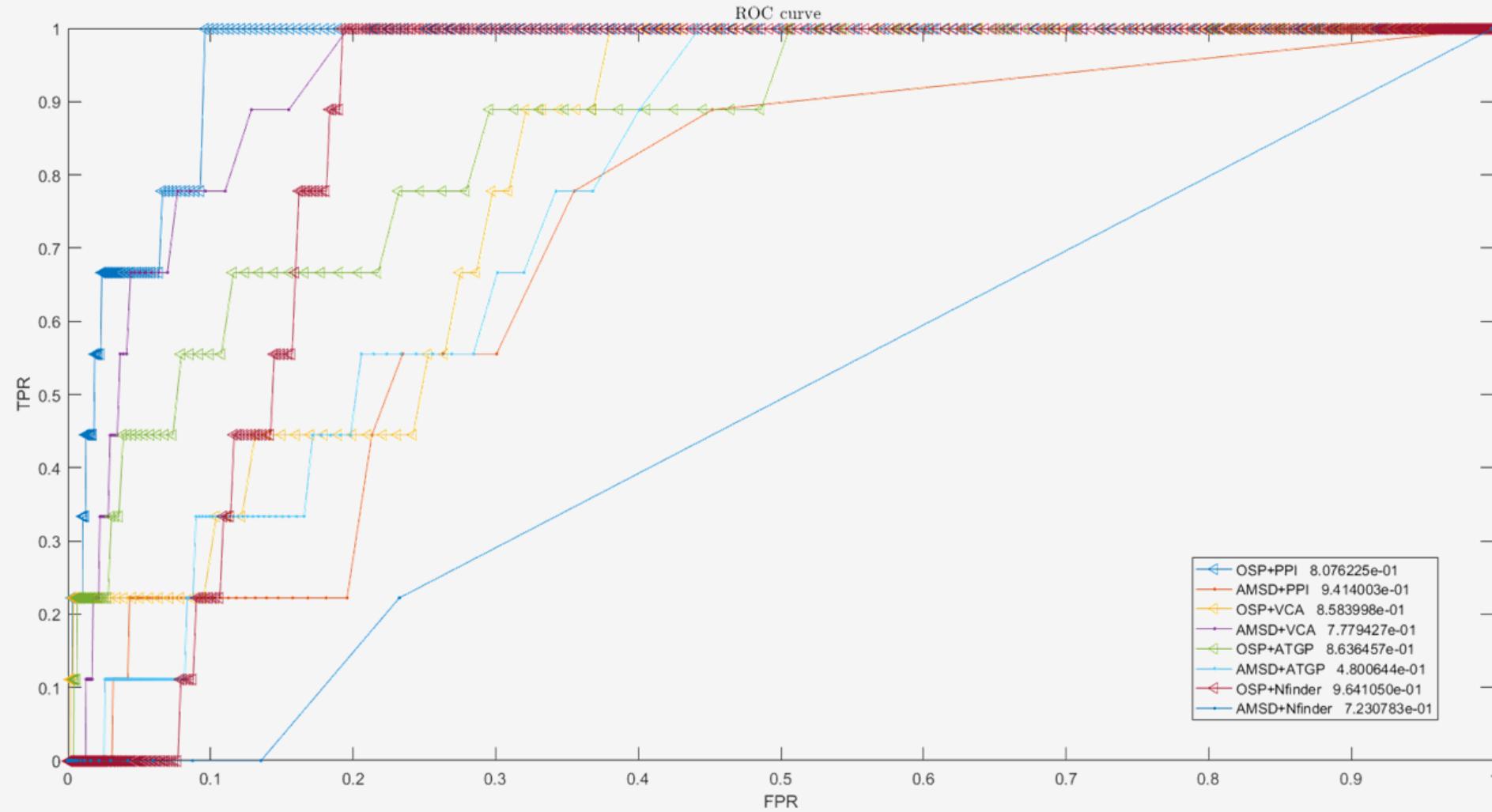
AMSD + VCA

Vehicle 1



- ROC curve of Vehicle 1 data for 1000 different thresholds
- The AUC of each curve calculated

Vehicle 1



- ROC curve of Vehicle 1 data for 1000 different thresholds
- The AUC of each curve calculated

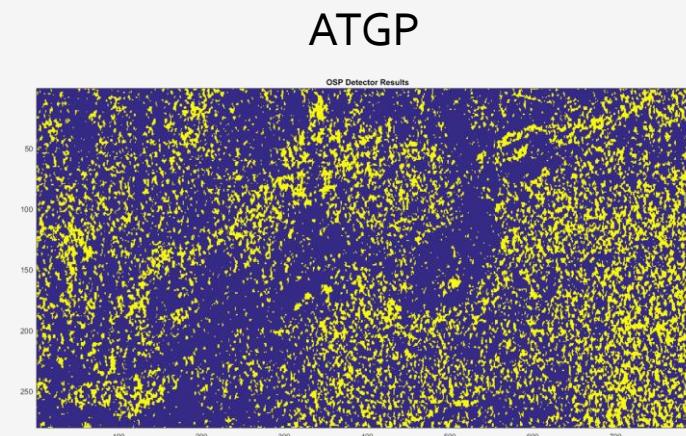
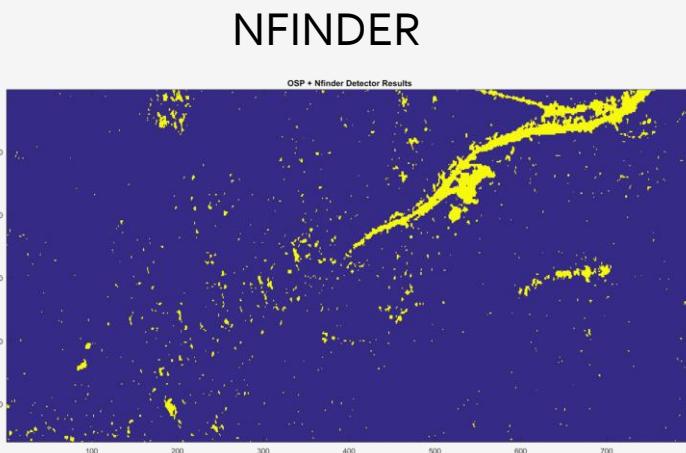
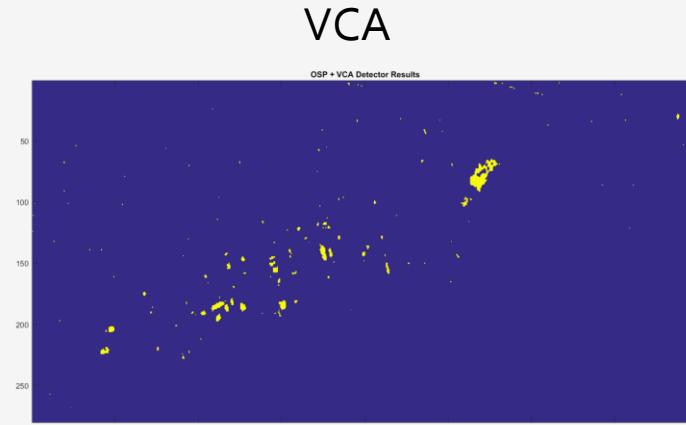
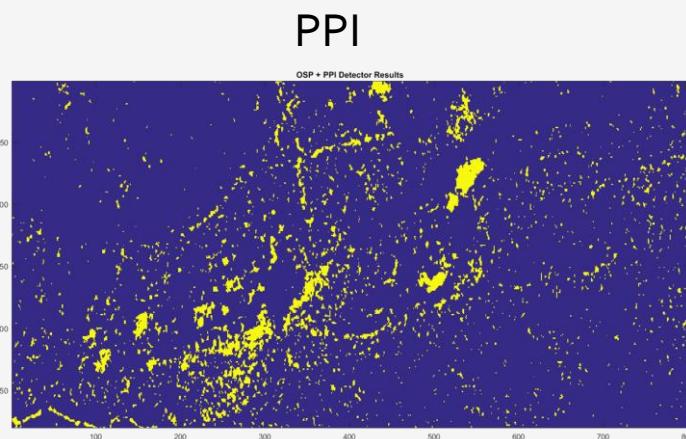
Vehicle 1

Method	AUC	ACC	PPV* 10^{-3}
OSP+PPI	0.8076	0.5635	0.3261
AMSD+PPI	0.9414	0.9964	0.0919
OSP+VCA	0.8583	0.6557	0.160
AMSD+VCA	0.7779	0.9856	0.0458
OSP+ATGP	0.8636	0.6558	0.0589
AMSD+ATGP	0.4800	0.8323	0.0401
OSP+Nfinder	0.9641	0.5750	0.3695
AMSD+Nfinder	0.7230	0.9921	0.0405

Method	AUC	ACC	PPV* 10^{-3}
CEM	0.981	0.6205	5.63
ACE	0.926	0.9945	31.77
SACE	0.980	0.6210	55.55
MF	0.982	0.6211	5.84
GLRT	0.926	0.9946	31.74
OSP	0.522	0.6558	0.0589
AMSD	0.901	0.8323	0.0401

Result of OTSU Threshold Selection

Method	Fabric 2	Fabric 3	Vehicle 1
CEM	0.0028	0.0035	0.0032
ACE	0.0182	0.0183	0.0150
S-ACE	0.0166	0.0155	0.0122
MF	0.0027	0.0035	0.0032
GLRT	0.0180	0.0181	0.0149
OSP	0.0064	0.0011	0.0068
AMSD	0.0783	0.0648	0.0903
OSP+PPI	0.0103	0.0019	0.0078
AMSD+PPI	0.1611	0.0404	0.0565
OSP+Nfinder	0.0329	0.0029	0.0260
AMSD+Nfinder	0.1561	0.2872	0.1648
OSP+VCA	0.0086	0.0085	0.0312
AMSD+VCA	0.1258	0.0720	0.1628

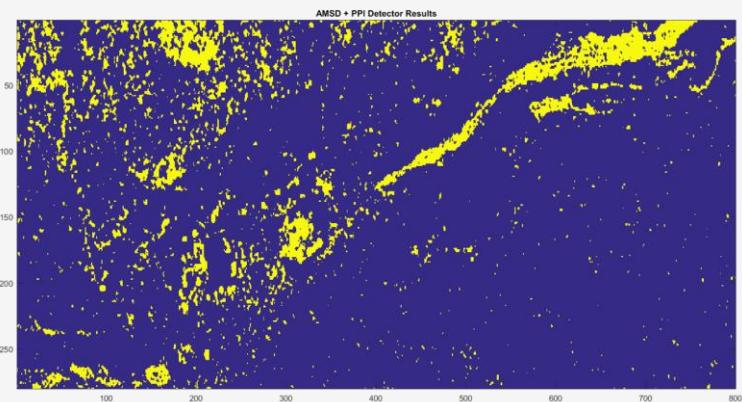


Threshold Selection Result on OSP Method

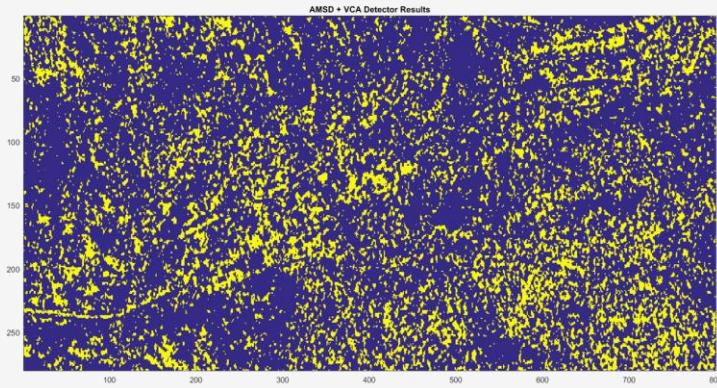
- This algorithm seems to work optimistically or because the amount of target data is small, this algorithm has low accuracy

Vehicle 1

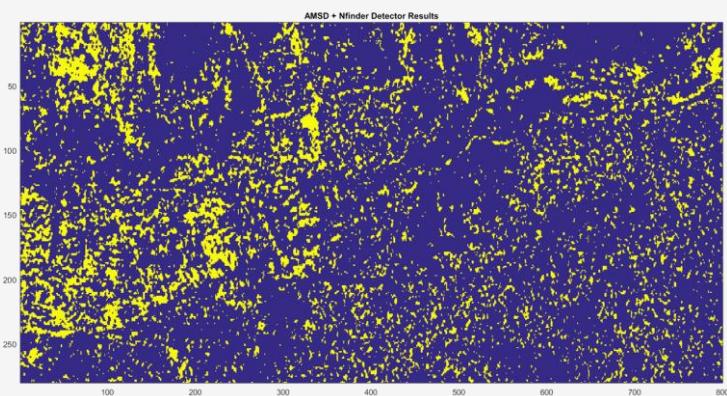
PPI



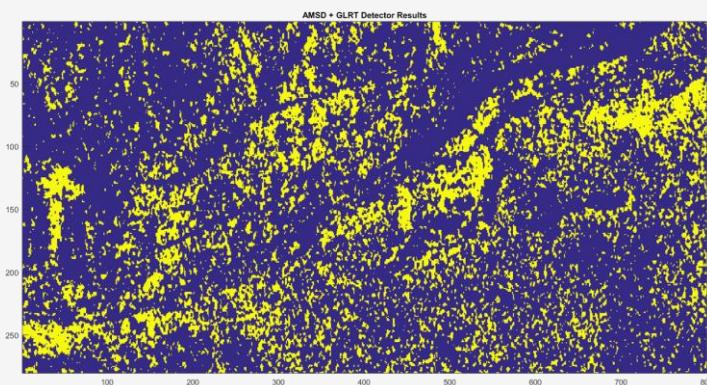
VCA



NFINDER



ATGP



Threshold Selection Result on AMSD Method

52

- This algorithm seems to work optimistically or because the amount of target data is small, this algorithm has low accuracy

Thank You

 Faezeh Zamiri

 aghdam.zamiri.fa@ut.ac.ir

 [Linkedin.com/in/faezeh-Zamiri-1b51081bb](https://www.linkedin.com/in/faezeh-zamiri-1b51081bb)

 09224015584

The End

References for code ,data and results:

<https://github.com/FaezehZamiri/Hyperspectralremotesensing/>