

COMP110: Principles of Computing

2: Basic Principles for Computation



Learning outcomes

By the end of this week's sessions, you should be able to:

- Use binary, decimal and hexadecimal notation to represent and operate on numerical values
- ► Explain the basic architecture of a computer
- Distinguish the most common programming languages and paradigms in use today





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 - With reference to appropriate academic sources



Marking rubric

See assignment brief on LearningSpace/GitHub





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- Finding and reading academic papers takes time and effort — don't leave it until the last minute!





Binary notation

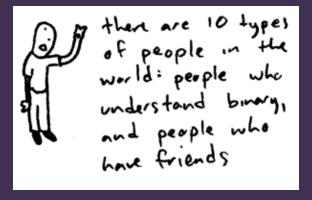


Image credit: http://www.toothpastefordinner.com

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Converting to binary

https://www.youtube.com/watch?v=OezK_zTyvAQ

Bits, bytes and words

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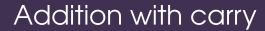
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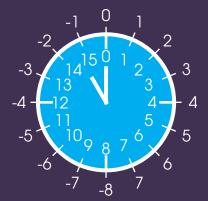
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 - \triangleright 2⁶⁴ 1 = 18, 446, 744, 073, 709, 551, 615









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$$14 + 7 = 5$$

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- Note that the left-most bit can be interpreted as a sign bit: 1 if negative, 0 if positive or zero

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- ► (This is equivalent to subtracting the number from 2ⁿ... why?)
- This is also the process for converting back from 2's complement, i.e. doing it twice should give the original number

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- ► In fact, subtraction can just be done as addition
- ▶ I.e. a b is the same as a + (-b), where a and -b are just n-bit numbers

Exercise Sheet i

Due next Tuesday!





What is a programming language?

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- A program is a sequence of instructions for a computer to perform a specific task
- A programming language is a formal language for communicating these sequences of instructions

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- There are hundreds of programming languages, each better suited to some tasks than others
- Sometimes your choice is dictated by your choice of platform, framework, game engine etc.
- To become a better programmer (and maximise your employability) you should learn several languages (but one at a time!)

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- Lower level languages were once the choice of game programmers, but advances in hardware mean that higher level languages are often a better choice

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- ▶ Declarative: does not define the control flow of a program, but rather defines logical relations

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- Most commonly used languages today are a mixture of procedural and object-oriented paradigms, with many also incorporating ideas from functional programming

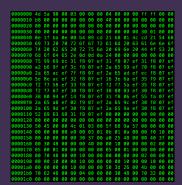
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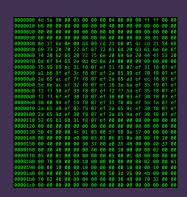
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- Purely declarative languages have uses in academia and some special-purpose languages







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- Nobody has actually written programs in machine code since the 1960s...

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            start
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    mov
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- Also not portable between CPU architectures

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- Also used by developers of operating systems and embedded systems, but falling out of favour with other software developers

Often favoured by smaller indie teams for rapid development

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There are many others, but these are the most commonly used in game development

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► UnrealScript, Blueprint (Unreal Engine)

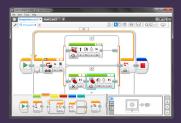
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- UnrealScript, Blueprint (Unreal Engine)
- GML (GameMaker)

Visual programming languages





Visual programming languages



Based on connecting graphical blocks rather than writing code as text

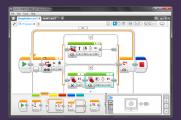




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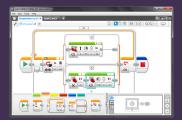
Scratch (used for teaching in school)





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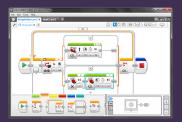
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- ► Blueprint (Unreal)





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Note: despite the name, Microsoft Visual Studio is **not** a visual programming environment!

SQL (database queries)

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- ► LEX, YACC (script interpreters)



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- ► XML, JSON (data storage)

Which programming language is most popular?

http://githut.info

"Family tree" of programming languages

https://www.levenez.com/lang/lang.pdf





► Introduced in 1936 by Alan Turing

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- ► Introduced in 1936 by Alan Turing
- Theoretical model of a "computer"
 - I.e. a machine that carries out computations (calculations)

► Has a finite number of **states**

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- Each space on the tape holds a symbol from a finite alphabet
- Has a tape head pointing at one space on the tape
- Has a transition table which, given:
 - The current state
 - The symbol under the tape head

specifies:

- A new state
- A new symbol to write to the tape, overwriting the current symbol
- Where to move the tape head: one space to the left, or one space to the right



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- Repeatedly apply the rules on the next slide
- What computation does this machine perform?
 - Hint: Milk = 0, White = 1, and remember yesterday's lecture...

Current	Current	New	New	Move
lolly	chocolate	lolly	chocolate	direction
Drumstick	Blank	Fruit	Blank	\leftarrow
Drumstick	Milk	Drumstick	White	\rightarrow
Drumstick	White	Drumstick	Milk	\rightarrow
Fruit	Blank	Swizzels	White	\rightarrow
Fruit	Milk	Swizzels	White	\leftarrow
Fruit	White	Fruit	Milk	\leftarrow
Swizzels	Blank	Stop	Blank	\rightarrow
Swizzels	Milk	Swizzels	Milk	\leftarrow
Swizzels	White	Swizzels	White	\leftarrow

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- ➤ A machine, language or system is Turing complete if it can simulate a Turing machine





