

COMP110: Principles of Computing

2: Basic Principles for Computation

Learning outcomes

By the end of this week's sessions, you should be able to:

- ▶ **Use** binary, decimal and hexadecimal notation to represent and operate on numerical values
- ▶ **Explain** the basic architecture of a computer
- ▶ **Distinguish** the most common programming languages and paradigms in use today

Research journal

Research journal

- ▶ **Read** some seminal papers in computing (listed on the assignment brief)
- ▶ **Choose** one of them
- ▶ **Research** how this paper has influenced the field of computing
- ▶ **Write up** your findings
 - ▶ Maximum 1500 words
 - ▶ With reference to appropriate academic sources

Marking rubric

See assignment brief on LearningSpace/GitHub

Timeline

- ▶ **Peer review** in week 11 (4th December)
- ▶ **Deadline** shortly after (check MyFalmouth)
- ▶ Finding and reading academic papers takes time and effort — don't leave it until the last minute!

Binary notation

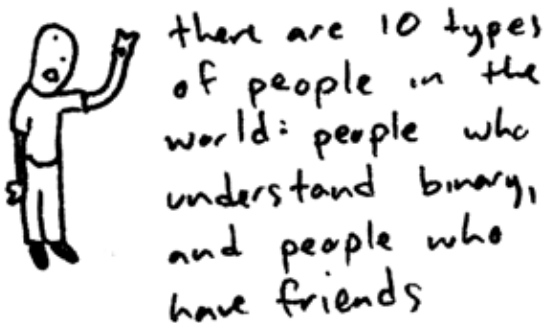


Image credit: <http://www.toothpastefordinner.com>

How we write numbers

- ▶ We write numbers in **base 10**
- ▶ We have 10 **digits**: 0, 1, 2, ..., 8, 9
- ▶ When we write 6397, we mean:
 - ▶ Six thousand, three hundred and ninety seven
 - ▶ (Six thousands) and (three hundreds) and (nine tens) and (seven)
 - ▶ $(6 \times 1000) + (3 \times 100) + (9 \times 10) + (7)$
 - ▶ $(6 \times 10^3) + (3 \times 10^2) + (9 \times 10^1) + (7 \times 10^0)$
 - ▶

Thousands	Hundreds	Tens	Units
6	3	9	7

Binary

- ▶ Binary notation works the same, but is **base 2** instead of **base 10**
- ▶ We have 2 **digits**: 0, 1
- ▶ When we write 10001011 in binary, we mean:
$$\begin{aligned}& (1 \times 2^7) + (0 \times 2^6) + (0 \times 2^5) + (0 \times 2^4) \\& + (1 \times 2^3) + (0 \times 2^2) + (1 \times 2^1) + (1 \times 2^0) \\& = 2^7 + 2^3 + 2^1 + 2^0 \\& = 128 + 8 + 2 + 1 \text{ (base 10)} \\& = 139 \text{ (base 10)}\end{aligned}$$

Converting to binary

https://www.youtube.com/watch?v=OezK_zTyvAQ

Bits, bytes and words

- ▶ A **bit** is a binary digit
 - ▶ Can store a 0 or 1 (i.e. a boolean value)
- ▶ A **byte** is 8 **bits**
 - ▶ Can store a number between 0 and 255 in binary
- ▶ A **word** is the number of bits that the CPU works with at once
 - ▶ 32-bit CPU: 32 bits = 1 word
 - ▶ 64-bit CPU: 64 bits = 1 word
- ▶ An n -bit word can store a number between 0 and $2^n - 1$
 - ▶ $2^{16} - 1 = 65,535$
 - ▶ $2^{32} - 1 = 4,294,967,295$
 - ▶ $2^{64} - 1 = 18,446,744,073,709,551,615$

Addition with carry

In base 10:

$$\begin{array}{rcccc} & 1 & 2 & 3 & 4 \\ + & 5 & 6_1 & 7_1 & 8 \\ \hline & 6 & 9 & 1 & 2 \end{array}$$

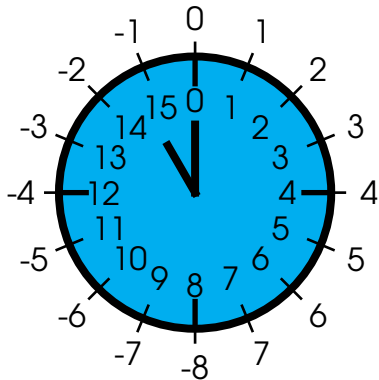
Addition with carry

In base 2:

$1 + 1 = 10$	$1 + 1 + 1 = 11$
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	0	1	1	0	1	1	1	0
+	0 ₁	0 ₁	1	0 ₁	0 ₁	1 ₁	1	1
<hr/>								
	1	0	0	1	0	1	0	1

Modular arithmetic



- ▶ Arithmetic **modulo** N
- ▶ Numbers “wrap around” between 0 and $N - 1$
- ▶ E.g. modulo 16:
 - ▶ $14 + 7 = 5$
 - ▶ $4 - 7 = 13$

2's complement

- ▶ How can we represent negative numbers in binary?
- ▶ Represent them modulo 2^n (for n bits)
- ▶ I.e. represent $-a$ as $2^n - a$
- ▶ Instead of an n -bit number ranging from 0 to $2^n - 1$, it ranges from -2^{n-1} to $+2^{n-1} - 1$
- ▶ E.g. 16-bit number ranges from -32768 to $+32767$
- ▶ Note that the left-most bit can be interpreted as a **sign** bit: 1 if negative, 0 if positive or zero

Converting to 2's complement

- ▶ Convert the absolute value to binary
- ▶ Invert all the bits (i.e. change $0 \leftrightarrow 1$)
- ▶ Add 1
- ▶ (This is equivalent to subtracting the number from 2^n ... why?)

Why 2's complement?

- ▶ Allows all addition and subtraction to be carried out modulo 2^n without caring whether numbers are positive or negative
- ▶ In fact, subtraction can just be done as addition
- ▶ I.e. $a - b$ is the same as $a + (-b)$, where a and $-b$ are just n -bit numbers

Exercise Sheet i

Due next Tuesday!