

1.

2.4.1.a

$$x(n) = x(n-1) + 5, \quad n > 1, \quad x(1) = 0.$$

$$\begin{aligned}
 \text{Proof } x(n) &= x(n-1) + 5 \\
 &= [x(n-2) + 5] + 5 = x(n-2) + 5 \cdot 2 \\
 &= [x(n-3) + 5] + 5 \cdot 2 \\
 &= x(n-3) + 5 \cdot 3 \\
 &= \dots \\
 &= x(n-i) + 5i \\
 &= x(1) + 5 \cdot (n-1) = 5(n-1)
 \end{aligned}$$

2.4.1.c

$$x(n) = \cancel{x(n-1)} + n, \quad n > 0, \quad x(0) = 0$$

$$\begin{aligned}
 \text{Proof } x(n) &= x(n-1) + n \\
 &= [x(n-2) + (n-1)] + n \\
 &= x(n-2) + (n-1) + n \\
 &= [x(n-3) + (n-2)] + (n-1) + n \\
 &= x(n-3) + (n-2) + (n-1) + n \\
 &= \dots \\
 &= x(n-i) + (n-i+1) + \dots + n \\
 &= x(0) + 1 + 2 + \dots + n = \frac{n(n+1)}{2}
 \end{aligned}$$

9.

Taco

T(n):

$$T(n) = T(n-1) + 1$$

$$T(n) = T(n-1) + 1, \quad T(0) = 1$$

$$\begin{aligned} \text{Taco } T(n) &= T(n-1) + 1 = [T(n-2) + 1] + 1 \\ &= T(n-2) + 2 = \dots \\ &= T(n-i) + i \\ &= T(0) + n \\ &= 1 + n \end{aligned}$$