

Question 3

1)

Assuming `fmap = <$>`,

```
(<$>) :: (a -> b) -> [a] -> [b]
_ <$> [] = []
f <$> (x:xs) = (f $ x) : (f <$> xs)
```

2)

```
pure :: a -> [a]
pure a = [a]

(<*>) :: [a -> b] -> [a] -> [b]
[] <*> _ = []
_ <*> [] = []
(f:fs) <*> (x:xs) = (f <$> pure x) ++ (fs <*> xs)
```

3)

Assuming `x = [x']`,

Note : `(\g -> g y) = ($ y)`,

<code>x <*> pure y</code>	<code>[by assumption]</code>
<code>= [x'] <*> pure y</code>	<code>[apply pure]</code>
<code>= [x'] <*> [y]</code>	<code>[apply <*>]</code>
<code>= (x' <\$> pure y) ++ ([] <*> [])</code>	<code>[apply pure]</code>
<code>= (x' <\$> [y]) ++ ([] <*> [])</code>	<code>[apply <*>]</code>
<code>= (x' <\$> [y]) ++ []</code>	<code>[apply ++]</code>
<code>= (x' <\$> [y])</code>	<code>[apply <\$>]</code>
<code>= (x' \$ y) : (x' <\$> [])</code>	<code>[apply <\$>]</code>
<code>= (x' \$ y) : []</code>	<code>[apply (:)]</code>
<code>= [(x' \$ y)]</code>	<code>[unapply (\$ y)]</code>
<code>= [(\$ y) x']</code>	<code>[unapply <\$>]</code>
<code>= [(\$ y)] <\$> [x']</code>	<code>[unapply <*>]</code>
<code>= pure (\$ y) <*> [x']</code>	<code>[note]</code>
<code>= pure (\g -> g y) <*> [x']</code>	<code>[by assumption]</code>
<code>= pure (\g -> g y) <*> x</code>	