FOX Specifications Version 1.2

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In this document, we describe the design of a new family of block ciphers, named FOX. The main goals of this design, besides a very high security level, are a large implementation flexibility on various platforms as well as high performances. The high-level structure is based on a Lai-Massey scheme, while the round functions are substitution-permutation networks. In addition, we propose a new design of strong and efficient key-schedule algorithms. FOX is the result of a joint project with the company MediaCrypt AG in Zürich, Switerland (http://www.mediacrypt.com); the design has furthermore benefited from expert reviews of Prof. Jacques Stern, École Normale Supérieure, Paris (France) and of Prof. David Wagner, University of California, Berkeley (USA). FOX may be subject to patenting and licensing issues: please contact MediaCrypt (email info@mediacrypt.com) for more information about them. This document is organized as follows: in §1, the conventions and mathematical notations used throughout this document are described. §2 describes formally the cipher family, while §3 gives the mathematical foundations and rationales behind FOX. §4 discusses several issues related to the implementation of FOX. Finally, a reference implementation written in C is given; its sole goal is to help to understand how FOX is defined and to furnish test vectors.

 $^{^1}$ This document is the extended version of [JV04a]; it superseeds EPFL technical reports IC/2003/82 and IC/2004/75 entitled respectively "FOX Specifications Version 1.0" and "FOX Specifications Version 1.1".

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Name	Block size (in bits)	Key size (in bits)	Rounds number
FOX64	64	128	16
FOX128	128	256	16
FOX64/k/r	64	k	r
FOX128 $/k/r$	128	k	r

Figure 1: Members of the FOX family

1 Notations

The purpose of this section is to define the mathematical notations, conventions and symbols used throughout this document.

1.1 The FOX Family

The family consists in two main block cipher designs, the first one having a 64-bit blocksize and the other one a 128-bit blocksize. Each design allows a variable number of rounds and a variable key size up to 256 bits. The different members of the FOX family are listed in Fig. 1. The following conditions must hold in the case of FOX64/k/r and FOX128/k/r: the number of rounds r must satisfy $12 \le r \le 255$, while the key length k must satisfy $0 \le k \le 256$, with k multiple of 8.

1.2 Hexadecimal Notation

The hexadecimal notation will be intensively used in this document to write binary strings in a compact way. Numbers written in hexadecimal notations begins with the prefix 0x. For instance, 0x01234567 is a 32-bit value. The following table gives the correspondance between decimal digits, hexadecimal digits and binary values.

Decimal	0	1	2	3	4	5	6	7
Binary	0000	0001	0010	0011	0100	0101	0110	0111
Hexadecimal	0x0	0x1	0x2	0x3	0x4	0x5	0x6	0x7
D 1		^	4.0		4.0	4.0		
Decimal	8	9	10	11	12	13	14	15
Binary	1000	1001	1010	1011	12 1100	13 1101	14 1110	15 1111

1.3 Mathematical Operations

Fig. 2 is a list of the mathematical operations used throughout this document together with their meanings. Note that the GF (2^8) representation is defined in §1.6.

1.4 Prefixes, Indices and Suffixes

Here are some generic conventions used in the notation:

- A variable x written with the suffix (n) (i.e. $x_{(n)}$) indicates that x has a length of n bits. For instance, $y_{(1)}$ is a single-bit variable and $F_{(64)}$ is a 64-bit value. The suffix will be omitted if the context is clear.
- A variable x written with the suffix [a...n] (i.e. $x_{[a...b]}$) indicates the bit subset of the variable x beginning at position a (inclusive) and ending at position b (inclusive).

	Mathematical Sym	nbols
Operation	Description	Example
$\lfloor a \rfloor$	"Floor" function	$\lfloor 12.34 \rfloor = 12$
$\lceil a \rceil$	"Ceil" function	$\lceil 12.34 \rceil = 13$
$a\oplus b$	Bitwise exclusive-OR	$0xABCD \oplus 0x1234 = 0xB9F9$
$a \wedge b$	Bitwise AND	$0xABCD \land 0x1234 = 0x0204$
$a \vee b$	Bitwise OR	$0xABCD \lor 0x1234 = 0xBBFD$
$a \ll n$	Logical left shift of n positions	$0x03 \ll 1 = 0x06$
$a \gg n$	Logical right shift of n positions	$0x03 \gg 1 = 0x01$
\overline{a}	Logical negation	$\overline{\text{OxA}} = \text{Ox5}$
a b	Concatenation	0xABCD 0x1234 = 0xABCD1234
$a \oplus b$	Addition in $GF(2^8)$	$0x02 \oplus 0x06 = 0x04$
$a \cdot b$	Multiplication in $GF(2^8)$	$0x02 \cdot 0x60 = 0xC0$

Figure 2: Mathematical Operations

- Indexed variables are denoted as follows: x_i is a variable x indexed by i. A variable x indexed by i with a length of ℓ bits is denoted $x_{i(\ell)}$. A C-like notation is used for indexing which means that indices begin with 0.
- The suffix I is used to denote the left half of a variable. For instance, x_{I} is the left half of the variable x.
- The suffix r is used to denote the right half of a variable. For instance, x_r is the right half of the variable x.
- The suffixes II, Ir, rI, rr are used to denote quarters of a variable. For instance, $x = x_{\text{II}} ||x_{\text{Ir}}||x_{\text{rI}}||x_{\text{rr}}$.
- In general, the input of a function f is denoted x and its output y.

1.5 Byte Ordering

In this document, a big-endian ordering is assumed. The index of the most significant part in a variable is equal to 0, while the index corresponding to the least significant part is the largest one. Here is an example: a 128-bit value $q_{(128)}$ can be written as

$$\begin{array}{lcl} q_{(128)} & = & r_{0(64)}||r_{1(64)} \\ & = & s_{0(32)}||s_{1(32)}||s_{2(32)}||s_{3(32)} \\ & = & t_{0(8)}||t_{1(8)}||\dots||t_{14(8)}||t_{15(8)} \\ & = & u_{0(1)}||u_{1(1)}||\dots||u_{126(1)}||u_{127(1)} \end{array}$$

1.6 Finite Field $GF(2^8)$

Some of the mathematical operations used in FOX are the addition and the multiplication in the finite field with 256 elements, which is denoted GF (2^8). We describe now the *representation* of GF (2^8) used in the FOX definition. Let be the following irreducible polynomial $P(\alpha)$ over GF (2^8):

$$P(\alpha) = \alpha^8 + \alpha^7 + \alpha^6 + \alpha^5 + \alpha^4 + \alpha^3 + 1 \tag{1}$$

Elements of the field are polynomials in α of degree at most 7 with coefficients in GF (2). Let s be an 8-bit binary string

$$s = s_{0(1)}||s_{1(1)}||s_{2(1)}||s_{3(1)}||s_{4(1)}||s_{5(1)}||s_{6(1)}||s_{7(1)}|$$

The corresponding field element is

$$s_{0(1)}\alpha^7 + s_{1(1)}\alpha^6 + s_{2(1)}\alpha^5 + s_{3(1)}\alpha^4 + s_{4(1)}\alpha^3 + s_{5(1)}\alpha^2 + s_{6(1)}\alpha + s_{7(1)}$$

1.6.1 Addition in GF (2^8)

The addition in GF (2^8) , denoted \oplus , is the usual addition of polynomials where the respective coefficients are added modulo 2. For instance,

$$(\alpha^7 + \alpha^6 + \alpha^3 + \alpha^2 + 1) \oplus (\alpha^6 + \alpha^5 + \alpha + 1) = \alpha^7 + \alpha^5 + \alpha^3 + \alpha^2 + \alpha^4 +$$

Note that the addition $a \oplus b$ of two elements of GF (2⁸) is equivalent to a bitwise exclusive-OR operation of their representation as an 8-bit binary string.

1.6.2 Multiplication in GF (2^8)

The multiplication in GF (2⁸), denoted "·", is the usual multiplication of polynomials where the result is taken modulo the polynomial defined in Eq. (1) and coefficients are reduced modulo 2. The reduction modulo $P(\alpha)$ can be computed by taking the rest of the Euclidean division of the product by $P(\alpha)$. For instance,

$$(\alpha^5 + \alpha^4 + \alpha^3) \cdot (\alpha^3 + \alpha + 1) = \alpha^8 + \alpha^7 + \alpha^3$$

$$\equiv \alpha^6 + \alpha^5 + \alpha^4 + 1 \pmod{P(\alpha)}$$

2 Description

In this part of the document, we describe precisely both versions of FOX, *i.e.* the one having a 64-bit block size (FOX64/k/r) and the one with a block size of 128 bits (FOX128/k/r).

This chapter is organized as follows: in $\S 2.1.1$, the high-level structure of $\mathsf{FOX64}/k/r$, which is a $Lai\text{-}Massey\ scheme$, is formally described, together with the encryption and decryption operations. In $\S 2.1.2$, the same is done for $\mathsf{FOX128}/k/r$, which is built on an $Extended\ Lai-Massey\ scheme$. In $\S 2.2$, the $internal\ functions\ f32$ and f64 used in both algorithms are formally defined, together with their building blocks. Finally, in $\S 2.3$, the key-schedule algorithm is described.

2.1 High-Level Structure

In this part, we describe the skeleton and the encryption/decryption processes for FOX64 and FOX128. For this purpose, we will follow a top-down approach.

2.1.1 FOX64/k/r Skeleton

The 64-bit version of FOX is the (r-1)-times iteration of a round function denoted Imor64, followed by the application of a slightly modified version of Imor64, named Imid64. Imio64 is a function used during the decryption operation. Formally, Imor64, Imio64 and Imid64 take all a 64-bit input $x_{(64)}$, a 64-bit round key $rk_{(64)}$ and return a 64-bit output $y_{(64)}$:

$$\mathsf{Imor64}, \mathsf{Imio64}, \mathsf{Imid64}: \left\{ \begin{array}{ccc} \{0,1\}^{64} \times \{0,1\}^{64} & \to & \{0,1\}^{64} \\ (x_{(64)}, rk_{(64)}) & \mapsto & y_{(64)} \end{array} \right.$$

FOX64 Encryption The encryption $c_{(64)}$ by FOX64/k/r of a 64-bit plaintext $p_{(64)}$ is defined as

$$c_{(64)} = \mathsf{Imid64}(\mathsf{Imor64}(\dots(\mathsf{Imor64}(p_{(64)}, rk_{0(64)}), \dots, rk_{r-2(64)}), rk_{r-1(64)})$$

where

$$rk_{(r\cdot 64)} = rk_{0(64)}||rk_{1(64)}||\dots||rk_{r-1(64)}|$$

is the subkey stream produced by the key schedule algorithm from the key $k_{(\ell)}$.

FOX64 **Decryption** The decryption $p_{(64)}$ by FOX64/k/r of a 64-bit ciphertext $c_{(64)}$ is defined as

$$p_{(64)} = \text{Imid64}(\text{Imio64}(\dots(\text{Imio64}(c_{(64)}, rk_{r-1(64)}), \dots, rk_{1(64)}), rk_{0(64)})$$

where

$$rk_{(r\cdot 64)} = rk_{0(64)}||rk_{1(64)}||\dots||rk_{r-1(64)}|$$

is the subkey stream produced by the key schedule algorithm from the key $k_{(\ell)}$, as for the encryption.

2.1.2 FOX128/k/r Skeleton

Similarly to the definition of FOX64, the 128-bit version of FOX is the (r-1)-times iteration of a round function denoted elmor128, followed by the application of a modified version of elmor128 named elmid128. elmio128 is a function used during the decryption operation. Formally, elmor128, elmio128 and elmid128 all take a 128-bit input $x_{(128)}$, a 128-bit round key $rk_{(128)}$ and return a 128-bit output $y_{(128)}$:

elmor128, elmio128, elmid128 :
$$\left\{ \begin{array}{ccc} \{0,1\}^{128} \times \{0,1\}^{128} & \to & \{0,1\}^{128} \\ (x_{(128)}, rk_{(128)}) & \mapsto & y_{(128)} \end{array} \right.$$

FOX128 Encryption The encryption $c_{(128)}$ by FOX128/k/r of a 128-bit plaintext $p_{(128)}$ is defined as

$$c_{(128)} =$$
 elmid128(elmor128(...elmor128($p_{(128)}, rk_{0(128)}), \ldots, rk_{r-2(128)}), rk_{r-1(128)})$

where

$$rk_{(r\cdot 128)} = rk_{0(128)} ||rk_{1(128)}|| \dots ||rk_{r-1(128)}||$$

is the subkey stream produced by the key schedule algorithm from the key $k_{(\ell)}$.

FOX128 Decryption The decryption $p_{(128)}$ by FOX128/k/r of a 128-bit ciphertext $c_{(128)}$ is defined as

$$p_{(128)} =$$
 elmid128(elmio128(...elmio128($C_{(128)}, rk_{r-1(128)}), \ldots, rk_{1(128)}), rk_{0(128)}$)

where

$$rk_{(r\cdot 128)} = rk_{0(128)} ||rk_{1(128)}|| \dots ||rk_{r-1(128)}||$$

is the subkey stream produced by the key schedule algorithm from the key $k_{(\ell)}$, as for the encryption operation.

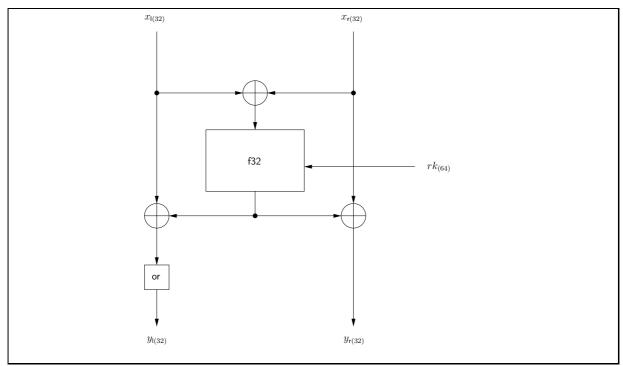


Figure 3: Imor64 Round Function

2.2 Internal Functions

In this part, we describe formally all the functions used internally in the core of both algorithms FOX64/k/r and FOX128/k/r.

2.2.1 Definitions of Imor64, Imid64, Imio64

In the 64-bit version of the algorithm, one uses three slightly different round functions. The first one, Imor64, illustrated in Fig. 3, is built as a Lai-Massey scheme combined with an orthomorphism² or. This function transforms a 64-bit input $x_{(64)}$ split in two parts $x_{(64)} = x_{I(32)}||x_{r(32)}|$ and a 64-bit round key $rk_{(64)}$ in a 64-bit output $y_{(64)} = y_{I(32)}||y_{r(32)}|$ as follows:

$$\begin{array}{lll} y_{(64)} & = & y_{\mathsf{I}(32)} || y_{\mathsf{r}(32)} = \mathsf{Imor64} \left(x_{\mathsf{r}(32)} || x_{\mathsf{r}(32)} \right) \\ & = & \mathsf{or} \left(x_{\mathsf{I}(32)} \oplus \mathsf{f32} \left(x_{\mathsf{I}(32)} \oplus x_{\mathsf{r}(32)}, rk_{(64)} \right) \right) \big| \big| \\ & & \left(x_{\mathsf{r}(32)} \oplus \mathsf{f32} \left(x_{\mathsf{I}(32)} \oplus x_{\mathsf{r}(32)}, rk_{(64)} \right) \right) \end{array}$$

The Imid64 function is a slightly modified version of Imor64, namely it is the same one without the orthomorphism or:

$$\begin{array}{lll} y_{(64)} & = & y_{\mathsf{I}(32)} || y_{\mathsf{r}(32)} = \mathsf{Imid64} \left(x_{\mathsf{I}(32)} || x_{\mathsf{r}(32)} \right) \\ & = & \left(x_{\mathsf{I}(32)} \oplus \mathsf{f32} \left(x_{\mathsf{I}(32)} \oplus x_{\mathsf{r}(32)}, rk_{(64)} \right) \right) \big| \big| \\ & & \left(x_{\mathsf{r}(32)} \oplus \mathsf{f32} \left(x_{\mathsf{I}(32)} \oplus x_{\mathsf{r}(32)}, rk_{(64)} \right) \right) \end{array}$$

²An orthomorphism o on a group $(\mathcal{G},+)$ is a permutation $x\mapsto o(x)$ on \mathcal{G} such that $x\mapsto o(x)-x$ is also a permutation.

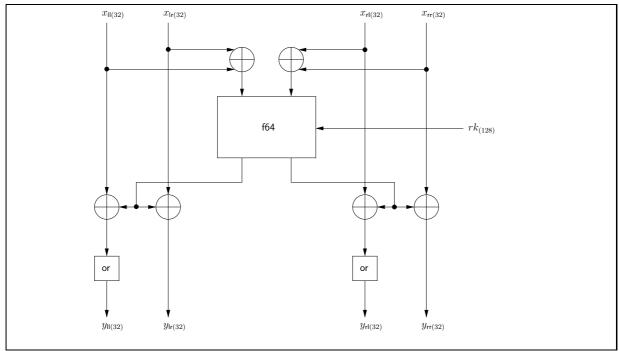


Figure 4: Round function elmor128

Finally, Imio64 is defined by

$$\begin{array}{lll} y_{(64)} & = & y_{\mathsf{I}(32)} || y_{\mathsf{r}(32)} = \mathsf{Imio64} \left(x_{\mathsf{I}(32)} || x_{\mathsf{r}(32)} \right) \\ & = & \mathsf{io} \left(x_{\mathsf{I}(32)} \oplus \mathsf{f32} \left(x_{\mathsf{I}(32)} \oplus x_{\mathsf{r}(32)}, rk_{(64)} \right) \right) \big| \big| \\ & & \left(x_{\mathsf{r}(32)} \oplus \mathsf{f32} \left(x_{\mathsf{I}(32)} \oplus x_{\mathsf{r}(32)}, rk_{(64)} \right) \right) \end{array}$$

where io is the inverse of the orthormorphism or.

2.2.2 Definitions of elmor128, elmid128, elmio128

In the 128-bit version of the algorithm, one uses three slightly different round functions, as in the 64-bit version. The first one, elmor128, illustrated in Fig. 4, is built as an *Extended Lai-Massey scheme* combined with two orthomorphisms or. This function transforms a 128-bit input $x_{(128)}$ split in four parts $x_{(128)} = x_{\text{II}(32)} ||x_{\text{Ir}(32)}||x_{\text{rl}(32)}||x_{\text{rr}(32)}$ and a 128-bit round key $rk_{(128)}$ in a 128-bit output $y_{(128)} = y_{\text{II}(32)} ||y_{\text{Ir}(32)}||y_{\text{rl}(32)}||y_{\text{rr}(32)}$ as follows:

$$\begin{array}{lll} y_{(128)} & = & y_{\mathrm{II}(32)} || y_{\mathrm{Ir}(32)} || y_{\mathrm{rI}(32)} || y_{\mathrm{rr}(32)} = \mathrm{elmor} 128 \left(x_{\mathrm{II}(32)} || x_{\mathrm{Ir}(32)} || x_{\mathrm{rI}(32)} || x_{\mathrm{rr}(32)} \right) \\ & = & \mathrm{or} \left(x_{\mathrm{II}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{I}(32)} \right) \Big| \Big| \\ & & \left(x_{\mathrm{Ir}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{I}(32)} \right) \Big| \Big| \\ & & & \mathrm{or} \left(x_{\mathrm{rI}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{r}(32)} \right) \Big| \Big| \\ & & & \left(x_{\mathrm{rr}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{r}(32)} \right) \Big| \Big| \end{array}$$

The elmid128 function is a slightly modified version of elmor128, namely it is the same one without the orthomorphism or:

$$\begin{array}{lll} y_{(128)} & = & y_{\mathrm{II}(32)} || y_{\mathrm{Ir}(32)} || y_{\mathrm{rI}(32)} || y_{\mathrm{rr}(32)} = \mathrm{elmid} 128 \left(x_{\mathrm{II}(32)} || x_{\mathrm{Ir}(32)} || x_{\mathrm{rI}(32)} || x_{\mathrm{rr}(32)} \right) \\ & = & \left(x_{\mathrm{II}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{I}(32)} \right) \Big| \Big| \\ & & \left(x_{\mathrm{Ir}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{I}(32)} \right) \Big| \Big| \\ & & \left(x_{\mathrm{rI}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{r}(32)} \right) \Big| \Big| \\ & & \left(x_{\mathrm{rr}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{r}(32)} \right) \Big| \Big| \end{array}$$

Finally, elmio128 is defined by

$$\begin{array}{lll} y_{(128)} & = & y_{\mathrm{II}(32)} || y_{\mathrm{Ir}(32)} || y_{\mathrm{rI}(32)} || y_{\mathrm{rr}(32)} = \mathrm{elmio} 128 \left(x_{\mathrm{II}(32)} || x_{\mathrm{Ir}(32)} || x_{\mathrm{rI}(32)} || x_{\mathrm{rr}(32)} \right) \\ & = & \mathrm{io} \left(x_{\mathrm{II}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{I}(32)} \right) \Big| \Big| \\ & & \left(x_{\mathrm{Ir}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{I}(32)} \right) \Big| \Big| \\ & & \mathrm{io} \left(x_{\mathrm{rI}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{r}(32)} \right) \Big| \Big| \\ & & \left(x_{\mathrm{rr}(32)} \oplus \mathrm{f64} \left((x_{\mathrm{II}(32)} \oplus x_{\mathrm{Ir}(32)}) || (x_{\mathrm{rI}(32)} \oplus x_{\mathrm{rr}(32)}), rk_{(128)} \right)_{\mathrm{r}(32)} \right) \Big| \Big| \end{array}$$

2.2.3 Definitions of or and io

The orthomorphism or is a function taking a 32-bit input $x_{(32)} = x_{l(16)} || x_{r(16)}$ and returning a 32-bit output $y_{(32)} = y_{l(16)} || y_{r(16)}$. It is defined as

$$y_{\mathsf{I}(16)}||y_{\mathsf{r}(16)} = \mathsf{or}\left(x_{\mathsf{I}(16)}||x_{\mathsf{r}(16)}\right) = x_{\mathsf{r}(16)}||\left(x_{\mathsf{I}(16)} \oplus x_{\mathsf{r}(16)}\right)$$

or is in fact a one-round Feistel scheme with the identity function as round function. The inverse function of or, denoted io, is defined as

$$y_{\mathsf{I}(16)}||y_{\mathsf{r}(16)} = \mathsf{io}\left(x_{\mathsf{I}(32)}||x_{\mathsf{r}(32)}\right) = \left(x_{\mathsf{I}(16)} \oplus x_{\mathsf{r}(16)}\right)||x_{\mathsf{I}(16)}|$$

2.2.4 Definition of f32

The function f32 builds the core of FOX64/k/r. It is built of three main parts: a substitution part, denoted sigma4, a diffusion part, denoted mu4, and a round key addition part (see Fig. 5). Formally, the f32 function takes a 32-bit input $x_{(32)}$, a 64-bit round key $rk_{(64)} = rk_{0(32)}||rk_{1(32)}|$ and returns a 32-bit output $y_{(32)}$. The f32 function is then formally defined as

$$\begin{array}{lll} y_{(32)} & = & \mathrm{f32}\left(x_{(32)}, rk_{(64)}\right) \\ & = & \mathrm{sigma4}(\mathrm{mu4}(\mathrm{sigma4}(x_{(32)} \oplus rk_{0(32)})) \oplus rk_{1(32)}) \oplus rk_{0(32)} \end{array}$$

2.2.5 Definition of f64

The function f64 builds the core of FOX128/k/r. It is built of three main parts: a substitution part, denoted sigma8, a diffusion part, denoted mu8, and a round key addition part (see Fig. 6). Formally, the f64 function takes a 64-bit input $x_{(64)}$, a 128-bit round key $rk_{(128)} = rk_{0(64)}||rk_{1(64)}|$ and returns a 64-bit output $y_{(64)}$. The f64 function is then defined as

$$\begin{array}{lcl} y_{(64)} & = & \mathsf{f64}\left(x_{(64)}, rk_{(128)}\right) \\ & = & \mathsf{sigma8}(\mathsf{mu8}(\mathsf{sigma8}(x_{(64)} \oplus rk_{0(64)})) \oplus rk_{1(64)}) \oplus rk_{0(64)} \end{array}$$

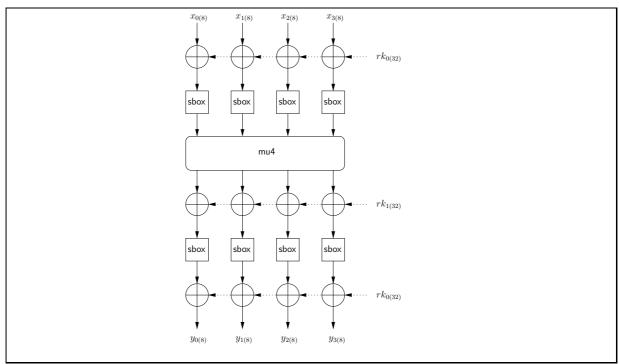


Figure 5: Function f32

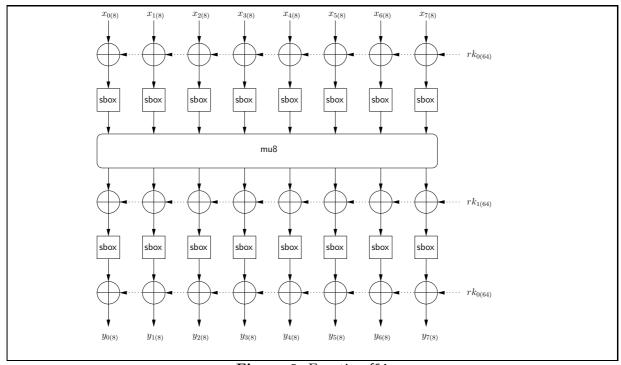


Figure 6: Function f64

	.0	.1	.2	.3	.4	.5	.6	.7	.8	.9	. A	.B	.C	.D	.E	.F
0.	5D	DE	00	В7	D3	CA	3C	OD	C3	F8	CB	8D	76	89	AA	12
1.	88	22	4F	DB	6D	47	E4	4C	78	9A	49	93	C4	CO	86	13
2.	A9	20	53	1C	4E	CF	35	39	B4	A1	54	64	03	C7	85	5C
3.	5B	CD	D8	72	96	42	В8	E1	A2	60	EF	BD	02	AF	8C	73
4.	7C	7F	5E	F9	65	E6	EB	AD	5A	A5	79	8E	15	30	EC	A4
5.	C2	3E	EO	74	51	FB	2D	6E	94	4D	55	34	ΑE	52	7E	9D
6.	4A	F7	80	FO	DO	90	A7	E8	9F	50	D5	D1	98	CC	AO	17
7.	F4	В6	C1	28	5F	26	01	AB	25	38	82	7D	48	FC	1B	CE
8.	3F	6B	E2	67	66	43	59	19	84	3D	F5	2F	C9	BC	D9	95
9.	29	41	DA	1A	ВО	E9	69	D2	7B	D7	11	9B	33	88	23	09
Α.	D4	71	44	68	6F	F2	ΟE	DF	87	DC	83	18	6A	EE	99	81
В.	62	36	2E	7A	FE	45	9C	75	91	OC	OF	E7	F6	14	63	1D
C.	OB	8B	ВЗ	F3	B2	3B	80	4B	10	A6	32	В9	8A	92	F1	56
D.	DD	21	BF	04	BE	D6	FD	77	EA	ЗА	C8	8F	57	1E	FA	2B
E.	58	C5	27	AC	E3	ED	97	BB	46	05	40	31	E5	37	2C	9E
F.	OA	B1	В5	06	6C	1F	AЗ	2A	70	FF	BA	07	24	16	C6	61

Figure 7: Mapping sbox

2.2.6 Definition of sigma4, sigma8 and sbox

The function sigma takes a 32-bit input $x_{(32)} = x_{0(8)} ||x_{1(8)}|| x_{2(8)} ||x_{3(8)}||$ and returns a 32-bit output $y_{(32)}$. It is defined as

$$\begin{array}{lll} y_{(32)} & = & \operatorname{sigma4} \left(x_{0(8)} || x_{1(8)} || x_{2(8)} || x_{3(8)} \right) \\ & = & \operatorname{sbox}(x_{0(8)}) || \operatorname{sbox}(x_{1(8)}) || \operatorname{sbox}(x_{2(8)}) || \operatorname{sbox}(x_{3(8)}) \end{array}$$

The function sigma8 takes a 64-bit input

$$x_{(64)} = x_{0(8)}||x_{1(8)}||x_{2(8)}||x_{3(8)}||x_{4(8)}||x_{5(8)}||x_{6(8)}||x_{7(8)}|$$

and returns a 64-bit output $y_{(64)}$. It is defined as

$$\begin{array}{lll} y_{(64)} & = & \operatorname{sigma8} \left(x_{0(8)} || x_{1(8)} || x_{2(8)} || x_{3(8)} || x_{4(8)} || x_{5(8)} || x_{6(8)} || x_{7(8)} \right) \\ & = & \operatorname{sbox}(x_{0(8)}) || \operatorname{sbox}(x_{1(8)}) || \operatorname{sbox}(x_{2(8)}) || \operatorname{sbox}(x_{3(8)}) || \\ & & \operatorname{sbox}(x_{4(8)}) || \operatorname{sbox}(x_{5(8)}) || \operatorname{sbox}(x_{6(8)}) || \operatorname{sbox}(x_{7(8)}) \end{array}$$

Finally, the sbox function is the lookup-up table defined in Fig. 7. We read this table as follows: to compute sbox(4C), one selects first the row named 4. (i.e. the fifth row), and then one selects the column named .C (i.e. the thirteenth column) and we get finally

$$sbox(4C) = 15$$

2.2.7 Definition of mu4

The diffusive part of f32 is a linear (4,4)-multipermutation defined on $GF(2^8)$. Formally, it is a function taking a 32-bit input

$$x_{(32)} = x_{0(8)} ||x_{1(8)}||x_{2(8)}||x_{3(8)}$$

and returning a 32-bit output

$$y_{(32)} = y_{0(8)} ||y_{1(8)}||y_{2(8)}||y_{3(8)}$$

and defined by

$$\begin{pmatrix} y_{0(8)} \\ y_{1(8)} \\ y_{2(8)} \\ y_{3(8)} \end{pmatrix} = \begin{pmatrix} 1 & 1 & 1 & \alpha \\ 1 & c & \alpha & 1 \\ c & \alpha & 1 & 1 \\ \alpha & 1 & c & 1 \end{pmatrix} \times \begin{pmatrix} x_{0(8)} \\ x_{1(8)} \\ x_{2(8)} \\ x_{3(8)} \end{pmatrix}$$

where

$$c = \alpha^{-1} + 1 = \alpha^7 + \alpha^6 + \alpha^5 + \alpha^4 + \alpha^3 + \alpha^2 + 1$$

All the additions and multiplications are defined in $GF(2^8)$ using the representation described in §1.6.

2.2.8 Definition of mu8

The diffusive part of 64 is a linear (8,8)-multipermutation defined on $GF(2^8)$. Formally, it is a function taking a 64-bit input

$$x_{(64)} = x_{0(8)} ||x_{1(8)}||x_{2(8)}||x_{3(8)}||x_{4(8)}||x_{5(8)}||x_{6(8)}||x_{7(8)}|$$

and returning a 64-bit output

$$y_{(64)} = y_{0(8)} ||y_{1(8)}||y_{2(8)}||y_{3(8)}||y_{4(8)}||y_{5(8)}||y_{6(8)}||y_{7(8)}||y_{7(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_{1(8)}||y_$$

f64 is defined as

$$\begin{pmatrix} y_{0(8)} \\ y_{1(8)} \\ y_{2(8)} \\ y_{3(8)} \\ y_{4(8)} \\ y_{5(8)} \\ y_{6(8)} \\ y_{7(8)} \end{pmatrix} = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 & 1 & a \\ 1 & a & b & c & d & e & f & 1 \\ a & b & c & d & e & f & 1 & 1 \\ b & c & d & e & f & 1 & a & 1 \\ c & d & e & f & 1 & a & b & 1 \\ d & e & f & 1 & a & b & c & 1 \\ e & f & 1 & a & b & c & d & 1 \\ f & 1 & a & b & c & d & e & 1 \end{pmatrix} \times \begin{pmatrix} x_{0(8)} \\ x_{1(8)} \\ x_{2(8)} \\ x_{3(8)} \\ x_{4(8)} \\ x_{5(8)} \\ x_{6(8)} \\ x_{7(8)} \end{pmatrix}$$

where

$$a = \alpha + 1$$

$$b = \alpha^{-1} + \alpha^{-2} = \alpha^7 + \alpha$$

$$c = \alpha$$

$$d = \alpha^2$$

$$e = \alpha^{-1} = \alpha^7 + \alpha^6 + \alpha^5 + \alpha^4 + \alpha^3 + \alpha^2$$

$$f = \alpha^{-2} = \alpha^6 + \alpha^5 + \alpha^4 + \alpha^3 + \alpha^2 + \alpha$$

All the additions and multiplications are defined in $\mathrm{GF}(2^8)$ using the representation described in §1.6.

2.3 Key-Schedule Algorithms

The key schedule is the algorithm which derives the subkey material

$$rk_{(r\cdot 64)} = rk_{0(64)} || rk_{1(64)} || \dots || rk_{r-1(64)}$$

and

$$rk_{(r\cdot 128)} = rk_{0(128)} ||rk_{1(128)}|| \dots ||rk_{r-1(128)}||$$

(for FOX64 and FOX128, respectively) from the key $k_{(\ell)}$.

_	Design	Block size	Key size	Key-Schedule Version	ek
_	FOX64	64	$0 \le \ell \le 128$	KS64	128
-	FOX64	64	$136 \le \ell \le 256$	KS64h	256
-	FOX128	128	$0 \le \ell \le 256$	KS128	256

Figure 8: Key-Schedule Algorithms Characteristics

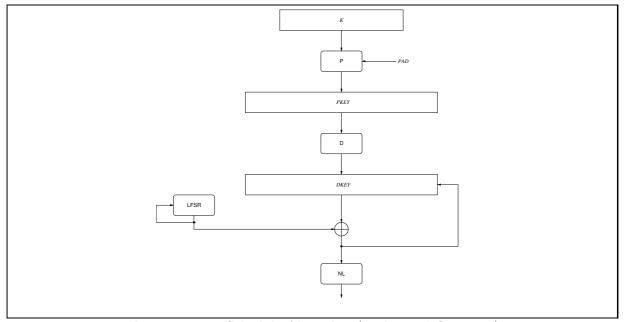


Figure 9: Key-Schedule Algorithm (High-Level Overview)

2.3.1 General Overview

A FOX key $k_{(\ell)}$ must have a bit-length ℓ such that $0 \le \ell \le 256$, and ℓ must be a multiple of 8. Depending on the key length and the block size, a member of the FOX block cipher family may use one among three different key-schedule algorithm versions, denoted respectively KS64, KS64h and KS128. A constant, ek, depends on these values as well. The table in Fig. 8 defines precisely the relation between the key size, the block size, the constant ek and the key-schedule algorithm version.

The three different versions of the key-schedule algorithm are constituted of four main parts: a padding part, denoted P, expanding $k_{(\ell)}$ into ek bits, a mixing part, denoted M, a diversification part, denoted D, whose core consists mainly in a linear feedback shift register denoted LFSR, and finally, a non-linear part, denoted NLx (see Fig. 9 and Alg. 1 for a high-level overview of the key-schedule algorithm design). As outlined above, the key-schedule algorithm definition depends on a the number of rounds r, on the key length ℓ and on the cipher (FOX64 or FOX128). In fact, NLx is the only part which differs between the different versions, and we will denote the three variants NL64, NL64h and NL128.

2.3.2 Definition of KS64

This key-schedule algorithm is designed to be used by FOX64 with keys smaller or equal to 128 bits. It takes the following parameters as input: a key k of length ℓ bits, with $0 \le \ell \le 128$ and a number of rounds r. It returns in output r 64-bit subkeys. KS64 is formally defined in Alg. 2.

Algorithm 1 Key-Schedule Algorithm (High-Level Description)

```
/* Preprocessing */
pkey \leftarrow P(k)
mkey \leftarrow M(pkey)
/* Initialization of the loop */
i \leftarrow 1
/* Loop */
while i \leq r do
dkey \leftarrow D(mkey, i, r)
Output rk_{i-1(x)} \leftarrow NLx(dkey)
i \leftarrow i+1
end while
```

Algorithm 2 Key-Schedule Algorithm KS64

```
/* Preprocessing */

if \ell < ek then

pkey = P(k)

mkey = M(pkey)

else

pkey = k

mkey = pkey

end if

/* Initialization of the loop */
i = 1

/* Loop */

while i \le r do

dkey = D(mkey, i, r)

Output rk_{i-1(64)} = NL64(dkey)

i = i + 1

end while
```

2.3.3 Definition of KS64h

This key schedule algorithm is designed to be used by FOX64 with keys larger than 128 bits. It takes the following parameters as input: a key k of length ℓ bits, with $136 \le \ell \le 256$ and a number of rounds r. It returns in output r 64-bit subkeys. KS64h is formally defined in Alg. 3.

Algorithm 3 Key-Schedule Algorithm KS64h

```
/* Preprocessing */
if \ell < ek then
  pkey = P(k)
  mkey = M(pkey)
else
  pkey = k
  mkey = pkey
end if
/* Initialization of the loop */
i = 1
/* Loop */
while i \leq r do
  dkey = D(mkey, i, r)
  Output rk_{i-1(64)} = NL64h(dkey)
  i = i + 1
end while
```

2.3.4 Definition of K\$128

This key schedule algorithm is designed to be used by FOX128. It takes the following parameters as input: a key k of length ℓ bits, with $0 \le \ell \le 256$ and a number of rounds r. It returns in output r 128-bit subkeys. KS128 is formally defined in Alg. 4.

Algorithm 4 Key-Schedule Algorithm KS128

```
/* Preprocessing */
if \ell < ek then
  pkey = P(k)
  mkey = M(pkey)
else
  pkey = k
  mkey = pkey
end if
/* Initialization of the loop */
i = 1
/* Loop */
while i \leq r do
  dkey = D(mkey, i, r)
  Output rk_{i-1(128)} = NL128(dkey)
  i = i + 1
end while
```

2.3.5 Definition of P

The P-part, taking ek and ℓ as input, is basically a function expanding a bit string by $\frac{ek-\ell}{8}$ bytes. More precisely, then P concatenates the input key k with the first $ek - \ell$ bits of the constant pad, giving pkey as output. The P function is defined formally in Alg. 5. The pad

Algorithm 5 P-Part

Output
$$pkey = k||pad_{[0...ek-\ell-1]}|$$

constant value is defined in the following section.

2.3.6 Definition of pad

The constant pad is defined as being the first 256 bits of the hexadecimal development of e-2:

$$e - 2 = \sum_{n=0}^{+\infty} \frac{1}{n!} - 2$$

Thus, it is the concatenation of the four following 64-bit constants

2.3.7 Definition of M

The M-part is used to mix the padded key pkey, such that the constant words are mixed uo by using the randomness provided by the key. This is done with help of a Fibonacci recursion. It takes as input a key pkey with length ek (expressed in bits). More formally, the padded key pkey is seen as an array of $\frac{ek}{8}$ bytes $pkey_{i(8)}, 0 \le i \le \frac{ek}{8} - 1$, and is mixed according to

$$mkey_{i(8)} = pkey_{i(8)} \oplus \left(mkey_{i-1(8)} + mkey_{i-2(8)} \mod 2^8\right) \quad 0 \le i \le \frac{ek}{8} - 1$$

with the convention that

$$mkey_{-2(8)} = 0x6A$$
 and $mkey_{-1(8)} = 0x76$

Note here that + denotes the addition performed modulo 2^8 while \oplus denotes the addition in GF (2^8), which is actually a XOR operation.

2.3.8 Definition of D

The D-part is a diversification part. It takes a key mkey having a length in bits equal to ek, the total round number r, and the current round number i, with $1 \le i \le r$; it modifies mkey with help of the output of a 24-bit Linear Shift Feedback Register (LFSR) denoted LFSR. More precisely, mkey is seen as an array of $\left\lfloor \frac{ek}{24} \right\rfloor$ 24-bit values $mkey_{j(24)}$, with $0 \le j \le \left\lfloor \frac{ek}{24} \right\rfloor - 1$ concatenated with one residue byte $mkeyrb_{(8)}$ (if ek = 128) or two residue bytes $mkeyrb_{(16)}$ (if ek = 256), and is modified according to

$$dkey_{j(24)} \ = \ mkey_{j(24)} \oplus \mathsf{LFSR}\left((i-1) \cdot \left\lceil \frac{ek}{24} \right\rceil + j, r \right)$$

for $0 \le j \le \lfloor \frac{ek}{24} \rfloor - 1$; the $dkeyrb_{(8)}$ value $(dkeyrb_{(16)})$ is obtained by XORing the most 8 (16) significant bits of LFSR $((i-1) \cdot \lceil \frac{ek}{24} \rceil + \lfloor \frac{ek}{24} \rfloor, r)$ with $mkeyrb_{(8)}$ $(mkeyrb_{(16)})$, respectively. The remaining 16 (8) bits of the LFSR routine output are discarded.

2.3.9 Definition of LFSR

The diversification part D needs a stream of pseudo-random values; it is produced by a 24-bit linear feedback shift register, denoted LFSR. This algorithm takes two inputs, the total number of rounds r and a number of preliminary clocking c. It is based on the following primitive polynomial of degree 24 over GF(2).

Definition 2.1 (Irreducible Polynomial $PKS(\xi)$). The polynomial representing $GF(2^{24})$ in the FOX block cipher family is the irreducible polynomial over GF(2) defined by

$$\mathsf{PKS}(\xi) = \xi^{24} + \xi^4 + \xi^3 + \xi + 1$$

The register is initially seeded with the value $0x6A||r_{(8)}||\overline{r_{(8)}}$, where $r_{(8)}$ is expressed as an 8-bit value, and $\overline{r_{(8)}}$ is its bitwise complemented version (i.e. $r_{(8)} = \overline{r_{(8)}} \oplus 0xFF$). LSFR is described formally in Alg. 6.

Algorithm 6 LFSR Algorithm

```
/* Initialization */
reg = 0x6A||r||\overline{r}
/* Pre-Clocking */
p = 0
while p < c do
p = p + 1
if (reg \text{ AND } 0x800000) \neq 0x000000 \text{ then}
reg = (reg \ll 1) \oplus 0x00001B
else
reg = (reg \ll 1)
end if
end while
Output reg
```

2.3.10 Definition of NL64

The NL64-part takes a single input: the 128-bit value dkey corresponding to the current round. The dkey value passes through a substitution layer (made of four parallel sigma4 functions), a diffusion layer (made of four parallel mu4 functions) and a mixing layer called mix64. Then, the constant $pad_{[0...127]}$ is XORed and the result is flipped if and only if k=ek. The result passes through a second substitution layer, it is hashed down to 64 bits and the resulting value is encrypted first with a lmor64 round function, where the subkey is the left half of the dkey value and second by a lmid64 function, where the subkey is the right half of dkey. The resulting value is defined to be the 64-bit round key. Fig. 10 illustrates the NL64 process and Alg. 7 describes it formally.

2.3.11 Definition of NL64h

The NL64h-part takes a single input: the 256-bit value dkey corresponding to the current round. The dkey value passes through a substitution layer (made of eight parallel sigma4 functions), a

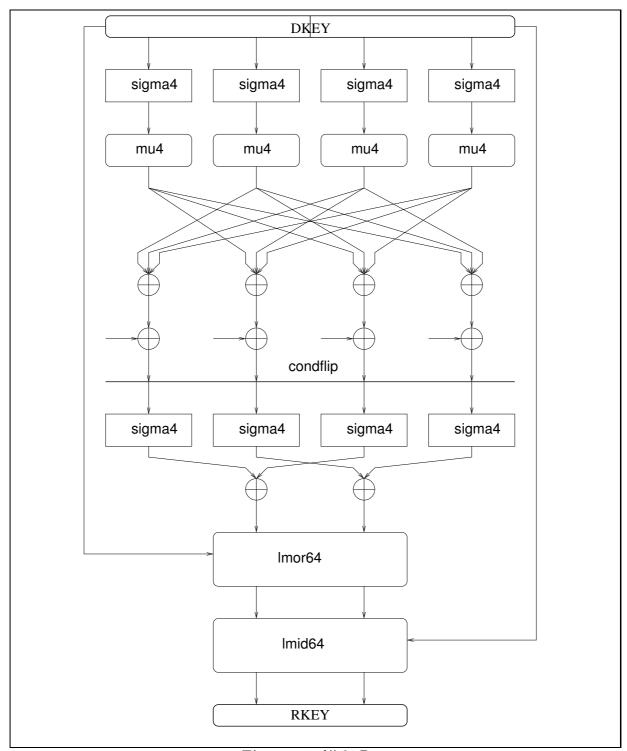


Figure 10: NL64 Part

Algorithm 7 NL64 Part

```
\begin{array}{c} t_{0(32)}||t_{1(32)}||\overline{t_{2(32)}||t_{3(32)}=dkey} \\ t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}=\operatorname{sigma4}(t_{0(32)})||\operatorname{sigma4}(t_{1(32)})||\operatorname{sigma4}(t_{2(32)})||\operatorname{sigma4}(t_{3(32)}) \\ t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}=\operatorname{mu4}(t_{0(32)})||\operatorname{mu4}(t_{1(32)})||\operatorname{mu4}(t_{2(32)})||\operatorname{mu4}(t_{3(32)}) \\ t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}=\operatorname{mix}64(t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}) \\ t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}=(t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)})\oplus\operatorname{pad}_{[0..127]} \\ \textbf{if }k=ek\ \textbf{then} \\ t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}=\overline{t_{0(32)}}||\overline{t_{1(32)}}||\overline{t_{2(32)}}||\overline{t_{3(32)}} \\ \textbf{end if} \\ t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}=\operatorname{sigma4}(t_{0(32)})||\operatorname{sigma4}(t_{1(32)})||\operatorname{sigma4}(t_{2(32)})||\operatorname{sigma4}(t_{3(32)}) \\ t_{0(32)}||t_{1(32)}=(t_{0(32)}\oplus t_{2(32)})||(t_{1(32)}\oplus t_{3(32)}) \\ t_{0(32)}||t_{1(32)}=\operatorname{lmor64}(t_{0(32)}||t_{1(32)},dkey_{[0...63]}) \\ t_{0(32)}||t_{1(32)}=\operatorname{lmid64}(t_{0(32)}||t_{1(32)},dkey_{[64...127]}) \\ \operatorname{Output}\ t_{0(32)}||t_{1(32)}\ \text{as round subkey}. \\ \end{array}
```

diffusion layer (made of eight parallel mu4 functions) and a mixing layer called mix64h. Then, the constant pad is XORed and the result is flipped if and only if k = ek. The result passes through a second substitution layer, it is hashed down to 64 bits and the resulting value is encrypted first with three lmor64 round functions, where the respective subkeys are the three left quarters of the dkey value and secondly by a lmid64 function, where the subkey is the rightmost quarter of dkey. The resulting value is defined to be the 64-bit round key. Fig. 11 illustrates the NL64h process and Alg. 8 describes it formally.

2.3.12 Definition of NL128

The NL128-part takes a single different input: the 256-bit value dkey corresponding to the current round. Basically, the dkey value passes through a substitution layer (made of four parallel sigma8 functions), a diffusion layer (made of four parallel mu8 functions) and a mixing layer called mix128. Then, the constant pad is XORed and the result is flipped if and only if k = ek. The result passes through a second substitution layer, it is hashed down to 128 bits and the resulting value is encrypted first with a elmor128 round function, where the subkey is the left half of the dkey value and second by a elmid128 function, where the subkey is the right half of dkey. The resulting value is defined to be the 128-bit round key. Fig. 12 illustrates the NL128 process and Alg. 9 describes it formally.

2.3.13 Definition of mix64

Given an input vector of four 32-bit values, denoted

$$x = x_{0(32)} ||x_{1(32)}||x_{2(32)}||x_{3(32)}|$$

the mix64 function consists in processing it by the following relations, resulting in an output vector denoted $y = y_{0(32)}||y_{1(32)}||y_{2(32)}||y_{3(32)}|$. More formally, mix64 is defined as

$$\begin{array}{rcl} y_{0(32)} & = & x_{1(32)} \oplus x_{2(32)} \oplus x_{3(32)} \\ y_{1(32)} & = & x_{0(32)} \oplus x_{2(32)} \oplus x_{3(32)} \\ y_{2(32)} & = & x_{0(32)} \oplus x_{1(32)} \oplus x_{3(32)} \\ y_{3(32)} & = & x_{0(32)} \oplus x_{1(32)} \oplus x_{2(32)} \end{array}$$

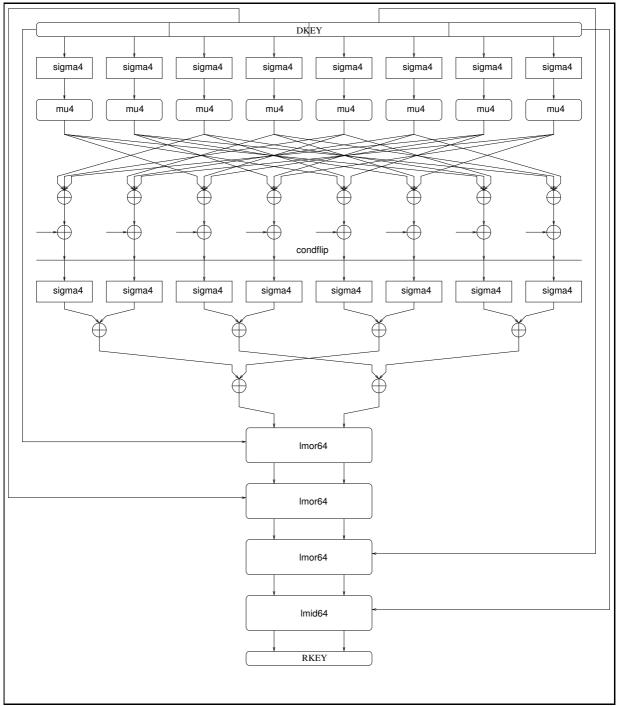


Figure 11: NL64h Part

Algorithm 8 NL64h Part

```
/* Initialization */
t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}||t_{4(32)}||t_{5(32)}||t_{6(32)}||t_{7(32)}\!=\!dkey
 /* Substitution Layer */
t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)} = \mathsf{sigma4}(t_{0(32)})||\mathsf{sigma4}(t_{1(32)})||\mathsf{sigma4}(t_{2(32)})||\mathsf{sigma4}(t_{3(32)})|
/* Diffusion Layer */
t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)} = \mathsf{mu4}(t_{0(32)})||\mathsf{mu4}(t_{1(32)})||\mathsf{mu4}(t_{2(32)})||\mathsf{mu4}(t_{3(32)})|
t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}||t_{4(32)}||t_{5(32)}||t_{6(32)}||t_{7(32)}\!=\!
                              \mathsf{mix64h}(t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}||t_{4(32)}||t_{5(32)}||t_{6(32)}||t_{7(32)})
t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}||t_{4(32)}||t_{5(32)}||t_{6(32)}||t_{7(32)}=
                              (t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}||t_{4(32)}||t_{5(32)}||t_{6(32)}||t_{7(32)})\oplus\mathsf{pad}
if k = ek then
              t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}||t_{4(32)}||t_{5(32)}||t_{6(32)}||t_{7(32)} = \overline{t_{0(32)}}||\overline{t_{1(32)}}||\overline{t_{2(32)}}||\overline{t_{3(32)}}||\overline{t_{4(32)}}||\overline{t_{5(32)}}||\overline{t_{6(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32)}}||\overline{t_{7(32
end if
 /* Substitution Layer */
/* Hashing Layer */
t_{0(32)}||t_{1(32)}||t_{2(32)}||t_{3(32)}=(t_{0(32)}\oplus t_{1(32)})||(t_{2(32)}\oplus t_{3(32)})||(t_{4(32)}\oplus t_{5(32)})||(t_{6(32)}\oplus t_{7(32)})||(t_{1(32)}\oplus t_{1(32)})||(t_{1(32)}\oplus t_{1(32)}\oplus t_{1(32)})||(t_{1(32)}\oplus t_{1(32)}\oplus t_{1(32)}\oplus t_{1(32)})||(t_{1(32)}\oplus t_{1(32)}\oplus t_{
t_{0(32)}||t_{1(32)}=(t_{0(32)}\oplus t_{2(32)})||(t_{1(32)}\oplus t_{3(32)})
 /* Encryption Layer */
t_{0(32)}||t_{1(32)}=\text{Imor64}(t_{0(32)}||t_{1(32)},dkey_{[0...63]})
t_{0(32)}||t_{1(32)}=\text{Imor64}(t_{0(32)}||t_{1(32)},dkey_{[64...127]})
t_{0(32)}||t_{1(32)}=Imor64(t_{0(32)}||t_{1(32)},dkey_{[128...191]})
t_{0(32)}||t_{1(32)}\!=\!\!\mathsf{Imid64}(t_{0(32)}||t_{1(32)},\!dkey_{[192...256]})
Output t_{0(32)}||t_{1(32)}| as round subkey.
```

Algorithm 9 NL128 Part

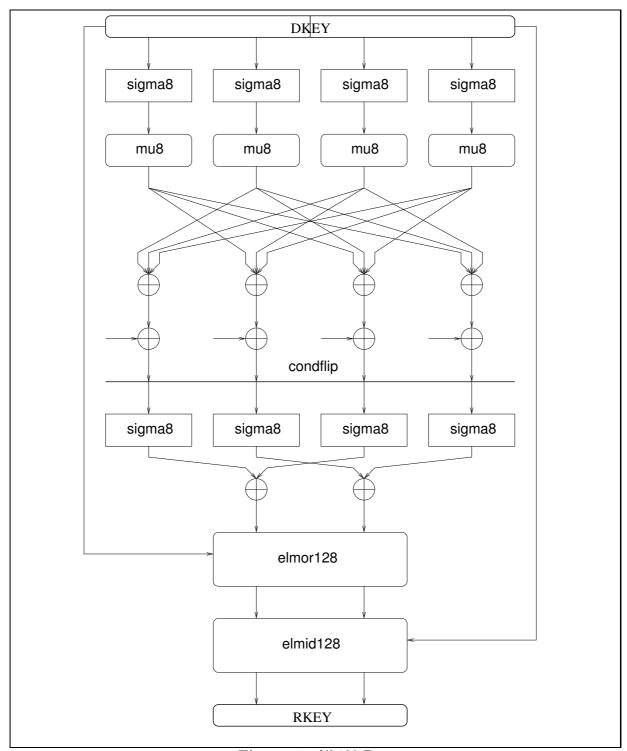


Figure 12: NL128 Part

2.3.14 Definition of mix64h

Given an input vector of eight 32-bit values, denoted

$$x = x_{0(32)} ||x_{1(32)}||x_{2(32)}||x_{3(32)}||x_{4(32)}||x_{5(32)}||x_{6(32)}||x_{7(32)}||$$

the mix64h function consists in processing it by the following relations, resulting in an output vector denoted

$$y = y_{0(32)}||y_{1(32)}||y_{2(32)}||y_{3(32)}||y_{4(32)}||y_{5(32)}||y_{6(32)}||y_{7(32)}|$$

More formally, mix64h is defined as

$$\begin{array}{rcl} y_{0(32)} & = & x_{2(32)} \oplus x_{4(32)} \oplus x_{6(32)} \\ y_{1(32)} & = & x_{3(32)} \oplus x_{5(32)} \oplus x_{7(32)} \\ y_{2(32)} & = & x_{0(32)} \oplus x_{4(32)} \oplus x_{6(32)} \\ y_{3(32)} & = & x_{1(32)} \oplus x_{5(32)} \oplus x_{7(32)} \\ y_{4(32)} & = & x_{0(32)} \oplus x_{2(32)} \oplus x_{6(32)} \\ y_{5(32)} & = & x_{1(32)} \oplus x_{3(32)} \oplus x_{7(32)} \\ y_{6(32)} & = & x_{0(32)} \oplus x_{2(32)} \oplus x_{4(32)} \\ y_{7(32)} & = & x_{1(32)} \oplus x_{3(32)} \oplus x_{5(32)} \end{array}$$

2.3.15 Definition of mix128

Given an input vector of four 64-bit values, denoted $x = x_{0(64)}||x_{1(64)}||x_{2(64)}||x_{3(64)}$, the mix64 function consists in processing it by the following relations, resulting in an output vector denoted $y = y_{0(64)}||y_{1(64)}||y_{2(64)}||y_{3(64)}$. More formally, mix128 is defined as

```
\begin{array}{lcl} y_{0(64)} & = & x_{1(64)} \oplus x_{2(64)} \oplus x_{3(64)} \\ y_{1(64)} & = & x_{0(64)} \oplus x_{2(64)} \oplus x_{3(64)} \\ y_{2(64)} & = & x_{0(64)} \oplus x_{1(64)} \oplus x_{3(64)} \\ y_{3(64)} & = & x_{0(64)} \oplus x_{1(64)} \oplus x_{2(64)} \end{array}
```

3 Rationales

In this part, we describe several rationales about important components building the FOX family of block ciphers.

3.1 Non-Linear Mapping sbox

As outlined earlier, our primary goal was to avoid a purely algebraic construction for the S-box; a secondary goal was the possibility to implement it in a very efficient way on hardware using ASIC or FPGA technologies. The sbox function is a non-linear bijective mapping on 8-bit values. It consists of a Lai-Massey scheme with 3 rounds taking three different substitution boxes as round function where the orthormorphism of the third round is omitted; these "small" S-boxes are denoted S_1 , S_2 and S_3 , and their content is given in Fig. 13. The orthomorphism or4 used in the Lai-Massey scheme is a single round of a 4-bit Feistel scheme with the identity function as round function. We describe now the generation process of the sbox transformation.

x	0	1	2	3	4	5	6	7	8	9	Α	В	С	D	Е	F
$S_1(x)$	2	5	1	9	E	Α	С	8	6	4	7	F	D	В	0	3
$S_2(x)$	В	4	1	F	0	3	Ε	D	Α	8	7	5	С	2	9	6
$S_3(x)$	D	Α	В	1	4	3	8	9	5	7	2	C	F	0	6	E

Figure 13: The three small S-boxes of FOX.

First a set of three different candidates for small substitution boxes, each having a LP_{max} and a DP_{max} smaller than 2^{-2} were pseudo-randomly chosen, where

$$LP^{f}(\mathbf{a}, \mathbf{b}) = \left(2 \Pr_{X}[\mathbf{a} \bullet X = \mathbf{b} \bullet f_{k}(X)] - 1\right)^{2}$$

$$LP^{f}_{\max} = \max_{\mathbf{a}, \mathbf{b} \neq \mathbf{0}} LP^{f}(\mathbf{a}, \mathbf{b})$$

with • denoting the scalar product over GF (2)-vectors, and

$$DP^{f}(a,b) = \Pr_{X} [f_{k}(X \oplus a) = f_{k}(X) \oplus b]$$

$$DP^{f}_{\max} = \max_{a \neq 0, b} DP^{f}(a,b)$$

Then, the candidate sbox mapping was evaluated and tested regarding its LP_{max} and DP_{max} values until a good candidate was found. The chosen sbox satisfies $DP_{max}^{sbox} = LP_{max}^{sbox} = 2^{-4}$ and its algebraic degree is equal to 6.

3.2 Linear Multipermutations mu4/mu8

Both mu4 and mu8 are linear multipermutations. This kind of construction was early recognized as being optimal for which regards its diffusion properties (see [SV95, Vau95]). As explained in [JV04b], not all constructions are very efficient to implement, especially on low-end smartcard, which have usually very few available memory and computational power. We have thus chosen a circulating-like construction. Furthermore, in order to be efficiently implementable, the elements of the matrix, which are elements of $GF(2^8)$, should be efficient to multiply to. The only really efficient operations are the addition, the multiplication by α and the division by α . Note that $\alpha^7 + \alpha = \alpha^{-1} + \alpha^{-2}$, $\alpha^7 + \alpha^6 + \alpha^5 + \alpha^4 + \alpha^3 + \alpha^2 = \alpha^{-1}$, and that $\alpha^6 + \alpha^5 + \alpha^4 + \alpha^3 + \alpha^2 + \alpha = \alpha^{-2}$.

3.3 Key-Schedule Algorithms

The FOX key-schedule algorithms were designed with several rationales in mind: first, the function, which takes a key k and the round number r and returns r subkeys should be a cryptographic pseudorandom, collision resistant and one-way function. Second, the sequence of subkeys should be generated in any direction without any complexity penalty. Third, all the bytes of mkey should be randomized even when the key size is strictly smaller than ek. Finally, the key-schedule algorithm should resist related-cipher attacks as described by Wu in [Wu02], since FOX can possibly use different number of rounds.

We are convinced that "strong" key-schedule algorithms have significant advantages in terms of security, even if the price to pay is a smaller key agility, as discussed earlier. In the case of FOX, we believe that the time needed to compute the subkeys, which is about equal to the time needed to encrypt 6 blocks of data (in the case of FOX64 with keys strictly larger than 128 bit, it takes the time to encrypt 12 blocks of data) remains acceptable in all kinds of applications.

During the AES effort, it was suggested that an example of extreme case would be a high-speed network switch having to maintain a million of contexts and switching bewteen them every four blocks of data. Under such extreme constraints, one can still keep in memory one million fully expanded keys at a negligible cost.

The second central property of FOX key-schedule algorithms is ensured by the LFSR construction. As it is possible to back-clock it easily, the subkey generation process can be computed in the encryption as well as in the decryption direction with no loss of speed. The third property is ensured by our "Fibonacci-like" construction (which is a bijective mapping). Furthermore, mkey is expanded by XORing constants depending on r and ek with no overlap on these constants sequences (this was checked experimentally). Finally, the fourth property is ensured by the dependency of the subkey sequence to the actual round number of the algorithm instance for which the sequence will be used.

We state now a sequence of properties of the building blocks of the key-schedule algorithm.

3.3.1 P-Part

The goal of the P-part consists in transforming the user-provided key, which may have any length multiple of 8 smaller or equal than 256, in a fixed-size value of 128-bit or 256-bit. The chosen padding constant e-2 was checked regarding the following property.

Lemma 3.1. It is impossible to find two values of k with a length strictly smaller than ek bits which lead to the same value of pkey.

Proof. In order for two different inputs to produce the same output during the padding operation, one has to concatenate the smaller one with a padding value which is contained in the one used for the larger input; this is only possible if the first ℓ bytes of the padding constant are present in another location. The lemma follows from the fact that the first byte 0xB7 is unique in the constant.

Note that in order to avoid that a padded key and non-padded key generate the same subkey sequence, a conditional negation has been incorporated in the NLx part of the key-schedule algorithm.

3.3.2 M-Part

When using small keys, a large part of the key-schedule state is known to a potential adversary: it is the padding constant. The goal of the M-part is hence to mix the entropy on all bytes. The following lemma insures that, when fed with two different inputs, the M-part will return two different outputs.

Lemma 3.2. The M-part is a permutation.

Proof. The lemma follows directly from the fact that the M-part is an invertible application. \Box

3.3.3 L-Part

The goal of the L-part is to diversify the dkey register (which serves as input for the NLx-part) at each round. The main design goals are its simplicity and its reversibility: as a LFSR step is equivalent to the multiplication by a constant in a finite field, the inverse operation is a division by the same constant. It is thus possible to evaluate the L in both directions. It was furthermore checked that the outputs (being 144 or 264 bits) for all $12 \le r \le 255$ and for all round numbers $1 \le i \le r$ are unique.

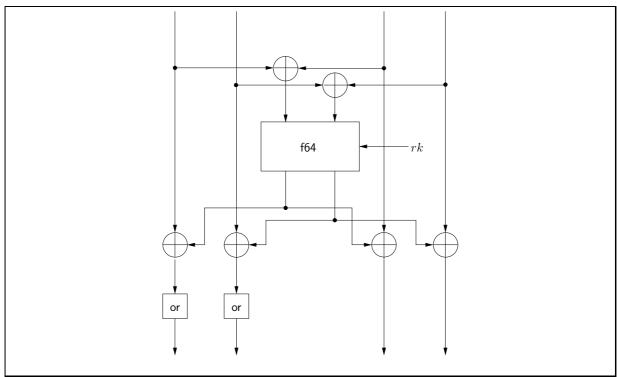


Figure 14: An alternate view of an extended Lai-Massey scheme

3.3.4 NLx-Part

The goal of the NL part is to generate a pseudorandom stream of data as "cryptographically secure" as possible and as fast as possible; it is actually the one-way part of the key-schedule. For this, it re-uses the round functions in its core, and it needs only a few supplementary operations.

3.4 Security Foundations

3.4.1 Security Properties of the Lai-Massey Scheme

Although less popular than the Feistel scheme or SPN structures, the Lai-Massey scheme offers similar (super-) pseudorandomness and decorrelation inheritance properties, as was demonstrated by Vaudenay [Vau00]. Note that we will indifferently use the term "Lai-Massey scheme" to denote both versions, as we can see the Extended Lai-Massey scheme as a Lai-Massey scheme: we can swap the two inner inputs as in Fig. 14, and we note that the function $(x,y)\mapsto \operatorname{or32}(x)||\operatorname{or32}(y)|$ builds an orthomorphism (see Lem. 3.3).

Lemma 3.3. The application defined by

$$\left\{ \begin{array}{lcl} (\{0,1\}^{32})^2 & \to & (\{0,1\}^{32})^2 \\ (x,y) & \mapsto & (\operatorname{or}(x),\operatorname{or}(y)) \end{array} \right.$$

is an orthomorphism, where or(.) is the orthomorphism defined in §2.2.3.

Proof. First, we show that this application is a permutation. This follows from the fact that the inverse application is given by

$$(x', y') \mapsto (\mathsf{io}(x'), \mathsf{io}(y'))$$

and that io is a permutation, too. Now, we have to check that

$$(x,y) \mapsto (\mathsf{or}(x) \oplus x, \mathsf{or}(y) \oplus y)$$
 (2)

is also a permutation. This follows easily from the fact that Eq. (2) is an invertible application.

From this point, we will make use of the following notation: given an orthomorphism o on a group $(\mathcal{G},+)$ and given r functions f_1, f_2, \ldots, f_r on \mathcal{G} , we note an r-rounds Lai-Massey scheme using the r functions and the orthomorphism by $\Lambda^o(f_1,\ldots,f_r)$. Then the following results are two Luby-Rackoff-like [LR88] results on the Lai-Massey scheme. We refer to [Vau00, Vau03] for proofs thereof.

Theorem 3.1 (Vaudenay). Let f_1^* , f_2^* and f_3^* be three independent random functions uniformly distributed on a group $(\mathcal{G}, +)$. Let \circ be an orthomorphism on \mathcal{G} . For any distinguisher limited to d chosen plaintexts, where $g = |\mathcal{G}|$ denotes the cardinality of the group, between $\Lambda^{\circ}(f_1^*, f_2^*, f_3^*)$ and a uniformly distributed random permutation c^* , we have

$$\operatorname{Adv}(\Lambda^{\circ}(f_1^*, f_2^*, f_3^*), c^*) \le d(d-1)(g^{-1} + g^{-2}).$$

Theorem 3.2 (Vaudenay). If f_1, \ldots, f_r are $r \geq 3$ independent random functions on a group $(\mathcal{G}, +)$ of order g such that $\mathrm{Adv}(f_i, f_i^*) \leq \frac{\varepsilon}{2}$ for any adaptive distinguisher between f_i and f_i^* limited to d queries for $1 \leq i \leq r$ and if o is an orthomorphism on \mathcal{G} , we have

$$\operatorname{Adv}(\Lambda^{\circ}(\mathsf{f}_{1},\ldots,\mathsf{f}_{r}),\mathsf{c}^{*}) \leq \frac{1}{2}(3\varepsilon + d(d-1)(2g^{-1}+g^{-2}))^{\left\lfloor \frac{r}{3}\right\rfloor}.$$

Basically, the first result proves that the Lai-Massey scheme provides pseudorandomness on three rounds unless the f_i 's are weak, like for the Feistel scheme [Fei73]. Super-pseudorandomness corresponds to cases where a distinguisher can query chosen ciphertexts as well; in this scenario, the previous result holds when we consider $\Lambda^{\circ}(f_1^*, \ldots, f_4^*)$ with a fourth round. The second result proves that the decorrelation bias of the round functions of a Lai-Massey scheme is inherited by the whole structure: provided the f_i 's are strong, so is the Lai-Massey scheme; in other words, a potential cryptanalysis will not be able to exploit the Lai-Massey's scheme only, but it will have to take advantage of weaknesses of the round functions' internal structure. We would like to stress out the importance of the orthomorphism \mathbf{o} : by omitting it, it is possible to distinguish a Lai-Massey scheme using pseudorandom functions from a pseudorandom permutation with overwhelming probability, and this for any number of rounds. Indeed, denoting the input and the output of a Lai-Massey scheme by $x_1||x_r|$ and $y_1||y_r$, respectively, the following equation holds with probability one:

$$x_{\mathsf{I}} \ominus x_{\mathsf{r}} = y_{\mathsf{I}} \ominus y_{\mathsf{r}} \tag{3}$$

where \ominus denote the inverse of the additive group law used in the scheme.

One should not misinterpret the results in the Luby-Rackoff scenario in terms of the overall block cipher security: FOX's round functions are far to be indistinguishable from random functions, as it is the case of DES round functions, for instance: the fact that DES is vulnerable to linear and differential cryptanalysis does not contradict Luby-Rackoff results. However, Th. 3.1 and Th. 3.2 give proper credit to the high-level structure of FOX.

3.4.2 Resistance w/r to Linear and Differential Cryptanalysis

It is possible to prove some important results about the security of both f32 and f64 functions towards linear and differential cryptanalysis, too. As these functions may be viewed as classical Substitution-Permutation Network constructions, we will refer to some well-known results on their resistance towards linear and differential cryptanalysis proved in [HLL+01] by Hong et al. For the sake of completeness, we recall the framework of consideration and the results they obtained using it. Then, we apply their result to the round functions of FOX, and we draw some conclusions about its security towards linear and differential cryptanalysis in functions of the round number. This will help us to fix the minimal number of rounds which results in a sufficient level of security.

Let S_i denote an $m \times m$ bijective substitution box, that is a bijection on $\{0,1\}^m$. We consider a standard kSPkSk structure (i.e. the one of FOX's round functions) on $m \times n$ bit strings, namely a key addition layer, a substitution layer, a diffusion layer, followed by a second key addition layer, a substitution layer, and a final key addition layer. We assume that the substitution layer consists of the parallel evaluation of $n \times m$ S-boxes S_i for $1 \le i \le n$, that the diffusion layer can be expressed as an invertible $n \times n$ MDS matrix \mathbf{M} with coefficients in $\mathrm{GF}(2^m)$, and that the key addition layer consists of XORing a mn-bit subkey to the state. Let us furthermore denote by

$$\pi_{\mathrm{DP}}^{\mathsf{S}} = \max_{1 \leq i \leq n} \mathrm{DP}_{\mathrm{max}}^{\mathsf{S}_i} \text{ and } \pi_{\mathrm{LP}}^{\mathsf{S}} = \max_{1 \leq i \leq n} \mathrm{LP}_{\mathrm{max}}^{\mathsf{S}_i}$$

the respective maximal differential and linear probabilities we can find in the S-boxes S_i . Finally, let us denote by

$$\beta = \mathfrak{B}(\mathbf{M}) = n + 1$$

the branch number of the diffusion layer M (according to [DR02]), which is defined to be maximal. Then the following theorem due to Hong. $et~al.~[\mathrm{HLL^+01}]$ states upper bounds on the maximal differential and linear hull probabilities, respectively.

Theorem 3.3 (Hong et al.[HLL $^+$ 01]). In a kSPkSk structure, if the round subkeys are statistically independent and uniformly distributed, then the probability of each differential with respect to \oplus is upper bounded by

$$\left(\pi_{\mathrm{DP}}^{\mathsf{S}}\right)^{\beta-1},$$

while the probability of each linear hull is upper bounded by

$$\left(\pi_{\mathrm{LP}}^{\mathsf{S}}\right)^{\beta-1}$$
.

In the case of FOX64, since $DP_{max}^{sbox} = LP_{max}^{sbox} = 2^{-4}$, since mu4 (resp. mu8) has a branch number equal to five (resp. nine), and since one can assume that the subkeys are uniformly distributed and statistically independent, due to the nature of the key-schedule algorithm, one can reasonably apply Th. 3.3 and get the following result.

Theorem 3.4. If the round subkeys are statistically independent and uniformly distributed, then the following bounds hold:

$$LP_{max}^{f32} = DP_{max}^{f32} \le 2^{-16},$$

and

$$LP_{max}^{f64} = DP_{max}^{f64} \le 2^{-32}.$$

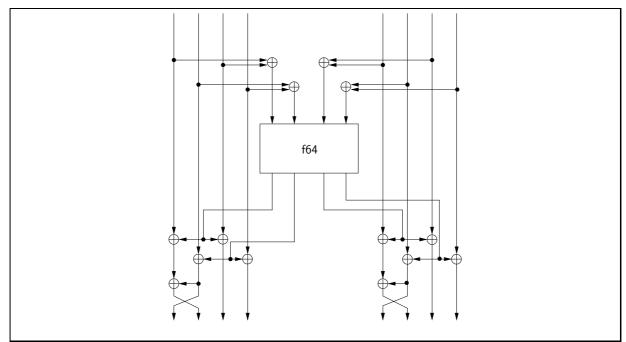


Figure 15: A detailed view of an extended Lai-Massey scheme

Let us now focus on embedding the round functions in the skeletons. For the sake of clarity³, we prove now some interesting properties of an Extended Lai-Massey scheme regarding differential and linear characteristics.

Lemma 3.4. In the Extended Lai-Massey scheme as defined in §2.1.2, any differential characteristic on two rounds must involve at least one f64-function.

Proof. We follow a top-down approach. If we stack up two rounds of an Extended Lai-Massey scheme (see Fig. 15 for a detailed illustration of one round) and we force a differential characteristic at the input of the first f64-function to be equal to 0, then a differential characteristic at the input of the two rounds must have the form (a,b,a,b,c,d,c,d) with $a,b,c,d \in \{0,1\}^{16}$ and a,b,c,d are not all equal to 0. At the end of the first round, the differential characteristic sounds $(b,a\oplus b,a,b,d,c\oplus d,c,d)$. At the input of the second f64-function, the differential characteristic is equal to $(a\oplus b,a,c\oplus d,c)$. We proceed by contraposition. If the input of the second f64-function is equal to zero, we have a=c=0. As $a\oplus b$ and $c\oplus d$ must be both equal to 0, the we conclude that a=b=c=d=0. This is a contradiction to our primary assumption about a,b,c and d, and the theorem follows.

Lemma 3.5. In the Extended Lai-Massey scheme as defined in Fig. 2.1.2, any linear characteristic on two rounds must involve at least one function f64.

Proof. We follow a bottom-up approach. By forcing a linear characteristic to be equal to (0,0,0,0,0,0,0,0) at the end of the second f64-function, we note that the output linear characteristic must have the form $(a,a\oplus d,a\oplus d,d,b,b\oplus c,b\oplus c,c)$ with $a,b,c,d\in\{0,1\}^{16}$ and a,b,c,d not all equal to 0. If we consider now the first f64-function, we note that a linear characteristic at its output must have the form $(d,a\oplus d,b,b\oplus c)$, which implies that a=b=0 and then that c=d=0, which is a contradiction to our assumption, and the theorem follows.

³These properties are actually trivial to prove in the case of a simple Lai-Massey scheme, and as discussed in §3.4.1, the Extended Lai-Massey scheme can be viewed as a simple Lai-Massey scheme.

By considering Th. 3.3, Lem. 3.4, and Lem. 3.5 together, we have thus the following result.

Theorem 3.5. The differential (resp. linear) probability of any single-path characteristic in FOX64/k/r is upper bounded by $(DP_{max}^{sbox})^{2r}$ (resp. $(LP_{max}^{sbox})^{2r}$). Similarly, the bounds are $(DP_{max}^{sbox})^{4r}$ (resp. $(LP_{max}^{sbox})^{4r}$) for FOX128/k/r.

Note that it is a kind of "hybrid" proof of security towards linear and differential cryptanalysis, as we have considered differential and linear hulls in the round functions, but characteristics in the high-level schemes. Thus, we have in reality slightly stronger results that the ones stated in Th. 3.5. Finally, we conclude that it is impossible to find any useful differential or linear characteristic after 8 rounds for both FOX64 and FOX128. Hence, a minimal number of 12 rounds provides a minimal safety margin.

3.4.3 Resistance Towards Other Attacks

In this part, we discuss the resistance of FOX towards various types of attacks.

Statistical Attacks Due to the very high diffusion properties of FOX's round functions, the high algebraic degree of the sbox mapping, and the high number of rounds, we are strongly convinced that FOX will resist to known variants of linear and differential cryptanalysis (like differential-linear cryptanalysis [LH94, BDK02], boomerang [Wag99] and rectangle [BDK01] attacks), as well as generalizations thereof, like Knudsen's truncated and higher-order differentials [Knu95], impossible differentials [BBS99], and Harpes' partitioning cryptanalysis [HM97], for instance.

Slide and Related-Key Attacks Slide attacks [BW99, BW00] exploit periodic key-schedule algorithms, which is not a property of FOX's key-schedule algorithms. Furthermore, due to very good diffusion and the high non-linearity of the key-schedule, related-key attacks are very unlikely to be effective against FOX.

Interpolation and Algebraic Attacks Interpolation attacks [JK97] take advantage of S-boxes exhibiting a simple algebraic structure. Since FOX's non-linear mapping sbox does not possess any simple relation over GF(2) or $GF(2^8)$, such attacks are certainly not effective.

One of our main concerns was to avoid a pure algebraic construction for the sbox mapping, as it is the case for a large number of modern designs of block ciphers. Although such S-boxes have many interesting non-linear properties, they probably form the best conditions to express a block cipher as a system of sparse, over-defined low-degree multivariate polynomial equations over GF(2) or $GF(2^8)$; this fact may lead to effective attacks, as argued by Courtois and Pieprzyk in [CP02].

Not choosing an algebraic construction for sbox does not necessarily ensure security towards algebraic attacks. Note that we base our non-linear mapping on "small" permutations, mapping 4 bits to 4 bits, and that, according to [CP02], any such mapping can always be written as an overdefined system of at least 21 quadratic equations: let us denote the input (resp. the output) of such a small S-box by $x_1||x_2||x_3||x_4$ (resp. by $y_1||y_2||y_3||y_4$), and if we consider a 16×37 matrix containing in each row the values of the t=37 monomials

$$\{1, x_1, \ldots, x_4, y_1, \ldots, y_4, x_1x_2, \ldots, x_1y_1, \ldots, y_3y_4\}$$

for each of the 16 possible entries, we note that its rank can be at most 16, thus, for any S-box, there will be at least $\rho \geq 37 - 16 = 21$ quadratic equations. We have checked that the rank

of these matrices for FOX's small S-boxes S_1 , S_2 , and S_3 are equal to 16, and there exist thus 21 quadratic equations describing it; furthermore, we are not aware of any quadratic relation over GF (2^8) for sbox. Following the very same methodology than [CP02], it appears that XSL attacks would break members of the FOX family within a complexity⁴ of 2^{139} to 2^{156} , depending on the block size and on the rounds number.

Namely, we can construct an overdefined multivariate system of quadratic equations describing FOX using the XSL approach, which aims at recovering all the subkeys, without taking care of the key-schedule algorithm. Let us assume that FOX has r rounds, and thus r subkeys with the same size than the plaintext. We need hence r known plaintext-ciphertext pairs to uniquely determine the key. We use from now on the same notations than in [CP02]. S is defined to be the total number of substitution boxes considered during an attack. Hence,

$$S_{\text{FOX64}} = 3 \cdot 8 \cdot r^2$$

for FOX64, and

$$S_{\text{FOX128}} = 3 \cdot 16 \cdot r^2$$

as each substitution box sbox is built from three small S-boxes on $\{0,1\}^s$, with s=4. Let t denote the number of monomials (i.e. t=37 in our case), let t' being the number of terms in the basis for one S-box that can be multiplied by some fixed variable and are still in the basis (we have t'=5 in the case of FOX). Then, Courtois and Pieprzyk [CP02] estimate that the complexity of a XSL attack can be estimated to

$$T^{\omega}$$
 with $T \approx (t - \rho)^P \cdot {S \choose P}$

where ω is the best possible exponent for Gaussian elimination, T represents the total number of terms, and where

$$P = \frac{t - \rho}{s + \frac{t'}{S}}$$

In the case of FOX, we get

$$P = \frac{16}{4 + \frac{5}{24r^2}} < 4$$

According to Courtois and Pieprzyk [CP02], in order that the attack works, as difference operation) it is necessary to choose P such that

$$\frac{R}{T - T'} \ge 1\tag{4}$$

where

$$R \approx S \cdot s(t - \rho)^{P-1} \cdot {S \choose P-1}$$

represents the total number of equations, and

$$T' \approx t'(t-\rho)^{P-1} \cdot {S-1 \choose P-1}$$

is the total number of terms in the basis that can be multiplied by some fixed variable and are still in the basis. Eq. (4), in the case which interests us, is already fullfiled for P=4, but $R\approx 1$. As the overall complexity of the attack is very sensitive to the value of P, and according to Courtois and Pieprzyk [CP02],

 $^{^4}$ Under the most pessimistic hypotheses.

		P = 0	4	P = 0	5
	S	$\omega = 2.376$	$\omega = 3$	$\omega = 2.376$	$\omega = 3$
FOX64/k/12	3456	2^{139}	2^{175}	2^{171}	2^{216}
FOX64/k/16	6144	2^{147}	2^{185}	2^{181}	2^{228}
FOX128/k/12	6912	2^{148}	2^{187}	2^{183}	2^{231}
FOX128/k/16	12288	2^{156}	2^{197}	2^{192}	2^{243}

Figure 16: Estimations of the complexity of Courtois-Pieprzyk attacks against FOX

Though XSL attacks will probably always work for some P, we considered the minimum value P for which $\frac{R}{T-T'} \geq 1$. This condition is necessary, but probably not sufficient.

we will consider the cases P=4 as well as P=5 in our estimations of the complexity of applying algebraic attacks to FOX.

Another subject of controversy is the value of ω , i.e. the complexity exponent of a Gaussian reduction. Courtois and Pieprzyk [CP02] assume that $\omega=2.376$, which is the best known value obtained by Coppersmith and Winograd [CW90]. According to [CP02], the constant factor in this algorithm is unknown to the authors of [CW90], and is expected to be very big. Accordingly, it is disputed whether such an algorithm can be applied efficiently in practice. For this reason, we will consider both $\omega=2.376$ and $\omega=3$ in our estimations.

A summary of our estimations is given in Fig. 16. At the light of the previous discussion, we should interpret these figures with an extreme care: on the one hand, the real complexity of XSL attacks is by no means clear at the time of writing and is the subject of much controversy [MR03]; one the other hand, we feel that the advantages of a small hardware footprint overcome such a (possible) security decrease.

Integral Attacks Integral attacks [KW02] apply to ciphers operating on well-aligned data, like SPN structures. As the round functions of FOX are SPNs, one can wonder whether it is possible to find an integral distinguisher on the whole structure and we show now that it is indeed the case. Let us consider the case of FOX64: we denote the input bytes by $x_{i(8)}$ with $0 \le i \le 7$ and the output of the third round lmid64 by $y_{i(8)}$ with $0 \le i \le 7$. We have the following integral distinguisher on 3 rounds of FOX64.

Theorem 3.6. Let $x_{3(8)} = a$, $x_{7(8)} = a \oplus c$, and $x_{i(8)} = c$ for i = 0, 1, 2, 4, 5, 6, where c is an arbitrary constant. We consider plaintext structures $x^{(j)}$ for $1 \le j \le 256$ where a takes all 256 possibles byte values. Then,

$$\bigoplus_{j=1}^{256} y_0^{(j)} \oplus y_6^{(j)} = 0 \text{ and } \bigoplus_{j=1}^{256} y_1^{(j)} \oplus y_7^{(j)} = 0$$

as well as

$$\bigoplus_{j=1}^{256} y_0^{(j)} \oplus y_2^{(j)} \oplus y_4^{(j)} = 0 \ \ and \ \ \bigoplus_{j=1}^{256} y_1^{(j)} \oplus y_3^{(j)} \oplus y_5^{(j)} = 0.$$

Proof. See Fig. 17, where "C" denotes a constant byte, "A" denotes an active byte, and "S" denotes a byte, whose sum under the structure is equal to zero. \Box

This integral distinguisher can be used to break (four, five) six rounds of FOX64 (by guessing the one, two, or three last round keys and testing the integral criterion for each subkey candidate on a few structures of plaintexts) within a complexity of about $(2^{72}, 2^{136}) 2^{200}$ partial decryptions and negligible memory. A similar property may be used to break up to 4 rounds of FOX128 (by guessing the last round key) with a complexity of about 2^{136} operations and negligible memory.

4 Implementation

In this part, we discuss several issues about the implementation of the FOX family on lowend 8-bit architectures and on high-end 32/64-bit ones. Finally, we give results about the performances of various implementations we have written on different platforms.

4.1 8-bit Architectures

The resources representing the most important bottleneck in a block cipher implementation on a smartcard (which uses typically low-cost, 8-bit microprocessors) is of course the RAM usage. The amount of efficiently usable RAM available on a smartcard is typically in the order of 256 bytes. It may be a bit larger depending on the cases, but as this type of smart card is devoted to contain more than a simple encryption routine, FOX implementations on this kind of platforms will minimize the amount of necessary RAM. ROM is not so scarce as RAM on a smartcard, so the code size can be greater than the RAM usage. It is usually reasonable not to have a ROM size (instructions + possible precomputed tables) greater than 1024 bytes.

4.1.1 Four Memory Usage Strategies

Obviously, the most intensive computation are related to the evaluation of the sbox mapping and of the mu4 and mu8 mappings. We propose in the following four different (the last one concerning uniquely FOX128) strategies using various amounts of precomputed data to implement these mappings; they are summarized in Fig. 18. Note that the precomputed data may be stored in ROM and that the constants needed in the key-schedule algorithm are not taken into account. Strategy A can be applied when extremely few memory is available. For this, one computes onthe-fly the sbox mapping, as it is described in §3.1, page 24, and all the operations in GF (2⁸). The sole needed constants are the small substitution boxes S_1 , S_2 and S_3 (see Fig. 13). Strategy A is clearly the slowest one. A significant speed gain can be obtained if one precomputes the sbox mapping (Strategy B), the finite field operations being all computed dynamically. A third possibility (Strategy C) is to precompute two more mappings: talpha(x) is a function mapping an element x to $\alpha \cdot x$, with the multiplication in GF (2⁸); dalpha(x) is a function mapping an element $x \in GF$ (2⁸) to $\alpha^{-1} \cdot x$. Finally, in the case of FOX128, a further speed gain may be obtained (Strategy D) by tabulating the five following mappings:

```
\begin{array}{lll} \operatorname{sbox}(x) & : & x \mapsto \operatorname{sbox}(x) \\ \operatorname{stalpha}(x) & : & x \mapsto \operatorname{sbox}(x) \cdot \alpha \\ \operatorname{sdalpha}(x) & : & x \mapsto \operatorname{sbox}(x) \cdot \alpha^{-1} \\ \operatorname{stalpha2}(x) & : & x \mapsto \operatorname{sbox}(x) \cdot \alpha^2 \\ \operatorname{sdalpha2}(x) & : & x \mapsto \operatorname{sbox}(x) \cdot \alpha^{-2} \end{array}
```

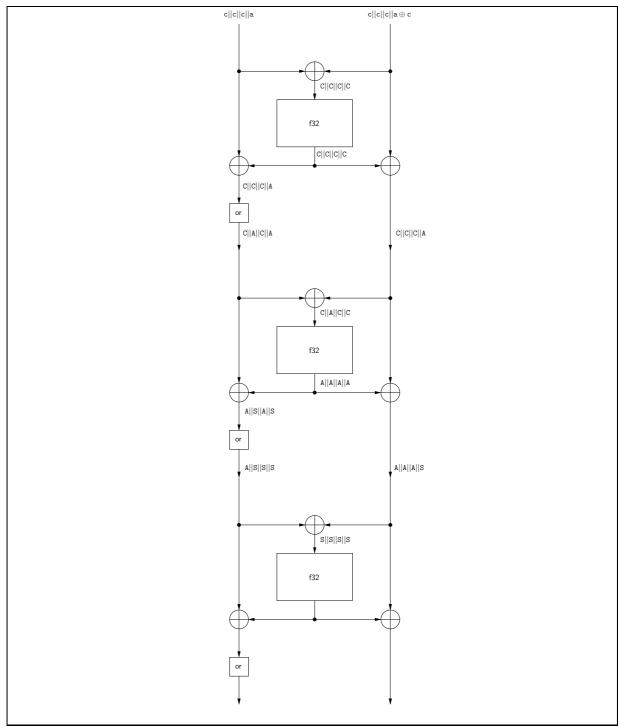


Figure 17: Integral Distinguisher in 3 rounds of FOX64.

Strategy	Precomputations	Data size
A	No precomputed data	24 B
В	sbox	256 B
С	sbox, talpha, dalpha	768 B
D	sbox, stalpha, sdalpha, stalpha2, sdalpha2	1280 B

Figure 18: Four different strategies to implement FOX on low-end microprocessors

The implementation of the sigma4/mu4 layer is relatively straighforward:

$$\begin{array}{lll} y_{0(8)} & = & \operatorname{sbox}(x_{0(8)}) \oplus \operatorname{sbox}(x_{1(8)}) \oplus \operatorname{sbox}(x_{2(8)}) \oplus \\ & & \alpha \cdot \operatorname{sbox}(x_{3(8)}) \\ y_{1(8)} & = & \operatorname{sbox}(x_{0(8)}) \oplus \operatorname{sbox}(x_{1(8)}) \oplus \operatorname{sbox}(x_{3(8)}) \oplus \alpha \cdot \operatorname{sbox}(x_{2(8)}) \\ & & \oplus \alpha^{-1} \cdot \operatorname{sbox}(x_{1(8)}) \\ y_{2(8)} & = & \operatorname{sbox}(x_{0(8)}) \oplus \operatorname{sbox}(x_{2(8)}) \oplus \operatorname{sbox}(x_{3(8)}) \oplus \alpha \cdot \operatorname{sbox}(x_{1(8)}) \\ & & \oplus \alpha^{-1} \cdot \operatorname{sbox}(x_{0(8)}) \\ \end{array}$$

By carefully rewriting the above equations and by re-using some temporary results, one can easily minimize the number of sbox, talpha, dalpha evaluations and the number of \oplus operations. However, the resulting implementation is strongly dependent of the chosen strategy.

The implementation of the sigma8/mu8 layer is not much complicated. By rewriting the operations as done above, one can easily obtain a fast implementation. For instance, in case of an implementation following memory strategy C, one can obtain the following computations:

```
y_{0(8)} = \operatorname{sbox}(x_{0(8)}) \oplus \operatorname{sbox}(x_{1(8)}) \oplus \operatorname{sbox}(x_{2(8)}) \oplus \operatorname{sbox}(x_{3(8)}) \oplus
                         \mathsf{sbox}(x_{4(8)}) \oplus \mathsf{sbox}(x_{5(8)}) \oplus \mathsf{sbox}(x_{6(8)}) \oplus \alpha \cdot \mathsf{sbox}(x_{7(8)})
y_{1(8)} = \operatorname{sbox}(x_{0(8)}) \oplus \operatorname{sbox}(x_{1(8)}) \oplus \operatorname{sbox}(x_{7(8)}) \oplus
                         \alpha \cdot (\mathsf{sbox}(x_{1(8)}) \oplus \mathsf{sbox}(x_{3(8)}) \oplus \alpha \cdot \mathsf{sbox}(x_{4(8)}) \oplus
                         \alpha^{-1} \cdot \left( \mathsf{sbox}(x_{2(8)}) \oplus \mathsf{sbox}(x_{5(8)}) \oplus \alpha^{-1} \cdot \left( \mathsf{sbox}(x_{2(8)}) \oplus \mathsf{sbox}(x_{6(8)}) \right) \right)
y_{2(8)} = \operatorname{sbox}(x_{0(8)}) \oplus \operatorname{sbox}(x_{6(8)}) \oplus \operatorname{sbox}(x_{7(8)}) \oplus
                         \alpha \cdot (\mathsf{sbox}(x_{0(8)}) \oplus \mathsf{sbox}(x_{2(8)}) \oplus \alpha \cdot \mathsf{sbox}(x_{3(8)}) \oplus
                         \alpha^{-1} \cdot (\operatorname{sbox}(x_{1(8)}) \oplus \operatorname{sbox}(x_{4(8)}) \oplus \alpha^{-1} \cdot (\operatorname{sbox}(x_{1(8)}) \oplus \operatorname{sbox}(x_{5(8)})))
y_{3(8)} = \operatorname{sbox}(x_{5(8)}) \oplus \operatorname{sbox}(x_{6(8)}) \oplus \operatorname{sbox}(x_{7(8)}) \oplus
                          \alpha \cdot (\operatorname{sbox}(x_{1(8)}) \oplus \operatorname{sbox}(x_{6(8)}) \oplus \alpha \cdot \operatorname{sbox}(x_{2(8)}) \oplus
                         \alpha^{-1} \cdot (\mathsf{sbox}(x_{0(8)}) \oplus \mathsf{sbox}(x_{3(8)}) \oplus \alpha^{-1} \cdot (\mathsf{sbox}(x_{0(8)}) \oplus \mathsf{sbox}(x_{4(8)})))
y_{4(8)} = \operatorname{sbox}(x_{4(8)}) \oplus \operatorname{sbox}(x_{5(8)}) \oplus \operatorname{sbox}(x_{7(8)}) \oplus
                         \alpha \cdot (\mathsf{sbox}(x_{0(8)}) \oplus \mathsf{sbox}(x_{5(8)}) \oplus \alpha \cdot \mathsf{sbox}(x_{1(8)}) \oplus
                         \alpha^{-1} \cdot (\mathsf{sbox}(x_{2(8)}) \oplus \mathsf{sbox}(x_{6(8)}) \oplus \alpha^{-1} \cdot (\mathsf{sbox}(x_{3(8)}) \oplus \mathsf{sbox}(x_{6(8)})))
y_{5(8)} \ = \ \operatorname{sbox}(x_{3(8)}) \oplus \operatorname{sbox}(x_{4(8)}) \oplus \operatorname{sbox}(x_{7(8)}) \oplus
                         \alpha \cdot (\mathsf{sbox}(x_{4(8)}) \oplus \mathsf{sbox}(x_{6(8)}) \oplus \alpha \cdot \mathsf{sbox}(x_{0(8)}) \oplus
                         \alpha^{-1} \cdot (\mathsf{sbox}(x_{1(8)}) \oplus \mathsf{sbox}(x_{5(8)}) \oplus \alpha^{-1} \cdot (\mathsf{sbox}(x_{2(8)}) \oplus \mathsf{sbox}(x_{5(8)})))
y_{6(8)} = \operatorname{sbox}(x_{2(8)}) \oplus \operatorname{sbox}(x_{3(8)}) \oplus \operatorname{sbox}(x_{7(8)}) \oplus
                         \alpha \cdot (\mathsf{sbox}(x_{3(8)}) \oplus \mathsf{sbox}(x_{5(8)}) \oplus \alpha \cdot \mathsf{sbox}(x_{6(8)}) \oplus
                         \alpha^{-1} \cdot (\mathsf{sbox}(x_{0(8)}) \oplus \mathsf{sbox}(x_{4(8)}) \oplus \alpha^{-1} \cdot (\mathsf{sbox}(x_{1(8)}) \oplus \mathsf{sbox}(x_{4(8)})))
y_{7(8)} = \operatorname{sbox}(x_{1(8)}) \oplus \operatorname{sbox}(x_{2(8)}) \oplus \operatorname{sbox}(x_{7(8)}) \oplus
                          \alpha \cdot (\mathsf{sbox}(x_{2(8)}) \oplus \mathsf{sbox}(x_{4(8)}) \oplus \alpha \cdot \mathsf{sbox}(x_{5(8)}) \oplus
                          \alpha^{-1} \cdot \left( \mathsf{sbox}(x_{3(8)}) \oplus \mathsf{sbox}(x_{6(8)}) \oplus \alpha^{-1} \cdot \left( \mathsf{sbox}(x_{0(8)}) \oplus \mathsf{sbox}(x_{3(8)}) \right) \right)
```

This computation flow (consisting of 71 \oplus , 15 talpha and 15 dalpha evaluations) is obviously not optimal in terms of operations; by using redundant temporary computations, one can spare a few more operations.

We give now a constant-time implementation of talpha and dalpha. The routines talpha2 and dalpha2 can be implemented by iterating twice talpha and dalpha, respectively. Note that these implementations do not take into account security issues related to other side-channel attacks, like SPA/DPA.

```
;; Implementation of talpha() on 8051
;;
;; RO
         : input
;; RO
         : output
MOV A, RO
                              ;; A := RO
RLC A
                              ;; left rotation through carry
                              ;; storing the result
MOV RO, A
                              ;; A := 0
CLR A
SUBB A, #0
                              ;; C set ? A = 0xFF : A = 0x00
ANL A, #F9
                              ;; C set ? A = 0xF9 : A = 0x00
XRL A, RO
                              ;; A := A XOR RO
MOV RO, A
                              ;; RO := A
;; Implementation of dalpha() on 8051
;;
;; R0
         : input
         : output
;; R0
MOV A, RO
                              ;; A := RO
RRC A
                              ;; left rotation through carry
MOV RO, A
                              ;; storing the result
CLR A
                              ;; A := 0
SUBB A, #0
                              ;; C set ? A = 0xFF : A = 0x00
ANL A, #FC
                              ;; C set ? A = 0xFC : A = 0x00
XRL A, RO
                              ;; A := A XOR RO
MOV RO, A
                              ;; RO := A
```

4.2 32/64-bit Architectures

Most modern CPUs architecture are 32- or 64-bit ones. In this section, we list several ways to optimize an implementation of FOX in terms of speed (i.e. of throughput).

4.2.1 Subkeys Precomputation

Most of the time, block ciphers are used to encrypt *several* blocks of data, so it is very time-sparing to precompute the subkeys once for all and to store them in a table. Typically, one needs 128 bytes of memory to store all the subkeys for an implementation of FOX64 with 16 rounds and twice as much for FOX128.

4.2.2 Implementation of f32 and f64 using Table-Lookups

The f32 and f64 functions can be implemented very efficiently using a combinations of table-lookups and XORs. We will focus on the f32 function, but the considerations are similar for which concerns f64. Let $x_{0(8)}||x_{1(8)}||x_{2(8)}||x_{3(8)}$ be an input of f32. We denote the temporary result obtained after the mu4 application by $t_{0(8)}||t_{1(8)}||t_{2(8)}||t_{3(8)}$. Let $rk_{0(8)}||rk_{1(8)}||rk_{2(8)}||rk_{3(8)}$ denote the first half of the round key. Finally, let $v_{i(8)} = x_{i(8)} \oplus rk_{i(8)}$ for $0 \le i \le 3$. We have

$$\begin{pmatrix} t_{0(8)} \\ t_{1(8)} \\ t_{2(8)} \\ t_{3(8)} \end{pmatrix} = \begin{pmatrix} 1 & 1 & 1 & \alpha \\ 1 & c & \alpha & 1 \\ c & \alpha & 1 & 1 \\ \alpha & 1 & c & 1 \end{pmatrix} \times \begin{pmatrix} \operatorname{sbox}(v_{0(8)}) \\ \operatorname{sbox}(v_{1(8)}) \\ \operatorname{sbox}(v_{2(8)}) \\ \operatorname{sbox}(v_{3(8)}) \end{pmatrix}$$

This equation may be rewritten as

$$\begin{pmatrix} t_{0(8)} \\ t_{1(8)} \\ t_{2(8)} \\ t_{3(8)} \end{pmatrix} = \operatorname{sbox}(v_{0(8)}) \times \begin{pmatrix} 1 \\ 1 \\ c \\ \alpha \end{pmatrix} \oplus \operatorname{sbox}(v_{1(8)}) \times \begin{pmatrix} 1 \\ c \\ \alpha \\ 1 \end{pmatrix} \oplus \operatorname{sbox}(v_{2(8)}) \times \begin{pmatrix} 1 \\ \alpha \\ 1 \\ c \end{pmatrix} \oplus \operatorname{sbox}(v_{3(8)}) \times \begin{pmatrix} \alpha \\ 1 \\ 1 \\ 1 \end{pmatrix}$$

Thus, one may precompte 4 tables of 256 4-bytes elements defined by

$$\begin{split} \text{TBSM}_0[a] &= \left(\begin{array}{c} 1 \cdot \text{sbox}(a) \\ 1 \cdot \text{sbox}(a) \\ c \cdot \text{sbox}(a) \\ \alpha \cdot \text{sbox}(a) \end{array} \right), \qquad \text{TBSM}_1[a] = \left(\begin{array}{c} 1 \cdot \text{sbox}(a) \\ c \cdot \text{sbox}(a) \\ \alpha \cdot \text{sbox}(a) \\ 1 \cdot \text{sbox}(a) \end{array} \right) \\ \text{TBSM}_2[a] &= \left(\begin{array}{c} 1 \cdot \text{sbox}(a) \\ \alpha \cdot \text{sbox}(a) \\ 1 \cdot \text{sbox}(a) \\ 1 \cdot \text{sbox}(a) \\ c \cdot \text{sbox}(a) \end{array} \right), \qquad \text{TBSM}_3[a] = \left(\begin{array}{c} \alpha \cdot \text{sbox}(a) \\ 1 \cdot \text{sbox}(a) \\ 1 \cdot \text{sbox}(a) \\ 1 \cdot \text{sbox}(a) \\ 1 \cdot \text{sbox}(a) \end{array} \right) \end{split}$$

and write

$$\begin{pmatrix} t_{0(8)} \\ t_{1(8)} \\ t_{2(8)} \\ t_{3(8)} \end{pmatrix} = \mathtt{TBSM_0}[v_{0(8)}] \oplus \mathtt{TBSM_1}[v_{1(8)}] \oplus \mathtt{TBSM_2}[v_{2(8)}] \oplus \mathtt{TBSM_3}[v_{3(8)}]$$

Similarly, we can denote the temporary result after the second key-addition layer of f32 before the last substitution layer by $u_{0(8)}||u_{1(8)}||u_{2(8)}||u_{3(8)}|$ and by $w_{0(8)}||w_{1(8)}||w_{2(8)}||w_{3(8)}|$, the temporary result after the last substitution layer, one can use the same strategy with the following tables:

$$\begin{aligned} \mathtt{TBS_0}[\mathtt{a}] &= \begin{pmatrix} \mathtt{sbox}(\mathtt{a}) \\ 0 \\ 0 \\ 0 \end{pmatrix}, \qquad \mathtt{TBS_1}[\mathtt{a}] &= \begin{pmatrix} 0 \\ \mathtt{sbox}(\mathtt{a}) \\ 0 \\ 0 \end{pmatrix} \\ \mathtt{TBS_2}[\mathtt{a}] &= \begin{pmatrix} 0 \\ 0 \\ \mathtt{sbox}(\mathtt{a}) \\ 0 \end{pmatrix}, \qquad \mathtt{TBS_3}[\mathtt{a}] &= \begin{pmatrix} 0 \\ 0 \\ 0 \\ \mathtt{sbox}(\mathtt{a}) \end{pmatrix} \end{aligned}$$

and write

$$\begin{pmatrix} w_{0(8)} \\ w_{1(8)} \\ w_{2(8)} \\ w_{3(8)} \end{pmatrix} = \mathtt{TBS_0}[u_{0(8)}] \oplus \mathtt{TBS_1}[u_{1(8)}] \oplus \mathtt{TBS_2}[u_{2(8)}] \oplus \mathtt{TBS_3}[u_{3(8)}]$$

As outlined before, the process is similar for the implementation of the f64 function. In this case, we have to define two times 8 tables of 256 64-bit elements. The following table summarizes the size of the various tables for a fully-precomputed implementation:

	number of tables	width [bytes]	total size [bytes]
FOX64	2×4	4	8192
FOX128	2×8	8	32768

Depending on the target processor, the nearest cache (i.e. the fastest memory) size may be smaller than 32768 bytes. In this case, one can spare half of the tables (at the cost of a few masking operations) by noting that all the TBS tables are "embedded" in the TBSM ones; this implementation strategy will by denoted *half-precomputed implementation*. This allows to reduce the fast memory needs to 4096 and 16384 bytes, respectively. Fig. 19 summarizes the best strategies for various amounts of L1 cache memory.

For most modern microprocessors (denoted by * in Fig. 19), a fully-precomputed implementation of FOX64 and FOX128 is probably the fastest possible solution. For the processors denoted by •, a half-precompted implementation is likely the best solution. The supplementary masking operations may be furthermore used to increase the instructions throughput on pipelined architectures.

Some microprocessors have a very small L1 data cache (they are denoted in \star in Fig. 19). In the case of FOX128, even a half-precomputed implementation will result in many caches misses, inducing a performance penalty. For early versions of Intel Pentium IV, a half-precomputed implementation of FOX64 is advantageous, while one can reduce the size of the precomputed data needed for a FOX128 implementation down to 8192 bytes at the cost of at most 18 supplementary PSHUFW instructions. Although these operations will result in a performance penalty, the latter will be reduced since the highly-parrallelizable structure of the f64 function allows to fully use the pipeline and thus to improve the instructions throughput. As most modern CPU architectures are pipelined ones, one can take this fact into account in order to improve performances of FOX implementations. There are two "dependency walls" in a FOX round function. The first one is just after the first subkey addition, the second one just after the second subkey addition. Inbetween, the additions of the table-lookup results may be done in any order, as an XOR is a commutative addition.

FOX128 is an excellent candidate for using the 64-bit instructions of actual 32-bit microprocessors. For instance, on the Intel architecture, the MMX/SSE/SSE2/SSE3 instruction sets may be used to "emulate" a 64-bit microprocessor. Furthermore, by expressing the Extended Lai-Massey scheme as in Fig. 14, one can compute very efficiently the two orthomorphisms as a single one on 64-bit architectures.

In order to get the best performances for FOX implementations written in a high-level language, one can get large speed differences when using different compilers. Furthermore, the choice of the data structure of the precomputed tables and of the data to be encrypted plays an important role: implementing a simple way to access these data will result in a speed increase.

4.2.3 Key-Schedule Algorithms

For applications needing a high key-agility, one can implement the various key-schedule algorithms using the same guidelines and tricks as for the core algorithm, since they share many

Processor	cache size [kB]	Note	Best Strategy
Alpha 21164	8	(data)	*
Alpha 21264	64	(data)	*
AMD Athlon XP	128	(data + code)	*
AMD Athlon MP	128	(data + code)	*
AMD Opteron	64	(data)	*
Intel Pentium III	16	(data)	•
Intel Pentium IV	8/16 (Prescott)	(data)	*/•
Intel Xeon	8	(data)	*
Intel Itanium	16	(data)	•
Intel Itanium2	16	(data)	•
PowerPC G4	32	(data + code)	•
PowerPC G5	32	(data)	*
UltraSparc II	16	(data)	•
UltraSparc III	64	(data)	*

Figure 19: Best implementation strategies on 32/64-bit microprocessors

common features.

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Test Vectors

```
2
3
      FOX test vectors generator v1.2
5
6
7
      F0X64/16/64 key : 00112233 44556677 F0X64/16/64 message : 01234567 89ABCDEF
8
9
      FOX64/16/64 ciphertext : 200E1F58 47D8A2CE
10
11
      FOX64/16/64 message : 01234567 89ABCDEF
12
13
14
                                : 00112233 44556677 8899AABB CCDDEEFF
15
      FOX64/16/128 key
      FOX64/16/128 message : 01234567 89ABCDEF
16
17
      FOX64/16/128 ciphertext : B85D6B76 6DCE952E
18
      FOX64/16/128 message : 01234567 89ABCDEF
19
20
21
22
      F0X64/16/192 key
                                : 00112233 44556677 8899AABB CCDDEEFF FFEEDDCC BBAA9988
      FOX64/16/192 message : 01234567 89ABCDEF
      FOX64/16/192 ciphertext : 2741D796 3406DACA
24
25
      F0X64/16/192 message
                                : 01234567 89ABCDEF
26
27
28
29
      F0X64/16/256 key
                                : 00112233 44556677 8899AABB CCDDEEFF FFEEDDCC BBAA9988 77665544 33221100
30
      FOX64/16/256 message : 01234567 89ABCDEF
31
      FOX64/16/256 ciphertext : 8A4EDFBC 36BEF7F6
32
      F0X64/16/256 message
                              : 01234567 89ABCDEF
33
34
35
      FOX128/16/64 key
                                : 00112233 44556677
      F0X128/16/64 key : 00112233 44556677 F0X128/16/64 message : 01234567 89ABCDEF FEDCBA98 76543210
37
38
      FOX128/16/64 ciphertext : 1EECBC7D EB66E7DA E1A7876D 90C0B239
                                : 01234567 89ABCDEF FEDCBA98 76543210
      FOX128/16/64 message
40
41
      FUALZE/16/128 key : 00112233 44556677 8899AABB CCDDEEFF FOX128/16/128 message : 01234567 89ARCDEE FOX128/16/102
42
43
44
45
      FOX128/16/128 ciphertext : 849E0F06 82F50CD5 88AE0730 06A10BEE
46
      FOX128/16/128 message
                                : 01234567 89ABCDEF FEDCBA98 76543210
```

```
47
48
49
      FOX128/16/192 key : 00112233 44556677 8899AABB CCDDEEFF FFEEDDCC BBAA9988 FOX128/16/192 message : 01234567 89ABCDEF FEDCBA98 76543210
50
51
      FOX128/16/192 ciphertext : 5934214E CBA2D5FD 58C261B2 8261B1BC
52
      FOX128/16/192 message : 01234567 89ABCDEF FEDCBA98 76543210
54
55
                                 : 00112233 44556677 8899AABB CCDDEEFF FFEEDDCC BBAA9988 77665544 33221100
57
      FOX128/16/256 key
      FOX128/16/256 message
58
                                 : 01234567 89ABCDEF FEDCBA98 76543210
      FOX128/16/256 ciphertext : 45CCB103 0F67B768 247F5302 66BC4996
59
                                 : 01234567 89ABCDEF FEDCBA98 76543210
60
      FOX128/16/256 message
```

Reference Implementations

File README

```
FOX / Reference implementation v1.2
      Pascal Junod <pascal@junod.info>
      The sole purpose of this reference code is to output
      a set of test vectors and to help understanding the
      structure of FOX. It is not fast, not portable, not
 8
      elegant and not secure. It implements a full
 q
      precomputed table-lookup strategy.
10
11
      The code has been written for the IA32 architecture,
12
      which is a little-endian architecture. It won't work
      on a big-endian architecture.
14
15
      Acknowledgments are due to Mounir Idrassi, Patrick Lattman,
16
      Marco Macchetti, Emmanuel Prouff, and Chen Wenyu for their
17
      help during the debugging process.
```

File Makefile

```
## FOX project / Reference implementation v1.2
     ## Pascal Junod <pascal@junod.info>
                                                   ##
4
                                                   ##
     6
7
    EXEC_NAME =
                       fox_util
8
g
    CFLAGS =
                       -W -Wall -pedantic -g
10
                       fox128.o fox64.o fox_ctx.o fox_cst.o fox_util.o
11
    objects =
12
13
                       $(objects)
14
                       $(CC) -o $(EXEC_NAME) $(objects)
15
16
    $(objects):
                       %.o: %.c %.h
17
                       $(CC) -c $(CFLAGS) $< -o $@
18
19
    .PHONY:
                       clean debug
20
21
     clean:
22
                       -rm -f $(objects) *~ $(EXEC_NAME)
23
```

File fox_portable.h

```
2
      /* FOX project / Reference implementation v1.2
 3
      /* Pascal Junod <pascal@junod.info>
 4
      /*
 5
      /* Base file is "nessie.h"
 6
      7
      #ifndef _FOX_PORTABLE_H_
 9
      #define _FOX_PORTABLE_H_
10
11
      #include <limits.h>
12
13
      typedef signed char sint8;
14
      typedef unsigned char uint8;
15
16
      #if UINT_MAX >= 4294967295UL
17
18
      typedef signed short sint16;
19
      typedef signed int sint32;
      typedef unsigned short uint16;
20
21
      typedef unsigned int uint32;
22
      #define ONE32 OxffffffffU
23
24
25
      #else
26
27
      typedef signed int sint16;
28
      typedef signed long sint32;
29
      typedef unsigned int uint16;
30
      typedef unsigned long uint32;
31
32
      #define ONE32 OxfffffffUL
33
34
      #endif
35
      #define ONE8
36
                      OxffU
37
      #define ONE16 OxffffU
38
39
      #define TO8(x) ((x) & ONE8)
40
      #define T016(x) ((x) & ONE16)
41
      #define T032(x) ((x) & ONE32)
42
43
      #define EXTRACT8_BIT(d, b)
                                       ((((uint8)(d)) & ((uint8)0x1 << (b))) >> (b))
      #define EXTRACT16_BIT(d, b)
                                       ((((uint16)(d)) & ((uint16)0x1 << (b))) >> (b))
44
45
      #define EXTRACT32_BIT(d, b)
                                       ((((uint32)(d)) & ((uint32)0x1 << (b))) >> (b))
46
      #define ROTL8(v, n)
                              ((uint8)((v) << (n)) | ((uint8)(v) >> (8 - (n))))
((uint16)((v) << (n)) | ((uint16)(v) >> (16 - (n))))
47
      #define ROTL16(v, n)
48
                              ((uint32)((v) << (n)) | ((uint32)(v) >> (32 - (n))))
49
      #define ROTL32(v, n)
50
51
      /* U8T032_BIG(c) returns the 32-bit value stored in big-endian convention
52
      /* in the unsigned char array pointed to by c.
53
54
      #define U8T032_BIG(c)
                             (((uint32)T08(*(c)) << 24) | ((uint32)T08(*((c) + 1)) << 16) | \
                              ((uint32)T08(*((c) + 2)) << 8) |
55
56
                              ((uint32)T08(*((c) + 3))))
57
58
      \slash U8T032_LITTLE(c) returns the 32-bit value stored in little-endian
                                                                                    */
59
      /* convention in the unsigned char array pointed to by c.
60
      #define U8T032_LITTLE(c) (((uint32)T08(*(c))) | ((uint32)T08(*(c) + 1)) << 8) | \
61
                            ((uint32)T08(*((c) + 2)) << 16) | ((uint32)T08(*((c) + 3)) << 24))
62
63
64
65
      /* U32T08_BIG(c, v) stores the 32-bit-value v in big-endian convention
66
      /* into the unsigned char array pointed to by c.
67
      #define U32T08_BIG(c, v)
68
                                 do { \
69
                      uint32 x = (v); \
70
                      uint8 *d = (c); \
                      d[0] = T08(x >> 24); \
71
```

```
72
                   d[1] = T08(x >> 16); \
73
                   d[2] = T08(x >> 8); \
                   d[3] = T08(x); \
74
75
            } while (0)
76
     /* U32T08\_LITTLE(c, v) stores the 32-bit-value v in little-endian
77
78
     /* convention into the unsigned char array pointed to by c.
79
80
     #define U32T08_LITTLE(c, v) do { \
81
82
                   uint32 x = (v); \setminus
                   uint8 *d = (c); \
83
84
                   d[0] = T08(x); \
                   d[1] = T08(x >> 8); \
85
86
                   d[2] = T08(x >> 16); \
                   d[3] = T08(x >> 24); \
87
            } while (0)
88
     #endif /* _FOX_PORTABLE_H_
                                                                        */
90
 File fox_error.h
     /* FOX project / Reference implementation v1.2
3
     /* Pascal Junod <pascal@junod.info>
                                                                        */
 4
                                                                        */
     6
7
     #ifndef _FOX_ERROR_H_
8
     #define _FOX_ERROR_H_
9
10
     #define FOX_ERROR_MEMORY_ALLOC
                                      "\nError: memory allocation"
     #define FOX_ERROR_CONTEXT_INIT
                                      "\nError: context initialization"
11
12
     #define FOX_ERROR_TABLE_INIT
                                      "\nError: table initialization"
13
     #define FOX_ERROR_KEY_INIT
                                      "\nError: key initialization"
                                      "\nError: unknown table ID"
     #define FOX_ERROR_UNKNOWN_TABLE_ID
14
                                      "\nError: unknown mode"
15
     #define FOX_ERROR_UNKNOWN_MODE
16
     #define FOX_BUG
                                      "\nError: bug"
17
     #endif /* _FOX_ERROR_H_ */
 File fox_cst.h
     2
     /* FOX project / Reference implementation v1.2
3
     /* Pascal Junod <pascal@junod.info>
                                                                        */
     5
6
     #ifndef _FOX_CST_H_
7
     #define _FOX_CST_H_
9
     #include "fox_portable.h"
10
11
12
     /* Constants
                                                                        */
13
     #define FOX_NUMBER_ROUNDS
14
                            FOX_NUMBER_ROUNDS_MIN
15
16
     #define FOX64_TABLE_SIGMA4_MU4_ID0
                                             0x00
     #define FOX64_TABLE_SIGMA4_MU4_ID1
                                             0x01
17
     #define FOX64_TABLE_SIGMA4_MU4_ID2
18
                                             0x02
19
     #define FOX64_TABLE_SIGMA4_MU4_ID3
                                             0x03
20
21
     #define FOX64_TABLE_SIGMA4_ID0
                                             0x04
22
     #define FOX64_TABLE_SIGMA4_ID1
                                             0x05
23
     {\tt \#define}\  \, {\tt FOX64\_TABLE\_SIGMA4\_ID2}
                                             0x06
24
     #define FOX64_TABLE_SIGMA4_ID3
                                             0x07
```

```
26
     #define FOX128_TABLE_SIGMA8_ID0
                                                 0x08
27
      #define FOX128_TABLE_SIGMA8_ID1
                                                 0x09
      #define FOX128_TABLE_SIGMA8_ID2
28
                                                 0x0A
29
      #define FOX128_TABLE_SIGMA8_ID3
                                                 0x0B
30
31
     #define FOX128_TABLE_SIGMA8_MU8_ID0
                                                 0x10
32
      #define FOX128_TABLE_SIGMA8_MU8_ID1
                                                 0x11
33
      #define FOX128_TABLE_SIGMA8_MU8_ID2
                                                 0x12
34
      #define FOX128_TABLE_SIGMA8_MU8_ID3
                                                 0x13
      #define FOX128_TABLE_SIGMA8_MU8_ID4
35
                                                 0x14
      #define FOX128_TABLE_SIGMA8_MU8_ID5
36
                                                 0x15
37
      #define FOX128_TABLE_SIGMA8_MU8_ID6
                                                 0x16
38
      #define FOX128_TABLE_SIGMA8_MU8_ID7
                                                 0x17
39
40
      /* FOX_IRRPOLY = x^8+x^7+x^6+x^5+x^4+x^3+1
41
     #define FOX_IRRPOLY
42
                                                0x1F9
43
      /* Constants used in the key-schedule algorithm
44
45
46
      #define FOX_MKEYM2
                                                 0x6A
      #define FOX_MKEYM1
47
                                                 0x76
48
49
      #define FOX_LFSR_C
                                         0x006A0000UL
50
      #define FOX_LFSR_FP
                                         0x0100001BUL
51
52
53
     /* These are the first decimal of e-2
54
55
     extern const uint8 FOX KEY PAD[32]:
56
57
     /* The three "small" S-boxes
58
59
      extern const uint8 FOX_S1[16];
60
      extern const uint8 FOX_S2[16];
61
      extern const uint8 FOX_S3[16];
62
      #endif /* _FOX_CST_H_
63
                                                                               */
 File fox_cst.c
      /* FOX project / Reference implementation v1.2
                                                                               */
 3
      /* Pascal Junod <pascal@junod.info>
                                                                               */
 4
                                                                               */
      6
      #include "fox_portable.h"
     #include "fox_cst.h"
 8
 9
10
     /* These are the first decimal of e-2
                                                                               */
11
12
      const uint8 FOX_KEY_PAD[32] = { 0xB7, 0xE1, 0x51, 0x62,
13
                                    Ox8A, OxED, Ox2A, Ox6A,
                                    0xBF, 0x71, 0x58, 0x80,
14
                                    0x9C, 0xF4, 0xF3, 0xC7,
15
16
                                    0x62, 0xE7, 0x16, 0x0F,
17
                                    0x38, 0xB4, 0xDA, 0x56,
18
                                    0xA7, 0x84, 0xD9, 0x04,
                                    0x51, 0x90, 0xCF, 0xEF };
19
20
21
     /* The three "small" S-boxes
                                                                               */
22
23
      const uint8 FOX_S1[16] = \{ 0x2, 0x5, 0x1, 0x9, \}
24
                               0xE, 0xA, 0xC, 0x8,
25
                               0x6, 0x4, 0x7, 0xF,
26
                               0xD, 0xB, 0x0, 0x3 };
27
      const uint8 FOX_S2[16] = \{ OxB, Ox4, Ox1, OxF,
```

```
29
                              0x0, 0x3, 0xE, 0xD,
30
                              0xA, 0x8, 0x7, 0x5,
31
                              0xC, 0x2, 0x9, 0x6 };
32
33
     const uint8 FOX_S3[16] = { OxD, OxA, OxB, Ox1, }
34
                              0x4, 0x3, 0x8, 0x9,
35
                              0x5, 0x7, 0x2, 0xC,
36
                              0xF, 0x0, 0x6, 0xE };
37
38
 File fox_ctx.h
     /* FOX project / Reference implementation v1.2
3
     /* Pascal Junod <pascal@junod.info>
                                                                           */
     5
6
     #ifndef _FOX_CTX_H_
7
     #define _FOX_CTX_H_
9
     #include "fox_portable.h"
10
     #include "fox_cst.h"
11
12
13
     /* Types
14
     typedef uint8 FOX_mode;
15
16
17
     typedef struct {
18
19
         uint32 *exp_key;
         uint8 raw_key[32];
20
21
         uint8 key_length;
22
         uint8 rounds;
23
     } FOX_key_;
24
25
     typedef FOX_key_ *FOX_key;
26
     typedef struct {
28
         uint32 *val;
         uint32 size_bytes;
29
30
         uint8 id;
     } FOX_table_;
31
32
33
     typedef FOX_table_ *FOX_table;
34
35
     typedef struct {
36
         FOX_table sigma4_mu4_0;
37
         FOX_table sigma4_mu4_1;
38
         FOX_table sigma4_mu4_2;
39
         FOX_table sigma4_mu4_3;
40
         FOX_table sigma4_0;
41
42
         FOX_table sigma4_1;
43
         FOX_table sigma4_2;
44
         FOX_table sigma4_3;
45
46
     } F0X64_ctx_;
47
48
     typedef F0X64_ctx_ *F0X64_ctx;
49
     typedef struct {
50
51
         FOX_table sigma8_mu8_0;
         FOX_table sigma8_mu8_1;
52
53
         FOX_table sigma8_mu8_2;
54
         FOX_table sigma8_mu8_3;
```

FOX_table sigma8_mu8_4;

FOX_table sigma8_mu8_5;

55

```
57
          FOX_table sigma8_mu8_6;
58
          FOX_table sigma8_mu8_7;
59
60
          FOX_table sigma8_0;
61
          FOX_table sigma8_1;
          FOX_table sigma8_2;
62
63
          FOX_table sigma8_3;
64
65
      } FOX128_ctx_;
66
      typedef FOX128_ctx_ *FOX128_ctx;
67
68
69
      /* Exportable routines
                                                                              */
70
71
      extern int FOX64_init_ctx (FOX64_ctx *);
72
      extern void F0X64_clean_ctx (F0X64_ctx);
73
74
      extern int FOX128_init_ctx (FOX128_ctx *);
75
      extern void FOX128_clean_ctx (FOX128_ctx);
76
77
78
      extern int FOX64_init_key (FOX_key *,
79
                               const FOX64_ctx,
80
                               const uint8 *,
81
                               const uint32,
82
                               const uint8);
83
84
      extern void FOX64_clean_key (FOX_key);
85
86
      extern int FOX128_init_key (FOX_key *,
87
                                const FOX128_ctx,
88
                                const uint8 *,
89
                                const uint32,
90
                                const uint8);
91
92
      extern void FOX128_clean_key (FOX_key);
93
94
      extern void FOX_io (uint32 *);
95
      extern void FOX_or (uint32 *);
96
97
98
      /* Internal routines
                                                                              */
99
100
      int FOX_init_table (FOX_table *, const uint8);
      void FOX_clean_table (FOX_table);
101
102
103
      uint32 FOX_times_alpha (const uint32);
104
      uint32 FOX_div_alpha (const uint32);
105
106
      uint32 FOX_eval_sbox (const uint32 x, const uint8 *s1,
107
                           const uint8 *s2, const uint8 *s3);
108
109
      #endif /* _FOX_CTX_H_
110
                                                                              */
  File fox_ctx.c
      /* FOX project / Reference implementation v1.2
 3
      /* Pascal Junod <pascal@junod.info>
                                                                             */
 4
      #include <stdlib.h>
      #include <stdio.h>
 8
 9
      #include <assert.h>
10
      #include <string.h>
11
12
      #include "fox_portable.h"
```

```
13
      #include "fox_error.h"
14
      #include "fox_ctx.h"
#include "fox64.h"
15
      #include "fox128.h"
16
17
18
19
     void FOX_or (uint32 *data)
20
21
          uint32 1, r;
22
23
          assert (data != NULL);
24
25
          1 = *data >> 16;
26
          r = *data & OxFFFF;
27
28
          *data = (r << 16) | (1 ^ r);
29
     }
30
31
      void FOX_io (uint32 *data)
32
33
          uint32 1, r;
34
35
          assert (data != NULL);
36
37
          1 = *data >> 16;
          r = *data & OxFFFF;
38
39
          *data = (( l ^ r) << 16) | 1;
40
41
     }
42
43
      uint32 FOX_times_alpha (const uint32 input)
44
45
46
          if (input) {
              return (input & 0x80) ? (input << 1) ^ FOX_IRRPOLY : input << 1;
47
48
          } else {
49
              return 0x00;
50
          }
51
      }
52
53
      uint32 FOX_div_alpha (const uint32 input)
55
56
          if (input) {
57
               return (input & 0x01) ? (input ^ FOX_IRRPOLY) >> 1 : input >> 1;
58
          } else {
59
              return 0x00;
60
      }
61
62
      int FOX64_init_ctx (FOX64_ctx *ptr)
63
64
65
          FOX64_ctx ctx;
66
67
          if ( (ctx = malloc (sizeof (FOX64_ctx_))) == NULL) {
              fprintf (stderr, FOX_ERROR_MEMORY_ALLOC);
68
69
              goto error_label;
70
71
          if (FOX_init_table (&ctx->sigma4_mu4_0, FOX64_TABLE_SIGMA4_MU4_ID0)) {
72
              goto error_label;
73
          }
74
          if (FOX_init_table (&ctx->sigma4_mu4_1, FOX64_TABLE_SIGMA4_MU4_ID1)) {
75
              goto error_label;
76
77
          if (FOX_init_table (&ctx->sigma4_mu4_2, FOX64_TABLE_SIGMA4_MU4_ID2)) {
78
              goto error_label;
79
          }
80
          if (FOX_init_table (&ctx->sigma4_mu4_3, FOX64_TABLE_SIGMA4_MU4_ID3)) {
              goto error_label;
82
```

```
83
           if (FOX_init_table (&ctx->sigma4_0, FOX64_TABLE_SIGMA4_ID0)) {
 84
               goto error_label;
 85
           }
 86
           if (FOX_init_table (&ctx->sigma4_1, FOX64_TABLE_SIGMA4_ID1)) {
               goto error_label;
 87
           }
88
           if (FOX_init_table (&ctx->sigma4_2, FOX64_TABLE_SIGMA4_ID2)) {
 90
               goto error_label;
91
 92
           if (FOX_init_table (&ctx->sigma4_3, FOX64_TABLE_SIGMA4_ID3)) {
 93
               goto error_label;
 94
 95
           *ptr = ctx;
 96
 97
98
           return 0:
99
100
        error_label:
           fprintf (stderr, FOX_ERROR_CONTEXT_INIT);
101
102
           FOX64_clean_ctx (ctx);
103
104
           return -1;
105
       }
106
107
108
       void F0X64_clean_ctx (F0X64_ctx ctx)
109
110
           if (ctx != NULL) {
               FOX_clean_table (ctx->sigma4_mu4_0);
111
112
               FOX_clean_table (ctx->sigma4_mu4_1);
113
               FOX_clean_table (ctx->sigma4_mu4_2);
114
               FOX_clean_table (ctx->sigma4_mu4_3);
115
116
               FOX_clean_table (ctx->sigma4_0);
               FOX_clean_table (ctx->sigma4_1);
117
118
               FOX_clean_table (ctx->sigma4_2);
119
               FOX_clean_table (ctx->sigma4_3);
120
121
               free (memset (ctx, 0x00, sizeof (F0X64_ctx_)));
122
           }
123
       }
124
125
       int F0X128_init_ctx (F0X128_ctx *ptr)
126
127
           FOX128_ctx ctx;
128
129
           if ( (ctx = malloc (sizeof (FOX128_ctx_))) == NULL) {
130
               fprintf (stderr, FOX_ERROR_MEMORY_ALLOC);
131
               goto error_label;
132
           if (FOX_init_table (&ctx->sigma8_mu8_0, FOX128_TABLE_SIGMA8_MU8_ID0)) {
133
134
               goto error_label;
135
           if (FOX_init_table (&ctx->sigma8_mu8_1, FOX128_TABLE_SIGMA8_MU8_ID1)) {
136
137
               goto error_label;
138
           }
139
           if (FOX_init_table (&ctx->sigma8_mu8_2, FOX128_TABLE_SIGMA8_MU8_ID2)) {
140
               goto error_label;
141
           }
142
           if (FOX_init_table (&ctx->sigma8_mu8_3, FOX128_TABLE_SIGMA8_MU8_ID3)) {
143
               goto error_label;
           }
144
145
           if (FOX_init_table (&ctx->sigma8_mu8_4, FOX128_TABLE_SIGMA8_MU8_ID4)) {
146
               goto error_label;
           }
147
148
           if (FOX_init_table (&ctx->sigma8_mu8_5, FOX128_TABLE_SIGMA8_MU8_ID5)) {
149
               goto error_label;
150
           }
           if (FOX_init_table (&ctx->sigma8_mu8_6, FOX128_TABLE_SIGMA8_MU8_ID6)) {
151
152
               goto error_label;
```

```
153
154
           if (FOX_init_table (&ctx->sigma8_mu8_7, FOX128_TABLE_SIGMA8_MU8_ID7)) {
155
               goto error_label;
156
           }
157
           if (FOX_init_table (&ctx->sigma8_0, FOX128_TABLE_SIGMA8_ID0)) {
158
                goto error_label;
159
160
           if (FOX_init_table (&ctx->sigma8_1, FOX128_TABLE_SIGMA8_ID1)) {
161
                goto error_label;
162
           }
163
           if (FOX_init_table (&ctx->sigma8_2, FOX128_TABLE_SIGMA8_ID2)) {
164
                goto error_label;
165
           if (FOX_init_table (&ctx->sigma8_3, FOX128_TABLE_SIGMA8_ID3)) {
166
167
               goto error_label;
168
169
170
           *ptr = ctx;
171
172
           return 0;
173
174
        error label:
175
           fprintf (stderr, FOX_ERROR_CONTEXT_INIT);
176
           FOX128_clean_ctx (ctx);
177
178
           return -1;
       }
179
180
181
       void FOX128_clean_ctx (FOX128_ctx ctx)
182
183
           if (ctx != NULL) {
               FOX_clean_table (ctx->sigma8_mu8_0);
184
               FOX_clean_table (ctx->sigma8_mu8_1);
185
186
                FOX_clean_table (ctx->sigma8_mu8_2);
               FOX_clean_table (ctx->sigma8_mu8_3);
187
188
               FOX_clean_table (ctx->sigma8_mu8_4);
189
               FOX_clean_table (ctx->sigma8_mu8_5);
190
               FOX_clean_table (ctx->sigma8_mu8_6);
191
               FOX_clean_table (ctx->sigma8_mu8_7);
192
193
               FOX_clean_table (ctx->sigma8_0);
194
               FOX_clean_table (ctx->sigma8_1);
195
               FOX_clean_table (ctx->sigma8_2);
196
               FOX_clean_table (ctx->sigma8_3);
197
198
               free (memset (ctx, 0x00, sizeof (F0X128_ctx_)));
199
           }
200
       }
201
202
       int FOX64_init_key (FOX_key *ptr,
203
                            const FOX64_ctx ctx,
204
                            const uint8 *bytes,
205
                            const uint32 length,
206
                            const uint8 rounds)
207
       {
208
           FOX_key key;
209
           uint32 i, j;
210
           uint32 o;
211
           uint8 pkey[32], mkey[32], dkey[32];
212
           uint32 dkey32[8], temp32[8], reg32[8];
213
           uint32 b, ek;
214
           uint32 lfsr_state;
215
           uint8 lfsr[4];
216
217
           assert (ctx != NULL);
218
           assert (length <= 256);
219
220
           assert (length \% 8 == 0);
221
           assert (rounds >= FOX64_NUMBER_ROUNDS_MIN);
222
```

```
if ( (key = malloc (sizeof (FOX_key_))) == NULL) {
223
224
                fprintf (stderr, FOX_ERROR_MEMORY_ALLOC);
225
                goto error_label;
226
            }
227
            if ( (key->exp_key = malloc (sizeof (uint32) * 2 * rounds )) == NULL) {
                fprintf (stderr, FOX_ERROR_MEMORY_ALLOC);
228
229
                goto error_label;
230
231
232
           memcpy (key->raw_key, bytes, (length >> 3));
233
           memcpy (pkey, bytes, (length >> 3));
234
235
            /* Size in bits
                                                                                        */
236
           key->key_length = length;
237
238
            key->rounds = rounds;
239
240
            /* Computation of the state bit b and of ek
                                                                                        */
241
242
            if ( (length == 128) || (length == 256) ) {
243
               b = 1;
244
            } else {
245
                b = 0;
246
247
248
            if (length <= 128) {
249
                ek = 128;
            } else {
250
251
                ek = 256;
252
253
254
            /* P-part
                                                                                        */
255
256
            if (length < ek) {
                for (i = (length >> 3), j = 0; i < (ek >> 3); i++, j++) {
257
258
                    pkey[i] = FOX_KEY_PAD[j];
259
260
           }
261
262
           memcpy (mkey, pkey, (ek >> 3));
263
264
            /* M-part
                                                                                        */
265
266
            if (length < ek) {
                mkey[0] ^= (FOX_MKEYM2 + FOX_MKEYM1);
267
                mkey[1] ^= (FOX_MKEYM1 + mkey[0]);
268
269
                for (i = 2; i < (ek >> 3); i++) {
                   mkey[i] ^= (mkey[i - 2] + mkey[i - 1]);
270
271
272
            }
273
            /* D-Part
274
                                                                                        */
275
276
            /* Initialization of the LFSR
                                                                                        */
277
           lfsr_state = FOX_LFSR_C | ((uint32)rounds << 8) | (~rounds & 0xFF);</pre>
278
279
            /* We back-clock the LFSR once
                                                                                        */
280
            if (lfsr_state & 0x1) {
                lfsr_state ^= FOX_LFSR_FP;
281
282
283
            lfsr_state >>= 1;
284
285
            for (i = 0; i < rounds; i++) {
                j = 0;
286
287
                while (j < (ek >> 3)) {
288
                    if ((j \% 3) == 0) {
289
                        /* We have to clock the LFSR
                                                                                        */
290
                        lfsr_state <<= 1;</pre>
291
                        if (lfsr_state & 0x01000000) {
                            lfsr_state ^= FOX_LFSR_FP;
292
```

```
293
                          }
294
                           /* Endianness issue here !
                                                                                                 */
                          U32T08_BIG (lfsr, lfsr_state);
295
296
297
                      dkey[j] = mkey[j] ^ lfsr[(j % 3) + 1];
298
299
                 }
300
301
                 for (j = 0; j < (ek >> 5); j++) {
302
                      dkey32[j] = U8T032_BIG (dkey + (j << 2));
303
304
305
                 /* NL-part : we feed the current DKEY to the NLx part
306
                 /* sigma4 - mu4 operation
307
                 for (j = 0; j < (ek >> 5); j++) {
308
                      o = ctx->sigma4_mu4_0->val[(dkey32[j] & 0xFF000000) >> 24];
309
                      o ^= ctx->sigma4_mu4_1->val[(dkey32[j] & 0x00FF0000) >> 16];
310
                      o ^= ctx->sigma4_mu4_2->val[(dkey32[j] & 0x0000FF00) >> 8];
                      o ^= ctx->sigma4_mu4_3->val[(dkey32[j] & 0x000000FF)];
311
312
                      reg32[j] = o;
313
314
315
                 if (ek == 128) {}
316
                      /* mix64 operation
                                                                                                 */
                      temp32[0] = reg32[1] ^ reg32[2] ^ reg32[3];
temp32[1] = reg32[0] ^ reg32[2] ^ reg32[3];
317
318
                      temp32[2] = reg32[0] ^ reg32[1] ^ reg32[3];
temp32[3] = reg32[0] ^ reg32[1] ^ reg32[2];
319
320
321
                 } else {
322
                      /* mix64h operation
                                                                                                 */
                      temp32[0] = reg32[2] ^ reg32[4] ^ reg32[6];
temp32[1] = reg32[3] ^ reg32[5] ^ reg32[7];
323
324
                      temp32[2] = reg32[0] ^ reg32[4] ^ reg32[6];
325
326
                      temp32[3] = reg32[1]
                                               reg32[5]
                                                             reg32[7];
                      temp32[4] = reg32[0] ^ reg32[2] ^ reg32[6];
327
                      temp32[5] = reg32[1] ^ reg32[3] ^ reg32[7];
328
                      temp32[6] = reg32[0] ^ reg32[2] ^ reg32[4];
temp32[7] = reg32[1] ^ reg32[3] ^ reg32[5];
329
330
331
332
                 /* Constant addition
333
                 /* Endianness issue here !
334
                 for (j = 0; j < (ek >> 5); j++) {
335
                      temp32[j] ^= U8T032_BIG (FOX_KEY_PAD + (j << 2));
336
337
                 /* Conditional flip
                                                                                                 */
338
                 if (b) {
339
                      for (j = 0; j < (ek >> 5); j++) {
                          temp32[j] = ~temp32[j];
340
341
342
                 }
343
344
                 /* sigma4 operation
                                                                                                 */
345
                 for (j = 0; j < (ek >> 5); j++) {
346
                          o = ctx->sigma4_0->val[(temp32[j] & 0xFF000000) >> 24];
347
                           o ^= ctx->sigma4_1->val[(temp32[j] & 0x00FF0000) >> 16];
348
                          o ^= ctx->sigma4_2->val[(temp32[j] & 0x0000FF00) >> 8];
349
                          o ^= ctx->sigma4_3->val[(temp32[j] & 0x000000FF)];
350
                          temp32[j] = o;
351
352
                 if (ek == 128) {}
353
354
                      /* Hashing
                                                                                                 */
                      reg32[0] = temp32[0] ^ temp32[2];
reg32[1] = temp32[1] ^ temp32[3];
355
356
357
358
                      /* Encryption phase
359
                      FOX_lmor64 (reg32, dkey32, ctx);
360
                      FOX_1mid64 (reg32, dkey32 + 2, ctx);
                      *(key->exp_key + 2*i) = reg32[0];
361
                      *(key->exp_key + 2*i + 1) = reg32[1];
362
```

```
363
                } else {
364
                     /* Hashing
                                                                                           */
                     reg32[0] = temp32[0] ^ temp32[1];
365
                     reg32[1] = temp32[2] ^ temp32[3];
366
                    reg32[2] = temp32[4] ^ temp32[5];
reg32[3] = temp32[6] ^ temp32[7];
367
368
369
370
                    temp32[0] = reg32[0] ^ reg32[2];
temp32[1] = reg32[1] ^ reg32[3];
371
372
373
                     /* Encryption phase
                                                                                           */
                     FOX_lmor64 (temp32, dkey32, ctx);
374
                     FOX_lmor64 (temp32, dkey32 + 2, ctx);
375
                     FOX_lmor64 (temp32, dkey32 + 4, ctx);
376
377
                     FOX_lmid64 (temp32, dkey32 + 6, ctx);
                     *(key->exp_key + 2*i) = temp32[0];
378
                     *(key->exp_key + 2*i + 1) = temp32[1];
379
380
                }
381
            }
382
383
            *ptr = key;
384
385
            return 0;
386
387
         error_label:
388
            FOX64_clean_key (key);
389
390
            return -1;
391
       }
392
393
       void FOX64_clean_key (FOX_key k)
394
395
            if (k != NULL) {
396
                if (k->exp_key != NULL) {
                    free (memset (k->exp_key, 0x00, k->rounds * 2 * sizeof (uint32)));
397
398
399
                free (memset (k, 0x00, sizeof (FOX_key_)));
400
            }
401
       }
402
403
       int FOX128_init_key (FOX_key *ptr,
404
                              const FOX128_ctx ctx,
                              const uint8 *bytes,
405
406
                              const uint32 length,
407
                              const uint8 rounds)
408
       {
409
            FOX_key key;
            uint32 i, j;
410
411
            uint32 o[2];
412
            uint8 dkey[32], pkey[32], mkey[32];
413
            uint32 dkey32[8], temp32[8], reg32[8];
414
            uint32 b, ek;
415
            uint32 lfsr_state;
            uint8 lfsr[4];
416
417
418
            assert (length <= 256);
419
            assert (length % 8 == 0);
420
            assert (rounds >= FOX64_NUMBER_ROUNDS_MIN);
421
            if ( (key = malloc (sizeof (FOX_key_))) == NULL) {
422
423
                fprintf (stderr, FOX_ERROR_MEMORY_ALLOC);
424
                goto error_label;
425
            if ( (key->exp_key = malloc (sizeof (uint32) * 4 * rounds )) == NULL) {
426
                fprintf (stderr, FOX_ERROR_MEMORY_ALLOC);
427
428
                goto error_label;
429
430
431
            memcpy (key->raw_key, bytes, (length >> 3));
432
            memcpy (pkey, bytes, (length >> 3));
```

```
433
434
            /* Size in bits
                                                                                         */
435
436
            key->key_length = length;
437
            key->rounds = rounds;
438
439
            /* Computation of the state bit b and of ek
440
441
            if ( length == 256 ) {
442
                b = 1;
443
            } else {
444
                b = 0;
445
446
            ek = 256;
447
448
449
            /* P-part
                                                                                         */
450
            if (length < ek) {
451
                for (i = (length >> 3), j = 0; i < 32; i++, j++) {
452
453
                    pkey[i] = FOX_KEY_PAD[j];
454
455
            }
456
457
           memcpy (mkey, pkey, (ek >> 3));
458
459
            /* M-part
                                                                                         */
460
461
            if (length < ek) {
                mkey[0] ^= (FOX_MKEYM2 + FOX_MKEYM1);
462
463
                mkey[1] ^= (FOX_MKEYM1 + mkey[0]);
                for (i = 2; i < (ek >> 3); i++) {
464
                    mkey[i] ^= (mkey[i - 2] + mkey[i - 1]);
465
466
            }
467
468
469
            /* D-Part
                                                                                         */
470
471
            /* Initialization of the LFSR
472
            lfsr_state = FOX_LFSR_C | ((uint32)rounds << 8) | (~rounds & 0xFF);</pre>
473
474
            /* We back-clock the LFSR once
                                                                                         */
475
            if (lfsr_state & 0x1) {
476
                lfsr_state ^= FOX_LFSR_FP;
477
478
           lfsr_state >>= 1;
479
            for (i = 0; i < rounds; i++) {</pre>
480
481
                j = 0;
482
                while (j < (ek >> 3)) {
                    if ((j % 3) == 0) {
483
484
                        /* We have to clock the LFSR
                                                                                         */
485
                        lfsr_state <<= 1;</pre>
                        if (lfsr_state & 0x01000000) {
486
487
                            lfsr_state ^= FOX_LFSR_FP;
488
489
                        /* Endianness issue here !
                                                                                         */
490
                        U32T08_BIG (lfsr, lfsr_state);
491
                    dkey[j] = mkey[j] ^ lfsr[(j % 3) + 1];
492
493
                    j++;
494
                }
495
                for (j = 0; j < 8; j++) {
496
497
                    dkey32[j] = U8T032_BIG (dkey + (j << 2));
498
499
500
                /* NL Part
                                                                                         */
501
                                                                                         */
502
                /* sigma8 - mu8 operation
```

```
503
               for (j = 0; j < 4; j++) {
                    o[0] = ctx->sigma8_mu8_0->val[ (dkey32[2*j] & 0xFF000000) >> 23];
504
505
                        = ctx->sigma8_mu8_0->val[((dkey32[2*j] & 0xFF000000) >> 23) + 1];
506
                    o[0] ^= ctx->sigma8_mu8_1->val[ (dkey32[2*j] & 0x00FF0000) >> 15];
                    o[1] ^= ctx->sigma8_mu8_1->val[((dkey32[2*j] & 0x00FF0000) >> 15) + 1];
507
                    o[0] ^= ctx->sigma8_mu8_2->val[ (dkey32[2*j] & 0x0000FF00) >> 7];
508
509
                    o[1] ^= ctx->sigma8_mu8_2->val[((dkey32[2*j] & 0x0000FF00) >> 7) + 1];
510
                    o[0] ^= ctx->sigma8_mu8_3->val[ (dkey32[2*j] & 0x000000FF) << 1];
511
                    o[1] ^= ctx->sigma8_mu8_3->val[((dkey32[2*j] & 0x000000FF) << 1)+ 1];
512
513
                    o[0] ^= ctx->sigma8_mu8_4->val[(dkey32[2*j+1] & 0xFF000000) >> 23];
514
                    o[1] ^= ctx->sigma8_mu8_4->val[((dkey32[2*j+1] & 0xFF000000) >> 23) + 1];
515
                    o[0] ^= ctx->sigma8_mu8_5->val[(dkey32[2*j+1] & 0x00FF0000) >> 15];
                    o[1] ^= ctx->sigma8_mu8_5->val[((dkey32[2*j+1] & 0x00FF0000) >> 15) + 1];
516
517
                    o[0] ^= ctx->sigma8_mu8_6->val[(dkey32[2*j+1] & 0x0000FF00) >> 7];
                   o[1] ^= ctx->sigma8_mu8_6->val[((dkey32[2*j+1] & 0x0000FF00) >> 7) + 1];
518
                    o[0] ^= ctx->sigma8_mu8_7->val[(dkey32[2*j+1] & 0x000000FF) << 1];
519
520
                    o[1] ^= ctx->sigma8_mu8_7->val[((dkey32[2*j+1] & 0x000000FF) << 1) + 1];
521
522
                    reg32[2*j] = o[0];
523
                   reg32[2*j + 1] = o[1];
               }
524
525
               /* mix128 operation
526
                                                                                       */
527
528
               temp32[0] = reg32[2] ^ reg32[4] ^ reg32[6];
               temp32[1] = reg32[3] ^ reg32[5] ^ reg32[7];
529
530
               temp32[2] = reg32[0]
                                       reg32[4]
                                                  reg32[6];
               temp32[3] = reg32[1] ^
531
                                       reg32[5]
                                                  reg32[7];
               temp32[4] = reg32[0] ^ reg32[2] ^ reg32[6];
532
533
               temp32[5] = reg32[1]
                                       reg32[3]
                                                  reg32[7];
               temp32[6] = reg32[0] ^ reg32[2] ^ reg32[4];
534
               temp32[7] = reg32[1] ^ reg32[3] ^ reg32[5];
535
536
537
               /* Constant addition
538
                /* Endianness issue here !
539
               for (j = 0; j < 8; j++) {
                    temp32[j] ^= U8T032_BIG (FOX_KEY_PAD + (j << 2));
540
541
542
               /* Conditional flip
                                                                                       */
543
               if (b) {
544
                   for (j = 0; j < 8; j++) {
                       temp32[j] = ~temp32[j];
545
546
547
               }
548
549
               /* sigma8 operation
               for (j = 0; j < 4; j++) {
550
551
                    o[0] = ctx->sigma8_0->val[(temp32[2*j] & 0xFF000000) >> 24];
552
                    o[0] ^= ctx->sigma8_1->val[(temp32[2*j] & 0x00FF0000) >> 16];
                    o[0] ^= ctx->sigma8_2->val[(temp32[2*j] & 0x0000FF00) >> 8];
553
                    o[0] ^= ctx->sigma8_3->val[(temp32[2*j] & 0x000000FF)];
554
555
                    o[1] = ctx->sigma8_0->val[(temp32[2*j+1] & 0xFF000000) >> 24];
556
557
                    o[1] ^= ctx->sigma8_1->val[(temp32[2*j+1] & 0x00FF0000) >> 16];
558
                   o[1] ^= ctx->sigma8_2->val[(temp32[2*j+1] & 0x0000FF00) >> 8];
559
                    o[1] ^= ctx->sigma8_3->val[(temp32[2*j+1] & 0x000000FF)];
560
561
                   temp32[2*j] = o[0];
562
                    temp32[2*j + 1] = o[1];
563
564
565
               reg32[0] = temp32[0] ^ temp32[4];
               reg32[1] = temp32[1] ^ temp32[5];
566
               reg32[2] = temp32[2] ^ temp32[6];
567
568
               reg32[3] = temp32[3] ^ temp32[7];
569
570
                /* Encryption phase
                                                                                       */
571
               FOX_elmor128 (reg32, dkey32, ctx);
572
               FOX_elmid128 (reg32, dkey32 + 4, ctx);
```

```
573
574
                *(key->exp_key + 4*i)
                                           = reg32[0];
                *(key-\exp_key + 4*i + 1) = reg32[1];
575
576
                *(key->exp_key + 4*i + 2) = reg32[2];
577
                *(key->exp_key + 4*i + 3) = reg32[3];
578
579
580
            *ptr = key;
581
582
           return 0;
583
584
         error_label:
585
           FOX128_clean_key (key);
586
587
            return -1;
588
589
590
       void FOX128_clean_key (FOX_key k)
591
592
            if (k != NULL) {
593
                if (k->exp_key != NULL) {
594
                    free (memset (k->exp_key, 0x00, k->rounds *
595
                                   4 * sizeof (uint32)));
596
597
                free (memset (k, 0x00, sizeof (FOX_key_)));
598
            }
599
       }
600
601
       int FOX_init_table (FOX_table *ptr, const uint8 id)
602
603
            uint32 i, size, tmp;
604
            FOX table table:
605
606
            if ( (table = malloc (sizeof (FOX_table_))) == NULL) {
                fprintf (stderr, FOX_ERROR_MEMORY_ALLOC);
607
608
                goto error_label;
609
610
611
            if (id >= 0x8) {
612
                size = 2;
            } else {
613
614
                size = 1;
615
616
            if ( (table->val = malloc (256 * sizeof(uint32) * size)) == NULL) {
617
                fprintf (stderr, FOX_ERROR_MEMORY_ALLOC);
618
619
                goto error_label;
620
            }
621
            table->id = id;
622
            table->size_bytes = 256 * sizeof(uint32) * size;
623
624
            switch (id) {
625
                case FOX64_TABLE_SIGMA4_MU4_ID0:
626
627
                    for (i = 0; i < 256; i++) {
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
628
629
                        table->val[i] = tmp << 24;</pre>
630
                        table->val[i] |= tmp << 16;
631
                        table->val[i] |= (FOX_div_alpha(tmp) ^ tmp) << 8;</pre>
632
                        table->val[i] |= FOX_times_alpha (tmp);
633
634
                    break;
635
                case FOX64_TABLE_SIGMA4_MU4_ID1:
636
637
                    for (i = 0; i < 256; i++) {
638
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
639
                        table->val[i] = tmp << 24;
                        table->val[i] |= (FOX_div_alpha(tmp) ^ tmp) << 16;</pre>
640
641
                        table->val[i] |= FOX_times_alpha (tmp) << 8;</pre>
                        table->val[i] |= tmp;
642
```

```
643
                    }
644
                    break;
645
646
                case FOX64_TABLE_SIGMA4_MU4_ID2:
647
                    for (i = 0; i < 256; i++) {
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
648
649
                        table->val[i] = tmp << 24;
650
                        table->val[i] |= FOX_times_alpha (tmp) << 16;
651
                        table->val[i] |= tmp << 8;
652
                        table->val[i] |= (FOX_div_alpha(tmp) ^ tmp);
653
654
                    break;
655
                case FOX64_TABLE_SIGMA4_MU4_ID3:
656
657
                    for (i = 0; i < 256; i++) {
658
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
659
                        table->val[i] = FOX_times_alpha (tmp) << 24;</pre>
                        table->val[i] |= tmp << 16;
660
                        table->val[i] |= tmp << 8;
661
662
                        table->val[i] |= tmp;
663
664
                    break:
665
666
                case FOX128_TABLE_SIGMA8_MU8_ID0:
667
                    for (i = 0; i < 256; i++) {
668
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
                        table->val[2*i] = tmp << 24;
669
                        table->val[2*i] |= tmp << 16;
670
                        table->val[2*i] |= (FOX_times_alpha (tmp) ^ tmp) << 8;</pre>
671
                        table->val[2*i] |= (FOX_div_alpha (tmp ^ FOX_div_alpha (tmp)));
672
673
                        table->val[2*i+1] = FOX_times_alpha (tmp) << 24;</pre>
                        table->val[2*i+1] |= FOX_times_alpha (FOX_times_alpha (tmp)) << 16;
674
675
                        table->val[2*i+1] |= FOX_div_alpha (tmp) << 8;
676
                        table->val[2*i+1] |= FOX_div_alpha (FOX_div_alpha (tmp));
677
                    }
678
                    break;
679
680
                case FOX128_TABLE_SIGMA8_MU8_ID1:
681
                    for (i = 0; i < 256; i++) {
682
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
683
                        table - val[2*i] = tmp << 24;
684
                        table->val[2*i] |= (FOX_times_alpha (tmp) ^ tmp) << 16;</pre>
                        table->val[2*i] |= (FOX_div_alpha (tmp ^ FOX_div_alpha (tmp))) << 8;</pre>
685
                        table->val[2*i] |= FOX_times_alpha (tmp);
686
687
                        table->val[2*i+1] = FOX_times_alpha (FOX_times_alpha (tmp)) << 24;</pre>
688
                        table->val[2*i+1] |= FOX_div_alpha (tmp) << 16;</pre>
689
                        table->val[2*i+1] |= FOX_div_alpha (FOX_div_alpha (tmp)) << 8;</pre>
690
                        table->val[2*i+1] |= tmp;
691
                    7
692
                    break;
693
694
                case FOX128_TABLE_SIGMA8_MU8_ID2:
695
                    for (i = 0; i < 256; i++) {
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
696
697
                        table - val[2*i] = tmp << 24;
                        table->val[2*i] |= (FOX_div_alpha (tmp ^ FOX_div_alpha (tmp))) << 16;</pre>
698
                        table->val[2*i] |= FOX_times_alpha (tmp) << 8;
699
700
                        table->val[2*i] |= FOX_times_alpha (FOX_times_alpha (tmp));
701
                        table->val[2*i+1] = FOX_div_alpha (tmp) << 24;</pre>
                        table->val[2*i+1] |= FOX_div_alpha (FOX_div_alpha (tmp)) << 16;</pre>
702
703
                        table->val[2*i+1] |= tmp << 8;
704
                        table->val[2*i+1] |= (FOX_times_alpha (tmp) ^ tmp);
705
706
                    break;
707
708
                case FOX128_TABLE_SIGMA8_MU8_ID3:
709
                    for (i = 0; i < 256; i++) {
710
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
                        table->val[2*i] = tmp << 24;
711
                        table->val[2*i] |= FOX_times_alpha (tmp) << 16;
712
```

```
713
                        table->val[2*i] |= FOX_times_alpha (FOX_times_alpha (tmp)) << 8;</pre>
714
                        table->val[2*i] |= FOX_div_alpha (tmp);
715
                        table->val[2*i+1] = FOX_div_alpha (FOX_div_alpha (tmp)) << 24;</pre>
716
                        table->val[2*i+1] |= tmp << 16;
717
                        table->val[2*i+1] |= (FOX_times_alpha (tmp) ^ tmp) << 8;</pre>
                        table->val[2*i+1] |= (FOX_div_alpha (tmp ^ FOX_div_alpha (tmp)));
718
719
720
                    break:
721
722
               case FOX128_TABLE_SIGMA8_MU8_ID4:
723
                    for (i = 0; i < 256; i++) {
724
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
                        table->val[2*i] = tmp << 24;
725
                        table->val[2*i] |= FOX_times_alpha (FOX_times_alpha (tmp)) << 16;</pre>
726
727
                        table->val[2*i] |= FOX_div_alpha (tmp) << 8;
                        table->val[2*i] |= FOX_div_alpha (FOX_div_alpha (tmp));
728
729
                        table \rightarrow val[2*i+1] = tmp << 24;
                        table->val[2*i+1] |= (FOX_times_alpha (tmp) ^ tmp) << 16;</pre>
730
                        table->val[2*i+1] |= (FOX_div_alpha (tmp ^ FOX_div_alpha (tmp))) << 8;
731
732
                        table->val[2*i+1] |= FOX_times_alpha (tmp);
733
734
                    break:
735
736
                case FOX128_TABLE_SIGMA8_MU8_ID5:
737
                    for (i = 0; i < 256; i++) {
738
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
                        table->val[2*i] = tmp << 24;
739
                        table->val[2*i] |= FOX_div_alpha (tmp) << 16;</pre>
740
741
                        table->val[2*i] |= FOX_div_alpha (FOX_div_alpha (tmp)) << 8;</pre>
742
                        table->val[2*i] |= tmp;
743
                        table->val[2*i+1] = (FOX_times_alpha (tmp) ^ tmp) << 24;</pre>
744
                        table->val[2*i+1] |= (FOX_div_alpha (tmp ^ FOX_div_alpha (tmp))) << 16;</pre>
745
                        746
                        table->val[2*i+1] |= FOX_times_alpha (FOX_times_alpha (tmp));
747
                    }
748
                    break;
749
750
                case FOX128_TABLE_SIGMA8_MU8_ID6:
751
                    for (i = 0; i < 256; i++) \{
752
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
753
                        table - val[2*i] = tmp << 24;
                        table->val[2*i] |= FOX_div_alpha (FOX_div_alpha (tmp)) << 16;</pre>
754
755
                        table->val[2*i] |= tmp << 8;
                        table->val[2*i] |= (FOX_times_alpha (tmp) ^ tmp);
756
                        table->val[2*i+1] = (FOX_div_alpha (tmp ^ FOX_div_alpha (tmp))) << 24;
757
758
                        table->val[2*i+1] |= FOX_times_alpha (tmp) << 16;</pre>
759
                        table->val[2*i+1] |= FOX_times_alpha (FOX_times_alpha (tmp)) << 8;
760
                        table->val[2*i+1] |= FOX_div_alpha (tmp);
761
                    7
762
                    break;
763
764
                case FOX128_TABLE_SIGMA8_MU8_ID7:
765
                    for (i = 0; i < 256; i++) {
766
                        tmp = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
767
                        table->val[2*i] = (FOX_times_alpha (tmp) ^ tmp) << 24;</pre>
                        table->val[2*i] |= tmp << 16;
768
                        table->val[2*i] |= tmp << 8;
769
770
                        table->val[2*i] |= tmp;
771
                        table->val[2*i+1] = tmp << 24;
772
                        table->val[2*i+1] |= tmp << 16;
                        table->val[2*i+1] |= tmp << 8;
773
                        table->val[2*i+1] |= tmp;
774
775
776
                    break:
777
778
                case FOX64_TABLE_SIGMA4_ID0:
779
               case FOX128_TABLE_SIGMA8_ID0:
780
                    for (i = 0; i < 256; i++) {
781
                        table->val[i] = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3) << 24;</pre>
782
```

```
783
                    break;
784
                case FOX64_TABLE_SIGMA4_ID1:
785
786
                case FOX128_TABLE_SIGMA8_ID1:
787
                    for (i = 0; i < 256; i++) {
                        table->val[i] = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3) << 16;</pre>
788
789
790
                    break:
791
792
                case FOX64_TABLE_SIGMA4_ID2:
793
                case FOX128_TABLE_SIGMA8_ID2:
794
                    for (i = 0; i < 256; i++) {
795
                        table->val[i] = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3) << 8;</pre>
796
                    }
797
                    break;
798
799
                case FOX64_TABLE_SIGMA4_ID3:
800
                case FOX128_TABLE_SIGMA8_ID3:
801
                    for (i = 0; i < 256; i++) {
802
                        table->val[i] = FOX_eval_sbox (i, FOX_S1, FOX_S2, FOX_S3);
803
804
                    break;
805
806
                default:
                    fprintf (stderr, FOX_ERROR_UNKNOWN_TABLE_ID);
807
808
                    goto error_label;
809
810
811
           *ptr = table;
812
813
           return 0;
814
815
        error_label:
816
            fprintf (stderr, FOX_ERROR_TABLE_INIT);
817
           FOX_clean_table (table);
818
819
           return -1;
820
       }
821
822
       void FOX_clean_table (FOX_table table)
823
824
            if (table != NULL) {
825
                if (table->val != NULL) {
826
                    free (memset (table->val, 0x00, table->size_bytes));
827
828
                free (memset (table, 0x00, sizeof (FOX_table_)));
829
830
       }
831
832
       uint32 FOX_eval_sbox (const uint32 x, const uint8 *s1,
                              const uint8 *s2, const uint8 *s3)
833
834
       {
835
            uint8 l, r, ll, lr, state;
836
837
            assert ( (x <= 0xFF) && (s1 != NULL) && (s2 != NULL) && (s3 != NULL) );
838
839
           1 = (x \& 0xF0) >> 4;
840
           r = (x \& 0x0F);
841
842
            /* Round 1
                                                                                        */
843
844
           state = s1[l ^ r];
845
            1 ^= state;
           r ^= state;
846
847
848
           11 = (1 \& OxC) >> 2;
849
           lr = (1 \& 0x3);
850
851
            1 = (lr << 2) | (l1 ^ lr);</pre>
852
```

```
853
         /* Stage 2
                                                                       */
854
         state = s2[1 ^ r];
855
856
         1 ^= state;
857
         r ^= state;
858
859
         11 = (1 \& 0xC) >> 2;
860
         lr = (1 \& 0x3);
861
862
         1 = (1r << 2) | (11 ^ 1r);
863
864
         /* Stage 3 (without orthomorphism)
865
         state = s3[1 ^ r];
866
867
         1 ^= state;
         r ^= state;
868
869
870
         /* Saving of the value */
871
872
         return (uint32)((1 << 4) | r);
873
  File fox64.h
      /* FOX project / Reference implementation v1.2
 3
      /* Pascal Junod <pascal@junod.info>
      /*
 4
      5
 6
      #ifndef _FOX64_H_
 8
      #define _FOX64_H_
 9
 10
      #include "fox_portable.h"
 11
      #include "fox_ctx.h"
12
 13
      #define FOX64_MODE_ENCRYPT
 14
      #define FOX64_MODE_DECRYPT
                                   0x1
15
      #define FOX64_NUMBER_ROUNDS_MIN
16
      #define FOX64_NUMBER_ROUNDS_GENERIC
17
18
19
      #define FOX64_encrypt(p, k, ctx) FOX64_process((p), (k), (ctx), FOX64_MODE_ENCRYPT)
      #define F0X64_decrypt(c, k, ctx) F0X64_process((c), (k), (ctx), F0X64_MODE_DECRYPT)
 20
 21
 22
      extern int F0X64_process (uint32 *, const F0X_key, const F0X64_ctx, const F0X_mode);
 23
 24
      void FOX_lmor64 (uint32 *, const uint32 *, const FOX64_ctx);
      void FOX_lmid64 (uint32 *, const uint32 *, const FOX64_ctx);
 25
 26
      void FOX_lmio64 (uint32 *, const uint32 *, const FOX64_ctx);
      void FOX_f32 (uint32 *, const uint32 *, const FOX64_ctx);
 27
 28
 29
      #endif /* _FOX64_H_
  File fox64.c
      /* FOX project / Reference implementation v1.2
 3
      /* Pascal Junod <pascal@junod.info>
      5
      #include <assert.h>
 8
      #include <stdlib.h>
 9
      #include <stdio.h>
 10
 11
      #include "fox_portable.h"
 12
      #include "fox_error.h"
```

```
13
      #include "fox_ctx.h"
14
      #include "fox64.h"
15
16
      int F0X64_process (uint32 *data,
17
                           const FOX_key k,
18
                           const FOX64_ctx ctx,
19
                           const FOX_mode mode)
20
      {
21
           int r;
           uint32 input[2];
22
23
           assert (data != NULL);
24
25
           assert (k != NULL);
           assert (ctx != NULL);
26
27
           assert (k->rounds >= FOX64_NUMBER_ROUNDS_MIN);
28
29
           input[0] = data[0];
input[1] = data[1];
30
31
32
33
           switch (mode) {
34
35
               case FOX64_MODE_ENCRYPT:
36
                   for (r = 0; r < k \rightarrow rounds - 1; r++) {
37
                        FOX_lmor64 (input, k\rightarrow exp_key + (r * 2), ctx);
38
39
                   FOX_1mid64 (input, k->exp_key + (k->rounds-1) * 2, ctx);
40
                   break;
41
               case FOX64_MODE_DECRYPT:
42
43
                   for (r = k->rounds - 1; r > 0; r--) {
44
                        FOX_lmio64 (input, k\rightarrow exp_key + (r * 2), ctx);
45
46
                   FOX_lmid64 (input, k->exp_key, ctx);
47
                   break:
48
49
               default:
50
                   fprintf (stderr, FOX_ERROR_UNKNOWN_MODE);
51
                   return -1;
52
          }
53
54
           data[0] = input[0];
           data[1] = input[1];
55
56
57
           return 0;
      }
58
59
      void FOX_lmor64 (uint32 *data,
60
                         const uint32 *key,
61
62
                         const FOX64_ctx ctx)
63
64
           uint32 tmp[2], f;
65
66
           tmp[0] = data[0];
67
           tmp[1] = data[1];
68
           f = tmp[0] ^ tmp[1];
69
           FOX_f32 (&f, key, ctx);
70
           tmp[0] ^= f;
tmp[1] ^= f;
71
72
73
           FOX_or (tmp);
74
75
           data[0] = tmp[0];
76
           data[1] = tmp[1];
77
      }
78
79
      void FOX_lmid64 (uint32 *data,
80
                         const uint32 *key,
81
                         const FOX64_ctx ctx)
82
      {
```

```
83
           uint32 tmp[2], f;
 84
           tmp[0] = data[0];
 85
 86
           tmp[1] = data[1];
 87
           f = tmp[0] ^ tmp[1];
 88
           FOX_f32 (&f, key, ctx);
 89
           tmp[0] ^= f;
tmp[1] ^= f;
 90
 91
 92
 93
           data[0] = tmp[0];
 94
           data[1] = tmp[1];
       }
 95
 96
 97
       void FOX_lmio64 (uint32 *data,
                        const uint32 *key,
 98
 99
                        const FOX64_ctx ctx)
100
       {
101
           uint32 tmp[2], f;
102
           tmp[0] = data[0];
tmp[1] = data[1];
103
104
105
           f = tmp[0] ^ tmp[1];
FOX_f32 (&f, key, ctx);
106
107
108
           tmp[0] ^= f;
109
           tmp[1] ^= f;
110
           FOX_io (tmp);
111
           data[0] = tmp[0];
112
113
           data[1] = tmp[1];
114
115
116
       void FOX_f32 (uint32 *data,
                     const uint32 *key,
117
118
                     const FOX64_ctx ctx)
119
120
           uint32 i, o;
121
122
           i = *data;
123
124
           i ^= key[0];
125
126
           o = ctx->sigma4_mu4_0->val[(i & 0xFF000000) >> 24];
127
           o ^= ctx->sigma4_mu4_1->val[(i & 0x00FF0000) >> 16];
           o ^= ctx->sigma4_mu4_2->val[(i & 0x0000FF00) >> 8];
128
129
           o ^= ctx->sigma4_mu4_3->val[(i & 0x000000FF)];
130
131
           o ^= key[1];
132
           i = ctx->sigma4_0->val[(o & 0xFF000000) >> 24];
133
134
           i ^= ctx->sigma4_1->val[(o & 0x00FF0000) >> 16];
135
           i ^= ctx->sigma4_2->val[(o & 0x0000FF00) >> 8];
           i ^= ctx->sigma4_3->val[(o & 0x000000FF)];
136
137
           *data = i ^ key[0];
138
       }
139
   File fox128.h
       /* FOX project / Reference implementation v1.2
                                                                                      */
  3
       /* Pascal Junod <pascal@junod.info>
                                                                                      */
  4
  5
       6
       #ifndef _FOX128_H_
#define _FOX128_H_
  7
  8
```

```
10
      #include "fox_portable.h"
11
      #include "fox_ctx.h"
12
13
      #define FOX128_MODE_ENCRYPT
                                             0x0
14
      #define FOX128_MODE_DECRYPT
                                             0x1
15
      #define FOX128_NUMBER_ROUNDS_MIN
                                              12
16
      #define FOX128_NUMBER_ROUNDS_GENERIC
17
                                              16
18
      \texttt{\#define FOX128\_encrypt(p, k, ctx) FOX128\_process((p), (k), (ctx), FOX128\_MODE\_ENCRYPT)}
19
20
      #define FOX128_decrypt(c, k, ctx) FOX128_process((c), (k), (ctx), FOX128_MODE_DECRYPT)
21
22
      extern int FOX128_process (uint32 *, const FOX_key, const FOX128_ctx, const FOX_mode);
23
24
      void FOX_elmor128 (uint32 *, const uint32 *, const FOX128_ctx);
25
      void FOX_elmid128 (uint32 *, const uint32 *, const FOX128_ctx);
26
      void FOX_elmio128 (uint32 *, const uint32 *, const FOX128_ctx);
27
28
      void FOX_f64 (uint32 *, const uint32 *, const FOX128_ctx);
29
      #endif /* _FOX128_H_
                                                                                  */
  File fox128.c
      /* FOX project / Reference implementation v1.2
      /* Pascal Junod <pascal@junod.info>
                                                                                  */
      /*
 4
      /***********************
 5
      #include <assert.h>
 8
      #include <stdlib.h>
      #include <stdio.h>
 9
10
11
      #include "fox_portable.h"
      #include "fox_error.h"
12
13
      #include "fox_ctx.h"
14
     #include "fox128.h"
15
     int F0X128_process (uint32 *data,
16
17
                         const FOX_key k,
18
                          const FOX128_ctx ctx,
19
                         const FOX_mode mode)
20
     {
21
          int r;
22
          uint32 input[4];
23
24
          assert (data != NULL);
25
          assert (k != NULL);
26
          assert (ctx != NULL);
27
          assert (k->rounds >= FOX128_NUMBER_ROUNDS_MIN);
28
29
          input[0] = data[0];
input[1] = data[1];
30
31
          input[2] = data[2];
33
          input[3] = data[3];
34
35
          switch (mode) {
36
37
              case FOX128_MODE_ENCRYPT:
38
                  for (r = 0; r < k \rightarrow rounds - 1; r++) {
                     FOX_elmor128 (input, k->exp_key + (r * 4), ctx);
39
40
                  FOX_elmid128 (input, k\rightarrow exp_key + (k\rightarrow rounds - 1) * 4, ctx);
41
42
                      break;
43
              case FOX128_MODE_DECRYPT:
44
45
                  for (r = k-) rounds - 1; r > 0; r--) {
```

```
46
                          FOX_elmio128 (input, k\rightarrow \exp_k + (r * 4), ctx);
 47
                     FOX_elmid128 (input, k->exp_key, ctx);
 48
 49
                     break;
 50
 51
                 default:
 52
                     fprintf (stderr, FOX_ERROR_UNKNOWN_MODE);
 53
                     return -1;
 54
 55
 56
            data[0] = input[0];
            data[1] = input[1];
 57
            data[2] = input[2];
 58
            data[3] = input[3];
 59
 60
 61
            return 0;
 62
        }
 63
 64
        void FOX_elmor128 (uint32 *data,
 65
                             const uint32 *key,
 66
                             const FOX128_ctx ctx)
 67
        {
 68
            uint32 tmp[4], f[2];
 69
 70
            tmp[0] = data[0];
            tmp[1] = data[1];
 71
            tmp[2] = data[2];
 72
 73
            tmp[3] = data[3];
 74
            f[0] = tmp[0] ^ tmp[1];
f[1] = tmp[2] ^ tmp[3];
 75
 76
 77
 78
            FOX_f64 (f, key, ctx);
 79
            tmp[0] ^= f[0];
 80
            tmp[1] ^= f[0];
 81
            tmp[2] ^= f[1];
tmp[3] ^= f[1];
 82
 83
 84
 85
            FOX_or (tmp);
            FOX_or (tmp + 2);
 86
 87
 88
            data[0] = tmp[0];
 89
            data[1] = tmp[1];
 90
            data[2] = tmp[2];
 91
            data[3] = tmp[3];
 92
 93
 94
        void FOX_elmid128 (uint32 *data,
 95
                             const uint32 *key,
 96
                             const FOX128_ctx ctx)
 97
        {
 98
            uint32 tmp[4], f[2];
 99
100
            tmp[0] = data[0];
101
            tmp[1] = data[1];
            tmp[2] = data[2];
102
103
            tmp[3] = data[3];
104
            f[0] = tmp[0] ^ tmp[1];
f[1] = tmp[2] ^ tmp[3];
105
106
107
108
            FOX_f64 (f, key, ctx);
109
            tmp[0] ^= f[0];
110
            tmp[1] ^= f[0];
tmp[2] ^= f[1];
111
112
            tmp[3] ^= f[1];
113
114
115
            data[0] = tmp[0];
```

```
116
            data[1] = tmp[1];
117
           data[2] = tmp[2];
data[3] = tmp[3];
118
119
120
       void FOX_elmio128 (uint32 *data,
121
122
                           const uint32 *key,
123
                           const FOX128_ctx ctx)
124
125
            uint32 tmp[4], f[2];
126
127
            tmp[0] = data[0];
            tmp[1] = data[1];
128
129
            tmp[2] = data[2];
130
            tmp[3] = data[3];
131
           f[0] = tmp[0] ^ tmp[1];
132
           f[1] = tmp[2] ^ tmp[3];
133
134
135
           FOX_f64 (f, key, ctx);
136
           tmp[0] ^= f[0];
137
138
            tmp[1] ^= f[0];
            tmp[2] ^= f[1];
139
            tmp[3] ^= f[1];
140
141
142
           FOX_io (tmp);
143
           FOX_io (tmp + 2);
144
145
           data[0] = tmp[0];
146
            data[1] = tmp[1];
           data[2] = tmp[2];
147
148
           data[3] = tmp[3];
149
150
151
       void FOX_f64 (uint32 *data,
152
                      const uint32 *key,
153
                      const FOX128_ctx ctx)
154
155
           uint32 i[2], o[2];
156
157
            i[0] = data[0];
           i[1] = data[1];
158
159
            i[0] ^= key[0];
160
           i[1] ^= key[1];
161
162
163
            o[0] = ctx->sigma8_mu8_0->val[(i[0] & 0xFF000000) >> 23];
164
            o[1] = ctx->sigma8_mu8_0->val[((i[0] & 0xFF000000) >> 23) + 1];
165
            o[0] ^= ctx->sigma8_mu8_1->val[(i[0] & 0x00FF0000) >> 15];
           o[1] ^= ctx->sigma8_mu8_1->val[((i[0] & 0x00FF0000) >> 15) + 1];
166
167
            o[0] ^= ctx->sigma8_mu8_2->val[(i[0] & 0x0000FF00) >> 7];
168
            o[1] ^= ctx->sigma8_mu8_2->val[((i[0] & 0x0000FF00) >> 7) + 1];
           o[0] ^= ctx->sigma8_mu8_3->val[(i[0] & 0x000000FF) << 1];
169
170
            o[1] ^= ctx->sigma8_mu8_3->val[((i[0] & 0x000000FF) << 1)+ 1];
171
172
           o[0] ^= ctx->sigma8_mu8_4->val[(i[1] & 0xFF000000) >> 23];
173
            o[1] ^= ctx->sigma8_mu8_4->val[((i[1] & 0xFF000000) >> 23) + 1];
174
            o[0] ^= ctx->sigma8_mu8_5->val[(i[1] & 0x00FF0000) >> 15];
175
            o[1] ^= ctx->sigma8_mu8_5->val[((i[1] & 0x00FF0000) >> 15) + 1];
176
            o[0] ^= ctx->sigma8_mu8_6->val[(i[1] & 0x0000FF00) >> 7];
177
           o[1] ^= ctx->sigma8_mu8_6->val[((i[1] & 0x0000FF00) >> 7) + 1];
178
            o[0] ^= ctx->sigma8_mu8_7->val[(i[1] & 0x000000FF) << 1];
           o[1] ^= ctx->sigma8_mu8_7->val[((i[1] & 0x000000FF) << 1) + 1];
179
180
181
            o[0] ^= key[2];
182
           o[1] ^= key[3];
183
184
            i[0] = ctx->sigma8_0->val[(o[0] & 0xFF000000) >> 24];
            i[0] ^= ctx->sigma8_1->val[(o[0] & 0x00FF0000) >> 16];
185
```

```
186
          i[0] ^= ctx->sigma8_2->val[(o[0] & 0x0000FF00) >> 8];
187
          i[0] ^= ctx->sigma8_3->val[(o[0] & 0x000000FF)];
188
189
          i[1] = ctx->sigma8_0->val[(o[1] & 0xFF000000) >> 24];
190
          i[1] ^= ctx->sigma8_1->val[(o[1] & 0x00FF0000) >> 16];
          i[1] ^= ctx->sigma8_2->val[(o[1] & 0x0000FF00) >> 8];
191
192
          i[1] ^= ctx->sigma8_3->val[(o[1] & 0x000000FF)];
193
          data[0] = i[0] ^ key[0];
194
          data[1] = i[1] ^ key[1];
195
196
  File fox_util.h
      /* FOX project / Reference implementation v1.2
 3
      /* Pascal Junod <pascal@junod.info>
                                                                           */
 5
      6
      #ifndef _FOX_UTIL_H_
 8
      #define _FOX_UTIL_H_
 9
      #include "fox_portable.h"
10
11
12
      int fox64_64_16_test (const uint8 *p, const uint8 *k);
13
      int fox64_128_16_test (const uint8 *p, const uint8 *k);
      int fox64_192_16_test (const uint8 *p, const uint8 *k);
14
15
      int fox64_256_16_test (const uint8 *p, const uint8 *k);
16
17
      int fox128_64_16_test (const uint8 *p, const uint8 *k);
18
      int fox128_128_16_test (const uint8 *p, const uint8 *k);
      int fox128_192_16_test (const uint8 *p, const uint8 *k);
19
20
      int fox128_256_16_test (const uint8 *p, const uint8 *k);
21
22
      #endif /* _FOX_UTIL_H_
                                                                           */
  File fox_util.c
      /*****************************
      /* FOX project / Reference implementation v1.2
                                                                           */
 3
      /* Pascal Junod <pascal@junod.info>
                                                                           */
 4
      6
      #include <stdio.h>
 8
      #include <stdlib.h>
 9
      #include <string.h>
10
      #include "fox_portable.h"
11
      #include "fox_error.h"
12
      #include "fox64.h"
#include "fox128.h"
13
14
      #include "fox_ctx.h"
15
      #include "fox_util.h"
16
17
18
      const uint8 p64[8] = \{0x01, 0x23, 0x45, 0x67,
19
                           0x89, 0xAB, 0xCD, 0xEF };
20
21
      const uint8 p128[16] = \{0x01, 0x23, 0x45, 0x67,
22
                            0x89, 0xAB, 0xCD, 0xEF,
23
                            OxFE, OxDC, OxBA, Ox98,
24
                            0x76, 0x54, 0x32, 0x10 };
25
26
      const uint8 k[32] =
                           \{0x00, 0x11, 0x22, 0x33,
27
                           0x44, 0x55, 0x66, 0x77,
28
                            0x88, 0x99, 0xAA, 0xBB,
```

OxCC, OxDD, OxEE, OxFF,

29

```
30
                               OxFF, OxEE, OxDD, OxCC,
31
                               0xBB, 0xAA, 0x99, 0x88,
32
                               0x77, 0x66, 0x55, 0x44,
33
                               0x33, 0x22, 0x11, 0x00 };
34
35
      int main ()
37
          int return_value = EXIT_SUCCESS;
38
39
          fprintf (stdout, "\n\nFOX test vectors generator v1.2");
40
          fprintf (stdout, "\n----\n\n");
41
42
           /* FOX64 test vectors
                                                                                       */
          if (fox64_64_16_test (p64, k)) {
43
44
               fprintf (stdout, "\nFatal error_exiting!\n");
              return_value = EXIT_FAILURE;
45
46
               goto error_label;
47
48
          if (fox64_128_16_test (p64, k)) {
               fprintf (stdout, "\nFatal error_exiting!\n");
49
50
              return_value = EXIT_FAILURE;
51
              goto error_label;
52
          if (fox64_192_16_test (p64, k)) {
   fprintf (stdout, "\nFatal error_exiting!\n");
53
54
              return_value = EXIT_FAILURE;
55
              goto error_label;
56
          }
57
58
          if (fox64_256_16_test (p64, k)) {
              fprintf (stdout, "\nFatal error_exiting!\n");
59
60
               return_value = EXIT_FAILURE;
61
              goto error_label;
          }
62
63
          /* FOX128 test vectors
                                                                                       */
64
65
          if (fox128_64_16_test (p128, k)) {
               fprintf (stdout, "\nFatal error_exiting!\n");
66
67
              return_value = EXIT_FAILURE;
68
              goto error_label;
69
70
          if (fox128_128_16_test (p128, k)) {
71
              fprintf (stdout, "\nFatal error_exiting!\n");
              return_value = EXIT_FAILURE;
72
73
              goto error_label;
74
75
          if (fox128_192_16_test (p128, k)) {
               fprintf (stdout, "\nFatal error_exiting!\n");
76
              return_value = EXIT_FAILURE;
77
78
              goto error_label;
79
          if (fox128_256_16_test (p128, k)) {
80
               fprintf \ (stdout, \ "\nFatal \ error\_exiting!\n");
81
82
              return_value = EXIT_FAILURE;
83
              goto error_label;
84
          }
85
86
87
       error_label:
88
89
          return return_value;
90
91
92
      int fox64_64_16_test (const uint8 *p, const uint8 *k)
93
94
          FOX64_ctx ctx;
95
          FOX_key key;
          uint8 c[8];
96
97
          uint32 c32[2];
98
          int i, return_value = EXIT_SUCCESS;
99
```

```
100
           if (FOX64_init_ctx (&ctx)) {
                fprintf (stderr, "\nFatal error...exiting!\n");
101
               return_value = EXIT_FAILURE;
102
103
                goto error_label;
104
           fprintf (stdout, "\nFOX64/16/64 key
                                                          : ");
105
106
           for (i = 0; i < 2; i++) {
               fprintf (stdout, "%08X ", U8T032_BIG (k + 4*i));
107
108
           fprintf (stdout, "nF0X64/16/64 message
109
110
           for (i = 0; i < 2; i++) {
                fprintf (stdout, "%08X ", U8T032_BIG (p + 4*i));
111
112
            if (FOX64_init_key (&key, ctx, k, 64, 16)) {
113
114
                fprintf (stderr, "\nFatal error...exiting!\n");
               return_value = EXIT_FAILURE;
115
116
                goto error_label;
117
118
           memcpy (c, p, 8);
119
            c32[0] = U8T032_BIG(c);
120
            c32[1] = U8T032_BIG (c + 4);
           FOX64_encrypt (c32, key, ctx);
121
122
            fprintf (stdout, "\nF0X64/16/64 ciphertext : ");
123
           for (i = 0; i < 2; i++) {
                fprintf (stdout, "%08X ", c32[i]);
124
125
126
           FOX64_decrypt (c32, key, ctx);
            fprintf (stdout, "\nFOX64/16/64 message
127
           for (i = 0; i < 2; i++) {
128
                fprintf (stdout, "%08X ", c32[i]);
129
130
131
           fprintf (stdout, "\n\n");
132
133
        error_label:
134
           FOX64_clean_ctx (ctx);
135
           FOX64_clean_key (key);
136
137
           return return_value;
138
       }
139
140
       int fox64_128_16_test (const uint8 *p, const uint8 *k)
141
           FOX64_ctx ctx;
142
143
           FOX_key key;
144
           uint8 c[8];
145
           uint32 c32[2];
146
           int i, return_value = EXIT_SUCCESS;
147
148
            if (FOX64_init_ctx (&ctx)) {
149
                fprintf (stderr, "\nFatal error...exiting!\n");
               return_value = EXIT_FAILURE;
150
151
               goto error_label;
152
           fprintf (stdout, "\nFOX64/16/128 key
                                                           : "):
153
154
           for (i = 0; i < 4; i++) {
                fprintf (stdout, "%08X ", U8T032_BIG (k + 4*i));
155
156
           fprintf (stdout, "\nF0X64/16/128 message
157
           for (i = 0; i < 2; i++) {
158
               fprintf (stdout, "%08X ", U8T032_BIG (p + 4*i));
159
160
161
           if (FOX64_init_key (&key, ctx, k, 128, 16)) {
162
                fprintf (stderr, "\nFatal error...exiting!\n");
               return_value = EXIT_FAILURE;
163
164
               goto error_label;
165
166
           memcpy (c, p, 8);
167
            c32[0] = U8T032_BIG (c);
            c32[1] = U8T032_BIG (c + 4);
168
169
           FOX64_encrypt (c32, key, ctx);
```

```
170
           fprintf (stdout, "\nFOX64/16/128 ciphertext : ");
           for (i = 0; i < 2; i++) {
171
               fprintf (stdout, "%08X ", c32[i]);
172
173
174
           FOX64_decrypt (c32, key, ctx);
           fprintf (stdout, "\nF0X64/16/128 message
175
176
           for (i = 0; i < 2; i++) {
               fprintf (stdout, "%08X ", c32[i]);
177
178
           fprintf (stdout, "\n");
179
180
181
        error_label:
182
           FOX64_clean_ctx (ctx);
183
           FOX64_clean_key (key);
184
185
           return return_value;
186
       }
187
       int fox64_192_16_test (const uint8 *p, const uint8 *k)
188
189
190
           FOX64_ctx ctx;
191
           FOX_key key;
192
           uint8 c[8];
193
           uint32 c32[2];
194
           int i, return_value = EXIT_SUCCESS;
195
           if (FOX64_init_ctx (&ctx)) {
196
197
                fprintf (stderr, "\nFatal error...exiting!\n");
               return_value = EXIT_FAILURE;
198
199
                goto error_label;
200
201
           fprintf (stdout, "\nFOX64/16/192 key
                                                          : ");
202
           for (i = 0; i < 6; i++) {
203
               fprintf (stdout, "%08X ", U8T032_BIG (k + 4*i));
204
205
           fprintf (stdout, "\nFOX64/16/192 message
206
           for (i = 0; i < 2; i++) {
207
               fprintf (stdout, "\%08X ", U8T032_BIG (p + 4*i));
208
209
           if (FOX64_init_key (&key, ctx, k, 192, 16)) {
               fprintf (stderr, "\nFatal error...exiting!\n");
210
211
               return_value = EXIT_FAILURE;
212
               goto error_label;
213
214
           memcpy (c, p, 8);
215
           c32[0] = U8T032_BIG (c);
216
            c32[1] = U8T032_BIG (c + 4);
           FOX64_encrypt (c32, key, ctx);
217
           fprintf (stdout, "\nFOX64/16/192 ciphertext : ");
218
219
           for (i = 0; i < 2; i++) {
               fprintf (stdout, "%08X ", c32[i]);
220
221
222
           FOX64_decrypt (c32, key, ctx);
           fprintf (stdout, "\nFOX64/16/192 message
223
                                                       : ");
224
           for (i = 0; i < 2; i++) {
225
                fprintf (stdout, "%08X ", c32[i]);
226
227
           fprintf (stdout, "\n\n");
228
229
        error_label:
230
           FOX64_clean_ctx (ctx);
231
           FOX64_clean_key (key);
232
233
           return return value:
       }
234
235
       int fox64_256_16_test (const uint8 *p, const uint8 *k)
236
237
           FOX64_ctx ctx;
238
           FOX_key key;
239
           uint8 c[8];
```

```
240
           uint32 c32[2];
241
           int i, return_value = EXIT_SUCCESS;
242
243
           if (FOX64_init_ctx (&ctx)) {
               fprintf (stderr, "\nFatal error...exiting!\n");
244
               return_value = EXIT_FAILURE;
245
246
               goto error_label;
247
           }
           fprintf (stdout, "\nFOX64/16/256 key
248
                                                           : ");
249
           for (i = 0; i < 8; i++) {
               fprintf (stdout, "%08X ", U8T032_BIG (k + 4*i));
250
251
252
           fprintf (stdout, "\nF0X64/16/256 message
253
           for (i = 0; i < 2; i++) {
254
               fprintf (stdout, "%08X ", U8T032_BIG (p + 4*i));
255
256
           if (FOX64_init_key (&key, ctx, k, 256, 16)) {
257
               fprintf (stderr, "\nFatal error...exiting!\n");
               return_value = EXIT_FAILURE;
258
259
               goto error_label;
260
261
           memcpy (c, p, 8);
262
           c32[0] = U8T032_BIG (c);
263
           c32[1] = U8T032_BIG (c + 4);
264
           FOX64_encrypt (c32, key, ctx);
           fprintf (stdout, "\nFOX64/16/256 ciphertext : ");
265
266
           for (i = 0; i < 2; i++) {
               fprintf (stdout, "%08% ", c32[i]);
267
268
269
           FOX64_decrypt (c32, key, ctx);
270
           fprintf (stdout, "\nFOX64/16/256 message
           for (i = 0; i < 2; i++) {
271
               fprintf (stdout, "%08X ", c32[i]);
272
273
274
           fprintf (stdout, "\n\n");
275
276
        error_label:
277
           FOX64_clean_ctx (ctx);
278
           FOX64_clean_key (key);
279
280
           return return_value;
281
282
283
       int fox128_64_16_test (const uint8 *p, const uint8 *k)
284
285
           FOX128_ctx ctx;
286
           FOX_key key;
287
           uint8 c[16];
288
           uint32 c32[4];
289
           int i, return_value = EXIT_SUCCESS;
290
291
           if (FOX128_init_ctx (&ctx)) {
292
               fprintf (stderr, "\nFatal error...exiting!\n");
               return_value = EXIT_FAILURE;
293
294
               goto error_label;
295
296
           fprintf (stdout, "\nFOX128/16/64 key
                                                           : ");
297
           for (i = 0; i < 2; i++) {
               fprintf (stdout, "%08X ", U8T032_BIG (k + 4*i));
298
299
300
           fprintf (stdout, "\nFOX128/16/64 message
301
           for (i = 0; i < 4; i++) {
               fprintf (stdout, "\%08X ", U8T032_BIG (p + 4*i));
302
303
304
           if (FOX128_init_key (&key, ctx, k, 64, 16)) {
305
               fprintf (stderr, "\nFatal error...exiting!\n");
306
               return_value = EXIT_FAILURE;
307
               goto error_label;
308
           memcpy (c, p, 16);
309
```

```
310
           c32[0] = U8T032_BIG (c);
311
           c32[1] = U8T032_BIG (c + 4);
           c32[2] = U8T032_BIG (c + 8);
312
313
            c32[3] = U8T032_BIG (c + 12);
           FOX128_encrypt (c32, key, ctx);
314
           fprintf (stdout, "\nFOX128/16/64 ciphertext : ");
315
           for (i = 0; i < 4; i++) {
316
               fprintf (stdout, "%08X ", c32[i]);
317
318
319
           FOX128_decrypt (c32, key, ctx);
           fprintf (stdout, "\nFOX128/16/64 message
320
                                                        : ");
321
           for (i = 0; i < 4; i++) {
               fprintf (stdout, "%08X ", c32[i]);
322
323
324
           fprintf (stdout, "\n');
325
326
        error_label:
327
           FOX128_clean_ctx (ctx);
328
           FOX128_clean_key (key);
329
330
           return return_value;
331
       }
332
       int fox128_128_16_test (const uint8 *p, const uint8 *k)
333
334
335
           FOX128_ctx ctx;
336
           FOX_key key;
337
           uint8 c[16];
338
           uint32 c32[4];
           int i, return_value = EXIT_SUCCESS;
339
340
341
            if (FOX128_init_ctx (&ctx)) {
                fprintf (stderr, "\nFatal error...exiting!\n");
342
343
               return_value = EXIT_FAILURE;
344
               goto error_label;
345
           }
346
           fprintf (stdout, "\nFOX128/16/128 key
                                                            : ");
347
           for (i = 0; i < 4; i++) \{
348
               fprintf (stdout, "%08X ", U8T032_BIG (k + 4*i));
349
           fprintf (stdout, "\nFOX128/16/128 message
350
                                                          : ");
351
           for (i = 0; i < 4; i++) {
               fprintf (stdout, "%08X ", U8T032_BIG (p + 4*i));
352
353
354
            if (FOX128_init_key (&key, ctx, k, 128, 16)) {
355
               fprintf (stderr, "\nFatal error...exiting!\n");
356
                return_value = EXIT_FAILURE;
357
               goto error_label;
358
           }
           memcpy (c, p, 16);
c32[0] = U8T032_BIG (c);
359
360
361
            c32[1] = U8T032_BIG (c + 4);
362
            c32[2] = U8T032_BIG (c + 8);
           c32[3] = U8T032_BIG (c + 12);
363
364
           FOX128_encrypt (c32, key, ctx);
365
           fprintf (stdout, "\nFOX128/16/128 ciphertext : ");
366
           for (i = 0; i < 4; i++) {
367
               fprintf (stdout, "%08X ", c32[i]);
368
369
           FOX128_decrypt (c32, key, ctx);
370
           fprintf (stdout, "\nFOX128/16/128 message
371
           for (i = 0; i < 4; i++) {
372
                fprintf (stdout, "%08X ", c32[i]);
373
374
           fprintf (stdout, "\n\");
375
376
        error_label:
377
           FOX128_clean_ctx (ctx);
378
            FOX128_clean_key (key);
379
```

```
380
           return return_value;
381
382
383
       int fox128_192_16_test (const uint8 *p, const uint8 *k)
384
           FOX128_ctx ctx;
385
386
           FOX_key key;
387
           uint8 c[16];
388
           uint32 c32[4];
389
           int i, return_value = EXIT_SUCCESS;
390
391
           if (FOX128_init_ctx (&ctx)) {
               fprintf (stderr, "\nFatal error...exiting!\n");
392
               return_value = EXIT_FAILURE;
393
394
               goto error_label;
395
396
           fprintf (stdout, "\nF0X128/16/192 key
                                                          : ");
397
           for (i = 0; i < 6; i++) {
               fprintf (stdout, "%08X ", U8T032_BIG (k + 4*i));
398
399
           fprintf (stdout, "\nFOX128/16/192 message
400
401
           for (i = 0; i < 4; i++) \{
402
               fprintf (stdout, "%08X ", U8T032_BIG (p + 4*i));
403
           }
404
           if (FOX128_init_key (&key, ctx, k, 192, 16)) {
405
               fprintf (stderr, "\nFatal error...exiting!\n");
               return_value = EXIT_FAILURE;
406
407
               goto error_label;
408
           }
409
           memcpy (c, p, 16);
410
           c32[0] = U8T032_BIG (c);
411
           c32[1] = U8T032_BIG (c + 4);
           c32[2] = U8T032_BIG (c + 8);
412
413
           c32[3] = U8T032_BIG (c + 12);
414
           FOX128_encrypt (c32, key, ctx);
415
           fprintf (stdout, "\nFOX128/16/192 ciphertext : ");
416
           for (i = 0; i < 4; i++) {
               fprintf (stdout, "%08X ", c32[i]);
417
418
419
           FOX128_decrypt (c32, key, ctx);
           fprintf (stdout, "\nFOX128/16/192 message
                                                        : ");
420
421
           for (i = 0; i < 4; i++) {
422
               fprintf (stdout, "%08X ", c32[i]);
423
424
           fprintf (stdout, "\n\n");
425
426
        error_label:
427
           FOX128_clean_ctx (ctx);
428
           FOX128_clean_key (key);
429
430
           return return_value;
       }
431
432
       int fox128_256_16_test (const uint8 *p, const uint8 *k)
433
434
435
           FOX128_ctx ctx;
436
           FOX_key key;
437
           uint8 c[16];
438
           uint32 c32[4];
439
           int i, return_value = EXIT_SUCCESS;
440
441
           if (FOX128_init_ctx (&ctx)) {
442
               fprintf (stderr, "\nFatal error...exiting!\n");
               return_value = EXIT_FAILURE;
443
444
               goto error_label;
445
           fprintf (stdout, "n\prox128/16/256 key
446
                                                           : "):
447
           for (i = 0; i < 8; i++) \{
448
               fprintf (stdout, "%08X ", U8T032_BIG (k + 4*i));
449
```

```
450
            fprintf (stdout, "\nF0X128/16/256 message : ");
451
            for (i = 0; i < 4; i++) {
               fprintf (stdout, "%08X ", U8T032_BIG (p + 4*i));
452
453
            if (FOX128_init_key (&key, ctx, k, 256, 16)) {
    fprintf (stderr, "\nFatal error...exiting!\n");
454
455
                 return_value = EXIT_FAILURE;
456
457
                goto error_label;
            }
458
            memcpy (c, p, 16);
c32[0] = U8T032_BIG (c);
c32[1] = U8T032_BIG (c + 4);
459
460
461
            c32[2] = U8T032_BIG (c + 8);
462
            c32[3] = U8T032_BIG (c + 12);
463
464
            FOX128_encrypt (c32, key, ctx);
            fprintf (stdout, "\nFOX128/16/256 ciphertext : ");
465
466
            for (i = 0; i < 4; i++) \{
467
                 fprintf (stdout, "%08X ", c32[i]);
468
            FOX128_decrypt (c32, key, ctx);
469
            fprintf (stdout, "\nF0X128/16/256 message
470
                                                            : ");
            for (i = 0; i < 4; i++) {
471
472
                fprintf (stdout, "%08X ", c32[i]);
473
474
            fprintf (stdout, "\n');
475
476
         error_label:
477
            FOX128_clean_ctx (ctx);
478
            FOX128_clean_key (key);
479
480
            return return_value;
       }
481
```