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COMP422 — Week 10

# **Advanced Topics in Evolutionary Computation**

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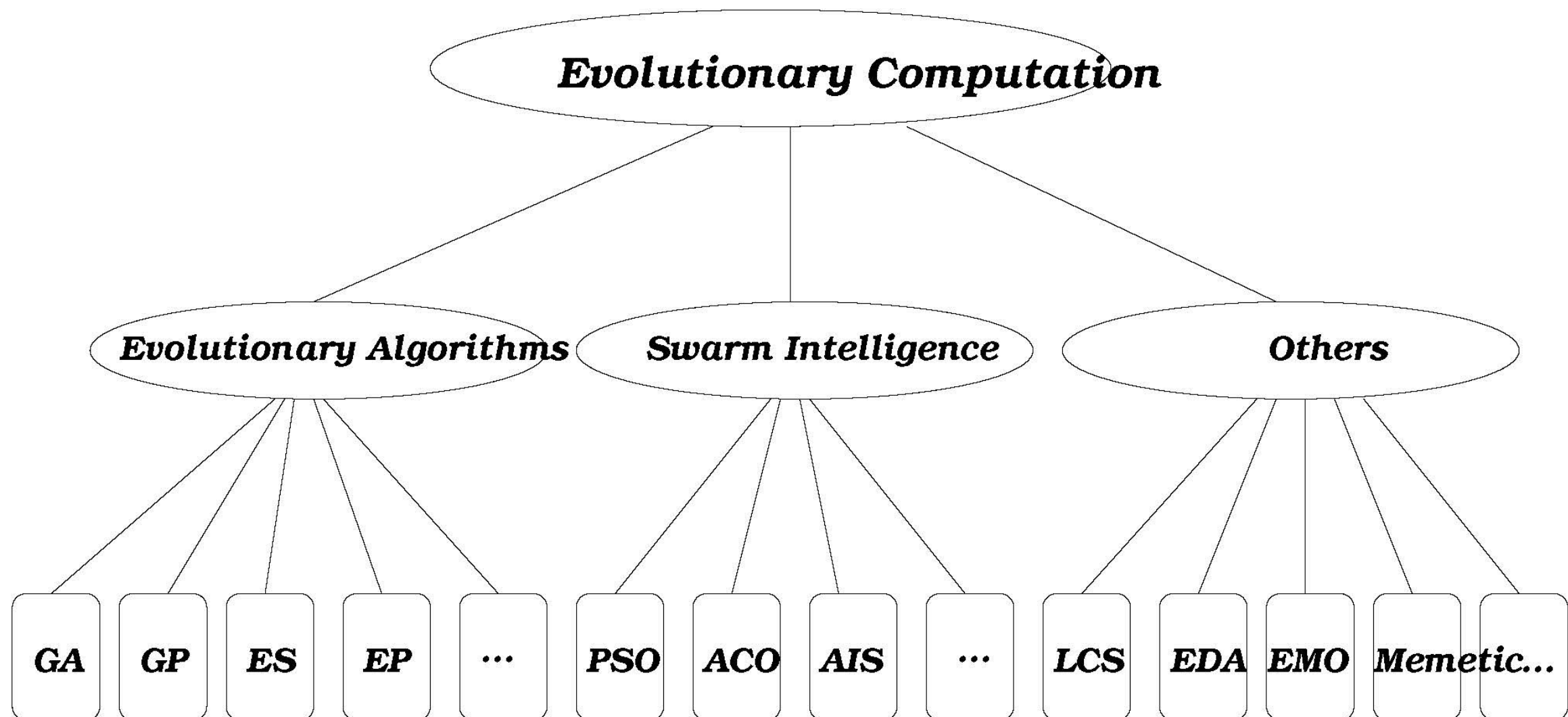
# Outline

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- Introduction: Evolutionary Computation
- Why Evolutionary Computation ?
- Strongly typed Genetic Programming
- Memetic Algorithms
- Differential Evolution
- Evolutionary Multi-objective Optimisation
  - Dr Yi Mei, next week
- Suggested Readings

# Evolutionary Computation (EC)

- A group of techniques inspired by the principles of biological evolution



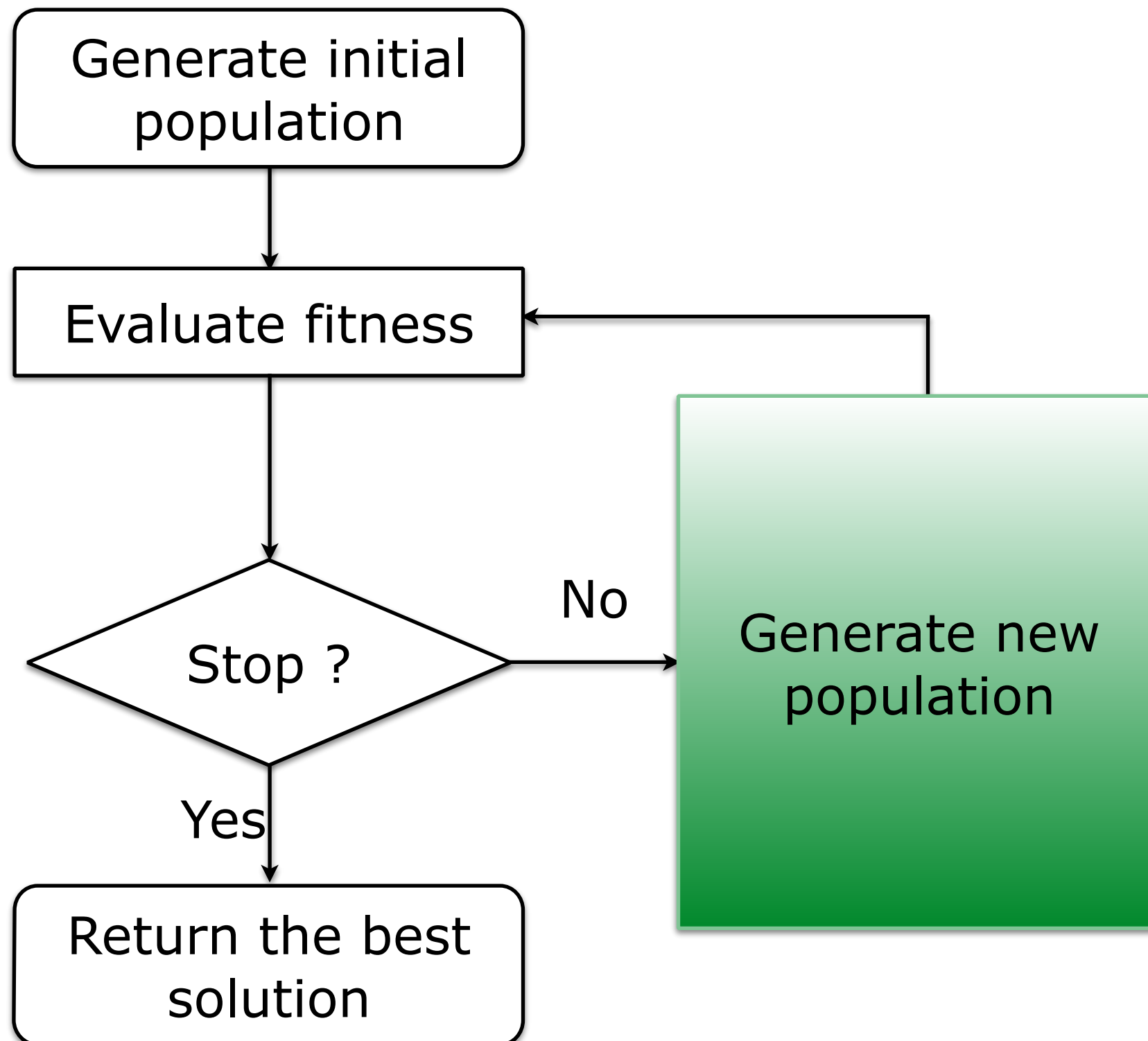
# Why Evolutionary Computation ?

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- Don't need domain knowledge
- Don't make any assumption
  - e.g. differentiable, linearity, separability, equality
  - EC can deal with non-differentiable, non-continuous, non-linear, noisy, flat, multi-dimensional, many local minima, constraints or stochasticity
- Easy to handle constraints
- EC can simultaneously build model structures and optimise parameters
- Population based search is particularly suitable for multi-objective optimisation

# Flowchart of an EC method

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# Strongly Typed GP

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- Evolved programs vs human-written programs
  - In standard GP systems, the inputs and outputs of the programs have **the same type**: float/double in general.
  - The type of terminals, the type of function arguments, and the return type of a function are the **same — closure property**.
  - **Human** written programs use **different data types and different data structures**.
  - Human written programs are more powerful.
- Can GP systems evolve computer programs with different data types, or automatically evolve different data structures?

# Strongly Typed GP

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- Montana[] introduced data types to GP and called the system **Strongly Typed Genetic Programming – STGP**.
- In STGP, each element in the **primitive set** is associated with a given data type, just as in the human-written programs.
  - The return type of a node can be any type which can be used as an argument type to its parent node.
  - In case the node is the root, the type returned is a solution of the problem.
  - Each function has the argument types associated with each element of its parameter list, constraining the types which subtrees of this function can take on.

# Genetic Operators in STGP

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- Crossover and mutation are restricted.
- Crossover:
  - In the first parent: starts by picking a random subtree
  - How to choose the crossover point for the second parent? – Randomly? restricted?
- Mutation:
  - How to select mutation point?
  - How to generate a replacement subtree? – Randomly? restricted?
- These constraints **ensure type safety** of the program.
- How about the reproduction?



# Generic types in STGP

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- Generic types are **equivalence classes** in a type system.
- Any member of one equivalence class may stand in for any other members of that class and the program will still be type safe.
- Example: VEC-2, VEC-3, ..., VEC-n can be replaced with VEC-k for a number of functions such as ADD, DOT-PRODUCT.
- Here VEC-k is a generic class with a parameterised size argument.

# Properties of STGP

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- STGP works by cutting down the search space:
  - Program generation process is restricted.
  - Closure in un-typed GP: any function is well-defined for all possible values that could be returned by other functions or terminals.
  - Closure in STGP is restricted to a particular data type: any function that needs to take an argument should consider the return type of the argument.
  - This immediately cuts down the number of branches by constraining the tree construction process.

# Properties of STGP

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- Each primitive can do a lot more “meaningful” work in the space of a single node.
  - Such work usually needs a large subtree to implement in an un-typed GP system.
  - Solutions obtained in this way can be often much smaller than in un-typed GP.
- Program evolved by STGP is generally easier to interpret.
  - In general GP, it usually needs to get the value of the fitness or program output.
  - The programs evolved are some kinds of transformation, not an algorithm.
  - STGP can produce “meaningful” results.
  - In STGP, the program domain can match the problem domain very closely.
- STGP can evolve complex data structures.

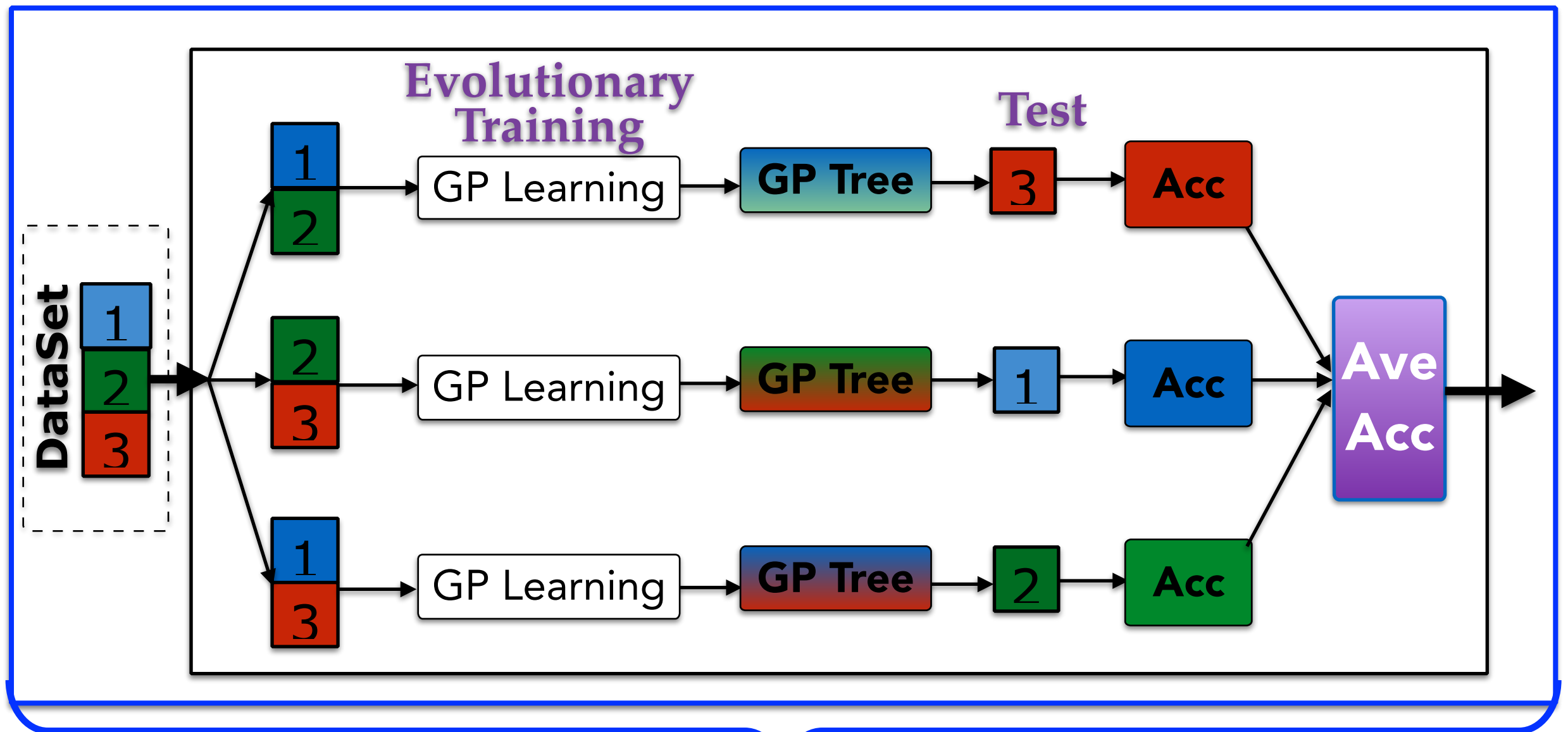
# Problems of STGP

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- Terminals and functions have to be carefully designed to be consistently matched.
- It is very difficult to define good fitness (evaluation) functions, even for relatively simple problems.
- A STGP system is usually a domain dependent system/method.
- The performance of such a system will be even worse than standard GP systems if primitive set and fitness were not properly defined.

# K-fold Cross Validation with GP

- Example: 3-fold cross validation in GP for classification



Repeat this process  $N$  ( $N \geq 30$ ) times with  $N$  different random seeds for GP

Same as any other stochastic method

# Differential Evolution (DE)

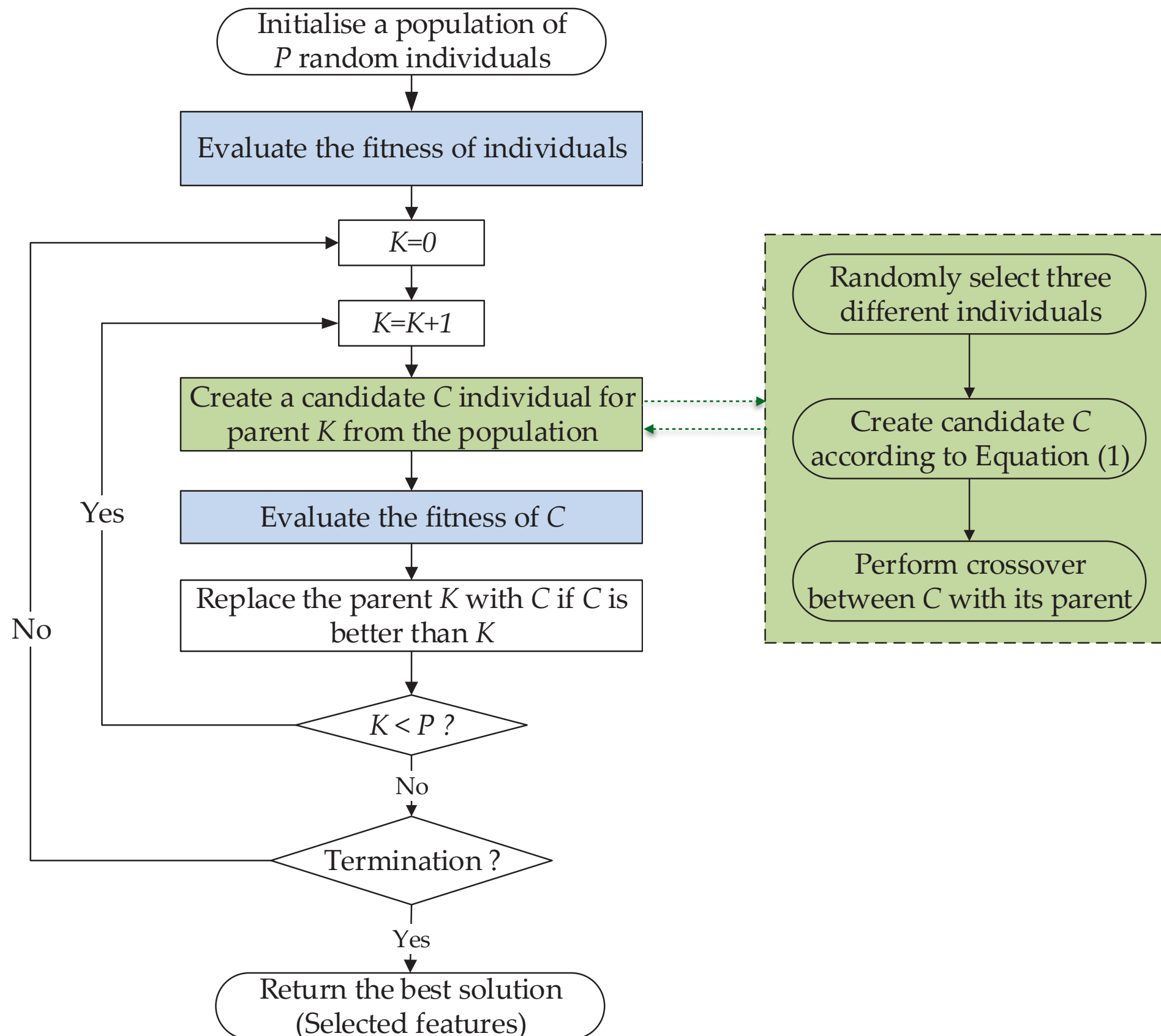
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- Differential evolution (DE) is an EC technique, first developed in 1997
- DE employs the **mutation** operation to produce a mutant candidate solution
- There are different types of **mutation** strategies
- **DE/rand/1** as an example:

$$C_{id} = \begin{cases} x_{id}^{i,r1} + F * (x_d^{i,r2} - x_{id}^{i,r3}), & \text{if } rand() < CR \\ x_{id}, & \text{otherwise} \end{cases}$$

- $F$  in  $(0,1)$ ,  $CR$  is the **crossover** rate

# Differential Evolution (DE)



# Five most frequently used DE mutation schemes

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“DE/rand/1”:  $\vec{V}_i(t) = \vec{X}_{r_1^i}(t) + F \cdot (\vec{X}_{r_2^i}(t) - \vec{X}_{r_3^i}(t)).$

“DE/best/1”:  $\vec{V}_i(t) = \vec{X}_{best}(t) + F \cdot (\vec{X}_{r_1^i}(t) - \vec{X}_{r_2^i}(t)).$

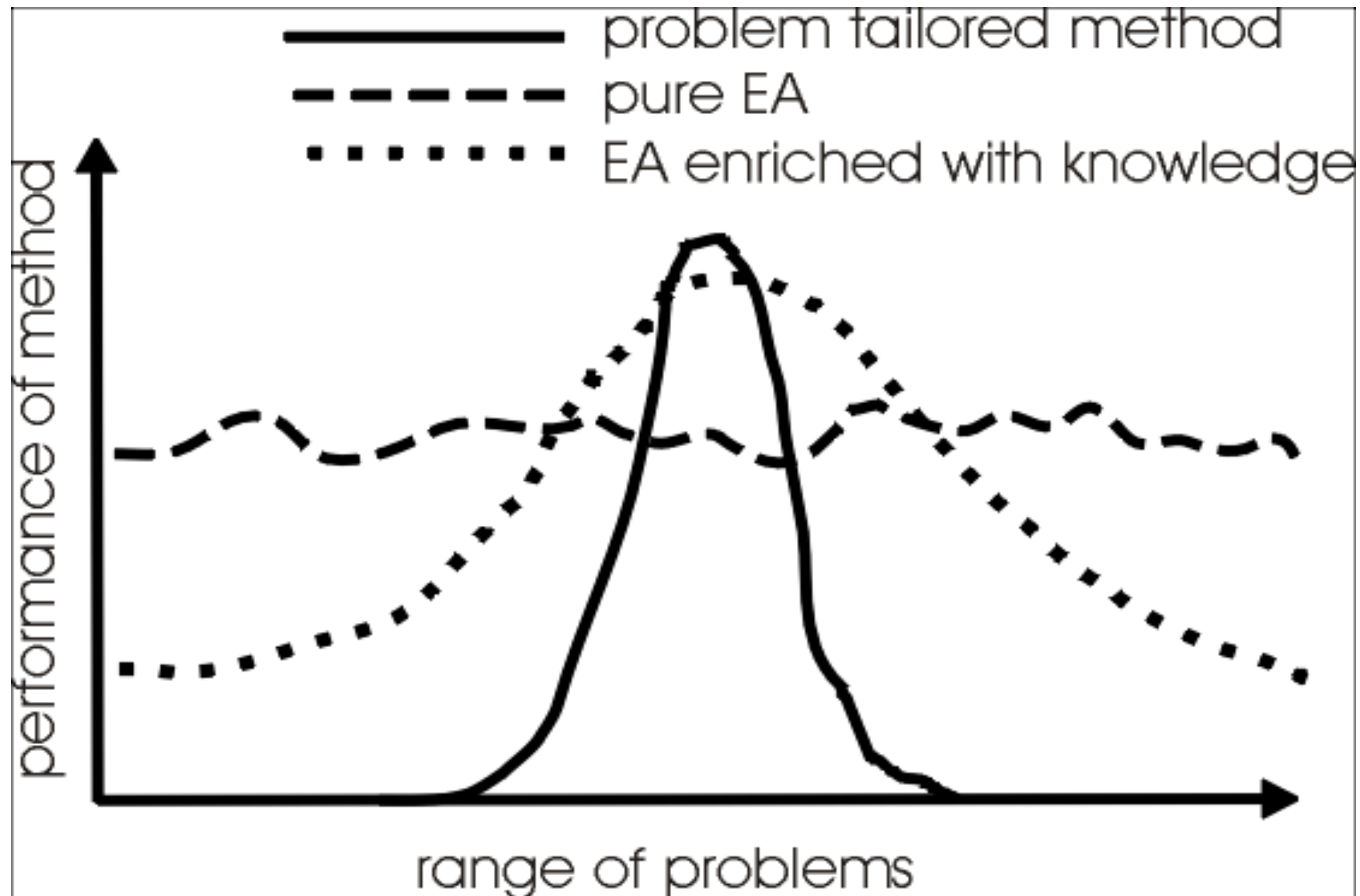
“DE/target-to-best/1”:  $\vec{V}_i(t) = \vec{X}_i(t) + F \cdot (\vec{X}_{best}(t) - \vec{X}_i(t)) + F \cdot (\vec{X}_{r_1^i}(t) - \vec{X}_{r_2^i}(t)),$

“DE/best/2”:  $\vec{V}_i(t) = \vec{X}_{best}(t) + F \cdot (\vec{X}_{r_1^i}(t) - \vec{X}_{r_2^i}(t)) + F \cdot (\vec{X}_{r_3^i}(t) - \vec{X}_{r_4^i}(t)).$

“DE/rand/2”:  $\vec{V}_i(t) = \vec{X}_{r_1^i}(t) + F_1 \cdot (\vec{X}_{r_2^i}(t) - \vec{X}_{r_3^i}(t)) + F_2 \cdot (\vec{X}_{r_4^i}(t) - \vec{X}_{r_5^i}(t)).$



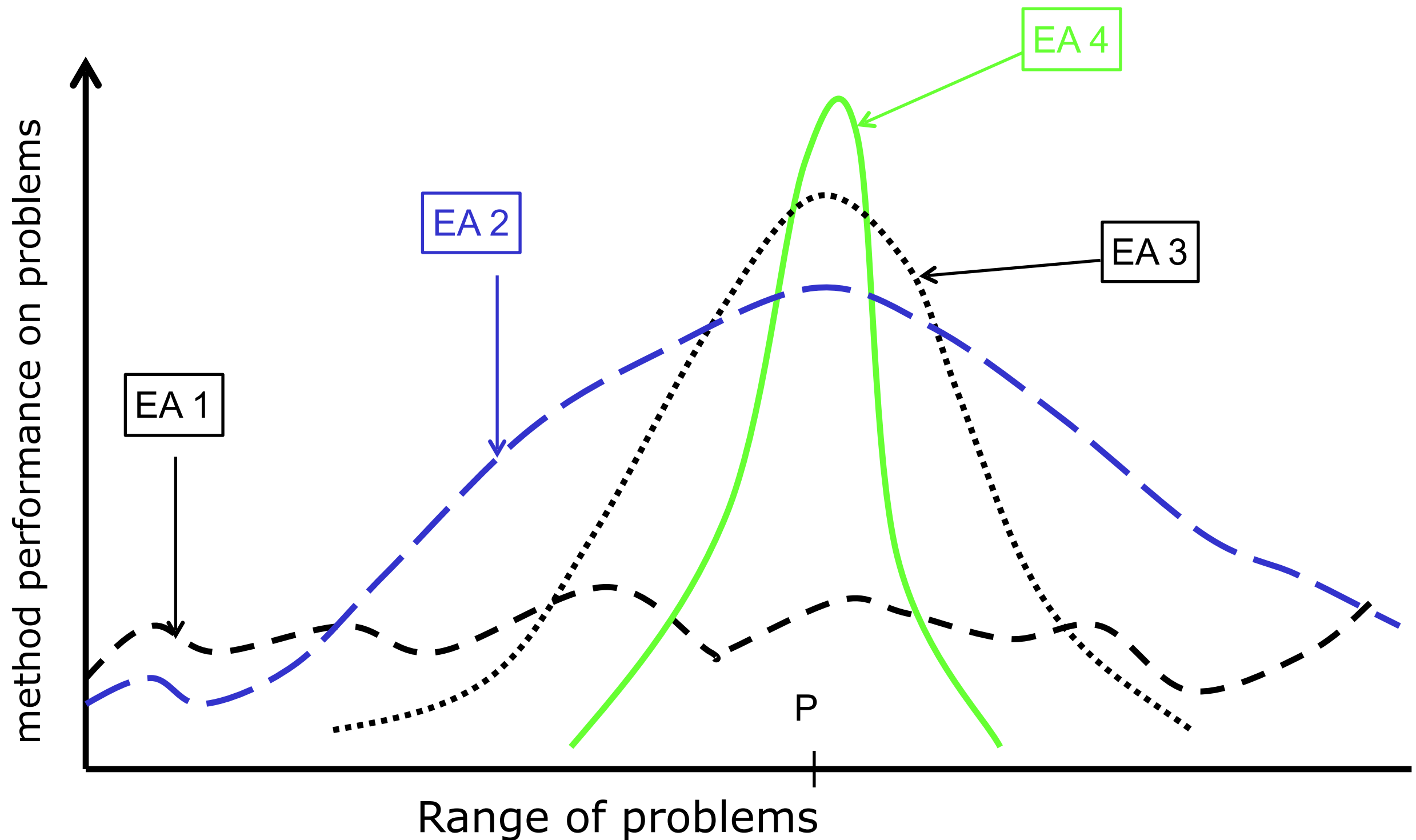
# Evolutionary Algorithms and domain knowledge



**Michalewicz's** view on EAs in context

A.E. Eiben and J.E. Smith, Introduction to Evolutionary Computing Hybridisation with other techniques: Memetic Algorithms

# Michalewicz's Interpretation

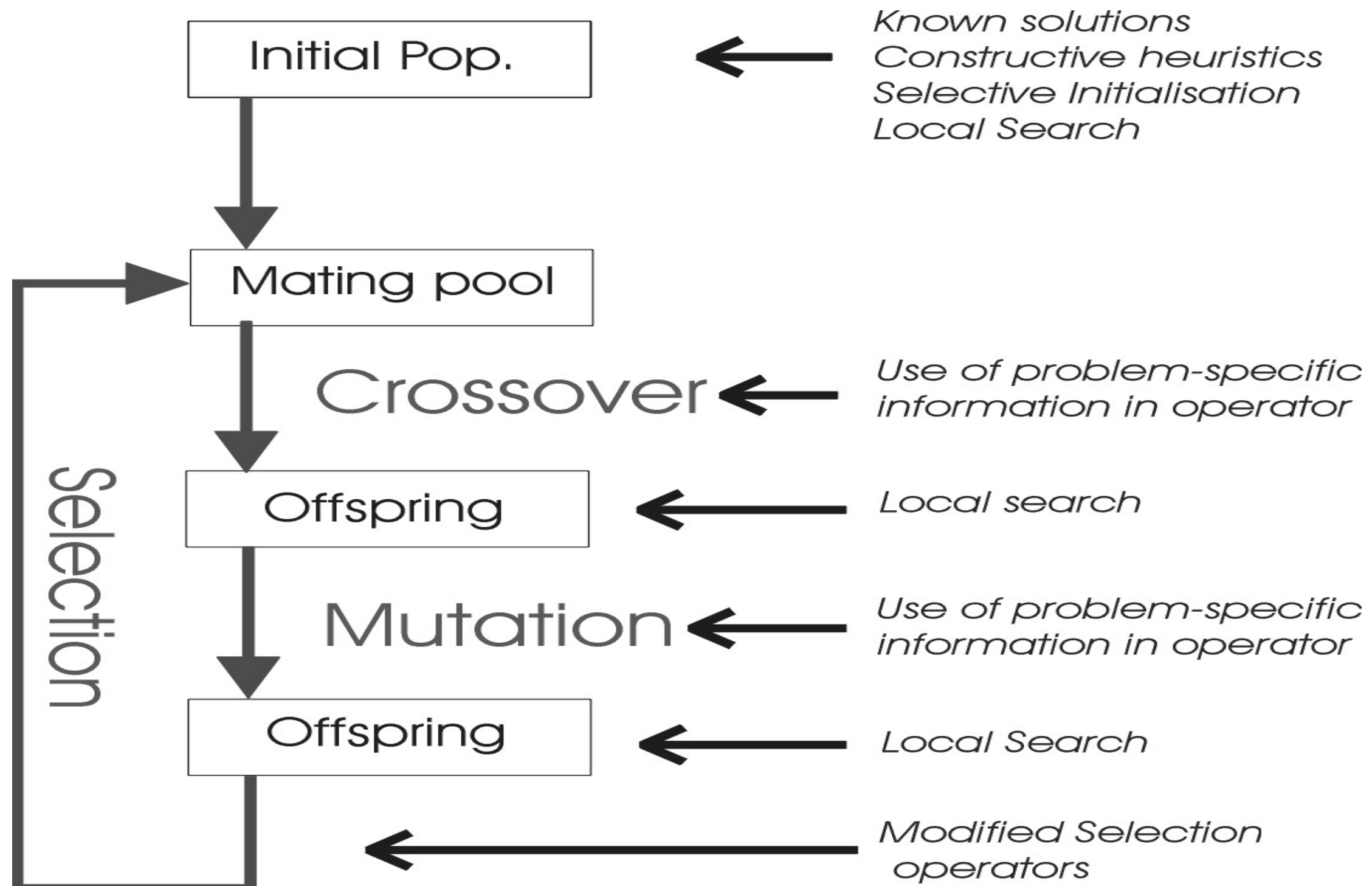


# Evolutionary Algorithms and Domain Knowledge

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- Fashionable after the 90's:
  - to add problem specific information into the **EAs** by means of specialised crossover, mutation, representations, and local search
- Result: The performance curve deforms and
  - makes EAs better in some problems,
  - worst on other problems
  - amount of problem specific is varied.
- Hybridised Evolutionary Computation
  - EA vs. EC

# Where to Hybridise ?



# Memetic Algorithms (MAs)

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- Memetic Algorithms:
  - MAs are carefully orchestrated interplay between (stochastic) **global** search and (stochastic) **local** search algorithms
  - **GA + local search**
  - More general now: EC + local search
- Adding Domain Knowledge to EAs

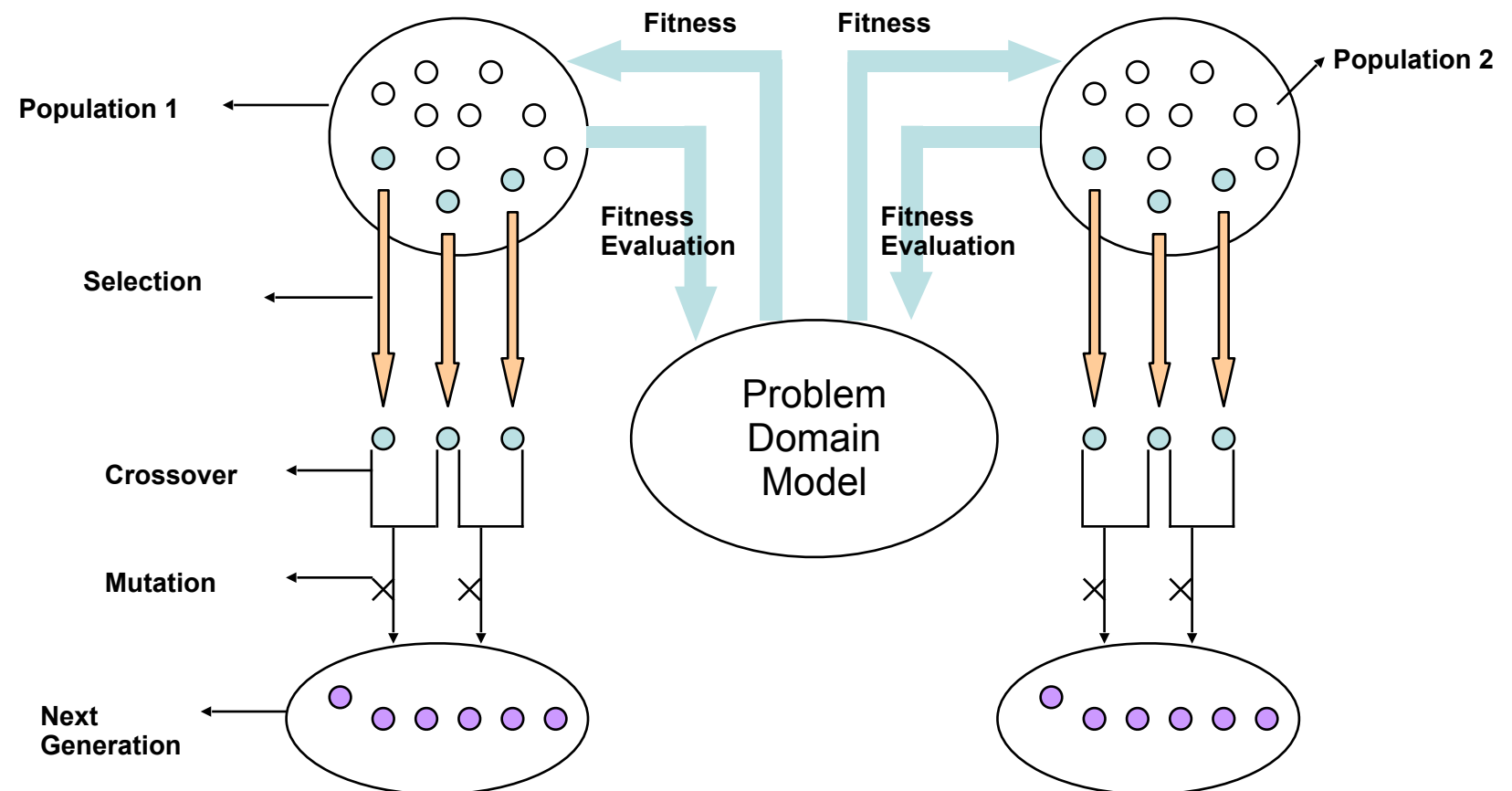
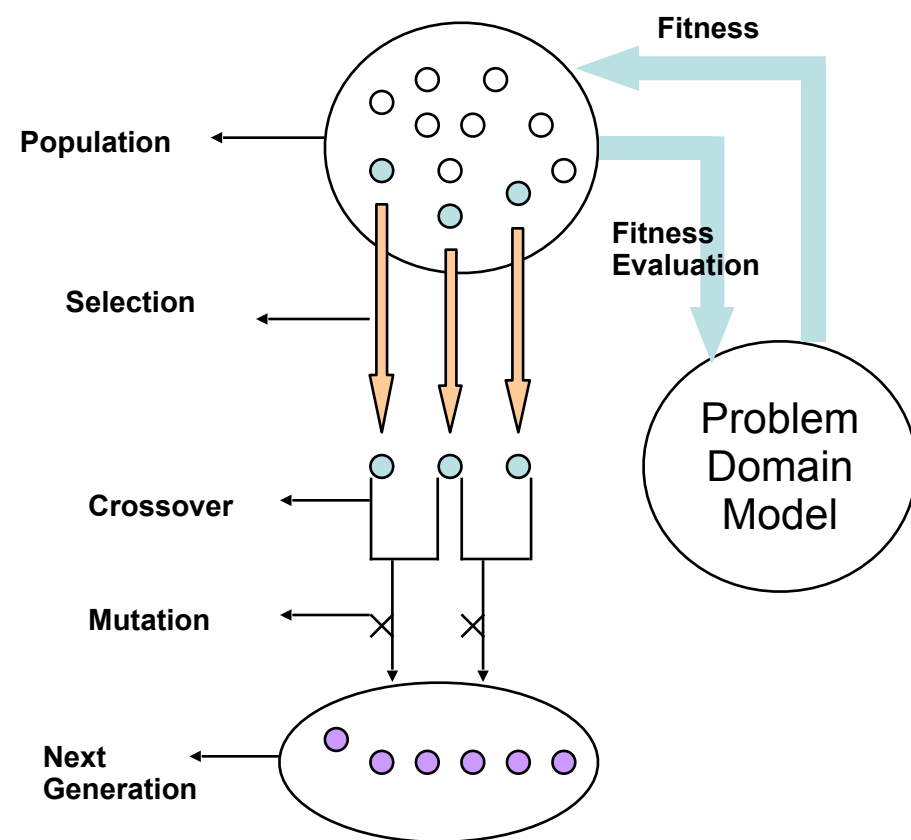
# Why Memetic Algorithms (MAs) ?

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- Complex problems can be partially decomposable:
  - different subproblems be better solved by different methods
  - Subproblem specific information can be placed into variation operators or into local searchers
  - In some cases there are exact/approximate methods for subproblems
- EC is good at **exploring** the search space but find it difficult to zoom-in good solutions
- Problems have constraints associated to solutions and heuristics/local search are used to **repair solutions found by EC**
- If heuristic/local search strategies in MAs are “first class citizens” then one can **raise the level of generality of the algorithm without sacrificing performance by letting the MA choose which local search to use.**
- ***hyper-heuristic***

# Coevolution

- Cooperative coevolution
- Competitive coevolution



# Other Important Topics

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- Evolutionary Multi-objective optimisation
  - Evolutionary Many-objective optimisation
  - Learning classifier systems
  - Large-scale optimisation
  - Dynamic optimisation
  - Constraint optimisation
  - Artificial immune systems
  - hybrid EC with other methods
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- EC for DM and ML
  - Real-world applications



# IEEE CIS Evolutionary Computation Pioneer award

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- 2016: Marco Dorigo
- 2015: Thomas Bäck
- 2014: George Burgin
- 2013: Xin Yao
- 2012: Russell C. Eberhart and James Kennedy
- 2012: J.David Schaffer
- 2011: Larry J. Eshelman
- 2010: John Greffentette
- 2009: David E. Goldberg
- 2008: David B. Fogel
- 2005: Kenneth De Jong
- 2004: Richard Friedberg
- 2003: John H. Holland
- 2002: Ingo Rechenberg
- 2002: Hans-Paul Schwefel
- 2001: Michael Conrad
- 2000: George Box
- 1999: Alex S. Fraser
- 1998: Lawrence J. Fogel

# IEEE Transactions on Evolutionary Computation

## Outstanding Paper Award (data until 2015)

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- Urvesh Bhowan, Mark Johnston, Mengjie Zhang and Xin Yao, "Evolving Diverse Ensembles Using Genetic Programming for Classification with Unbalanced Data," Vol. 17, No. 3, 2013, pp. 368-386.
- Oliver Schütze, Xavier Esquivel, Adriana Lara, and Carlos A. Coello Coello, "Using the Averaged Hausdorff Distance as a Performance Measure in Evolutionary Multi-Objective Optimization," Vol. 16, No. 4, August 2012, pp. 504-522.
- Adriana Lara, Gustavo Sanchez, Carlos A. Coello Coello and Oliver Schütze, "HCS: A New Local Search Strategy for Memetic Multiobjective Evolutionary Algorithms", Vol. 14, No. 1, February 2010, pp. 112-132.
- A. K. Qin, V. L. Huang and P.N. Suganthan, "Differential Evolution Algorithm with Strategy Adaptation for Global Numerical Optimization", Vol. 13, No. 2, April 2009, pp. 398-417.
- Q. H. Nguyen, Y. S. Ong and M. H. Lim, "A Probabilistic Memetic Framework" Evolution Algorithm with Strategy Adaptation for Global Numerical Optimization", Vol. 13, No. 3, June 2009, pp. 604-623.
- S. Y. Chong, P. Tino and X. Yao, "Measuring generalization performance in coevolutionary learning," Vol. 12, No. 4, August 2008, pp. 479-505.
- Qingfu Zhang and Hui Li, "MOEA/D: a multi-objective evolutionary algorithm based on decomposition," Vol. 11, No.6, December 2007, pp. 712-731.

# IEEE Transactions on Evolutionary Computation

## Outstanding Paper Award (data until 2015)

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- Joshua Knowles, "ParEGO: a hybrid algorithm with on-line landscape approximation for expensive multiobjective optimization", Vol. 10, No. 1, February 2006, pp. 50-66.
- C. Blum and M. Dorigo, Search Bias, "Ant-Colony Optimization: On the role of Competition-balanced Systems", Vol. 9, No. 2, April 2005, pp. 159-174.
- A. Pruegel-Bennett, "Symmetry breaking in population-based optimization," Vol. 8, No. 1, February 2004, pp. 63-79.
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- M. Clerc and J. Kennedy, "The particle swarm explosion: stability and convergence in a multi-dimensional complex space," Vol. 6, No. 1, February 2002, pp. 58-73.
- A. Sierra, J. A. Macias and F Corbacho, "Evolution of functional link networks," Vol. 5, No. 1, February 2001, pp. 54-65.
- C. Dimopoulous and A. M. S. Zalzala, "Recent developments in evolutionary computation for manufacturing optimization: problems, solutions, and comparisons," Vol. 4, No. 2, July 2000, pp. 93-113.
- A. E. Eiben, R. Hinterding, and Z. Michalewicz, "Parameter control in evolutionary algorithms," Vol. 3, No. 2, July 1999, pp. 124-141.

# IEEE CIS Task Forces

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- TF1: Theoretical Foundations of Bio-inspired Computation, Chair: Pietro Oliveto, Vice Chairs: Per Kristian Lehre and Frank Neumann
- TF2: Differential Evolution, Chair: Janez Brest, Vice Chairs: Ponnuthurai N Suganthan and Ferrante Neri
- TF3: Swarm Intelligence, Chair: Yuhui Shi, Vice Chairs: Marco Dorigo and Xiaodong Li
- TF4: Artificial Immune Systems, Chair: Mario Pavone, Vice Chair: Carlos A. Coello Coello
- TF5: Cultural Algorithms, Chair: Robert Reynolds, Vice Chairs: Yuhui Shi and Gary Yen
- TF6: Artificial Life and Complex Adaptive Systems, Chair: Chrystopher Nehaniv, Vice Chairs: Terry Bossomaier and Hiroki Sayama
- TF7: Evolutionary Algorithms Based on Probabilistic Models, Chair: John McCall, Vice Chairs: Qingfu Zhang and Aimin Zhou
- TF8: Evolutionary Computation in Dynamic and Uncertain Environments (ECiDUE), Chair: Shengxiang Yang, Vice Chairs: David Pelta and Changhe Li

# IEEE CIS Task Forces

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- TF9: Evolutionary Computer Vision and Image Processing, Chair: Sergio Damas, Vice Chairs: Mario Köppen and Mengjie Zhang
- TF10: Evolutionary Scheduling and Combinatorial Optimization, Chair: Su Nguyen, Vice Chairs: Rong Qu and Mark Johnston
- TF11: Evolvable Hardware, Chair: Andy Tyrrell, Vice Chairs: Martin Trefzer and Lukas Sekanina
- TF12: Large Scale Global Optimization, Chair: Daniel Molina, Vice Chair: Ponnuthurai N Suganthan
- TF13: Nature-Inspired Constrained Optimization, Chair: Efren Mezura-Montes, Vice Chair: Helio Barbosa
- TF14: Multi-Objective Evolutionary Algorithms, Chair: Sanaz Mostaghim, Vice Chairs: Katya Rodriguez-Vazquez and Andrew Lewis
- TF15: Evolutionary Computation for Feature Selection and Construction, Chair: Bing Xue, Vice Chairs: Yaochu Jin and Mengjie Zhang
- TF16: Data-Driven Evolutionary Optimization of Expensive Problems, Chair: Chaoli Sun, Vice Chairs: Jonathan Fieldsend and Yew-Soon Ong