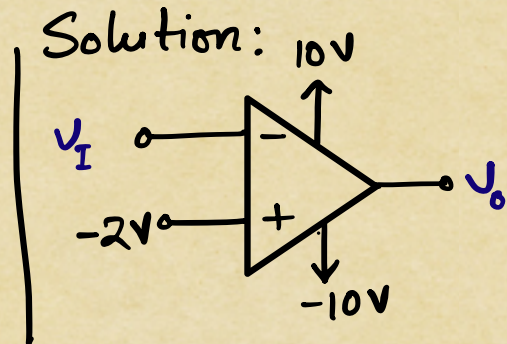
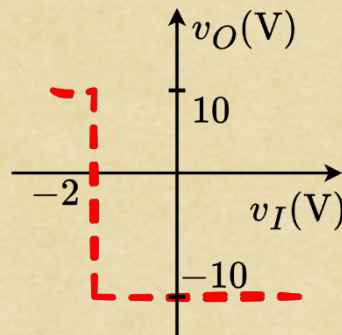


- ✓ Write down your student ID on the **top right corner of each of the pages**.
- ✓ Clearly write the solutions, along with the questions, on white paper with black ink (no need to use color pen, don't use pencils).
- ✓ Use **CamScanner**, or **Adobe Scan**, or **Microsoft Office Lens**, or any other software to scan the pages and make a **single PDF file**.
- ✓ After creating the PDF, make sure that (a) there are no pages missing, (b) all of the pages are legible, (c) your student ID on each page are visible.
- ✓ Please note, **collaboration ≠ copying**. You are allowed to discuss the questions and clear confusion you might have, but you have to write your solutions independently and be able to explain your answers during a random viva.
- ✓ **[Very Important]** Rename the PDF in the following format: "**A1\_StudentID\_FullNameWithoutSpace.pdf**". For example, if my student ID is 12345678 and my name is Shadman Shahid, the filename should be "**A1\_12345678\_ShadmanShahid.pdf**".
- ✓ **Submission Link:** <https://forms.gle/j81vXAmKcUwarxZy8>

### [CO3] Question 1:

14 Marks

- a) Design a circuit using **op-amp** that has the voltage transfer characteristics as shown in the figure below. 4  
 $v_O(V)$  is the **output voltage** and  $v_I(V)$  is the **input voltage**.



- b) A valve is used to release (when valve is OPEN,) or maintain (when valve is CLOSED,) water pressure 10 in a water tank. The valve operates on **ACTIVE LOW** logic. (i.e., the valve is OPENED when given a LOW voltage of 1 V, but remains CLOSED when provided a HIGH voltage of 6 V.)

A pressure sensor is installed in the water tank that outputs a voltage linearly proportional to pressure, as shown in the table below.

| At 0.5 atm pressure                   | At 1 atm pressure                 | At 1.5 atm pressure                               |
|---------------------------------------|-----------------------------------|---|
| $v_{0.5 \text{ atm}} = 0.5 \text{ V}$ | $v_{1 \text{ atm}} = 3 \text{ V}$ | $v_{\text{low}, 1.5 \text{ atm}} = 5.5 \text{ V}$ |

The pressure in the water tank can be measured by the formula  $P = h\rho g$ , where  $P$ , (in **Pascals (Pa)** unit) is the water pressure,  $h$  is the height of water in the tank (in **metres**),  $\rho$  (= 1000 kgm<sup>-3</sup>) is the density of water and  $g$  is the acceleration due to gravity (in ms<sup>-2</sup>).

**[1 atm = 101325 Pa]**

- Design** a circuit using Op-Amp comparator to automatically turn OPEN the valve if water level exceeds 10 m.
- Draw** the voltage transfer characteristics (VTC) of the designed Op-Amp.



Answer 1(b)

When  $h = 10 \text{ m}$  ;  $P = h\rho g = 98000 \text{ Pa} = 0.967 \text{ atm}$ .

From the table:  
find the exact  
voltage at this  
pressure .

$$\frac{V_{0.967 \text{ atm}} - V_{0.5 \text{ atm}}}{0.967 - 0.5} = \frac{V_{1 \text{ atm}} - V_{0.5 \text{ atm}}}{1 - 0.5}$$

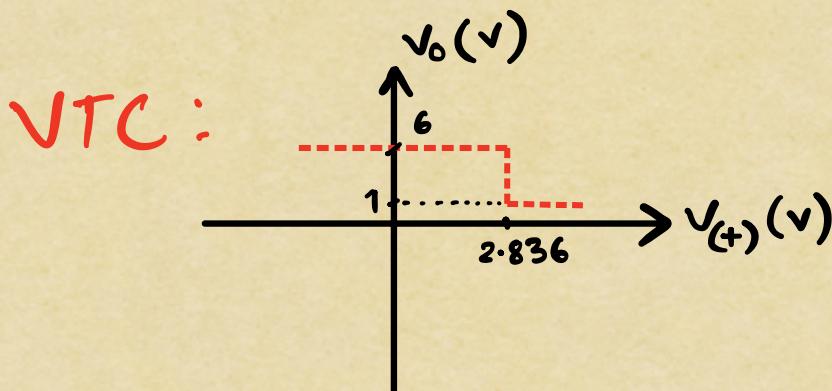
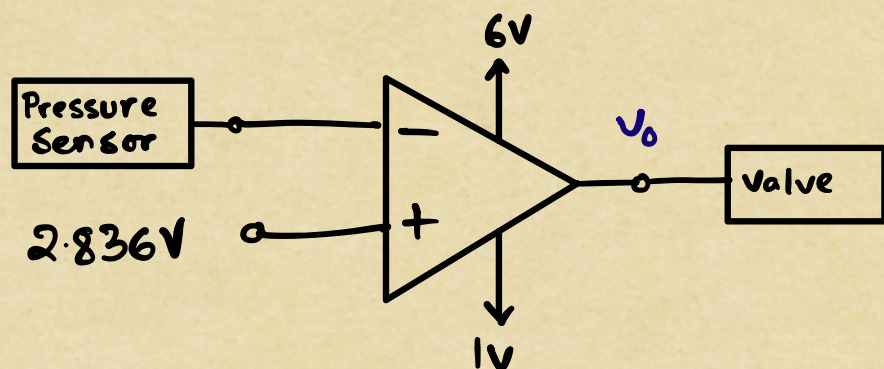
$$\Rightarrow V_{0.967 \text{ atm}} - V_{0.5 \text{ atm}} = \frac{3 - 0.5}{0.5} \times (0.967 - 0.5)$$

$$V_{0.967 \text{ atm}} = 0.5 \text{ V} + 5 \times (0.967 - 0.5)$$

$$V_{0.967 \text{ atm}} = 2.836 \text{ V}$$

$\therefore$  Active Low logic : High Pressure  $\rightarrow 1 \text{ V} \rightarrow \text{OPEN}$   
Low Pressure  $\rightarrow 6 \text{ V} \rightarrow \text{CLOSED}$

So, the comparator is in inverting configuration

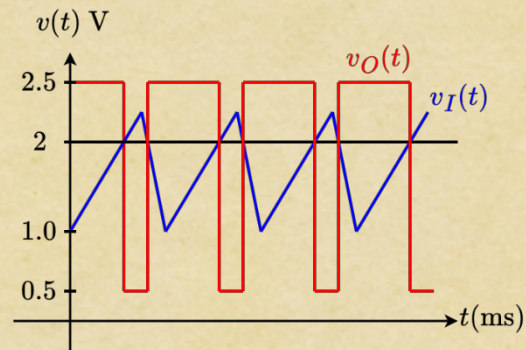
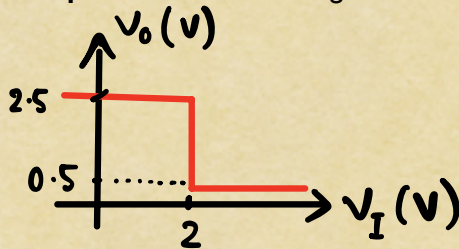




## Question 2:

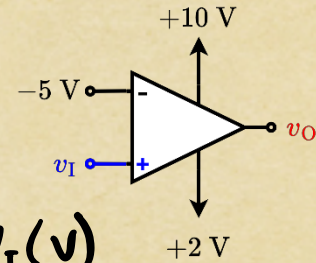
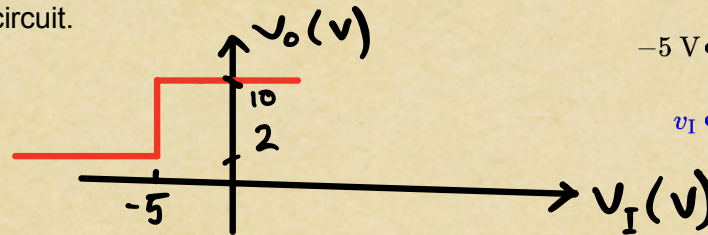
10 Marks

- a) Draw the voltage transfer characteristic (VTC) curve ( $v_O$  vs  $v_I$ ) from the adjacent waveform graph. Also draw the **Op-Amp Circuit** that would give rise to such a VTC.



[CO3] 3

- b) Draw the voltage transfer characteristic (VTC) curve ( $v_O$  vs  $v_I$ ) from the adjacent Op-Amp circuit.



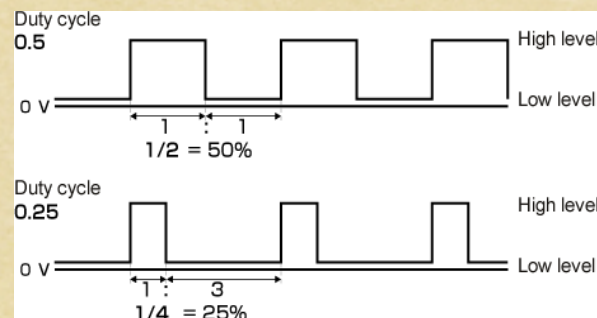
[CO2] 2

- c) **Design** an op-amp circuit to transform the sinusoidal voltage,  $v_I = 5 \cdot \sin\left(\frac{2\pi}{5} \cdot t\right)$  ( $t$  is in units of **ms**, and time-period  $T$  is 5 ms), to:  
[You must evaluate  $V_{REF}$ ]

- A square wave with a duty cycle of **50%**.
- A square wave with a duty cycle of **25%**.

[Duty Cycle: Time of positive half cycle  $\div$  Time period]

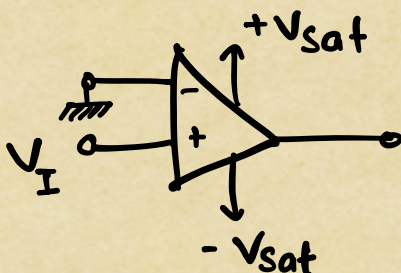
For more information on duty cycle, click [here!](#)



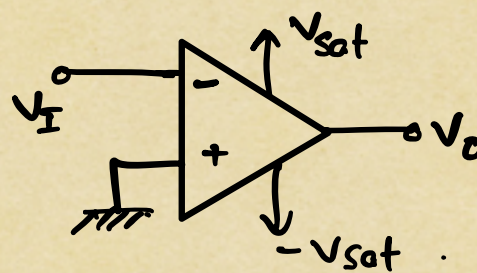
[CO3] 5

[Hint: If  $y = A \cdot \sin(\theta)$  is a sinusoidal function with period of  $2\pi$  then  $\theta = \sin^{-1}\left(\frac{y}{A}\right)$  and  $\pi - \sin^{-1}\left(\frac{y}{A}\right)$ . So, for 25% duty cycle find the value of  $y$  for which  $\Delta\theta = \left(\pi - \sin^{-1}\left(\frac{y}{A}\right)\right) - \sin^{-1}\left(\frac{y}{A}\right) = \frac{\text{Time period}}{4} = \frac{\pi}{2}$ ]

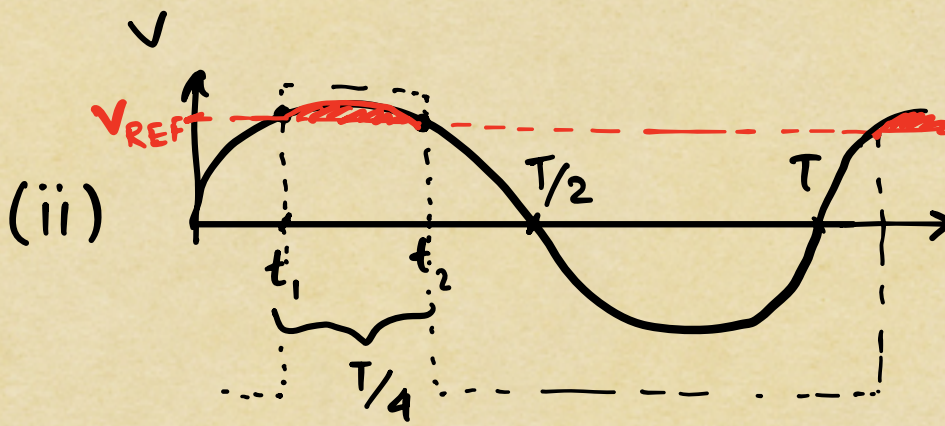
(i)



or







$$t_1 = \frac{5}{2\pi} \sin^{-1} \left( \frac{V_{REF}}{5} \right)$$

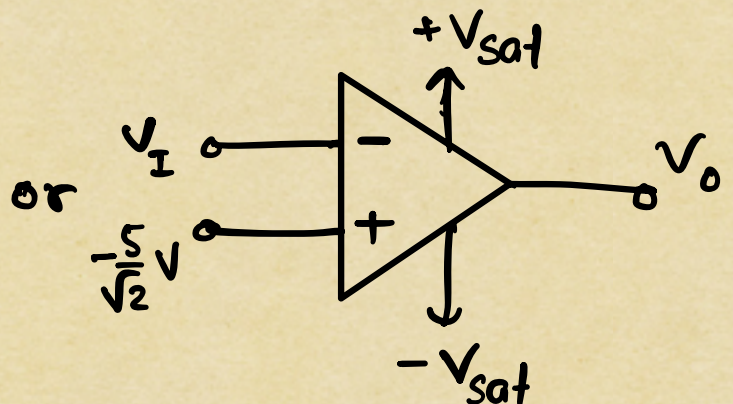
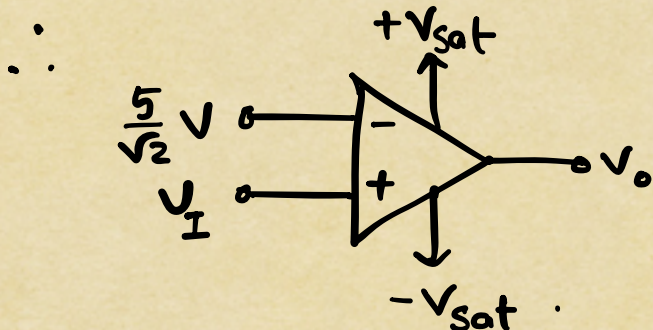
$$t_2 = \frac{T}{2} - t_1 = \frac{5}{2} - \frac{5}{2\pi} \sin^{-1} \left( \frac{V_{REF}}{5} \right)$$

$$\therefore t_2 - t_1 = \frac{T}{4} = \frac{5}{2} - 2 \cdot \frac{5}{2\pi} \sin^{-1} \left( \frac{V_{REF}}{5} \right)$$

$$\Rightarrow \frac{5}{4} = \frac{5}{2} - \frac{5 \times 2}{2\pi} \sin^{-1} \left( \frac{V_{REF}}{5} \right)$$

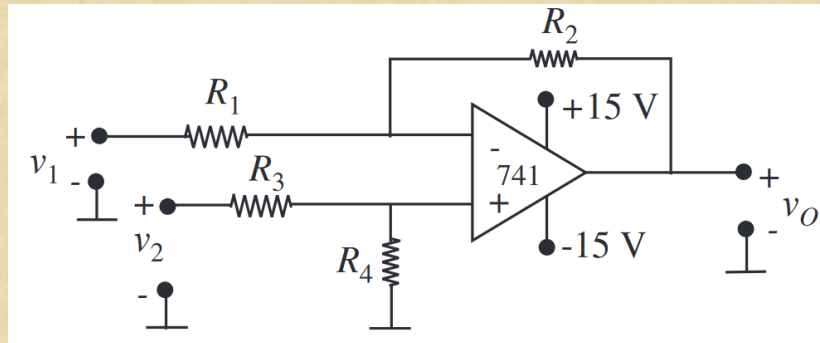
$$\Rightarrow V_{REF} = 5 \sin \left( \frac{2\pi}{5} \cdot \frac{5}{8} \right)$$

$$V_{REF} = \frac{5}{\sqrt{2}} V$$





[CO2] Question 3:  $\rightarrow$  Follow class lecture PDF. 10 Marks



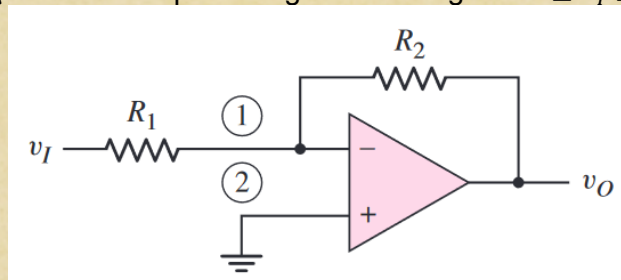
Answer the following questions dealing with the above circuit.

- Using the ideal Op Amp model, derive an expression for the output voltage  $v_O$  in terms of  $v_1$ ,  $v_2$ ,  $R_1$ ,  $R_2$ ,  $R_3$ , and  $R_4$ . 4
- Does connecting a load resistor  $R_L$  between the output and ground change the previous expression for  $v_O$ ? Why? 2
- Let  $v_1 = v_2$  and  $R_1 = 1 \text{ k}\Omega$ ,  $R_2 = 30 \text{ k}\Omega$ , and  $R_3 = 1.5 \text{ k}\Omega$ . Find  $R_4$  so that  $v_O = 0$ . 2
- Let  $v_2 = 0$  and  $v_1 = 1 \text{ V}$ . Using the preceding resistor values (including that computed for  $R_4$ ), find  $v_O$ . 2

[CO3] Question 4:

6 Marks

**Design** the circuit below such that the closed loop voltage gain is  $A_{CL} = -25$ . The maximum current in any resistor is to be limited to  $10 \mu\text{A}$  with the input voltage in the range  $-25 \leq v_I \leq 25 \text{ mV}$ .



- What are the values of  $R_1$  and  $R_2$ ?  $\rightarrow R_1 = \frac{25}{10} = 2.5 \text{ k}\Omega$  4
- What is the range of output voltage  $v_O$ ?  $R_2 = 62.5 \text{ k}\Omega$  2

$$\downarrow$$

$$-0.625 \text{ V} \leq v_O \leq 0.625 \text{ V}$$



3(c)

$$\frac{R_2}{R_1} = 30 ; \quad \frac{R_4}{R_3 + R_4} = \left(1 + \frac{1.5}{R_4}\right)^{-1}$$

$$V_o = -\frac{R_2}{R_1} V_1 + \left(1 + \frac{R_2}{R_1}\right) \left(\frac{R_4}{R_3 + R_4}\right) V_2$$

$$\therefore 30 \cancel{V_1} = \frac{31}{\left(1 + \frac{1.5}{R_4}\right)} \cancel{V_1}, \quad \left[ \text{As } V_1 = V_2 \text{ when } V_o = 0 \right]$$

$$\therefore 1 + \frac{1.5}{R_4} = \frac{31}{30}$$

$$\Rightarrow R_4 = 45 \text{ k}\Omega$$

$$3(d) \quad V_o = -15 \text{ V}.$$