In [1]:
```
#import packages needed for performing time series
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import matplotlib.dates as mdates
import seaborn as sns
from sklearn.model_selection import train_test_split
from sklearn.metrics import mean_squared_error
from statsmodels.tsa.stattools import adfuller
from statsmodels.tsa.seasonal import seasonal_decompose
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
from statsmodels.tsa.arima.model import ARIMA
#import dataset used for the analysis
df = pd.read_csv (r'C:\Users\fahim\Documents\0_WGUDocuments\d213\medical_time_series.csv')
# Check data types and number of values, as well as overall size of dataframe
df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 731 entries, 0 to 730
Data columns (total 2 columns):
 #   Column   Non-Null Count  Dtype
---  ------   --------------  -----
 0   Day      731 non-null    int64
 1   Revenue  731 non-null    float64
dtypes: float64(1), int64(1)
memory usage: 11.5 KB
```

In [2]:
```
# Visually inspect dataframe and see if there are any issues
pd.set_option("display.max_columns", None)
df
```

Out[2]:

	Day	Revenue
0	1	0.000000
1	2	-0.292356
2	3	-0.327772
3	4	-0.339987
4	5	-0.124888
...	...	...
726	727	15.722056
727	728	15.865822
728	729	15.708988
729	730	15.822867
730	731	16.069429

731 rows × 2 columns

In [3]:

```
# Main issues with the dataframe was that 'Day' doesn't tell us the start and end date, and 'Revenue' doesn't specify c
# Initialize a start date, in datetime format
start_date = pd.to_datetime('2008-01-01')
# Convert Day column to differences in time
df['Day'] = pd.to_timedelta(df['Day']-1, unit='D') + start_date
# Rename columns
df.columns = ['date', 'revenue']
# Set the index for the 'date' column
df.set_index('date', inplace=True)
# View the dataframe to make sure that all of the changes have been made and recognized
df
```

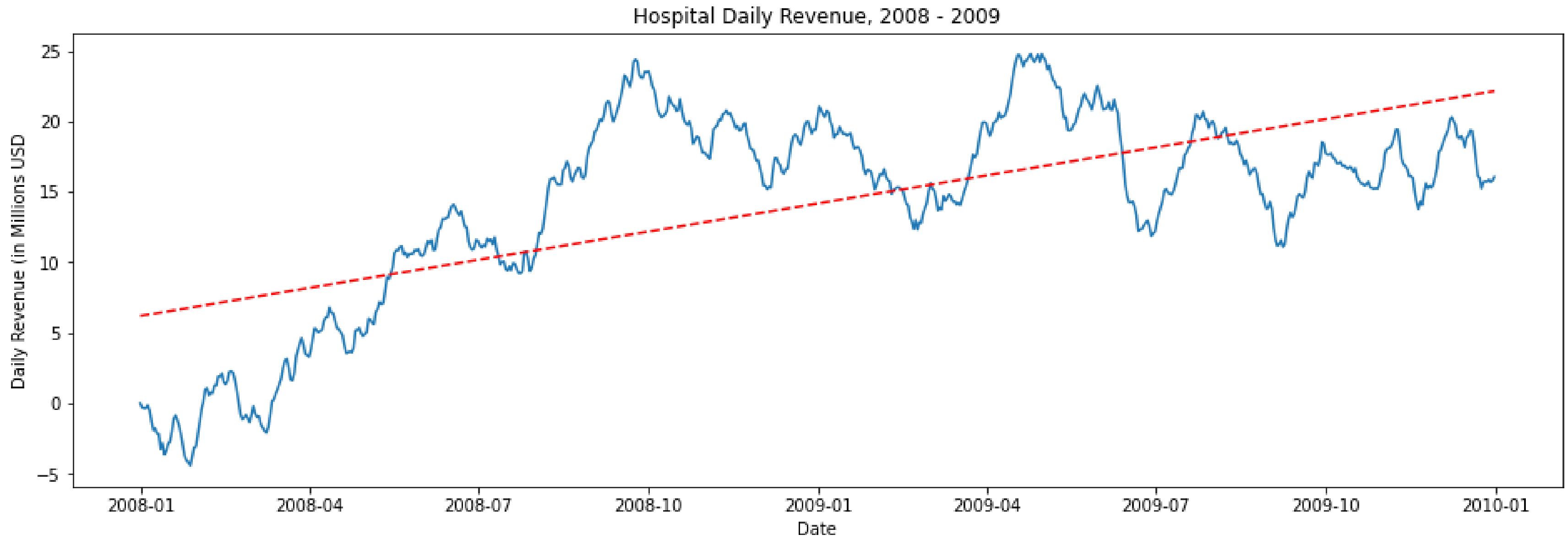
Out[3]:

date	revenue
2008-01-01	0.000000
2008-01-02	-0.292356
2008-01-03	-0.327772
2008-01-04	-0.339987
2008-01-05	-0.124888
...	...
2009-12-27	15.722056
2009-12-28	15.865822
2009-12-29	15.708988
2009-12-30	15.822867
2009-12-31	16.069429

731 rows × 1 columns

In [4]:

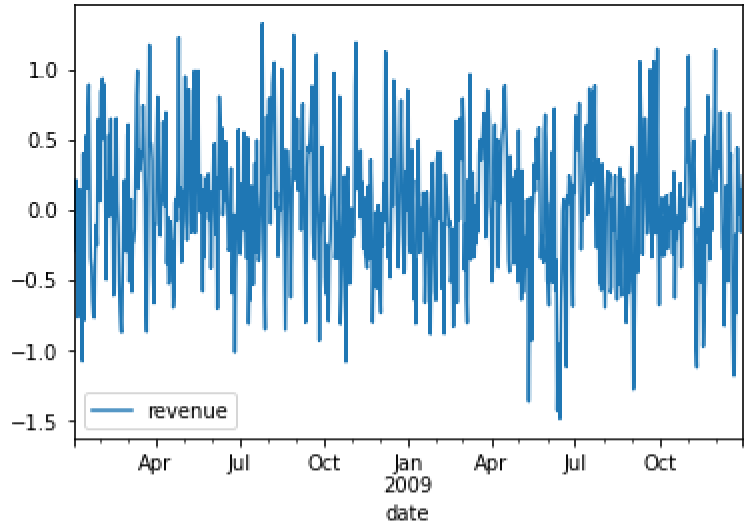
```
# Plot a line graph visualizing the realization of the time series
plt.figure(figsize = [16,5])
plt.title("Hospital Daily Revenue, 2008 - 2009")
plt.xlabel("Date")
plt.ylabel("Daily Revenue (in Millions USD")
# Plot time series data
plt.plot(df)
# Generate trend line
x = mdates.date2num(df.index)
y = df.revenue
z = np.polyfit(x, y, 1)
p = np.poly1d(z)
# Plot trendline
plt.plot(x, p(x), "r--")
plt.show()
```



In [5]:

```
# Perform Augmented Dicky-Fuller on the data to test if it is stationary
df_trans = df.diff().dropna()
adfuller_results = adfuller(df_trans.revenue)
# Print resulting test-statistic and p-value
print(f"Resulting Test statistic of an augmented Dicky-Fuller test on the data is {round(adfuller_results[0], 4)}, with
# Plot to verify stationarity
df_trans.plot();
```

```
Resulting Test statistic of an augmented Dicky-Fuller test on the data is -17.3748, with a p-value of 0.0
```



In [6]:
```
# Split time series into a training set and a test set
train, test = train_test_split(df_trans, test_size=0.2, shuffle=False, random_state=369)
train
```

Out[6]:

date	revenue
2008-01-02	-0.292356
2008-01-03	-0.035416
2008-01-04	-0.012215
2008-01-05	0.215100
2008-01-06	-0.366702
...	...
2009-08-03	-0.694370
2009-08-04	-0.282765
2009-08-05	0.104732
2009-08-06	0.275857
2009-08-07	0.126645

584 rows × 1 columns

In [7]:
```
test
```

Out[7]:

date	revenue
2009-08-08	0.263991
2009-08-09	-0.588690
2009-08-10	-0.550427
2009-08-11	0.081477
2009-08-12	-0.146587
...	...
2009-12-27	-0.032693
2009-12-28	0.143766
2009-12-29	-0.156834
2009-12-30	0.113880
2009-12-31	0.246562

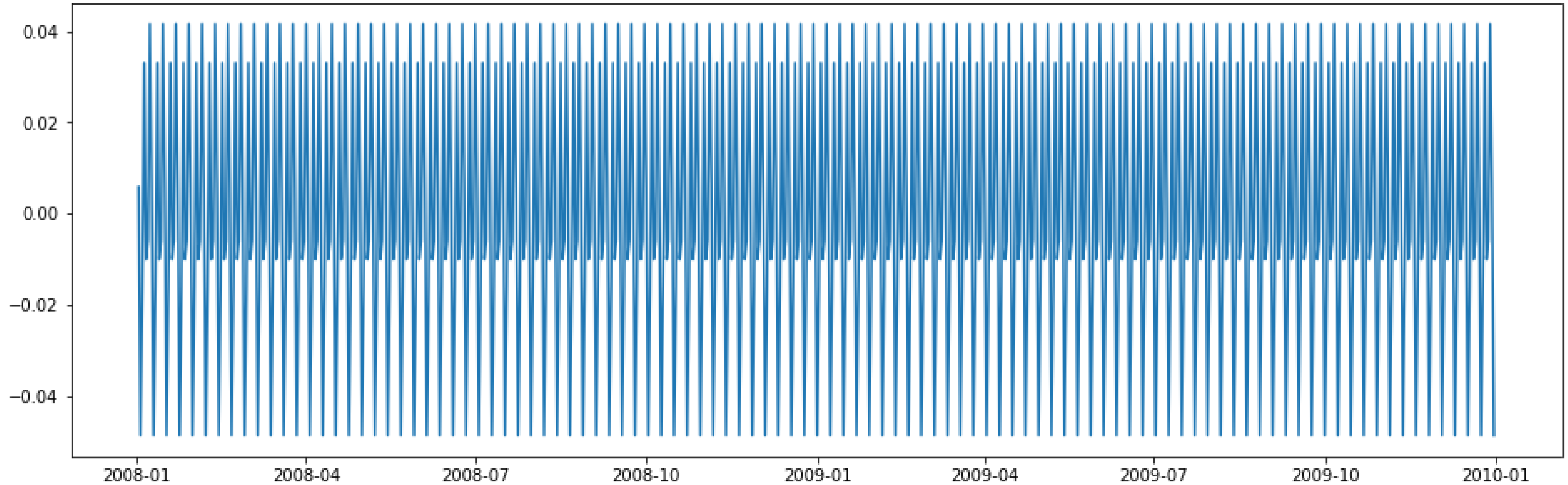
146 rows × 1 columns

In [8]:

```
# Now that the data has been split, provide a copy of the training and testing data sets.
# Save dataframe as CSV
train.to_csv('D213Task1_train_clean.csv')
# Save dataframe as CSV
test.to_csv('D213Task1_test_clean.csv')
```

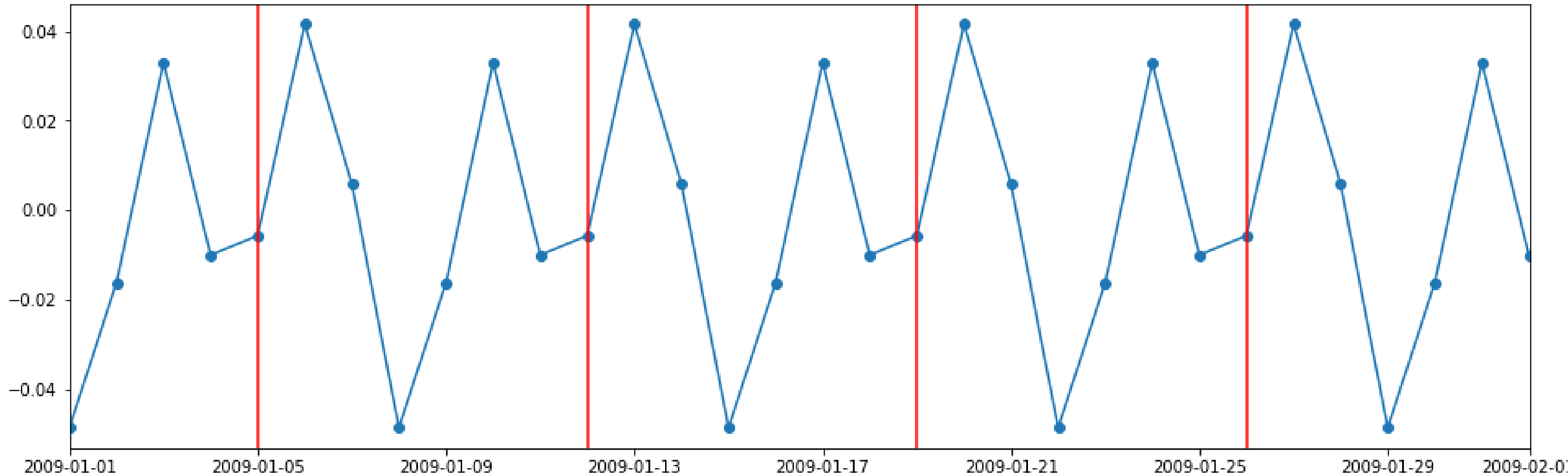
In [9]:

```
# Decompose the transformed data to showcase seasonality of the data
decomposed_data = seasonal_decompose(df_trans)
# Long X and small Y dictate a wide graph figure
plt.figure(figsize = [16,5])
# Plot seasonal component of the data
plt.plot(decomposed_data.seasonal);
```

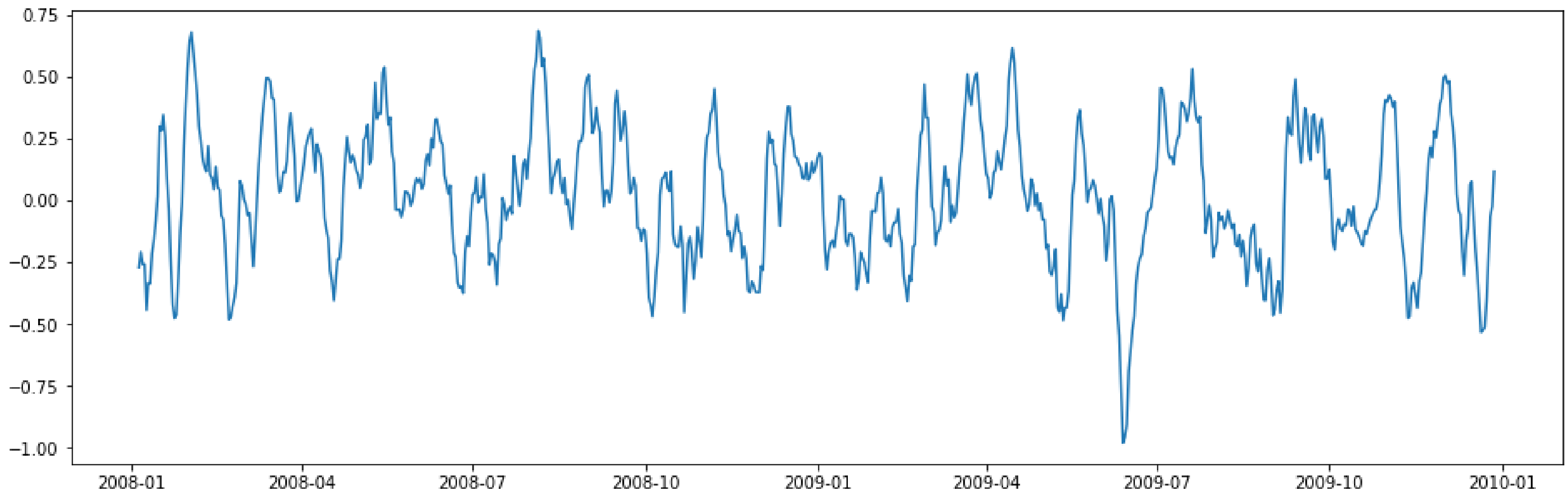


In [10]:

```
# Further showcase seasonality by plotting a month in the middle of the dataset for closer analysis and visualizations
# Long X and small Y dictate a wide graph figure
plt.figure(figsize = [16,5])
# Plot a seasonal component of the data
plt.plot(decomposed_data.seasonal, marker='o')
plt.xlim(pd.to_datetime('2009-01-01'), pd.to_datetime('2009-02-01'))
# Use red lines for Mondays
plt.axvline(x=pd.to_datetime('2009-01-05'), color='red')
plt.axvline(x=pd.to_datetime('2009-01-12'), color='red')
plt.axvline(x=pd.to_datetime('2009-01-19'), color='red')
plt.axvline(x=pd.to_datetime('2009-01-26'), color='red');
```



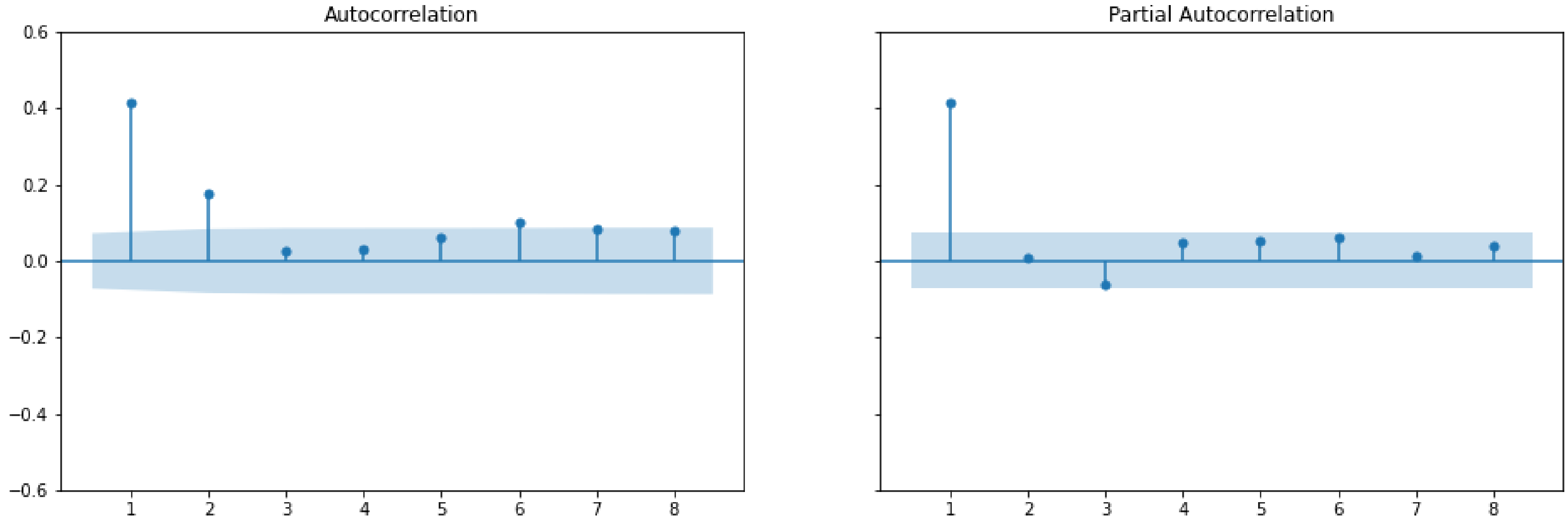
In [11]:
```
# Observe trend of the data
# Long X and small Y dictate a wide graph figure
plt.figure(figsize = [16,5])
# Plot trend component of the data
plt.plot(decomposed_data.trend);
```



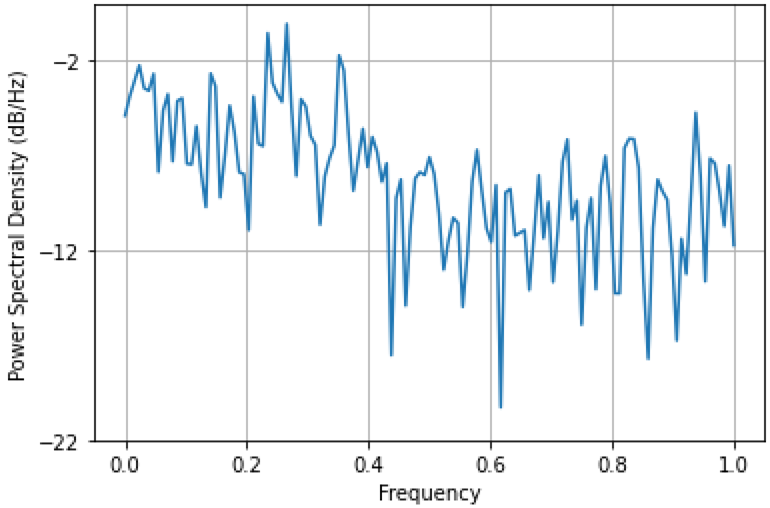
In [12]:
```
# Plot Autocorrelation and Partial Autocorrelation in one figure, sharing a y axis
fig, (ax1, ax2) = plt.subplots(1, 2, figsize=[16,5], sharey=True)
# Plot ACF to 8 lags (only 7 days in a week), ignore zero (zero always = 1)
```

```
plot_acf(df_trans, lags=8, zero=False, ax=ax1)
# Plot PACF to 8 lags (only 7 days in a week), ignore zero (zero always = 1)
plot_pacf(df_trans, lags=8, zero=False,ax=ax2)
# Zoom in on y axis to see points a little more clearly
plt.ylim(-0.6, 0.6);
```

```
C:\Users\fahim\AppData\Local\Programs\Python\Python310\lib\site-packages\statsmodels\graphics\tsaplots.py:348: FutureWarning: The default method 'yw' can produce PACF values outside of the [-1,1] interval. After 0.13, the default will change tounadjusted Yule-Walker ('ywm'). You can use this method now by setting method='ywm'.
  warnings.warn(
```

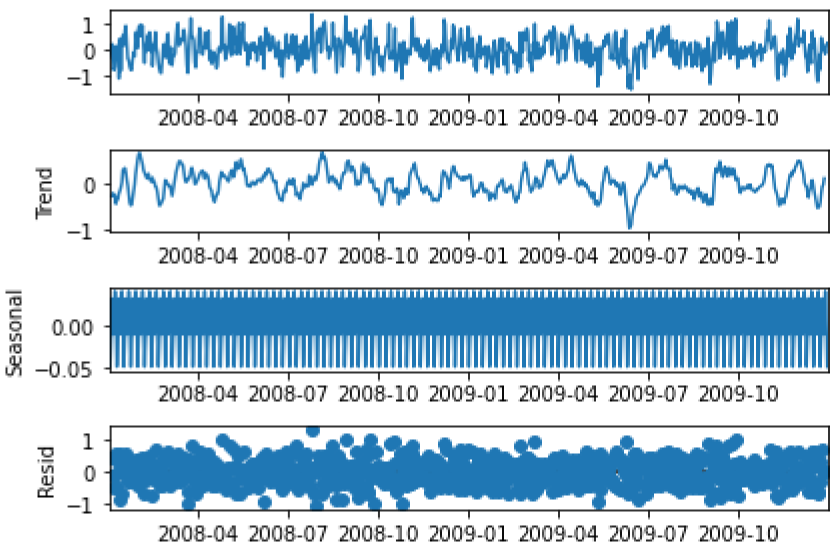


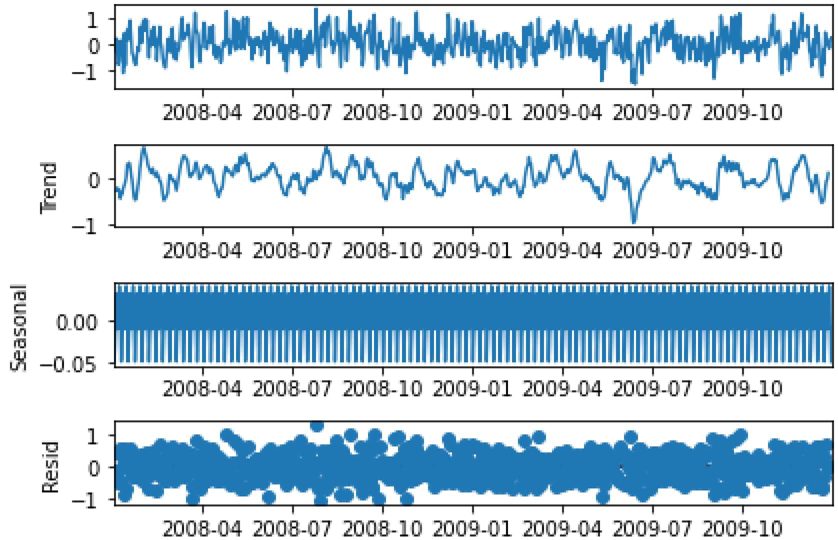
In [13]:
```
# Observe Spectral Density
plt.psd(x=df_trans.revenue);
```



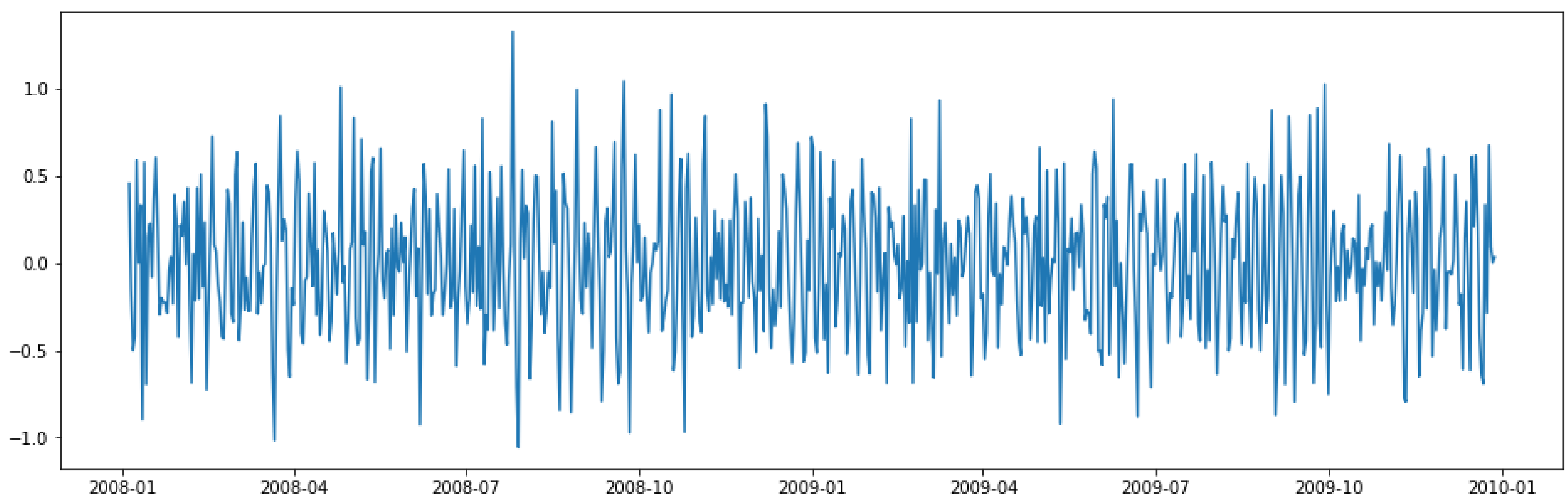
In [14]:
```
#Decomposed Time series
decomposed_data.plot()
```

Out[14]:





In [15]:
```
# Confirmed Lack of Trends in Residuals of Decomposition
# Long X and small Y dictate a wide graph figure
plt.figure(figsize = [16,5])
# Plot residual component of the data
plt.plot(decomposed_data.resid);
```



In [16]:
```
#Create an ARIMA Model of Time Series Data
model = ARIMA(train, order=(1, 0, 0), freq='D')
```

```
results = model.fit()
print(results.summary())
```

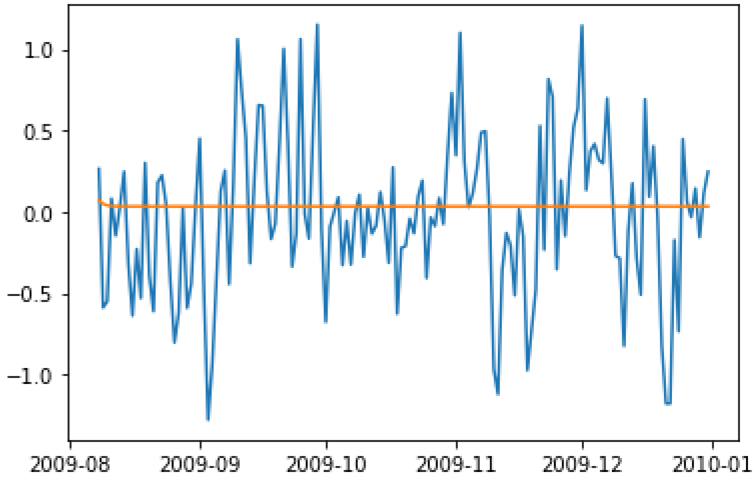
```
                               SARIMAX Results
==============================================================================
Dep. Variable:                revenue   No. Observations:                  584
Model:                 ARIMA(1, 0, 0)   Log Likelihood                -350.349
Date:                Sat, 14 Oct 2023   AIC                            706.698
Time:                        13:30:52   BIC                            719.808
Sample:                    01-02-2008   HQIC                           711.808
                         - 08-07-2009
Covariance Type:                  opg
==============================================================================
                 coef    std err          z      P>|z|      [0.025      0.975]
------------------------------------------------------------------------------
const          0.0328      0.031      1.063      0.288      -0.028       0.093
ar.L1          0.4079      0.038     10.748      0.000       0.333       0.482
sigma2         0.1943      0.012     15.948      0.000       0.170       0.218
===================================================================================
Ljung-Box (L1) (Q):                   0.10   Jarque-Bera (JB):                 1.80
Prob(Q):                              0.75   Prob(JB):                         0.41
Heteroskedasticity (H):               1.04   Skew:                            -0.05
Prob(H) (two-sided):                  0.78   Kurtosis:                         2.75
===================================================================================

Warnings:
[1] Covariance matrix calculated using the outer product of gradients (complex-step).
```

```
C:\Users\fahim\AppData\Local\Programs\Python\Python310\lib\site-packages\statsmodels\tsa\base\tsa_model.py:471: ValueWarning: No frequency information was provided, so inferred frequency D will be used.
  self._init_dates(dates, freq)
```

In [17]:

```
#Forecast
forecasted = results.get_prediction(start = 584, end = 729, dynamic = True)
plt.plot(test)
plt.plot(forecasted.predicted_mean);
```



In [18]:
```
print(forecasted.predicted_mean)
```

```
2009-08-08    0.071071
2009-08-09    0.048405
2009-08-10    0.039159
2009-08-11    0.035388
2009-08-12    0.033850
                ...
2009-12-27    0.032791
2009-12-28    0.032791
2009-12-29    0.032791
2009-12-30    0.032791
2009-12-31    0.032791
Freq: D, Name: predicted_mean, Length: 146, dtype: float64
```

In [19]:
```
# Place the forecasted differences into a temporary dataframe
forecast_temp = pd.DataFrame(forecasted.predicted_mean)
# Make consistent names for dataframe for concatenation
forecast_temp.rename(columns={'predicted_mean' : 'revenue'}, inplace=True)
# Concat a copy of Train (thru Aug 07 2009) and a copy of forecasted values (forward from Aug 08 2009)
df_w_forecast = pd.concat([train.copy(), forecast_temp.copy()])
# We've generated one DF with the differences in daily revenue for the entire 2-year period, invert the differences usi
df_w_forecast = df_w_forecast.cumsum()
# Check output to verify expected values
df_w_forecast
```

Out[19]:

	revenue
2008-01-02	-0.292356
2008-01-03	-0.327772
2008-01-04	-0.339987
2008-01-05	-0.124888
2008-01-06	-0.491590
...	...
2009-12-27	24.033683
2009-12-28	24.066474
2009-12-29	24.099265
2009-12-30	24.132056
2009-12-31	24.164846

730 rows × 1 columns

In [20]:

```
# Calculate confidence intervals from forecasted data
confidence_intervals = forecasted.conf_int()
# Like the forecast, these confidence limits are also differences in daily revenue, these need transformed back to dail
confidence_intervals
```

Out[20]:

	lower revenue	upper revenue
2009-08-08	-0.792856	0.934998
2009-08-09	-0.884621	0.981430
2009-08-10	-0.904871	0.983190
2009-08-11	-0.910461	0.981237
2009-08-12	-0.912301	0.980001
...	...	...
2009-12-27	-0.913421	0.979002
2009-12-28	-0.913421	0.979002
2009-12-29	-0.913421	0.979002
2009-12-30	-0.913421	0.979002
2009-12-31	-0.913421	0.979002

146 rows × 2 columns

In [21]:

```
# Establish a dataframe to match the confidence intervals dataframe, including the UNTRANSFORMED data from 2009-08-07
previous_row = pd.DataFrame({'lower revenue': [19.312734], 'upper revenue' : [19.312734], 'date' : ['2009-08-07']})
# Convert given date string to datetime and then set as index
previous_row['date'] = pd.to_datetime(previous_row['date'])
previous_row.set_index('date', inplace=True)
previous_row
```

Out[21]:

	lower revenue	upper revenue
date		
2009-08-07	19.312734	19.312734

In [22]:

```
# Concatenate the prior row and the confidence intervals data
confidence_intervals = pd.concat([previous_row, confidence_intervals])
# Un-transform the confidence intervals using cumsum()
confidence_intervals = confidence_intervals.cumsum()
# Make sure first row (data preceding the forecast) is omitted
confidence_intervals = confidence_intervals.loc['2009-08-08' : '2009-12-31']
```

```
# Verify un-transformed confidence intervals
confidence_intervals
```

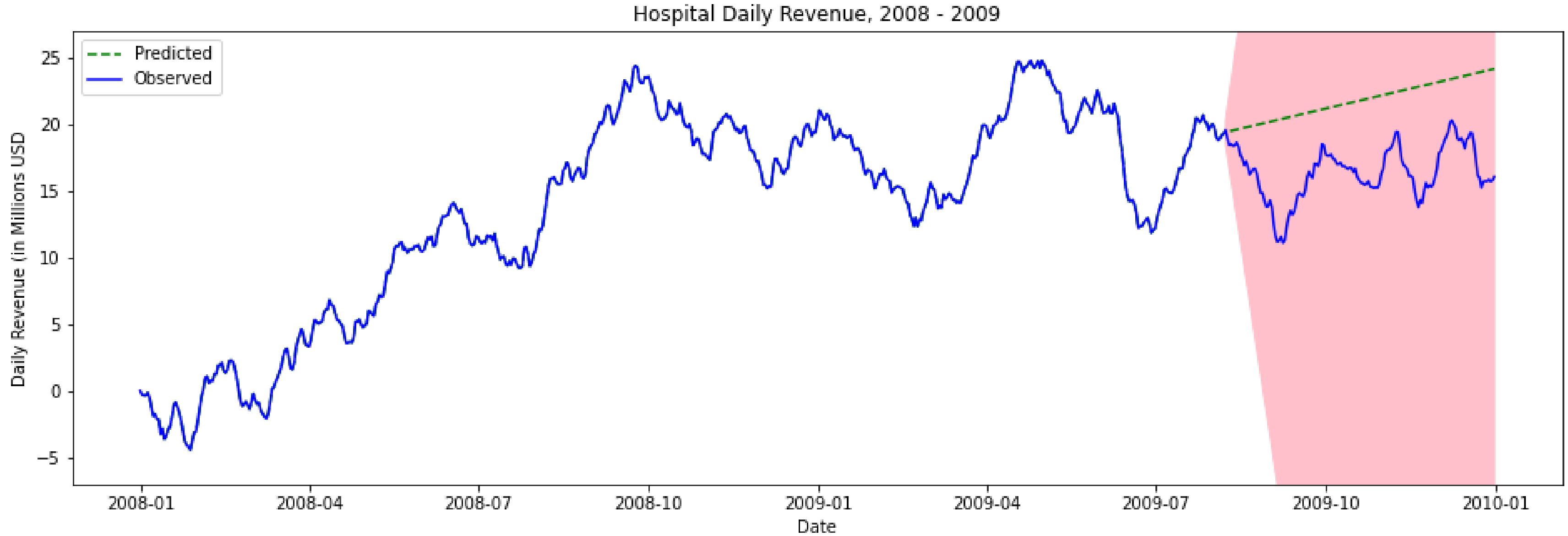
Out[22]:

	lower revenue	upper revenue
2009-08-08	18.519878	20.247732
2009-08-09	17.635257	21.229163
2009-08-10	16.730386	22.212353
2009-08-11	15.819925	23.193590
2009-08-12	14.907624	24.173592
...	...	...
2009-12-27	-110.230261	158.297627
2009-12-28	-111.143681	159.276629
2009-12-29	-112.057102	160.255632
2009-12-30	-112.970522	161.234634
2009-12-31	-113.883943	162.213636

146 rows × 2 columns

In [23]:

```
# Long X and small Y dictate a wide graph figure
plt.figure(figsize = [16,5])
# Prettify the graph
plt.title("Hospital Daily Revenue, 2008 - 2009")
plt.xlabel("Date")
plt.ylabel("Daily Revenue (in Millions USD")
# Plot the forecasted data
plt.plot(df_w_forecast, color = 'green', linestyle = 'dashed')
# Plot the original data (includes both the train set and the test set, untransformed - their actual observed values)
plt.plot(df, color = 'blue')
# Plot the confidence intervals
plt.fill_between(confidence_intervals.index, confidence_intervals['lower revenue'], confidence_intervals['upper revenue
# Keep the y-axis zoomed in, without expanding to fit the full confidence interval values
plt.ylim(-7, 27)
# Provide legend to distinguish predicted values from observed values
plt.legend(['Predicted', 'Observed'])
plt.show();
```

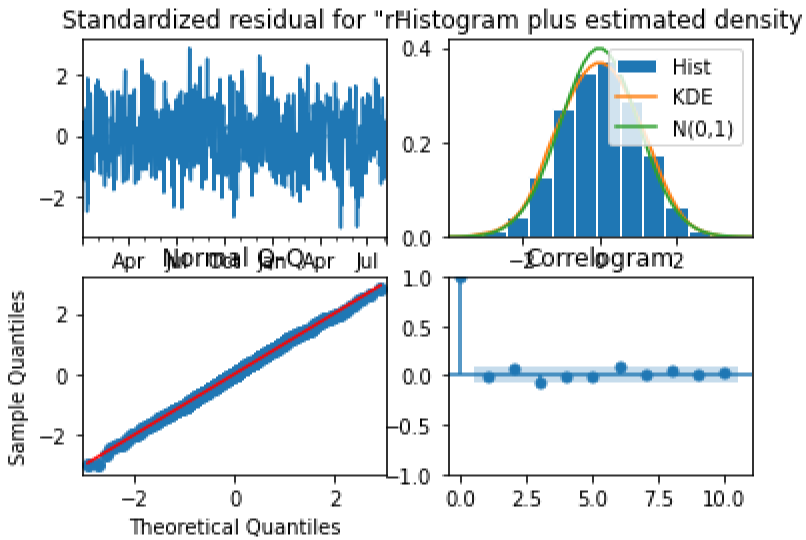


In [24]:
```
# Calculate root mean squared error of forecasted data against the observed data (both untransformed)
rmse = mean_squared_error(df.loc['2009-08-08' : '2009-12-31'], df_w_forecast.revenue.loc['2009-08-08' : '2009-12-31'],
print(f"The root mean squared error of this forecasting model is {round(rmse, 5)}")
```

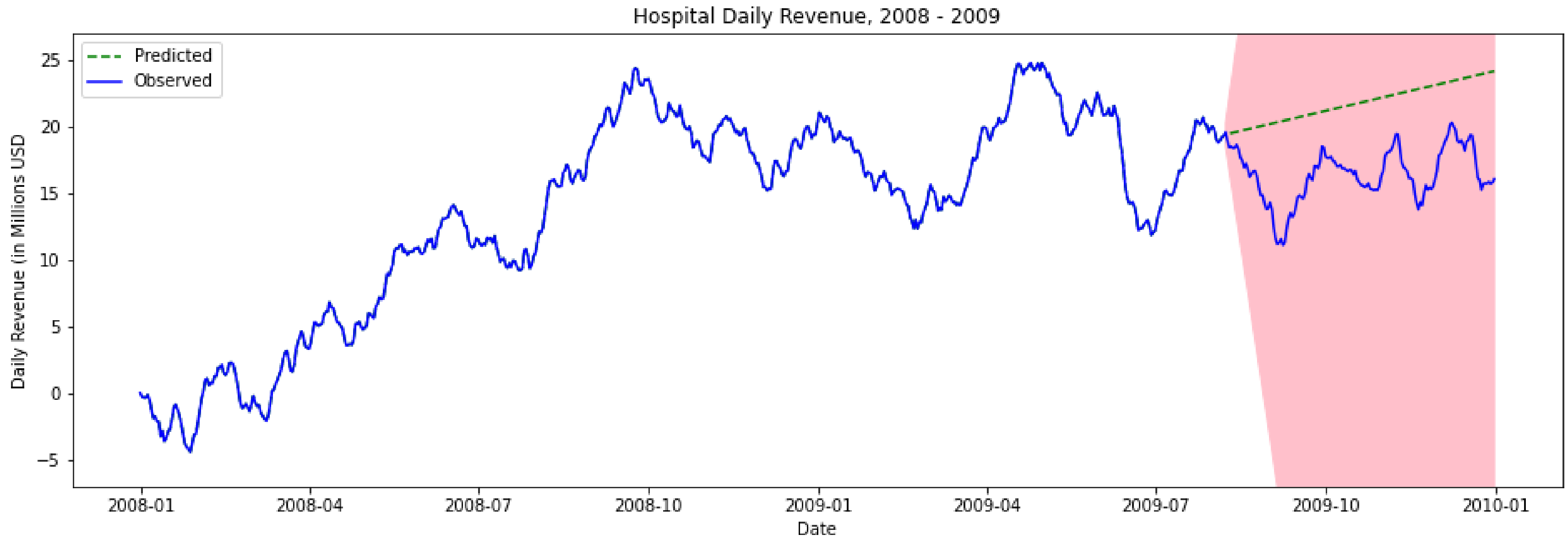
```
The root mean squared error of this forecasting model is 5.7584
```

In [25]:
```
plt.figure(figsize = [16,16])
results.plot_diagnostics();
```

```
<Figure size 1152x1152 with 0 Axes>
```



In [26]:
```
# Long X and small Y dictate a wide graph figure
plt.figure(figsize = [16,5])
# Prettify the graph
plt.title("Hospital Daily Revenue, 2008 - 2009")
plt.xlabel("Date")
plt.ylabel("Daily Revenue (in Millions USD")
# Plot the forecasted data
plt.plot(df_w_forecast, color = 'green', linestyle = 'dashed')
# Plot the original data (includes both the train set and the test set, untransformed - their actual observed values)
plt.plot(df, color = 'blue')
# Plot the confidence intervals
plt.fill_between(confidence_intervals.index, confidence_intervals['lower revenue'], confidence_intervals['upper revenue
# Keep the y-axis zoomed in, without expanding to fit the full confidence interval values
plt.ylim(-7, 27)
# Provide legend to distinguish predicted values from observed values
plt.legend(['Predicted', 'Observed'])
plt.show();
```


Hospital Daily Revenue, 2008 - 2009
Predicted
Observed
Daily Revenue (in Millions USD)
25
20
15
10
5
0
−5
2008-01
2008-04
2008-07
2008-10
2009-01
2009-04
2009-07
2009-10
2010-01
Date

```
In [ ]:
```