

MAT125: Introduction to Linear Algebra

Course Name: Introduction to Linear Algebra

Course Code: MAT 125.14 **Credit Hours**: 3 Credits **Pre-requisite**: MAT 130

Term : SUMMER 2024

| Instructor | Dr M Abdur Rab(AuR) |
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| Office Time | 3:00PM-4:20PM(RA) |
| Course Short Description: | This is an introductory course in linear algebra. The course will introduce the basic concepts and techniques of linear algebra, along with the insights of its wide applications in physics, economics and social sciences, natural sciences, and engineering. The course will require the development of theoretical results, which will require the use of mathematical rigor, algebraic manipulation, and geometry. This course covers, but is not limited to, the study of systems of linear equations, matrices, determinants, vectors and vector spaces, basis and dimension of vector spaces, linear transformations, eigenvalues and eigenvectors, and their applications. Computer software will be used to enhance the learning of the topics and techniques covered. |

Objective of the Course

- 1. To understand the fundamental properties of matrices including determinants, inverse matrices, matrix factorizations, eigenvalues, eigenvectors along with their application, and linear transformations.
- 2. Understanding the basic concepts of the system of linear equations, apply the matrix calculus to solve linear systems of equations.
- 3. To comprehend the Euclidean n-space, vector spaces, subspaces, linear span, and determine the basis and dimension of vector spaces.
- 4. Solving problems using computer programming and graphing calculators to gain an insight into the applicability of linear algebra.

Course Learning Outcomes:

| (CO-1) | Demonstrate the ability to understand the basic properties of matrices including determinants, inverse matrices, matrix factorizations, eigenvalues, eigenvectors, and linear transformations, the applications of eigenvectors including the investigation of the diagonalizability of matrices. | | | |
|--------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|--|--|
| (CO-2) | Explain the fundamental concepts of the system of linear equations using geometry and graphs; and apply the matrix calculus to solve linear systems of equations. | | | |
| (CO-3) | Comprehend the concept of Euclidean n-space, vector spaces, subspaces, linear span, and determine the basis and dimension of vector spaces. | | | |
| (CO-4) | Develop problem solving ability using computer programming and graphing calculators and have an appreciation of the wide application of this discipline within the scientific field. | | | |

Mapping of Course Outcomes

| CLOs | Course Outcomes (CO) | Bloom's taxonomy domain/level (C: Cognitive P: sychomotor A:Affective) | Delivery methods and activities | Assessment tools |
|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------|----------------------------------------|----------------------------------------------------------|
| CO-1 | Demonstrate the ability to understand the basic properties of matrices including determinants, inverse matrices, matrix factorizations, eigenvalues, eigenvectors, and linear transformations, the applications of eigenvectors including the investigation of the diagonalizability of matrices. | C1, C2, C3, C4 | Lectures, notes | Quiz, Assignment, Midterms, Final Exam |
| CO-2 | Explain the fundamental concepts of the system of linear equations using geometry and graphs; and apply the matrix calculus to solve linear systems of equations. | C2, C3, P2 | Lecture, notes, group discussion | Assignment, Class participation, Quiz, Midterms |
| CO-3 | Comprehend the concept of Euclidean n-space, vector spaces, subspaces, linear span, and determine the basis and dimension of vector spaces. | C1, C2, C3 | Lecture, notes | Discussion, Quiz, Midterms, Final Exam |
| CO-4 | Develop problem solving ability using computer programming and graphing calculators and have an appreciation of the wide application of this discipline within the scientific field. | C2, C3, C6, P3 | Lecture, notes, group discussion | Assignment, Discussion, Class participation |

Note: C2, C3, C4, and P2 indicate different subdomains of Bloom's Taxonomy. Please visit departmental website for details.

Marks Distribution:

| Attendance | 10% |
|-------------|-----|
| Assignments | 10% |
| Quizzes | 20% |
| Mid-Term | 25% |
| Final Exam | 35% |

Grading Policy:

| Letter Grade | Grade Points |
|--------------|-------------------------|
| A | 4.0 |
| A- | 3.7 |
| B+ | 3.3 |
| В | 3.0 |
| B- | 2.7 |
| C+ | 2.3 |
| С | 2.0 |
| C- | 1.7 |
| D+ | 1.3 |
| D | 1.0 |
| | A A- B+ B B- C+ C C- D+ |

Mapping of Course Outcomes Class Schedule

| Lecture | Topics | Article no. in the text book | Assessment tools | Learning Outcomes |
|----------|---------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------|---------------------------------------------|----------------------|
| 1 | Matrices and Matrix Operations, Inverse; Rules of Matrix Arithmetic, | 1.3, 1.4, 1.7 | Quiz1, Discussions | CO-1 |
| 2 | Diagonal, Triangular and Symmetric Matrices, Matrices and Matrix Operations, | 1.3, 1.4, | Quiz 1, Discussions | CO-1 |
| 3 | Inverse; Rules of Matrix Arithmetic, Diagonal, Triangular and Symmetric Matrices | 1.7 | Assignment I, Midterm | CO-1 |
| 4 | Elementary Matrices and a Method for Finding inverse of Assignment I, Matrix, Elementary Matrices and a Method for Finding inverse of Midterm of Matrix | | CO-1 | |
| 5 | Determinant by Cofactor Expansion | 2.1 | Quiz 1, Midterm | CO-1 |
| 6 | Evaluating Determinants by Row Reduction | 2.2 | Midterm | CO-1 |
| 7 | Properties of Determinant Function | 2.3 | Midterm, Assignment I | CO-1 |
| 8 | Introduction to System of Linear Equations, Gaussian Eliminations | 1.1, 1.2 | Discussions, Quiz 2 | CO-2 |
| 9 | Gaussian Eliminations (No solution and Unique solution) | 1.2 | Midterm, Assignment II | CO-2 |
| 10 | Gaussian Eliminations (many solutions), Solution of Homogeneous system of Linear Equations | 1.2 | Midterm, Assignment II | CO-2 |
| 11 | Further Results on Systems of Equations and Invertibility, | 1.2 | Midterm, Assignment II | CO-2 |
| 12 | Euclidean n-space and properties, Euclidean n-space and Gramsmith Orthogonalization | 1.6 | Discussions Midterm | CO-2, CO-3 |
| 13 14 | Midterm Exam | 4.2 | Final, | CO-1 |
| | Linear Transformation | | Assignment II | |
| 15 | Linear Transformation and properties, General Linear Transformations, Kernel and Range, | 4.2 , 4.3 | Final, Assignment II | CO-1 |
| 16 | | 8.1, 8.2, | Final, Assignment II | CO-2, CO-3 |
| 17 | Inverse Linear Transformations, Matrices of General Linear Transformations | 8.3, 8.4 | Final, Assignment II | CO-2, CO-3 |
| 18 | Real Vector Spaces, Subspaces | 5.1 | Quiz 3 | CO-1 |
| 19 | | 5.2 | Final | CO-3 |
| 20 | Linear combination,Linear Independence and Dependence | 5.3 | Final | CO-3 |
| 21 | Basis, Dimension, Solution Space and Null Space | 5.4 | Quiz 3, Final Exam | CO-3 |
| 22 | Fundamental Subspace of Linear Algebra (Row Space, Column Space and Null Space) | 5.5 | Quiz 3, Final Exam | CO-3 |
| 23 | Fundamental Subspace of Linear Algebra (Row Space, Column Space and Null Space) | 5.5 | Quiz 3, Final Exam | CO-3 |
| 24 | Rank and Nullity | 5.6 | Final Exam | CO-3 |
| 25 | Eigenvalues and Eigenvectors | 7.1 | Quiz 4 | CO-3 |
| 29 | Diagonalization | 7.2 | Final Exam | CO-3 |
| 26 | Algebraic and Geometric Multiplicity | 7.2 | Final exam, Assignment III | CO-3 |
| 27 | Cheley Hamilton Theorem (CHT) and its applications | 7.3 | Final exam, Assignment III | CO-3 |
| 28 | Applications of Linear Algebra | 11.2, 11.3 | Discussions, Assignment Iv Final exam | CO-4 |
| 29 | Applications of Linear Algebra | 11.6, 11.7 | Discussions, Assignment Iv Final exam | CO-4 |
| 30 | Applications of Linear Algebra Final Exam (Declared by the Controlle | 11.16 | Discussions, Assignment Iv Final exam | CO-4 |