

①

$$q = 11$$

$$q = 11$$

$$2^5 \bmod 11$$

$$32 \bmod 11$$

$$10$$

②

$$x < q$$

and (P.R) primitive root
mod 11

Power	1	2	3	4	5	6	7	8	9	10
1	1	1	1	1	1	1	1	1	1	1
α 2	2	4	8	5	10	9	7	3	6	1
3										
4										
5										
6										
7										
8										
9										
10										

$$x = 2$$

Private key

③

$$x_A < q$$

$$8 < 11 \Rightarrow x_A = 8$$

④

$$y_A = \alpha^{x_A} \bmod q$$

$$= 2^8 \bmod 11$$

$$= 256 \bmod 11$$

$$y_A = 3$$

$$x = 2$$

Private key

$$x_B < q$$

$$4 < 11 \Rightarrow x_B = 4$$

$$y_B = \alpha^{x_B} \bmod q$$

$$= 2^4 \bmod 11$$

$$= 16 \bmod 11$$

$$y_B = 5$$

$$y_B = 5$$

$$K = x_B^{x_A} \bmod q$$

$$= 5^8 \bmod 11$$

$$K = 4$$

$$y_A = 3$$

$$K = y_A^{x_B} \bmod q$$

$$= 3^4 \bmod 11$$

$$K = 4$$