

- ✓ Write down your student ID on the **top right corner** of each of the pages.
- ✓ Clearly write the solutions, along with the questions, on white paper with black ink (no need to use color pen, don't use pencils).
- ✓ Use **CamScanner**, or **Adobe Scan**, or **Microsoft Office Lens**, or any other software to scan the pages and make a **single PDF file**.
- ✓ After creating the PDF, make sure that (a) there are no pages missing, (b) all of the pages are legible, (c) your student ID on each page are visible.
- ✓ Please note, **collaboration ≠ copying**. You are allowed to discuss the questions and clear confusion you might have, but you have to write your solutions independently and be able to explain your answers during a random viva.
- ✓ **[Very Important]** Rename the PDF in the following format: "A1_StudentID_FullNameWithoutSpace.pdf". For example, if my student ID is 12345678 and my name is Shadman Shahid, the filename should be "A1_12345678_ShadmanShahid.pdf".
- ✓ **Submission Link:** <https://forms.gle/UhtL5NgJ5sVW3MU56>

Question 1:

8 Marks

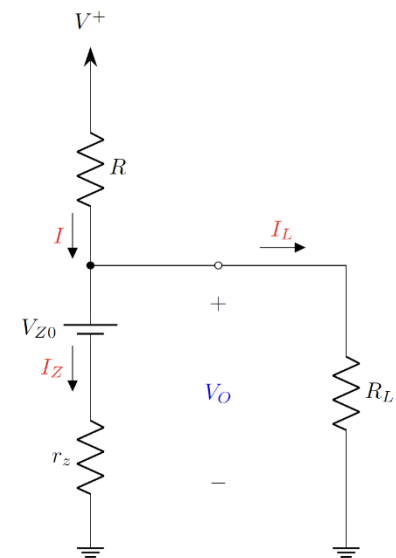
For $R = 80 \Omega$, $R_L = 15 \text{ k}\Omega$, $r_z = 30 \Omega$, $V_{Z0} = 4 \text{ V}$, and $I_Z = 1 \text{ mA}$.

a) Find V_O , I_L

[CO2] 4

b) Find I , V^+ .

[CO2] 4



$$a) V_O = V_{Z0} + I_Z r_z = (4 + 0.03) \text{ V} = 4.03 \text{ V}$$

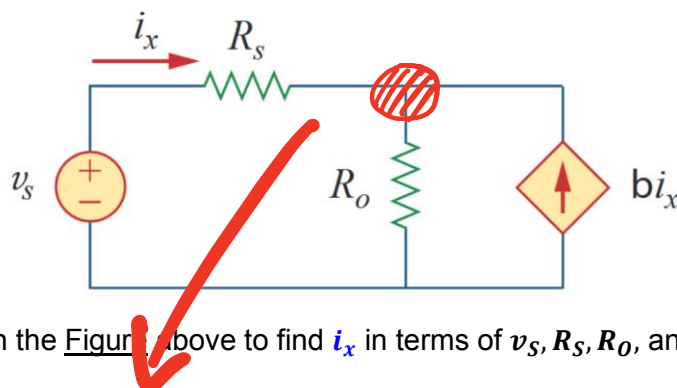
$$I_L = \frac{V_O}{R_L} = \frac{4.03}{15} \text{ mA} = 0.2687 \text{ mA}$$

$$b) I = I_L + I_Z = (0.269 + 1) \text{ mA} = 1.269 \text{ mA}$$

$$V^+ = V_O + I R = (4.03 + 1.269 \times 0.08) \text{ V} = 4.1315 \text{ V}$$

Question 2:

12 Marks

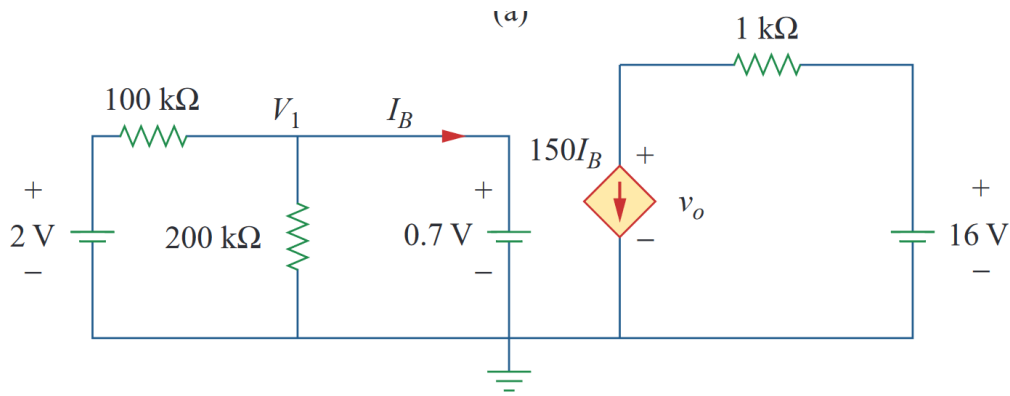


a) Analyze the circuit in the Figure above to find i_x in terms of v_s , R_s , R_o , and b .

[CO1] 2

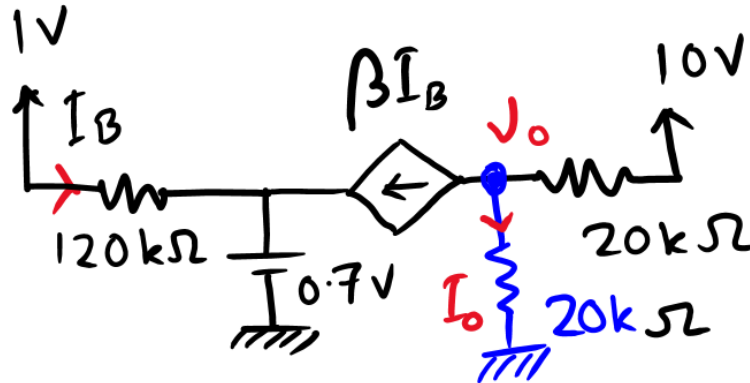
KCL:

$$i_x + b i_x = \frac{v_s - i_x R_s}{R_o} \Rightarrow i_x = \frac{v_s}{R_o(1+b) + R_s}$$



b) For the above circuit, find the value of v_o .

[CO2] 4



c) In the above circuit, $\beta = 120$. Find the current I_o and v_o from the given circuit.

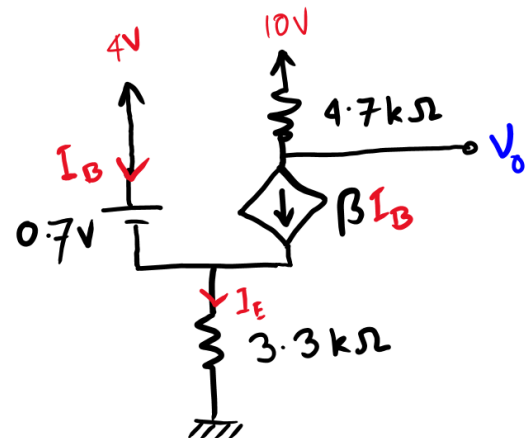
[CO2] 6

Question 3:

10 Marks

In the adjacent circuit $\beta = 80$.

- Derive an expression of I_E in terms of I_B and β . [CO1] 2
- Find the value of the currents I_E , and I_B . [CO2] 3
- Find the value of the voltage at the output node v_o . [CO2] 2
- Express v_o in terms of I_B and β . Thereafter, determine how v_o would change for changing the value of β . Show the change in v_o for $\beta = 50$ and $\beta = 20$. [CO2] 3



$$(2b) \quad I_B = \frac{2-0.7}{100} - \frac{0.7}{200} = 9.5 \mu A \quad [\text{KCL at } V_1]$$

$$\therefore V_o = 16 - 1 \times 150 I_B = 14.575 V \quad [\text{KVL at right loop}]$$

② Solution (c):

$$I_B = \frac{1-0.7}{120} \text{ mA} = 2.5 \mu A :$$

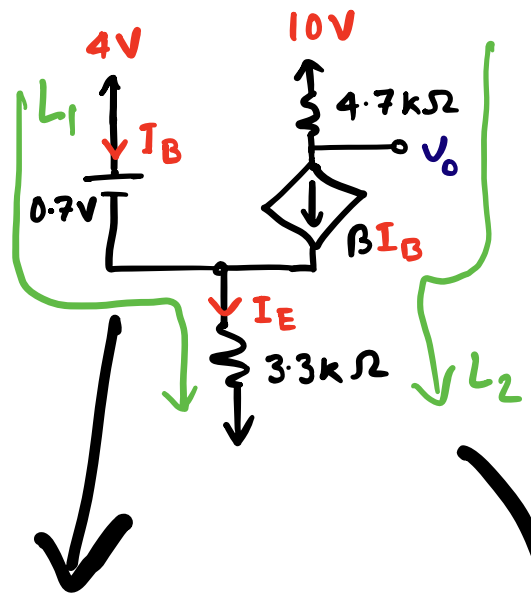
$$\begin{aligned} \beta I_B &= (80 \times 2.5 \times 10^{-3}) \text{ mA} \\ &= 0.2 \text{ mA} \end{aligned}$$

$$\text{KCL at } V_o : \beta I_B = \frac{10-V_o}{20} - \frac{V_o}{20}$$

$$\Rightarrow V_o = \left(\frac{10}{20} - 0.2 \right) 10 = 3 V$$

$$I_o = \frac{3}{20} \text{ mA} = 0.15 \text{ mA}$$

Q.3



a) $I_E = I_B + \beta I_B$

b) Taking KVL along L_1 : $4 - 0.7 - 3.3I_E = 0$
 $\Rightarrow I_E = \frac{3.3}{3.3} \text{ mA} = 1 \text{ mA}$

c) $V_o = 10 - 4.7\beta I_B$
 $= 10 - 4.7 \times \frac{80}{81}$
 $= 5.36 \text{ V}$

$$I_B = \frac{I_E}{\beta + 1} = \frac{1}{81} \text{ mA}$$

KVL along line L_2 :

d) $V_o = 10 - 4.7\beta I_B$

When; $\beta = 50$,

$$I_B = \frac{I_E}{\beta + 1} = \frac{1}{51}$$

$$\therefore V_o = 10 - 4.7 \times \frac{50}{51}$$

$$= 5.392 \text{ V}$$

$\beta = 20$

$$I_B = \frac{I_E}{\beta + 1} = \frac{1}{21}$$

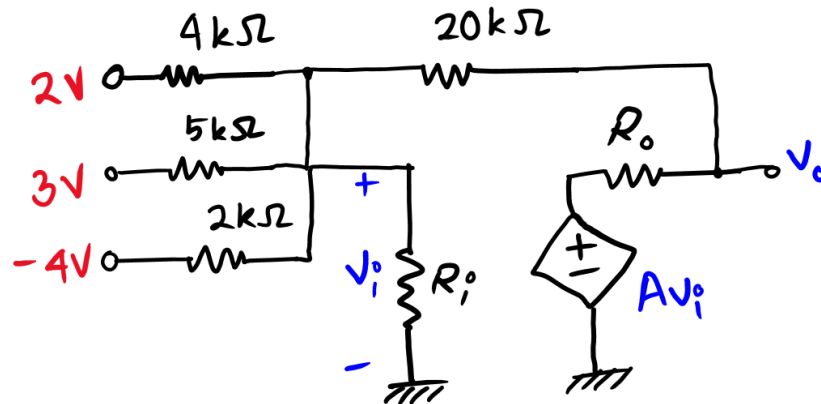
$$V_o = 10 - 4.7 \times \frac{20}{21}$$

$$= 5.524 \text{ V}$$

V_o will remain almost constant.

Question 4:

10 Marks



In the above circuit $A = 50$, $R_i = 80 \text{ k}\Omega$ and $R_o = 800 \Omega$. Answer the following questions

- Write the node equations for the nodes indicated by v_i and v_o . [CO1] 4
- Solve the node equations to find the values of v_i and v_o . [CO2] 3
- Can circuit theorems based on linearity principle (such as superposition principle) be applied to the above circuit? Explain in short why or why not. [CO1] 3

Solution:

a) At node v_i :

$$\frac{2-v_i}{4} + \frac{3-v_i}{5} + \frac{-4-v_i}{2} = \frac{v_i-v_o}{20} + \frac{v_i}{80} \quad \dots\dots(i)$$

At node v_o :

$$\frac{v_i-v_o}{20} + \frac{Av_i-v_o}{0.8} = 0 \quad \dots\dots(ii)$$

b) Simplifying:

(i) becomes:

$$v_i \left(\frac{1}{4} + \frac{1}{5} + \frac{1}{2} + \frac{1}{20} + \frac{1}{60} \right) - v_o \left(\frac{1}{20} \right) = \frac{2}{4} + \frac{3}{5} - \frac{4}{2}$$

$$\therefore 1.0125 v_i - 0.05 v_o = -0.9 \text{ ————— (iii)}$$

(ii) becomes:

$$v_i \left(-\frac{1}{20} - \frac{50}{0.8} \right) + v_o \left(\frac{1}{0.8} + \frac{1}{20} \right) = 0$$

$$-62.55 v_i + 1.3 v_o = 0 \text{ ————— (iv)}$$

Solving (iii) & (iv) we get:

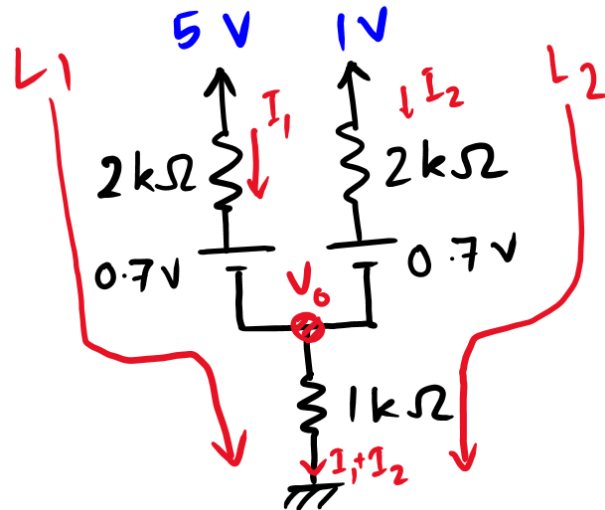
$$v_i = 0.645 \text{ V}$$

$$v_o = 31.0807 \text{ V}$$

c) Yes! Because all the circuit elements are linear. (Even the voltage dependent voltage source, because the voltage dependence (Av_i) is linear.)

Question 5:

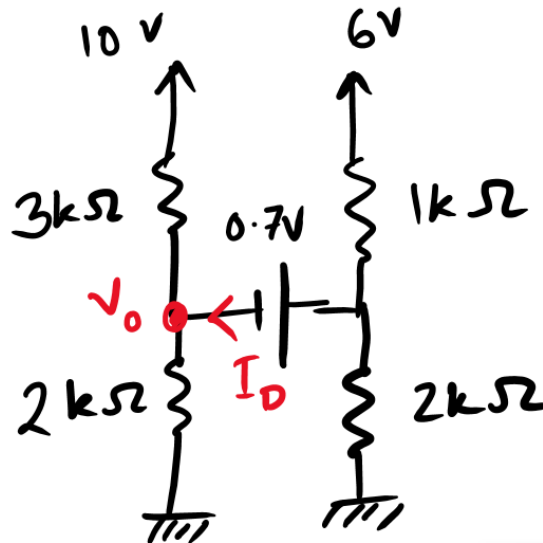
10 Marks



- a) Write down the two KVL equations for the lines (loops) indicated by the red lines L_1 and L_2 .
 b) Solve the circuit to find v_0 , I_1 and I_2 . You may use either mesh analysis or nodal analysis.

[CO1] 3

[CO2] 4



- c) Analyze the circuit to find v_0 and I_0 . [Use any technique of your choice.]

[CO2] 3

$$(a, b) \text{ KVL at } L_1: 5 - 2I_1 - 0.7 - (I_1 + I_2) = 0$$

$$3I_1 + I_2 = 4.3 \text{ --- (i)}$$

$$\text{KVL at } L_2: 1 - 2I_2 - 0.7 - (I_1 + I_2) = 0$$

$$I_1 + 3I_2 = 0.3 \text{ --- (ii)}$$

Solving:

$$I_1 = 1.575 \text{ mA}$$

$$I_2 = -0.425 \text{ mA}$$

$$V_o = (I_1 + I_2) \times 1 = 1.15 \text{ V}$$

$$c) \frac{10 - V_o}{3} + \frac{6 - (V_o + 0.7)}{1} = \frac{V_o}{2} + \frac{V_o + 7}{2}$$



$$\text{Shortcut: } V_o \left(\frac{1}{3} + \frac{1}{2} \right) + (V_o + 0.7) \left(\frac{1}{1} + \frac{1}{2} \right) = \frac{10}{3} + \frac{6}{1}$$

$$V_o = \frac{3.33 + 6 - 0.7 \times 1.5}{\frac{1}{3} + \frac{1}{2} + 1 + \frac{1}{2}} = 3.55 \text{ V}$$

$$I_o = \frac{V_o - 10}{3} + \frac{V_o}{2} = -0.375 \text{ mA}$$