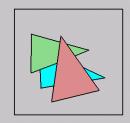




Hidden Surface Removal



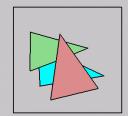
Visible Surface

- Problem: Given a set of 3D objects and a viewing specification, determine which lines or surfaces are visible
- This is called visible surface(line) determination, or hidden surface(line) removal
- Two general approaches:
 - Image precision
 - Object precision



Invisible Primitives

- Why might a polygon be invisible?
 - Polygon outside the field of view
 - Polygon is backfacing
 - Polygon is occluded by object(s) nearer the viewpoint
- For efficiency reasons, we want to avoid spending work on polygons outside field of view or backfacing
- For efficiency and correctness reasons, we need to know when polygons are occluded



HSR algo classes

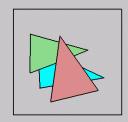
Three classes of algorithms

- "Conservative" visibility testing: only trivial reject does not give final answer!
 - e.g., back-face culling, canonical view volume clipping, spatial subdivision
 - have to feed results to algorithms mentioned below
- Image precision resolve visibility at discrete points in image
 - sample model, then resolve visibility i.e., figure out which objects it makes sense to compare with
 - e.g., ray tracing, or Z-buffer and scan-line algo.
- Object precision resolve for all possible view directions from a given eye point
 - irrespective of view direction or sampling density
 - resolve visibility exactly, then sample the results
 - e.g., 3-D depth sort, BSP trees

Image Precision

for each pixel in the image
determine the closest object pierced by
the ray through the pixel
draw the pixel in the appropriate color

- Brute force approach:
 - For each pixel, examine all n objects, find which is closest
- O(np) where p = #pixels
- Needs to be redone if the image is resized



Object Precision

for each object in the world

determine the parts of the object that

are unobscured by other parts

of it or other objects

draw those parts in the appropriate color

Brute force approach:

For each object, examine all n objects $O(n^2)$

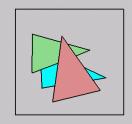
 $n \le p$, so this seems good...

But each computation much more expensive Tends to be slower in practice

Outline



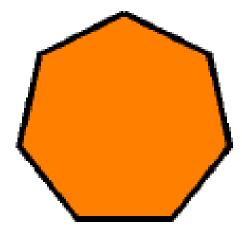
- 1. Back- Face Culling
- 2. z- Buffer (Depth- Buffer)
- 3. Depth- Sort
- 4. BSP- Tree
- 5. Scanline Algorithm

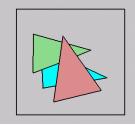


Back Face Culling

Back-face culling addressing a special case of occlusion called convex self-occlusion. Basically, if an object is closed (having a well defined inside and outside) then some parts of the outer surface must be blocked by other parts of the same surface. We'll be more precise with our definitions in a minute. On such surfaces we need only consider the normals of surface elements to determine if they are invisible.







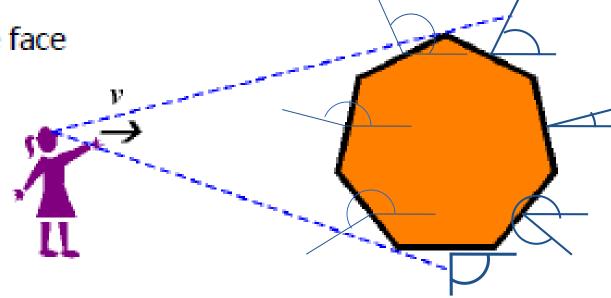
Removing Back Faces

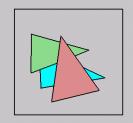
Idea: Compare the normal of each face with the viewing direction

Given n, the outward-pointing normal of F

foreach face F of object if (n·v > 0) throw away the face

Does it work?



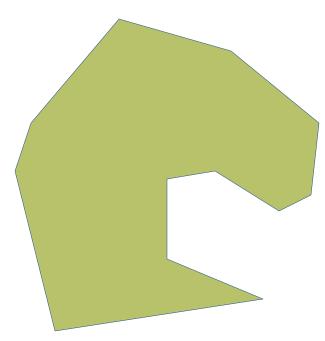


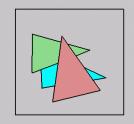
Back-Face Culling

On the surface of a closed manifold, polygons whose normals point away from the camera are always occluded:

Plane Normal ■ (Point on plane - COP) > 0 ----- Backface

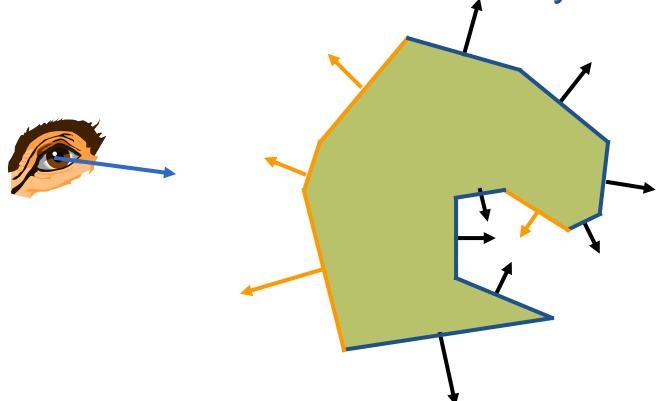


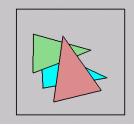




Back-Face Culling

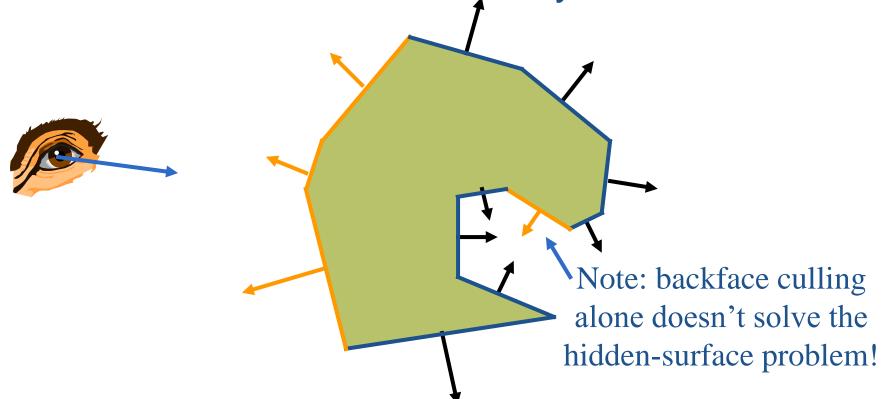
 On the surface of a closed manifold, polygons whose normals point away from the camera are always occluded:

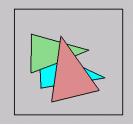




Back-Face Culling - Problems

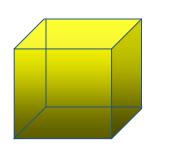
 On the surface of a closed manifold, polygons whose normals point away from the camera are always occluded:

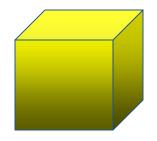


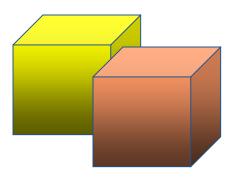


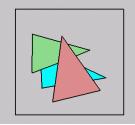
Back-Face Culling - Problems

one polyhedron may obscure another







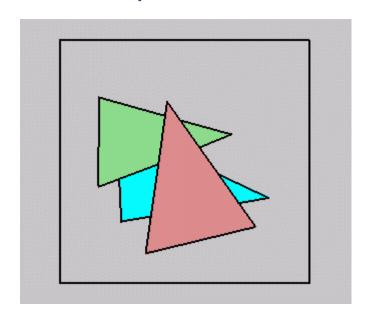


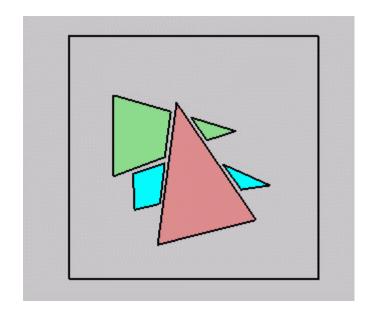
Back-Face Culling - Advantages

- On average, approximately one-half of a polyhedron's polygons are back-facing.
- Back-Face culling halves the number of polygons to be considered for each pixel in an image precision algorithm.

Occlusion

For most interesting scenes, some polygons will overlap:





 To render the correct image, we need to determine which polygons occlude which



Painters Algorithm

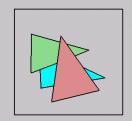
A Painter's Algorithm

The painter's algorithm, sometimes called depth-sorting, gets its name from the process which an artist renders a scene using oil paints. First, the artist will paint the background colors of the sky and ground. Next, the most distant objects are painted, then the nearer objects, and so forth. Note that oil paints are basically opaque, thus each sequential layer completely obscures the layer that its covers.

A very similar technique can be used for rendering objects in a threedimensional scene. First, the list of surfaces are sorted according to their distance from the viewpoint. The objects are then painted from back-tofront.

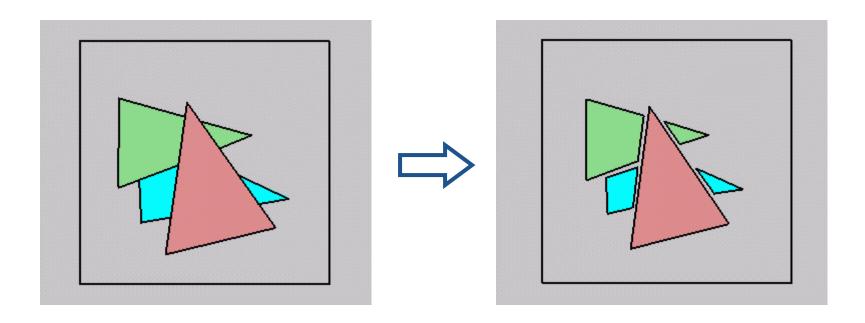
While this algorithm seems simple there are many subtleties. The first issue is which depth-value do you sort by? In general a primitive is not entirely at a single depth. Therefore, we must choose some point on the primitive to sort by.

The second secon

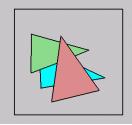


Painter's Algorithm

Simple approach: render the polygons from back to front, "painting over" previous polygons:



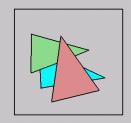
- Draw blue, then green, then pink
- Will this work in general?



Painter's Algorithm: Problems

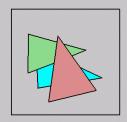
- Intersecting polygons present a problem
- Even non-intersecting polygons can form a cycle with no valid visibility order:





Z-Buffer – Image Precision

- Requires two "buffers"
 - **Intensity Buffer**
 - —our familiar RGB pixel buffer
 - —initialized to background color
 - Depth ("Z") Buffer
 - —depth of scene at each pixel
 - —initialized to far depth
- Polygons are scan-converted in arbitrary order. When pixels overlap, use Z-buffer to decide which polygon "gets" that pixel



Algorithm:

- Initialize:
 - Each z- buffer cell ← Max z value
 - Each frame buffer cell ← background color
- For each polygon:
 - Compute z(x, y), polygon depth at the pixel (x, y)
 - If z(x, y) < z buffer value at pixel (x, y) then
 - $z \text{ buffer}(x, y) \leftarrow z(x, y)$
 - $pixel(x, y) \leftarrow color of polygon at (x, y)$



Z-Buffer

255	255	255	255	255	255	255	255		127	127	127	127	127	127	12 7		127	127	127	127	127	127	127	255
255	255	255	255	255	255	255	255	+	127	127	127	127	127	127			127	127	127	127	127	127	255	255
255	255	255	255	255	255	255	255		127	127	127	127	127				127	127	127	127	127	255	255	255
255	255	255	255	255	255	255	255		127	127	127	127				_	127	127	127	127	255	255	255	255
255	255	255	255	255	255	255	255		127	127	127		ı			_	127	127	127	255	255	255	255	255
255	255	255	255	255	255	255	255		127	127							127	127	255	255	255	255	255	255
255	255	255	255	255	255	255	255		127								127	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255										255	255	255	255	255	255	255	255
127	127	127	127	127	127	127	255	+									127	127	127	127	127	127	127	255
127	127	127	127	127	127	255	255										127	127	127	127	127	127	255	255
127	127	127	127	127	255	255	255										127	127	127	127	127	255	255	255
127	127	127	127	255	255	255	255		128								127	127	127	127	255	255	255	255
127	127	127	255	255	255	255	255		127	127						=	127	127	127	255	255	255	255	255
127	127	255	255	255	255	255	255		120	120	120						120	120	120	255	255	255	255	255
127	255	255	255	255	255	255	255		115	115	115	115					115	115	115	115	255	255	255	255
255	255	255	255	255	255	255	255		115	115	115	115	115				115	115	115	115	115	255	255	255

Above: example using integer Z-buffer with near = 0, far = 255

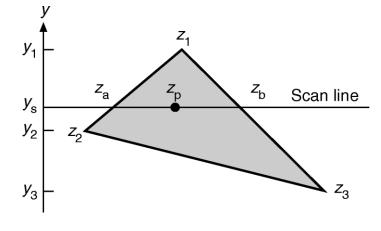


Computing Z values

- Interpolation along scan line
- Interpolation along edge
- How do we compute it efficiently?
 - Answer is simple: do it incrementally!
 - Remember scan conversion/polygon filling? As we move along Yaxis, track x position where each edge intersects scan-line

• do same thing for z coordinate using "remainder" calculations

with y-z slope

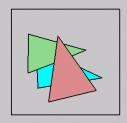


$$z_a = z_1 - (z_1 - z_2) \frac{y_1 - y_s}{y_1 - y_2}$$

Scan line
$$z_b = z_1 - (z_1 - z_3) \frac{y_1 - y_s}{y_1 - y_3}$$

$$z_p = z_b - (z_b - z_a) \frac{x_b - x_p}{x_b - x_a}$$

o Once we have $z_{\rm a}$ and $z_{\rm b}$ for each edge, can **incrementally** calculate $z_{\rm p}$ as we scan. Did something similar with calculating color per pixel in Gouraud shading



- Simplicity lends itself well to hardware implementations:
 - used by all graphics cards
- Polygons do not have to be compared in any particular order: no presorting in z necessary, big gain!
- Only consider one polygon at a time
- Z-buffer can be stored with an image; allows you to correctly composite multiple images (easy!) without having to merge models (hard!)
- Can be used for non-polygonal surfaces

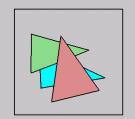


Z-Buffer: Disadvantages

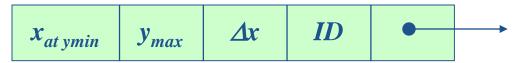
- A pixel may be drawn many times
 - A rough front to back depth sort can be performed
- High amount of memory required due to Z buffer
 - Image can be scan converted in strips, at the expense of multiple passes over the objects
- Lower precision for higher depth
 - Do not have enough precision for objects with millimeter detailed, positioned at kilometer apart
 - Shared edges of polyhedron where some visible pixels come from one polygon, and other come from neighbor



- Image precision algorithm
- Renders scene scan line by scan line
- Maintain various lists
 - Edge Table
 - Active Edge Table
 - Polygon Table
 - Active Polygon Table



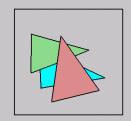
- Edge Table (ET)
 - Horizontal edges are ignored
 - Sorted into buckets based on each edge's smaller y-coordinate
 - Within buckets, edges are ordered by increasing x-coordinate of their lower end point



 $\Delta x = \Delta y/m \rightarrow used in stepping from one scan line to next$ $<math>\Delta y = 1$

Polygon Table (PT)

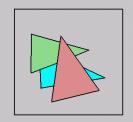


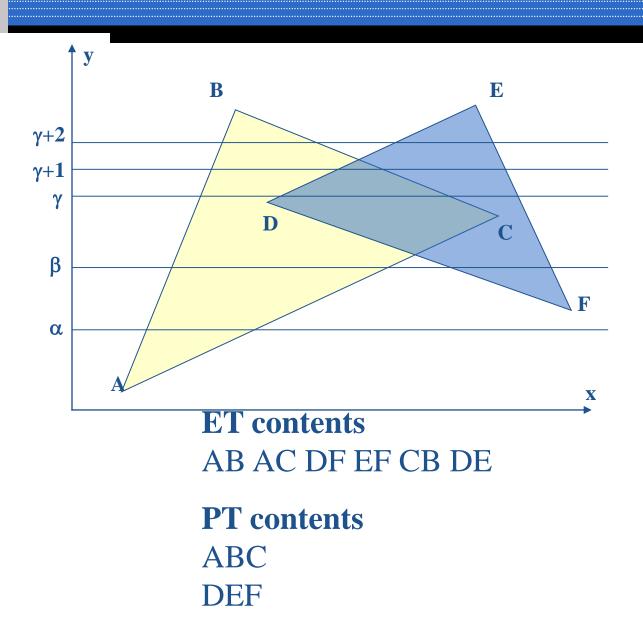


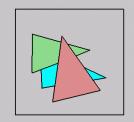
- Active Edge Table (AET)
 - Stores the list of edges intersecting current scanline in increasing order of current x-coordinate

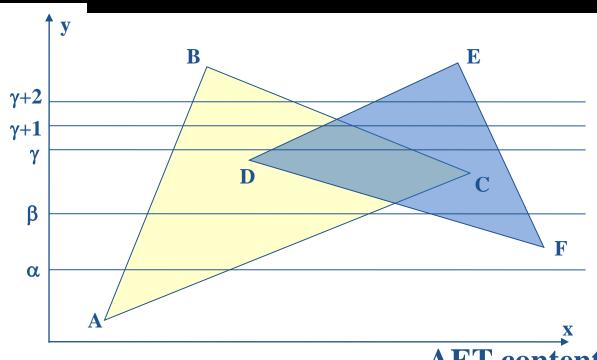


- Active Polygon Table (APT)
 - At each x-scan value this table contains the list of polygons whose in-out flag is set to true









AET contents

 $y_{max} \mid x_A \mid \Delta x \mid \bullet$

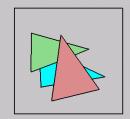
Scan line Entries

α ABAC

β ABACFD FE

 γ , γ +1 AB DE CB FE

γ+2ABCB DE FE



- Initialization
 - Initialize the AET to empty
 - Initialize each screen pixel to bk-color
 - Set y to the first nonempty cell value in edge table

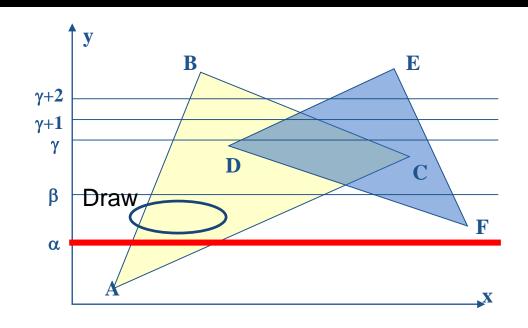
- For each scan line y do
 - AET ← AET∪ Edges from ET that are in current scanline
 - sort AET in order of increasing x_A
 - For each edge e (except last one) in AET do
 - invert in-out flag of the polygon that contains e
 - Update APT
 - Determine polygon p in APT with smallest z value at (e.x_A, y)
 - The pixels from **e** upto next edge in AET are set to the color of **p**
 - AET \leftarrow AET Edges from ET with $y_{max} = y$
 - for each edge e in AET do $\mathbf{e.x_A} = \mathbf{e.x_A} + \mathbf{e.\Delta x}$
 - Sort AET on x_A



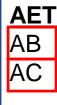
Simulation

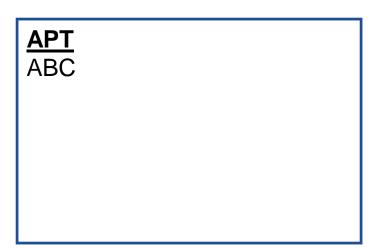
Toggle: ABC.inout=0→1

Toggle: ABC.inout=1→0



Draw up to next edge in AET







Simulation

Toggle: ABC.inout=0→1

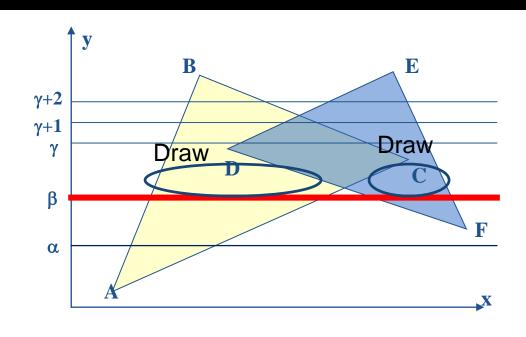
Toggle: ABC.inout=1→0

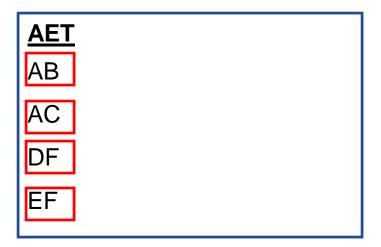
Toggle:

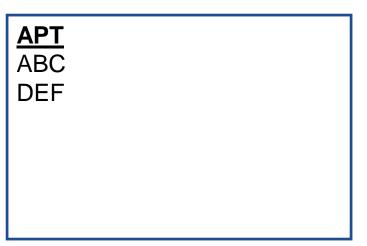
DEF.inout=0→1

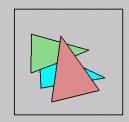
Toggle:

DEF.inout= $1 \rightarrow 0$









Simulation

Toggle: ABC.inout=0→1

Toggle:

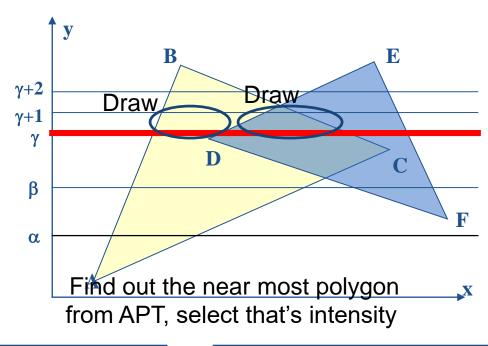
DEF.inout=0→1

Toggle:

ABC.inout= $1 \rightarrow 0$

Toggle:

DEF.inout= $1 \rightarrow 0$



Draw up to next edge in AET

Draw with selected intensity up to next edge in AET

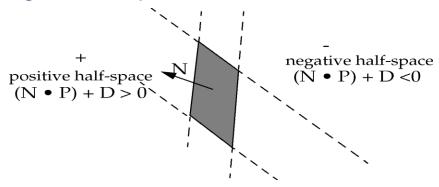


APT ABC DEF

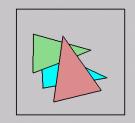


Plane-Half Space interpretation

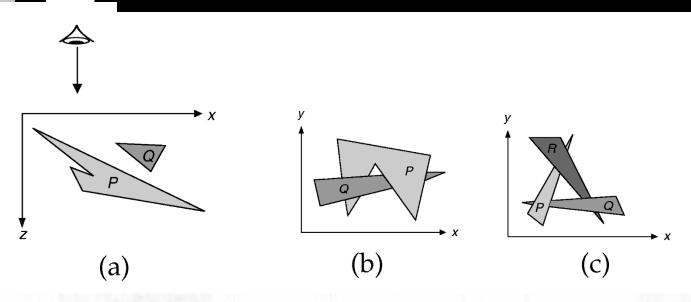
- A plane can be defined by a normal N and any point, P₀, on the plane:
 - plane satisfied by $N_xP_x + N_yP_y + N_zP_z + D = 0$
 - pick another point, \hat{P} ; then we can say $N \cdot (P P_0) = 0$
 - notice that –N •P₀ is constant; let's call it D
 - solve for D using any point on the plane.
- Plane divides all points into two half-spaces
 - $(N \cdot P) + D = 0$, P is on plane
 - (N P) + D > 0, P is in positive half-space
 - (N P) + D < 0, P is in negative half-space



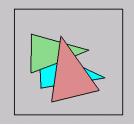
- Polygon faces away for eye points in negative half-space
 - if (N Eye) + D < 0, discard</p>



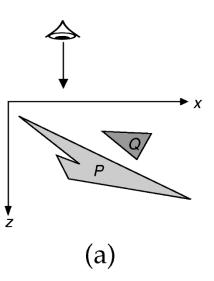
Depth-Sort Algorithm

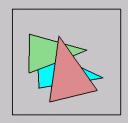


- 1. Sort all polygons according to the smallest (farthest) z coordinate of each
- Resolve any ambiguities this may cause when the polygons' z extents overlap, splitting polygons if necessary
- Scan convert each polygon in ascending order of smallest z coordinate (i.e., back to front).



- Select P → Polygon at the far end of the sorted list
- Before scan converting P,
 - Test against each polygon Q with which it's z-extent overlaps
 - If P cannot obscure any such Q, then P can be scan converted
- 5 tests are performed in successive order

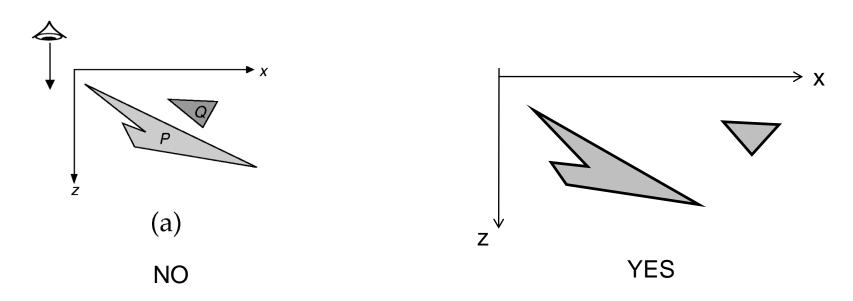




- Checking 5 tests to see whether polygon P obscures polygon Q
 - 1. Are the x-extents of P and Q disjoint?
 - 2. Are the y-extents of P and Q disjoint?
 - 3. Is P entirely on the opposite side of Q's plane from the eye?
 - 4. Is Q entirely on the same side of P's plane as the eye?
 - 5. Are the projections of P and Q on the screen are disjoint?



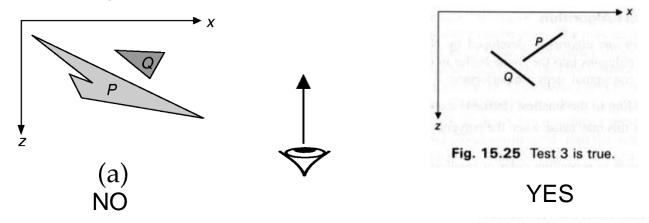
- Checking 5 tests to see whether polygon P obscures polygon Q
 - 1. Are the x-extents of P and Q disjoint?



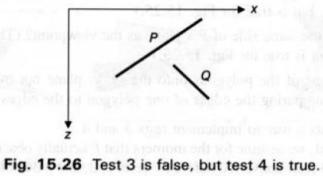
1. Are the y-extents of P and Q disjoint?



- Checking 5 tests to see whether polygon P obscures polygon Q
 - Is P entirely on the opposite side of Q's plane from the viewpoint?



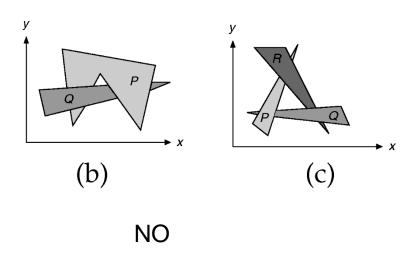
Is Q entirely on the same side of P's plane as the eye?

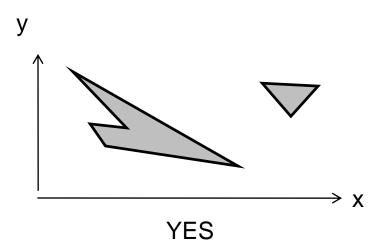


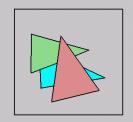
YES



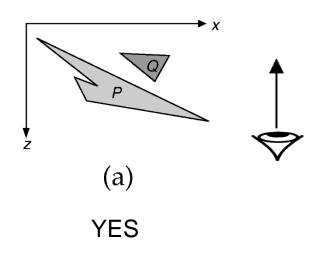
- Checking 5 tests to see whether polygon P obscures polygon Q
 - Are the projections of P and Q on the screen are disjoint?

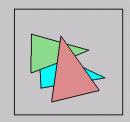




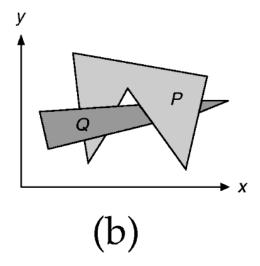


- Checking 5 tests to see whether polygon P obscures polygon Q
- As soon as a test returns TRUE → P does not obscure Q
 - So P can be scan converted before Q
 - If there are other polygons whose z extent overlaps P, then repeat the 5 tests for those also
- If all tests return FALSE → P obscures Q
 - Can we scan convert Q before P?
 - 3'. Is Q entirely on the opposite side of P's plane from the eye?
 - 4'. Is P entirely on the same side of Q's plane as the eye?
 - -- If returns YES → Q becomes the new P and included at the end of the list





- What if both tests 3' and 4' return NO?
 - Q cannot totally obscure P



- So SPLIT (since none obscure other fully)
 - Original unsplit polygons are discarded
 - Pieces are inserted into the list in proper z order

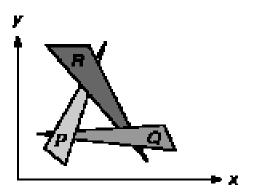


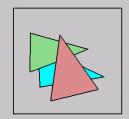
Special Case:

P, Q, R → any one of them can be inserted at the end of the list to place it in correct order relative to one other polygon, but not two others → results in infinite loop

Solution:

- mark the polygon once it is moved to the end of the list
- If 5 tests return NO
 - do not try steps 3' and 4'
 - Split the polygons and insert the pieces in to the list





Advantages:

- Fast enough for simple scenes
- Fairly intuitive

Disadvantages

- Slow for even moderately complex scenes
- Hard to implement and debug
- Lots of special cases
 - May cause unnecessary split



Unnecessary Split:

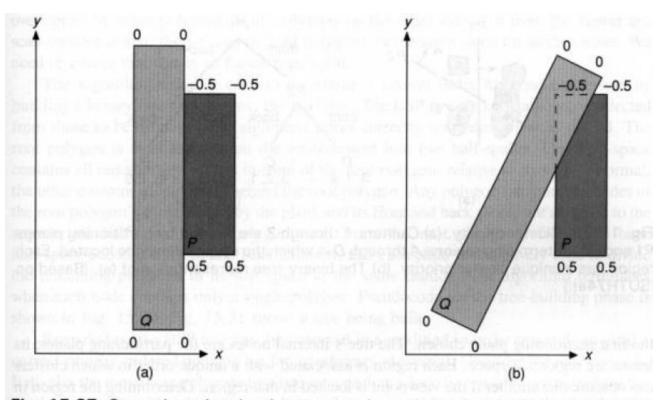
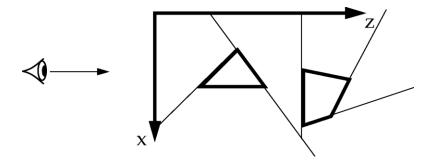


Fig. 15.27 Correctly ordered polygons may be split by the depth-sort algorithm. Polygon vertices are labeled with their z values. (a) Polygons P and Q are scan-converted without splitting. (b) Polygons P and Q fail all five tests even though they are correctly ordered.



Binary Space Partioning (BSP) Tree

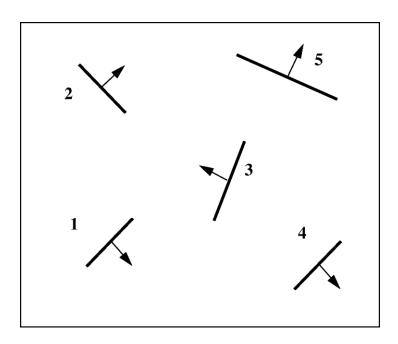
- Split space with any line (2D) or plane (3D)
- Repetitive subdivision of space to give a draw order



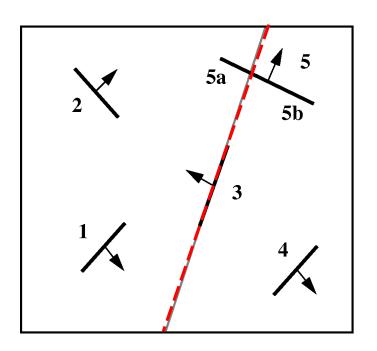
- Divide and conquer:
 - Select any polygon as root
 - Then display all polygons on "far" (relative to viewpoint) side of that polygon, then that polygon, then all polygons on polygon's "near" side
- Runs an initial time and space intensive preprocessing step
 - View independent subdivision of the space
- Allows a linear time display algorithm that is executed whenever viewing direction change
- Suitable for cases where the view point changes but objects remain static

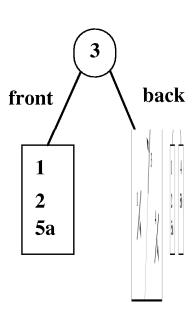


- Perform view-independent step once each time scene changes:
 - recursively subdivide environment into a hierarchy of half-spaces by dividing polygons in a half-space by the plane of a selected polygon
 - build a BSP tree representing this hierarchy
 - each selected polygon is the root of a sub-tree
- An example:

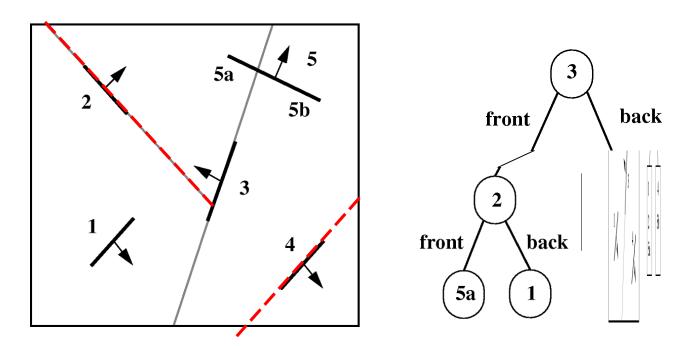




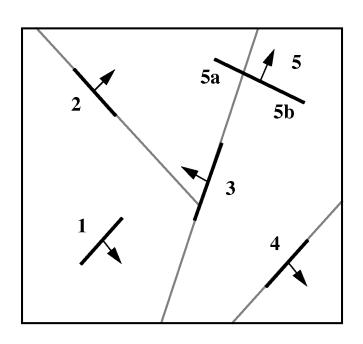


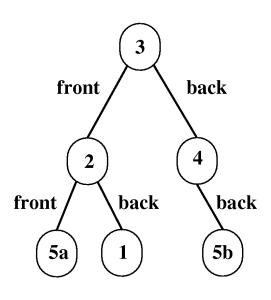


Step-1: Choose any polygon (e.g., polygon 3) and subdivide others by its plane, splitting polygons when necessary



Step-2: Process front sub-tree recursively

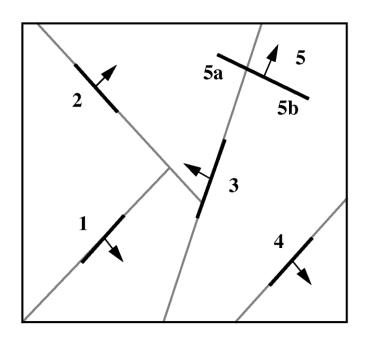


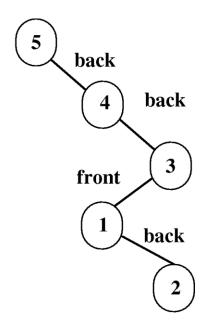


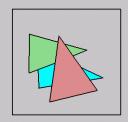
Step-3: Process back sub-tree recursively



An alternative BSP tree with polygon 5 at the root



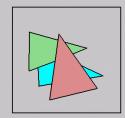




Pseudo code for Building BSP Tree

Pseudocode for Building BSP Tree

```
typedef struct {
    polygon root;
    BSP tree *backChild, *frontChild;
    } BSP tree;
BSP_tree *BSP_makeTree(polygon *polylist)
    polygon root, *backList, *frontList, p, backPart, frontPart,
   if (polyList == NULL) return NULL;
    else
    root = BSP_selectAndRemovePoly( &polyList );
    backList = frontList = NULL:
    for (each remaining polygon p in polylist)
         if (polygon p in front of root)
               BSP_addToLkist(p, & frontList);
         else if (polygon p in back of root)
               BSP addToLkist(p, &backList);
         else
               BSP_splitPoly(p, root, &fronPart, &backPart);
               BSP_addToList(frontPart, & frontList);
               BSP addToList(backPart, &backList);
   return BSP combineTree(BSP makeTree(frontList), root,
                                                      BSP makeTree(backList)
```



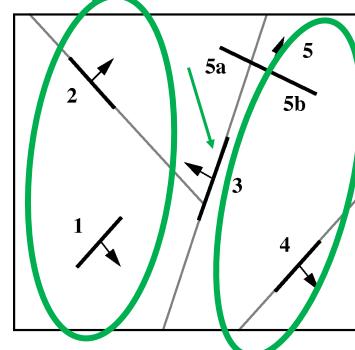
Pseudo code for Building BSP Tree

```
void BSP_displayTree(BSP_tree *tree) {
   if (tree!= NULL) {
       if (viewer is in front of tree->root) {
           /*Display back child, root, and front child */
           BSP_displayTree(tree->backChild);
           displayPolygon(tree->root);
           BSP_displayTree(tree->frontChild);
       } else {
          /*Display front child, root, and back child */
           BSP_displayTree(tree->frontChild);
           displayPolygon(tree->root);
           BSP_displayTree(tree->backChild);
```

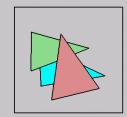


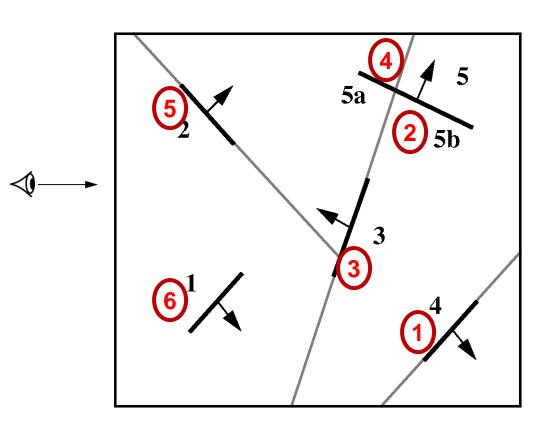
- Given a viewpoint, apply modified in-order tree traversal
- If viewer is in the root polygon's front half space
 - Display all the polygons in the root's rear half space
 - Then display the root
 - Finally display the polygons in its front half space
- If viewer is in the root polygon's rear half space
 - Display all the polygons in the root's front half space
 - Then display the root
 - Finally display the polygons in its rear half space

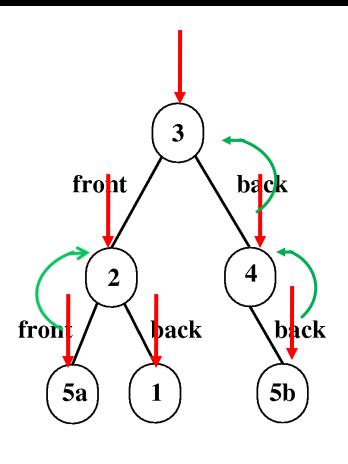




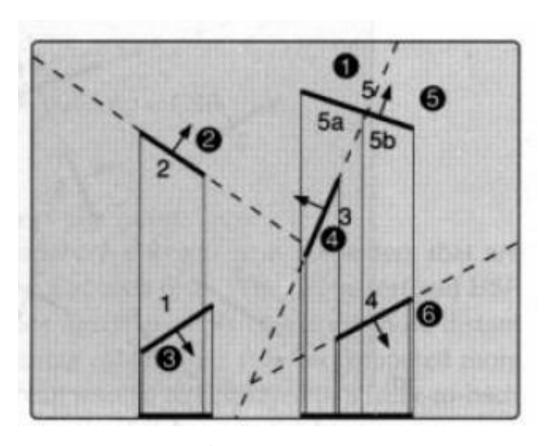
- If viewer is looking along the edge of the root polygon
 - Follow any display order provided above

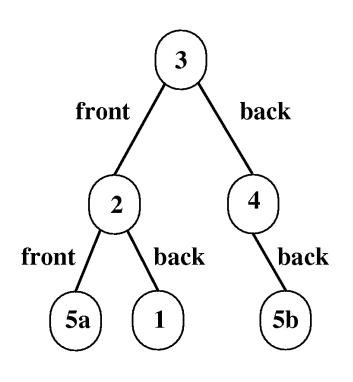












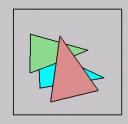




```
void BSP_displayTree (BSP_tree *tree)
   if (tree != NULL) {
      if (viewer is in front of tree->root) {
          /* Display back child, root, and front child. */
          BSP_displayTree (tree->backChild);
          displayPolygon (tree->root);
          BSP_displayTree (tree->frontChild);
       else {
          /* Display front child, root, and back child. */
          BSP_displayTree (tree->frontChild);
          displayPolygon (tree->root); /* Only if back-face culling not desired */
          BSP_displayTree (tree->backChild);
   /* BSP_displayTree */
          Fig. 15.32 Pseudocode for displaying a BSP tree.
```



- Painter's Algorithm with BSP Trees
 - Each face has form Ax + By + Cz + D
 - Plug in coordinates and determine
 - Positive: front side
 - Zero: on plane
 - Negative: back side
 - Back-to-front: postorder traversal, farther child first
 - Front-to-back: inorder traversal, near child first
 - Do backface culling with same sign test
 - Clip against visible portion of space (portals)



- Root should be selected such that fewer polygons are split among all of its descendants
 - Easy heuristic: Select the polygon which cause fewest split in its children
 - Testing five / six polygons gives best case



BSP vs. Depth Sort

- Both performs the object splitting and intersections at object precision
- Both Depends on image precision for pixel overwriting
- Unlike depth sort, BSP splits and order the polygons during preprocessing step
- In BSP, more polygon can be split than depth sort
- List Priority vs. Z buffer ?
- How BSP tree can assist in 3D Clipping?



• FV: 15.2.4, 15.4, 15.5.1, 15.5.2, 15.6