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Introduction

In this worksheet you will use cubic Bézier curves to implement a top-down 2D race track.

Begin by **forking** the following git repository:

https://github.com/Falmouth-Games-Academy/comp270-worksheet-A

Complete the tasks described below, remembering to **commit** your work regularly. To submit your work, open a **pull request** from your forked repository to the original repository.

The template program in this repository has a number of empty functions which the tasks below ask you to fill in. Feel free to add or modify any other code that makes your solutions easier to write or maintain — for example you are encouraged to add your own helper methods to the provided classes in order to enable code reuse.

The following video demonstrates what successfully completed solutions to the tasks should look like:

https://youtu.be/KugZcz6YZTQ

Background

Given four points in 2D space

$$\mathbf{p}_0 = \begin{pmatrix} x_0 \\ y_0 \end{pmatrix}, \mathbf{p}_1 = \begin{pmatrix} x_1 \\ y_1 \end{pmatrix}, \mathbf{p}_2 = \begin{pmatrix} x_2 \\ y_2 \end{pmatrix}, \mathbf{p}_3 = \begin{pmatrix} x_3 \\ y_3 \end{pmatrix},$$

a cubic Bézier curve is defined by

$$b(t) = (1-t)^3 \mathbf{p}_0 + 3(1-t)^2 t \mathbf{p}_1 + 3(1-t)t^2 \mathbf{p}_2 + t^3 \mathbf{p}_3$$

where $0 \le t \le 1$. See Figure 1.

The provided template program defines a Bezier class which represents a cubic Bézier curve. The program also defines a race track as a chain of Bézier curves, stored as std::vector<Bezier> m_track. The curves are set up such that the end point of one equals the start point of the next, and the start point of the first equals the end point of the last, giving the appearance of a continuous loop.

Task 1: drawing Bézier curves

For the purposes of rendering, a Bézier curve can be approximated by a series of straight lines. If b(t) denotes the point on the curve with parameter t, then

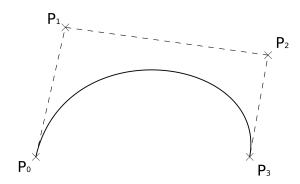


Figure 1: A cubic Bézier curve. Image source: https://commons.wikimedia.org/wiki/File:Bezier_curve.svg

the curve can be drawn as a sequence of n line segments by drawing lines between points

 $b\left(\frac{i}{n}\right)$ and $b\left(\frac{i+1}{n}\right)$

for $i=0,\ldots,n-1$. For example if n=2, the curve is approximated by two lines: one from b(0.0) to b(0.5), and one from b(0.5) to b(1.0). The larger n is, the smoother the curve appears.

In the code, the Bezier class has a draw method which currently does nothing. **Implement** the method so that it draws the curve, using SDL_RenderDrawLine or SDL_RenderDrawLineF to draw the line segments. The number of segments (n in the above discussion) should be defined as a constant so that it can be tuned; a value of 20 is a good default.

Task 2: following the curve

If the track is made up of n curves, denoted b_0,\ldots,b_{n-1} , then we can represent a position along the track as a number s with $0 \le s \le n$. The integer part of s gives the curve number, and the fractional part gives the t parameter along the curve. For example, s=1.2 represents curve 1 and parameter value 0.2, so $b_1(0.2)$.

In C++, the integer part of a floating point number can be found¹ by using static_cast<int>(s). The fractional part can be found using fmodf(s, 1.0f).

The Application class has a drawCarOnTrack method which currently does nothing. It takes a single argument, position, which acts as s in the discussion above. **Implement** the method so that it draws a car sprite at the given position on the track; when done correctly, the sprite will be animated performing laps of the track.

Your implementation should call drawCar to actually draw the sprite. This function takes two arguments: a position (as a Vector2), and an angle. Pass an angle of 0 for now; the next task is to calculate a more appropriate angle.

Task 3: facing the tangent

At a point with parameter t, the tangent to the cubic Bézier curve is given by²

$$b'(t) = 3(1-t)^{2}(\mathbf{p}_{1} - \mathbf{p}_{0}) + 6(1-t)t(\mathbf{p}_{2} - \mathbf{p}_{1}) + 3t^{2}(\mathbf{p}_{3} - \mathbf{p}_{2}).$$

 $^{^{\}rm 1}$ Some caution is required using these with negative numbers; however we always have $s\geq 0$ so this is not an issue here.

²Those of you who know calculus can verify that this is the derivative of b(t) with respect to t.

Modify your implementation of Application::drawCarOnTrack such that the car is drawn facing along the tangent to the curve — that is, in the direction of the track. Modify the angle passed to drawCar to achieve this. You will find the atan2f function useful in converting from the tangent vector to the required angle; however note that atan2f returns an angle in radians whereas drawCar expects an angle in degrees.

Task 4: movement speed

You will notice that the car appears to speed up and slow down on certain parts of the track. This is because we are incrementing t by a constant amount every frame (in Application::updateCarPosition, but this does not necessarily correspond to a constant distance along the curve.

Modify the implementation of Application::updateCarPosition to achieve a more consistent movement speed. Figuring out exactly how to achieve this is part of the exercise.

Marking Rubric

All submissions and assessment criteria for this assignment are individual.

Criterion	Weight	Near Pass	Adequate	Competent	Very Good	Excellent	Outstanding
Basic competency threshold	30%	A reasonable attempt at the worksheet was not submitted by the formative deadline.	A reasonable attempt at the worksheet was submitted by the formative deadline. There is no evidence of academic misconduct.				
Functional coherence	40%	None of the tasks have been attempted.	Task 1 has been attempted and partially completed.	Task 1 has been successfully completed.	Tasks 1 and 2 have been successfully completed.	Tasks 1–3 have been successfully completed.	Tasks 1–4 have been successfully completed.
Maintainability	30%	The code is only sporadically commented, if at all, or comments are unclear.	The code is well commented.	The code is reasonably well commented.	The code is reasonably well commented, with appropriate high-level	The code is very well commented, with comprehensive appropriate	The code is commented extremely well, with comprehensive appropriate
		Few identifier names are	Some identifier names are descriptive and	Most identifier names are descriptive and	documentation.	high-level documentation.	high-level documentation.
		clear or inappropriate.	appropriate.	appropriate.	Almost all identifier names	All identifier names are	All identifier names are
		Code formatting hinders readability.	An attempt has been made to adhere to a consistent	Most code adheres to a sensible formatting style.	are descriptive and appropriate.	descriptive and appropriate.	descriptive and appropriate.
		,	formatting style.	There is almost no obvious	Almost all code adheres to a sensible formatting style.	All code adheres to a sensible formatting style.	All code adheres to a sensible formatting style.
			There is little obvious duplication of code or of	duplication of code or of literal values.	There is no obvious	There is no obvious	There is no duplication of
			literal values.	illeral values.	duplication of code or of literal values. Some literal values can be easily "tinkered".	duplication of code or of literal values. Most literal values are, where appropriate, easily "tinkered".	nete is no adplication of code or of literal values. Nearly all literal values are, where appropriate, easily "tinkered".