

**1-What quantity of water should be added to the milk water mixture so that the milk water ratio changes from 2:3 to 4:11. The quantity of milk in the mixture is 40 litres?**

Initial quantity of water =  $(\frac{3}{2}) \times$  Initial quantity of milk

$$= (\frac{3}{2}) \times 40$$

= 60 liters

The final quantity of milk in the mixture remains 40 liters.

Final quantity of water =  $(\frac{11}{4}) \times$  Final quantity of milk

$$= (\frac{11}{4}) \times 40$$

= 110 liters

Quantity of water to be added = 110 - 60

= 50 liters

**2-Linear equation  $2x+3y=0$  meets the x & y-axis at the point?**

When the equation intersects the x-axis, the value of y is 0. Substituting  $y = 0$  into the equation:

$$2x + 3(0) = 0$$

$$x = 0$$

So, the point of intersection with the x-axis is (0, 0).

When the equation intersects the y-axis, the value of x is 0. Substituting  $x = 0$  into the equation:

$$2(0) + 3y = 0$$

$$y = 0$$

So, the point of intersection with the y-axis is (0, 0).

Therefore, the linear equation  $2x + 3y = 0$  intersects both the x-axis and y-axis at the point (0, 0).

**3-a & b are positive integers such that  $a^2-b^2=19$ . Find a & b?**

$$a^2 - b^2 = 19 \rightarrow (a - b)(a + b) = 19.$$

a-b can be negative or positive, but a+b will always be positive

The factors of 19 are 1 and 19, or -1 and -19, but -1 and -19 can not be true for our equation

Case 1:

$$(a - b) = 1$$

$$(a + b) = 19$$

By solving this system, we find  $a = 10$  and  $b = 9$ .

Case 2:

$$(a - b) = 19$$

$$(a + b) = 1$$

This equation is not possible for any real values of  $a$  and  $b$

Therefore, the solution to the equation  $a^2 - b^2 = 19$ , with  $a$  and  $b$  as positive integers, is  $a = 10$  and  $b = 9$ .

**5- Sum of two, two-digit numbers is a perfect square. The digits of the first two-digit number are two consecutive positive integers; also, when the digits of the first number are reversed, the second number is formed. Find these numbers & the square root of their sum.**

Since first number digits are consecutive positive integers, then the two-digit numbers formed by the consecutive positive integers can be assumed as  $a$  and  $a + 1$ .

The first two-digit number can be represented as  $10a + (a + 1) = 11a + 1$ .

The second two-digit number, formed by reversing the digits of the first number, is

$$10(a + 1) + a = 11a + 10.$$

Given that the sum of these two-digit numbers is a perfect square, we can write the equation as:

$$(11a + 1) + (11a + 10) = n^2,$$

$$22a + 11 = n^2,$$

$$11(2a + 1) = n^2.$$

$$11 \cdot 11 = 11^2$$

$$\text{Therefore, } 2a + 1 = 11$$

$$a = 5$$

Thus, the two numbers are 56 and 65, and the square root of their sum is 11.