

(1)

①

$$\alpha^r = 11$$

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$$\begin{cases} 2^5 \bmod 11 \\ 3^2 \bmod 11 \end{cases}$$

$$\alpha < q$$

and  
 $\bmod 11$

(P.R) primitive root

10

②

Power	1	2	3	4	5	6	7	8	9	10
$\alpha$	1	1	1	1	1	1	1	1	1	1
2	2	4	8	5	10	9	7	3	6	1
3										
4										
5										
6										
7										
8										
9										
10										

$$\alpha = 2$$

$$\alpha = 2$$

private key

private key

③

$$X_A < q$$

$$X_B < q$$

$$8 < 11 \Rightarrow X_A = 8$$

$$4 < q \Rightarrow X_B = 4$$

④

$$Y_A = \alpha^{X_A} \bmod q$$

$$Y_B = \alpha^{X_B} \bmod q$$

$$= 2^8 \bmod 11$$

$$= 2^4 \bmod 11$$

$$= 256 \bmod 11$$

$$= 16 \bmod 11$$

$$Y_A = 3$$

$$Y_B = 5$$

$$Y_B = 5$$

$$Y_A = 3$$

$$K = \frac{Y_A^{X_B}}{Y_B^{X_A}} \bmod q$$

$$K = Y_A^{X_B} \bmod q$$

$$= 3^4 \bmod 11$$

$$= 81 \bmod 11$$

$$K = 4$$

$$K = 4$$