

Autonomous Robotic Systems

Bayes Filter

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1 Introduction

The Bayes filter, in the context of mobile robot localization also called *Recursive Bayesian Estimation*, uses sensor measurements and a mathematical process model to estimate an unknown probability density function recursively over time. This document describes the implementation of a Bayes filter in the Robot Operating System (ROS) framework and reflects on the filter's performance with regard to its localization capabilities in different situations. The world in which the robot is situated consists of a corridor with several doors.

2 The world model

The environment the robot is situated in consists of a corridor with several doors. The corridor is discretized into ten cells, which can be traversed either from left to right or the other way around. The cell the robot is located in together with the direction it is facing make up a belief state, which results in 20 possible states.

The wall layout for each state is represented with an enumeration. This enumeration contains the four values L, LR, LRF and R . The characters express whether a wall has been measured to the left (L), to the right (R) or in front (F) of the robot, with a combination indicating that multiple walls have been found. Therefore, the world model is represented through a 20-dimensional vector and information about which measurements should be true in this state contained in the respective enumeration value.

3 The Bayes filter

The Bayes filter is initialized with a uniformly distributed belief state. Since there are 20 states, this results in an initial probability of $p(x_i) = \frac{1}{20} = 0.05$ for each state. Afterwards the probabilities for the next belief state are calculated by alternating the *control update* and the *measurement update* step.

3.1 Control update

The control update is executed whenever the robot moves forward or makes a 180 degree turn. The belief state $\overline{bel}(x_t)$ represents the next belief state before the measurement is taken into account and is calculated according to the following formula:

$$\overline{bel}(x_t) = \sum p(x_t | u_t, x_{t-1}) bel(x_{t-1})$$

To practically calculate the new belief $\overline{bel}(x_t)$ after the *move forward* command, we take a belief state x_i and consider the states x_i , x_{i-1} and x_{i-2} , from which x_i can be reached. The probabilities of these three possible starting locations is weighted according to the given transition probabilities and summed up. For the *move forward* command, this equates to:

$$\overline{bel}(x_t) = 0.8 \times p(x_{i-1}) + 0.1 \times p(x_{i-2}) + 0.1 \times p(x_i)$$

However, two extra cases have to be considered. The first extra case are the states x_i for which $i \bmod 10 = 0$ holds true, i.e. the states x_0 and x_{10} . Since the world is not cyclic, there are no states x_{i-1} and x_{i-2} from which the states x_0 and x_{10} could be reached. Therefore, the probability of these two states is calculated according to

$$\overline{bel}(x_t) = 0.1 \times p(x_i)$$

The second extra case are the states x_i for which $i \bmod 10 = 1$ holds true. Explicitly, these are the states x_1 and x_{11} . Similarly to the above reasoning, there are no states x_{i-2} from which the states x_1 and x_{11} could be reached. Therefore, the probability of these two states is calculated according to

$$\overline{bel}(x_t) = 0.8 \times p(x_{i-1}) + 0.1 \times p(x_i)$$

Due to these extra cases, the resulting values for $\overline{bel}(x_t)$ do not sum to 1 anymore and need to be normalized again.

The new belief state for the *turn* command is calculated according to

$$\overline{bel}(x_t) = 0.9 \times p(x_{N-1-i}) + 0.1 \times p(x_i)$$

where N is the number of belief states.

3.2 Measurement update

The belief state after incorporating the measurement probability is represented by

$$bel(x_t) = \eta p(z_t|x_t) \overline{bel}(x_t)$$

where $\overline{bel}(x_t)$ is the previously calculated belief state after the control update but before taking the measurement into account, $p(z_t|x_t)$ is the probability that the measurement z_t has been taken in the state x_t and η is a normalization constant.

To calculate the new belief state $bel(x_t)$, a measurement is taken. This measurement consists of checking whether there is a wall to the left, to the right and in front of the robot. Then, for each belief state x_i it is checked whether the measurement agrees with the layout of the current cell, i.e. if the value for the boolean variables `wall_left`, `wall_right` and `wall_front` corresponds to state x_i having a wall to the left, right or front, respectively. If the measurement agrees with there being a wall, the probability for being in the corresponding state is multiplied by a factor of 0.6. The probability for every other state is multiplied by 0.2.

During this first loop, the resulting products are also summed up. In a second loop, the calculated values are then divided by the sum, such that they represent proper probabilities again.

4 Results

There is practically no information that needs to be remembered to calculate the next belief state, so we can assume that the state is complete and that the Markov assumption holds.

Most states in the corridor have a wall on both sides, which makes them indistinguishable. When issuing the *measurement* command in a state that has a door, the probabilities of the three states containing a door raises. Multiple continuous measurements cause the robot's confidence for being in one of these three states to grow.

States that are opposite to a door are also easily identified. Noise in sensing, moving and turning cause the certainty to drop. However, the robot quickly recovers from that when reaching another location that is easily distinguishable from the rest. Most of the time the robot tracks two hypotheses. After taking measurements at two unique locations in a row, most of the probability focusses

on only one state. This certainty is kept when alternating movement (including *move forward* and *turn*) and sensing, until one of these actions fails.

Consider the example case in which the robot should move one cell forward. If it fails to do so and stays at its location, still 80% of the probability of the current state are convolved to the next state. However, after reaching the next state that either has a door, is opposite to a door or has a wall in front of the robot, the probability quickly focusses on the right state again.

5 Conclusion

The results showed that our implementation behaves according to the theory of Bayes filters. If the robot reaches a location that it can distinguish from most of the other locations, its certainty for being in one of these states grows. After reaching a second location that differs from most of the other locations, most of the probability focusses on the right state. The implementation is also robust to noise in the robot's measurements and actions.