I terated Integral - function more than one variables.

Exampless a
$$\int_{V_2}^{\pi} \int_{0}^{\pi} \int_{x}^{2} \int_{x}^{2} \cos \frac{y}{x} dy dx$$

$$= \int_{V_2}^{\pi} \int_{0}^{x^2} \int_{x}^{2} \cos \left(\frac{1}{x} \cdot y\right) dy dx$$

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$$= \int_{V_2}^{\pi} \int_{x}^{2} \sin \left(\frac{1}{x} \cdot x\right) dx$$

$$= \int_{v}^{\pi} \int_{v}^{2} \cos \left(\frac{1}{x} \cdot x\right) dx$$

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$$= \int_{v}^{\pi} \int_{v}^{2} \sin \left($$

$$\int_{0}^{1} \int_{0}^{1} \frac{x}{(xy+1)^{2}} dy dx$$

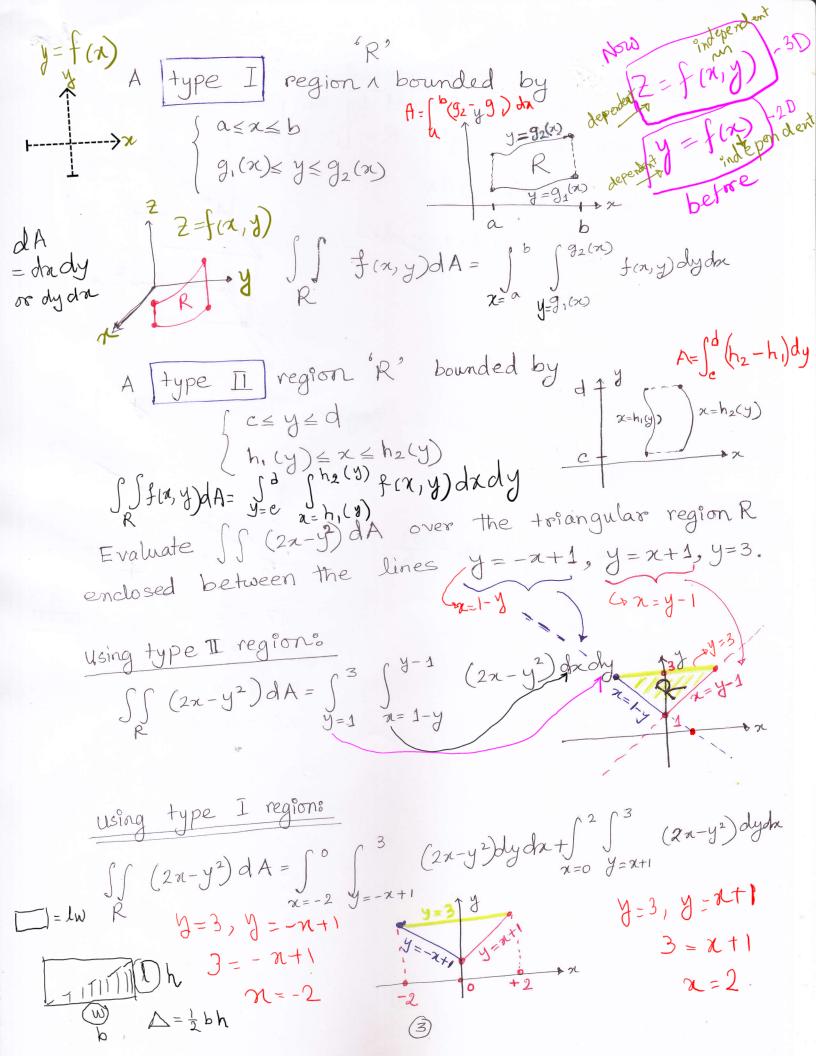
$$= \int_{0}^{1} x \int_{0}^{1} \frac{1}{(xy+1)^{2}} dy dx$$

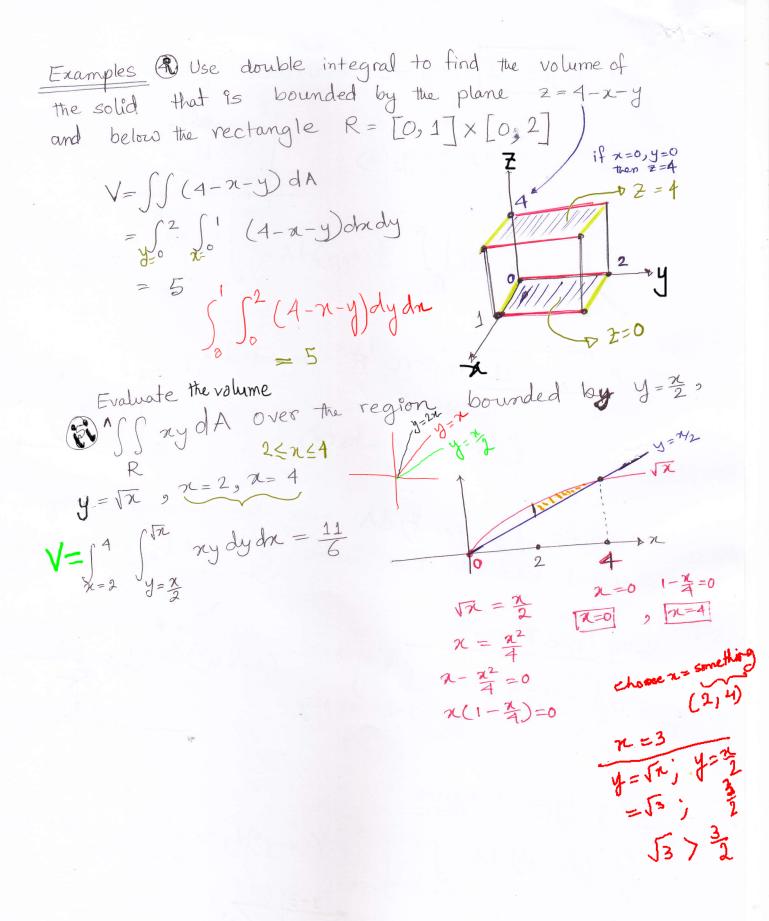
$$= \int_{0}^{1} x \int_{0}^{1+x} \frac{1}{(x-1)^{2}} dy dx$$

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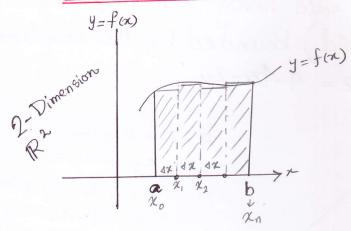
$$= \int_{0}^{1} x \int_{0}^{1+x} \frac{1}{(x-1)^{2}} dx$$

$$= \int_{0}^{1} \left[\frac{1+x}{1+x} - \frac{1}{1} \right] dx$$



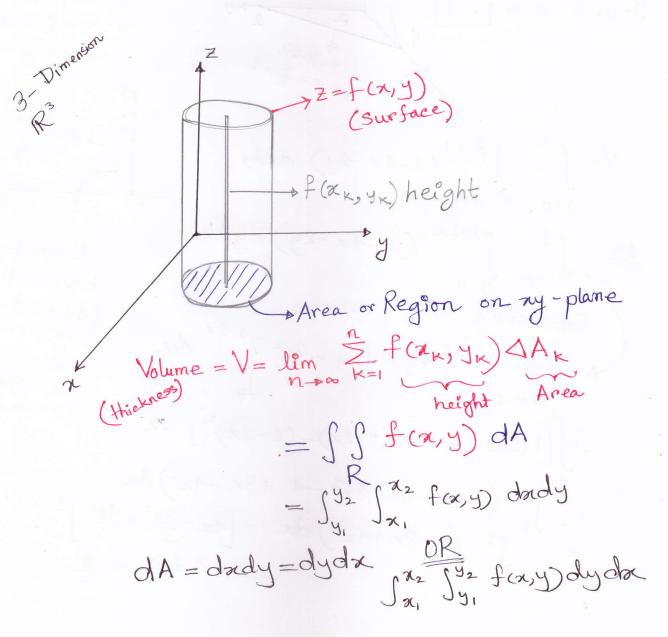


Concept of Double Integral:



$$A = \int_{a}^{b} f(x) dx \quad (ungth \times height)$$
width/height
$$area = \lim_{n \to \infty} \sum_{k=1}^{n} f(x_{k}) dx_{k}$$

$$dx_{k} = b - a$$



Example Use double integral to find the volume of the tetrahedron (A solid having 4 plane triangular faces. A triangular pyramid) bounded by the coordinate planes and the plane 2 = 4-4x-2y

planes $R \longrightarrow Region on$ Z=4-4x-2y xy plane $\chi=0, y=0 \Rightarrow z=4$ Z= 0 in my plane 00 Z = 4-4x-2y $\chi=0, Z=0 \Rightarrow y=2$ ⇒0=4-4x-2y $y=0, z=0 \Rightarrow x=1$ ⇒ y=2-22 OF X= =+1 $V = \int_{0}^{2} \int_{0}^{\frac{y}{2}+1} (4-4x-2y) dady$ $\int_{0}^{1} \int_{0}^{1} \int_{0}^{2-2x} (4-4x-2y) \, dy \, dx$ R can be bounded by Considering the 2rd option: $A = \int_{x=0}^{1} \left[4y - 4xy - \frac{2y^2}{2} \right]_{0}^{2-2x} dx$ SO≤x≤1 CO≤y≤2-2x or f 0 ≤ y ≤ 2 f 0 ≤ x ≤ 支+1 $= \left[4(2-2x) - 4x(2-2x) - (2-2x)^2 \right] dx$ $= \int_{0}^{1} \left(8-8x-8x+8x^{2}-4+8x-4x^{2}\right) dx$ $= \int_{0}^{1} \left(4-8x+4x^{2}\right) dx = \left[4x-\frac{8x^{2}}{2}+\frac{4x^{3}}{3}\right]_{0}^{1}$

=4-4+43=4