

COMP250: Artificial Intelligence
6: Navigation

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Pathfinding

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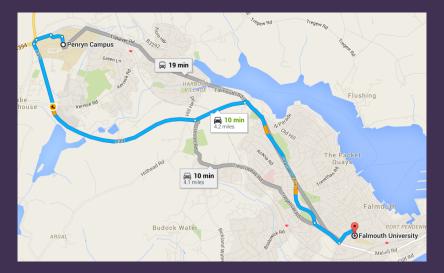
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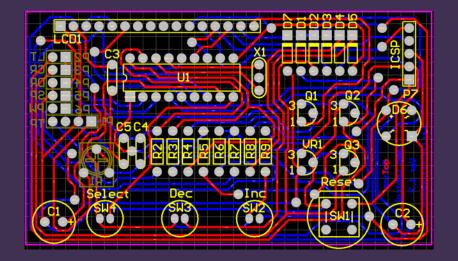
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 - "Shortest" in terms of edge lengths could be distance, time, fuel cost, ...









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- ▶ Puzzle solving

Pathfinding example

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- ► Open 06_pathfinding in PyCharm

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 - ... but implementations are available for all popular programming languages

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- Recall: can be implemented with a stack or a queue respectively
- Inefficient generally has to explore the entire map
- Finds a path, but probably not the shortest

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- Not guaranteed to find the shortest path

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 - ightharpoonup Contrast with greedy search, which just minimises h(x)

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 - Heuristics are often used to prioritise search, i.e. explore the most promising options first

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- Different h(x) can lead to different paths (if there are multiple "shortest" paths)

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 - Repeat until there are no more points that can be removed



Navigation meshes



Pathfinding in videogames

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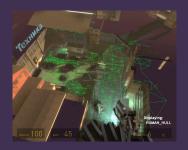
Pathfinding in videogames

- ▶ A* works on any graph
- But what if the game world is not a graph? E.g. complex 3D environments





 Manually place graph nodes in the world



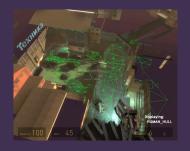
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 - No good for dynamic environments



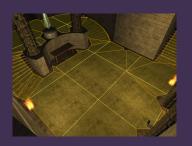




 Automatically generate navigation graph from level geometry



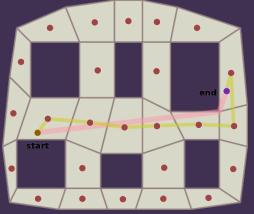
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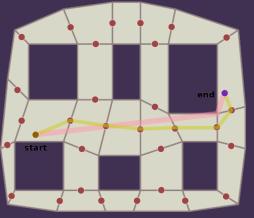
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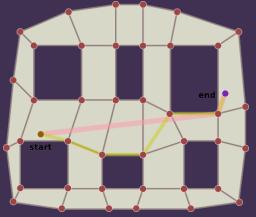
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 - Generate graph from polygons



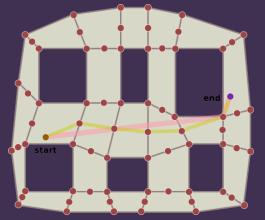
Centres of polygons



Centres of edges



Vertices of polygons



Hybrid approach: edges and vertices

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- Dynamic environments: may need to re-run pathfinder if environment changes (e.g. movable obstacles, destructible terrain)



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 - Pub crawls
 (http://www.math.uwaterloo.ca/tsp/pubs/)

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- Entire research field devoted to finding efficient search algorithms and heuristics