



# **IE 222: Operation Research**

## **Case Study of RUKN MULTAGA ALHALWA Factory**

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**Abstract:** This study aims to use the linear programming model to increase the profits of RUKN

MULTAGA ALHALWA factory by optimizing the available raw materials. We collected five

products, and it turned out that they have many problems and wasted capabilities. Their total profit per

day was 1628 SR. After applying the study and making maximum possible use of the raw materials,

the daily profit becomes 4020 SR.

**Introduction:** 

Due to the importance of analysis and operations research in finding optimal solutions with high

accuracy and relatively short time.

We visited one of the sweets products factories, which is the RUKN MULTAGA ALHALWA, to

implement the study of this project. RUKN MULTAGA ALHALWA Factory is a sweets factory that

has affiliated stores with the same name. It produces daily quantities and distributes them in a way to

meet the demand for each store. The factory contains 14 workers, each worker works 8 hours per day,

which is equivalent to 112 working hours per day (6,720 minutes per day).

Our aim in this study is to increase the profit of the factory by analyzing the data and designing a linear

programming model that finds the optimal solution.

**Problem Statement:** 

Many factories face problems in making full use of the available resources, some of them do not know

how to increase profit through the available resources, especially in the food processing sector, because

of the amount of raw materials in each product and the time of preparation. Some of them may

eventually resort to getting rid of these raw materials because they have expired. The problem facing

the factory is to determine the optimal quantity for each product according to the available resources

to obtain the highest possible profit.

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## Data:

Table 1: the demand, profit, and preparation time for each product.

| Products     | Daily demand<br>(Unit) | Preparation time (Min/unit) | Profit (SR/unit) |
|--------------|------------------------|-----------------------------|------------------|
| Regular cake | 53                     | 10                          | 2.1              |
| Saffron cake | 190                    | 1.5                         | 1.54             |
| kiryatus     | 9                      | 4.5                         | 0.5              |
| Latte sweet  | 248                    | 5                           | 0.2              |
| cheesecake   | 150                    | 2                           | 7.8              |

Table 2: The amount, number of raw materials in each product. And Availability of raw materials per day .

|                        | Regular cake | Saffron cake | kiryatus | Latte sweet | cheesecake | available |
|------------------------|--------------|--------------|----------|-------------|------------|-----------|
| egg (piece)            | 3            | 0.5          | 0        | 0           | 0          | 729       |
| butter (g)             | 283          | 0            | 0        | 0           | 5.5        | 20000     |
| sugar (g)              | 0            | 11.12        | 0        | 0           | 15         | 32000     |
| cream (piece)          | 0            | 0            | 0        | 2           | 2          | 1776      |
| white cream (g)        | 50           | 10           | 0        | 0           | 4          | 14500     |
| Liquid milk (piece)    | 0            | 0.2          | 0.2      | 0           | 0          | 58        |
| Condensed milk (piece) | 0            | 0            | 0.4      | 0.5         | 0          | 163       |
| yogurt (g)             | 0            | 0            | 0        | 0           | 90         | 46250     |
| Milk Powder (g)        | 0            | 0            | 0        | 0           | 40         | 17500     |
| Lotus biscuit (g)      | 0            | 0            | 40       | 0           | 0          | 600       |
| Gelatin (g)            | 0            | 0            | 0        | 0           | 0.5        | 650       |
| Max Mix (g)            | 250          | 47           | 0        | 0           | 0          | 67000     |
| Caramel powder (g)     | 0            | 0            | 0        | 45          | 0          | 14880     |
| filling (g)            | 250          | 0            | 0        | 0           | 0          | 13250     |
| Croissant (piece)      | 0            | 0            | 7        | 0           | 0          | 108       |
| Salty biscuits (g)     | 0            | 0            | 0        | 43          | 0          | 15000     |

**Modeling:** 

The aim of this study is to develop a linear programming model designed to increase the daily profits

of a sweets factory by increasing the production of the highest profit product, considering the amount

of available raw materials.

**Sets:** 

Product: the set of products given that  $p \in \{1,...,5\}$ .

Raw: the set of raw materials given that  $r \in \{1,...,16\}$ .

**Constants:** 

- Demand<sub>p</sub>: The demand of product type p.

- Profit<sub>p</sub>: The profit of product type p.

- Ravial<sub>r</sub>: The availability of raw material type r.

- Manhour: The available man hours.

-  $Araw_{rp}$ : The amount of raw material r in product p.

- Ntime<sub>p</sub>: The needed time to produce product type p.

**Decision variables:** 

- X<sub>p</sub>:The number of units produced of product type p.

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**Objective function:** 

 $Max \ z = \sum_{p \in Product} Profit_p \ X_p$ 

#### **Constraints:**

For all  $p \in Product: X_p \ge Demand_p$ . (Demand for each product produced per day).  $For \ all \ r \in Raw: \sum_{p \in Product} Araw_{rp} \quad X_p \leq Ravial_r$ (Available of each raw material per day).  $\sum_{p \in Product} Ntime_p \ X_p \leq Manhour$ (Available of manhour per day). For all  $p \in Product: X_p \in IN$ . (Integer constraint). **Lingo Code:** Sets: Product/1..5/: Demand, Profit, Ntime, x; Raw/1..16/: Ravail; RP(Raw, Product): Araw; **Endsets** Data: Demand = @ole(); Profit = @ ole(); Ntime = @ ole(); Manhour = 6720; Ravail = @ole(); Araw = @ole();Enddata !Objective function; Max = Z;Z = @sum(Product(p): Profit(p) \* x(p));!Constraints; !Demand for each product produced per day; @ for (Product(p): x(p) >= Demand(p));!Available of each raw material per day; @for (Raw(r): @sum(Product(p): Araw(r,p)\*x(p))  $\leq$  Ravail(r)); !Available of man hour per day; @sum(Product(p): Ntime(p) \* x(p)) <= Manhour; !integer constraint; @ for (Product(p): @gin(x(p)));

# Production per day before the model:

Table 3: Production information per day before the model:

|                        |                 |                 |          | -              | -          |        | A :1 -1-1-                      | T1                      |
|------------------------|-----------------|-----------------|----------|----------------|------------|--------|---------------------------------|-------------------------|
| Products               | Regular<br>cake | Saffron<br>cake | kiryatus | Latte<br>sweet | Cheesecake | Total  | Available<br>of raw<br>material | The raw material unused |
| Units produced         | 53              | 190             | 9        | 248            | 150        | 650    | -                               | -                       |
| Profit (SR)            | 111.3           | 292.6           | 4.5      | 49.6           | 1170       | 1628   | -                               | -                       |
| egg<br>(piece)         | 159             | 95              | 0        | 0              | 0          | 254    | 729                             | 475                     |
| butter<br>(g)          | 14999           | 0               | 0        | 0              | 825        | 15824  | 20000                           | 4176                    |
| sugar (g)              | 0               | 2112.8          | 0        | 0              | 2250       | 4362.8 | 32000                           | 27637.2                 |
| cream<br>( piece)      | 0               | 0               | 0        | 496            | 300        | 796    | 1776                            | 980                     |
| white cream (g)        | 2650            | 1900            | 0        | 0              | 600        | 5150   | 14500                           | 9350                    |
| Liquid milk (piece)    | 0               | 38              | 1.8      | 0              | 0          | 39.8   | 58                              | 18.2                    |
| Condensed milk (piece) | 0               | 0               | 3.6      | 124            | 0          | 127.6  | 163                             | 35.4                    |
| yogurt<br>(g)          | 0               | 0               | 0        | 0              | 13500      | 13500  | 46250                           | 32750                   |
| Milk Powder (g)        | 0               | 0               | 0        | 0              | 6000       | 6000   | 17500                           | 11500                   |
| Lotus biscuit (g)      | 0               | 0               | 360      | 0              | 0          | 360    | 600                             | 240                     |
| Gelatin<br>(g)         | 0               | 0               | 0        | 0              | 75         | 75     | 650                             | 575                     |
| Max Mix (g)            | 13250           | 8930            | 0        | 0              | 0          | 22180  | 67000                           | 44820                   |
| Caramel powder (g)     | 0               | 0               | 0        | 11160          | 0          | 11160  | 14880                           | 3720                    |
| Filling (g)            | 13250           | 0               | 0        | 0              | 0          | 13250  | 13250                           | 0                       |
| Croissant (piece)      | 0               | 0               | 63       | 0              | 0          | 63     | 108                             | 45                      |
| Salty biscuits (g)     | 0               | 0               | 0        | 10664          | 0          | 10664  | 15000                           | 4336                    |

# Production per day after the model (the optimal solution):

Table 4: Production information per day after the model:

| Products              | Regula<br>r cake | Saffron<br>cake | kiryatu<br>s | Latte<br>sweet | cheesecake | Total   | Available<br>of raw<br>material | The raw material unused |
|-----------------------|------------------|-----------------|--------------|----------------|------------|---------|---------------------------------|-------------------------|
| Units produced        | 53               | 281             | 9            | 318            | 437        | 1098    | -                               | -                       |
| Profit (SR)           | 111.3            | 432.74          | 4.5          | 63.6           | 3408.6     | 4020.74 | -                               | -                       |
| egg<br>(piece)        | 159              | 140.5           | 0            | 0              | 0          | 299.5   | 729                             | 429.5                   |
| butter (g)            | 14999            | 0               | 0            | 0              | 2403.5     | 17402.5 | 20000                           | 2597.5                  |
| sugar<br>(g)          | 0                | 3124.72         | 0            | 0              | 6555       | 9679.72 | 32000                           | 22320.28                |
| cream<br>( piece)     | 0                | 0               | 0            | 636            | 874        | 1510    | 1776                            | 266                     |
| white cream (g)       | 2650             | 2810            | 0            | 0              | 1748       | 7208    | 14500                           | 7292                    |
| Liquid milk (piece)   | 0                | 56.2            | 1.8          | 0              | 0          | 58      | 58                              | 0                       |
| Condensed milk(piece) | 0                | 0               | 3.6          | 159            | 0          | 162.6   | 163                             | 0.4                     |
| Yogurt (g)            | 0                | 0               | 0            | 0              | 39330      | 39330   | 46250                           | 6920                    |
| Milk Powder (g)       | 0                | 0               | 0            | 0              | 17480      | 17480   | 17500                           | 20                      |
| Lotus biscuit (g)     | 0                | 0               | 360          | 0              | 0          | 360     | 600                             | 240                     |
| Gelatin<br>(g)        | 0                | 0               | 0            | 0              | 218.5      | 218.5   | 650                             | 431.5                   |
| Max Mix (g)           | 13250            | 13207           | 0            | 0              | 0          | 26457   | 67000                           | 40543                   |
| Caramel powder (g)    | 0                | 0               | 0            | 14310          | 0          | 14310   | 14880                           | 570                     |
| filling<br>(g)        | 13250            | 0               | 0            | 0              | 0          | 13250   | 13250                           | 0                       |
| Croissant (piece)     | 0                | 0               | 63           | 0              | 0          | 63      | 108                             | 45                      |
| Salty biscuits (g)    | 0                | 0               | 0            | 13674          | 0          | 13674   | 15000                           | 1326                    |

The model has increased production by 281 unit of saffron cake, 318 unit of latte sweet, and 437 unit of cheesecake, in order to increase profit while not exceeding the available raw materials. The units produced of regular cake did not change due to the amount of filling available as well as kiryatus because liquid milk have been used for Saffron cake because saffron has more profit.

#### Comparison between results before and after modeling:

Table 5: Compare results before and after modeling:

|        | Total<br>units<br>produced | Total unused raw<br>material<br>(g) | Total<br>unused raw<br>material<br>(piece) | Production<br>hours<br>(Per day) | Workers            | Total<br>profit<br>(SR) |
|--------|----------------------------|-------------------------------------|--|----------------------------------|--------------------|-------------------------|
| Before | 650                        | 139104.2                            | 1553.6                                     | 39.925                           | 5                  | 1628                    |
| After  | 1098                       | 82260.28                            | 740.9                                      | 57.6                             | 7 (1.6h over time) | 4020.74                 |

As the table shows the profit has increased by 2392.74 SR per day, 873350.1 SR per year.

Total unused raw material reduced by 56843.92 g and 812.7 piece.

Production hours has increased by 17.675 hours per day which means need for two more workers and 1.6 hours over time.

#### **Conclusions and recommendations:**

As seen from the results, we advise the factory to consider the results of the study because it gives a higher profit compared to the current situation.

Of course, the demand for products is volatile, and the establishment may encounter difficulties in achieving the results of the study. Therefore, we propose the following solutions:

The first solution: Promote products for which the study has shown benefit by increasing production per day, in order to increase the demand for them, or contract with other selling stores in order to sell these products. Knowing that there will be some remaining quantities of raw materials that will not be used even after applying the results of the study.

The second solution: In the event of the inability to implement the first solution, we advise them to reduce the quantities of unused raw materials to reduce the cost and not to waste it.