
COMP110: Principles of Computing

# 4: Logic and memory

# Worksheet 4

Due **next Friday!**

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# Scholarly literature

# Scholarly work

- What is a "scholarly" work?
- How do we know if something is scholarly?

# Pyramid of sources

# Appropriateness of sources

It is important to question the **appropriateness** of sources you use in academic work

- **Validity**: Are claims based upon a correct interpretation of the evidence?
- **Rigor**: Was the method of collecting evidence appropriate to ensure comprehensive coverage while also avoiding bias?

# Appropriateness of sources

- **Reliability**: has the claim been replicated, or at least reviewed, by other academics?
- **Authoritativeness**: do we know who the author is? Does the author have enough experience in the field to present a fair and balanced argument?
- **Venue**: Is the publisher reputable and free of undue editorial influences?

# Appropriateness of sources

There are of course exceptions where sources are presented as **artefacts** and/or **archives**:

- Citing a newspaper as evidence for a claim based on the reception of a new technology
- Citing a manufacturer's technical manual when describing a technical feature of a platform
- Citing a Reddit post by a well-known industry figure as evidence for expert opinion

The **way** in which sources are **used** is therefore important

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# Library resources

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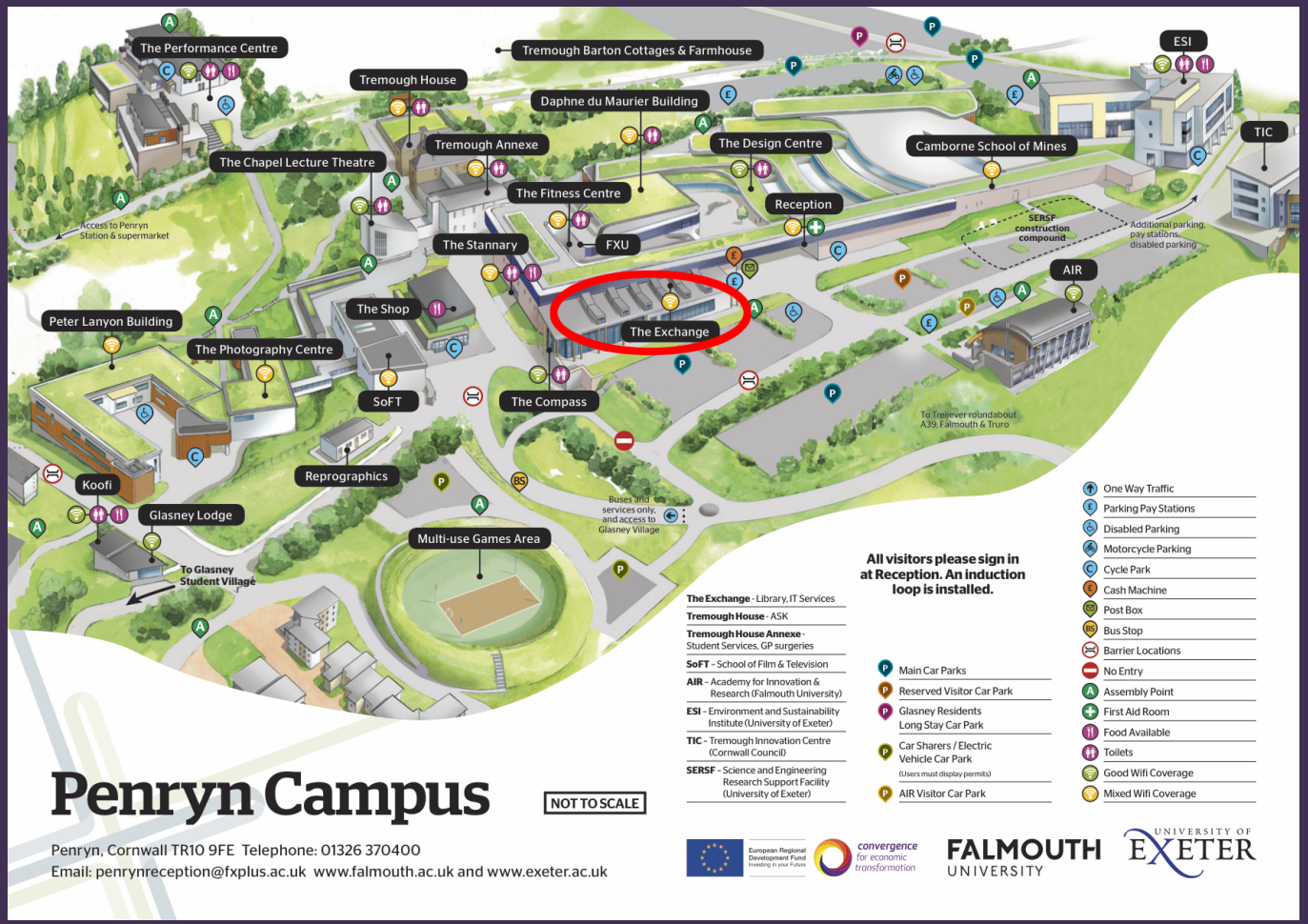
# The library




# Library catalogue

http://library.fxplus.ac.uk/

# Web proxy

- Some online resources are only available through the campus network
- If not physically on campus, you can access them via **VPN**
- `https://webvpn.falmouth.ac.uk/`
- Some resources can also be accessed by **web proxy** through the library website
- `https://library.fxplus.ac.uk/subject-guides/games/specialist-databases`

# ACM Digital Library

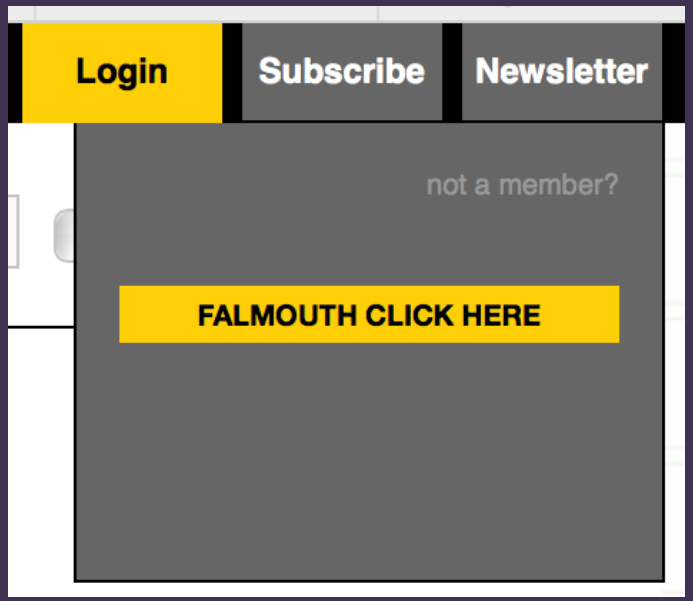
http://dl.acm.org.ezproxy.falmouth.ac.uk/

# IEEE Xplore

http://ieeexplore.ieee.org.ezproxy.falmouth.ac.uk/

# GDC Vault

http://www.gdcvault.com.ezproxy.falmouth.ac.uk/




There are only a limited number of login slots available —
**remember to log out when you have finished!**

# How to find papers to read?

- Specialist databases: ACM Digital Library, IEEE Xplore
- Google Scholar
  - Keyword searches
  - Other work by the same author
  - Work which has cited papers you have read
- Wikipedia
  - Not a reliable source itself!
  - However most articles have good bibiliographies
- Bibliographies of papers you have read

# Finding papers without paying

- Many papers are **paywalled**
- Little known fact: **none** of the money from paywalls goes to the authors of the paper!
- The university **subscribes** to ACM and IEEE to give free access to staff and students
- Many journals offer free **open access**
- Many authors put papers on their **personal websites**
- Many universities (all UK universities) have **open access repositories**
  - Falmouth: `http://repository.falmouth.ac.uk`
- Sites like **sci-hub** have sprung up, providing illegal downloads of papers

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# Referencing

# IEEE referencing style

https://ieeeauthorcenter.ieee.org/wp-content/uploads/IEEE-Reference-Guide.pdf

# BibTeX entry types

https://en.wikibooks.org/wiki/LaTeX/Bibliography_Management#BibTeX

# Writing BibTeX entries

- Some websites provide pre-written BibTeX entries for papers
- Beware of copying and pasting these as they are often incomplete, incorrectly formatted or just wrong!
- You must **always** check your bibliography in the compiled PDF and fix any errors
- You **will** lose marks on your written assignments otherwise!

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# Logic gates

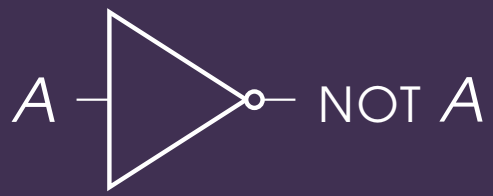
# Boolean logic

- Works with two values: TRUE and FALSE
- Foundation of the **digital computer**: represented in circuits as **on** and **off**
- Representing as 1 and 0 leads to **binary notation**
- One boolean value = one **bit** of information
- Programmers use boolean logic for conditions in `if` and `while` statements

# Not

NOT *A* is TRUE
if and only if
*A* is FALSE

| *A* | NOT *A* |
|---|---|
| FALSE | TRUE |
| TRUE | FALSE |



# And

*A* AND *B* is TRUE
if and only if
**both** *A* **and** *B* are TRUE

| *A* | *B* | *A* AND *B* |
|---|---|---|
| FALSE | FALSE | FALSE |
| FALSE | TRUE | FALSE |
| TRUE | FALSE | FALSE |
| TRUE | TRUE | TRUE |

# Or

*A* OR *B* is TRUE
if and only if
**either** *A* **or** *B*, **or both,** are TRUE

| *A* | *B* | *A* AND *B* |
|---|---|---|
| FALSE | FALSE | FALSE |
| FALSE | TRUE | TRUE |
| TRUE | FALSE | TRUE |
| TRUE | TRUE | TRUE |

# Socrative FALCOMPED

What is the value of

$$A \text{ AND } (B \text{ OR } C)$$

when

$$A = \text{TRUE}$$
$$B = \text{FALSE}$$
$$C = \text{TRUE}$$

?

# Socrative FALCOMPED

What is the value of

$$(\text{NOT } A) \text{ AND } (B \text{ OR } C)$$

when

$$A = \text{TRUE}$$
$$B = \text{FALSE}$$
$$C = \text{TRUE}$$

?

# Socrative FALCOMPED

For what values of $A, B, C, D$ is

$$A \text{ AND NOT } B \text{ AND NOT } (C \text{ OR } D) = \text{TRUE}$$

?

# Socrative FALCOMPED

What is the value of

*A* OR NOT *A*

?

# Socrative FALCOMPED

What is the value of

*A* AND NOT *A*

?

# Socrative FALCOMPED

What is the value of

*A* OR *A*

?

# Socrative FALCOMPED

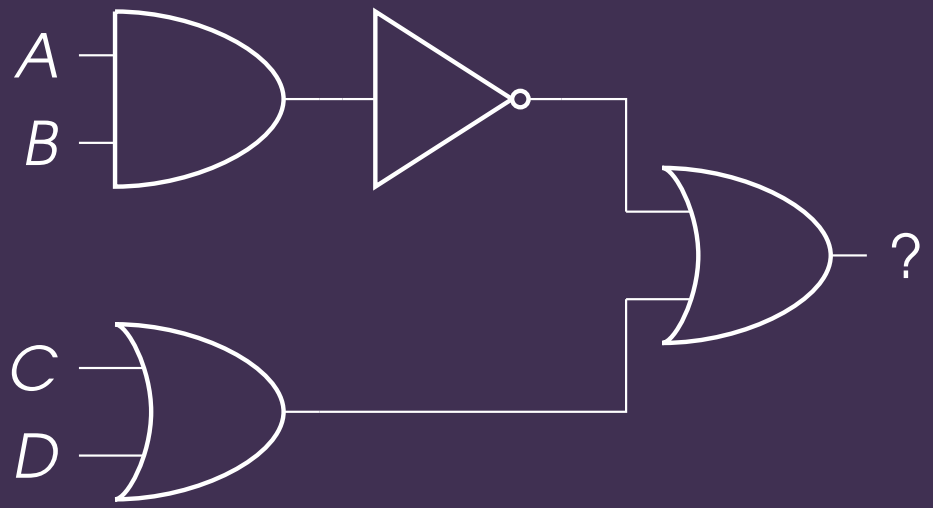
What is the value of

*A* AND *A*

?

# Socrative FALCOMPED

What expression is equivalent to this circuit?



# Writing logical operations

| Operation | Python | C family | Mathematics |
|---|---|---|---|
| NOT *A* | `not a` | `!a` | $\neg A$ or $\overline{A}$ |
| *A* AND *B* | `a and b` | `a && b` | $A \wedge B$ |
| *A* OR *B* | `a or b` | `a \|\| b` | $A \vee B$ |

Other operators can be expressed by combining these

# De Morgan's Laws

$$\text{NOT } (A \text{ OR } B) = (\text{NOT } A) \text{ AND } (\text{NOT } B)$$

$$\text{NOT } (A \text{ AND } B) = (\text{NOT } A) \text{ OR } (\text{NOT } B)$$

Proof: Worksheet 4, questions 3a and 3b

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# Truth tables

# Enumeration

- Since booleans have only two possible values, we can often **enumerate** all possible values of a set of boolean variables
- For $n$ variables there are $2^n$ possible combinations
- Essentially, all the $n$-bit binary numbers
- A **truth table** enumerates all the possible values of a boolean expression
- Can be used to prove that two expressions are equivalent

# Truth table example

(*A* OR NOT *B*) AND *C*

| *A* | *B* | *C* | NOT *B* | *A* OR NOT *B* | (*A* OR NOT *B*) AND *C* |
|---|---|---|---|---|---|
| FALSE | FALSE | FALSE | TRUE | TRUE | FALSE |
| FALSE | FALSE | TRUE | TRUE | TRUE | TRUE |
| FALSE | TRUE | FALSE | FALSE | FALSE | FALSE |
| FALSE | TRUE | TRUE | FALSE | FALSE | FALSE |
| TRUE | FALSE | FALSE | TRUE | TRUE | FALSE |
| TRUE | FALSE | TRUE | TRUE | TRUE | TRUE |
| TRUE | TRUE | FALSE | FALSE | TRUE | FALSE |
| TRUE | TRUE | TRUE | FALSE | TRUE | TRUE |

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# Other logic gates

# Exclusive Or

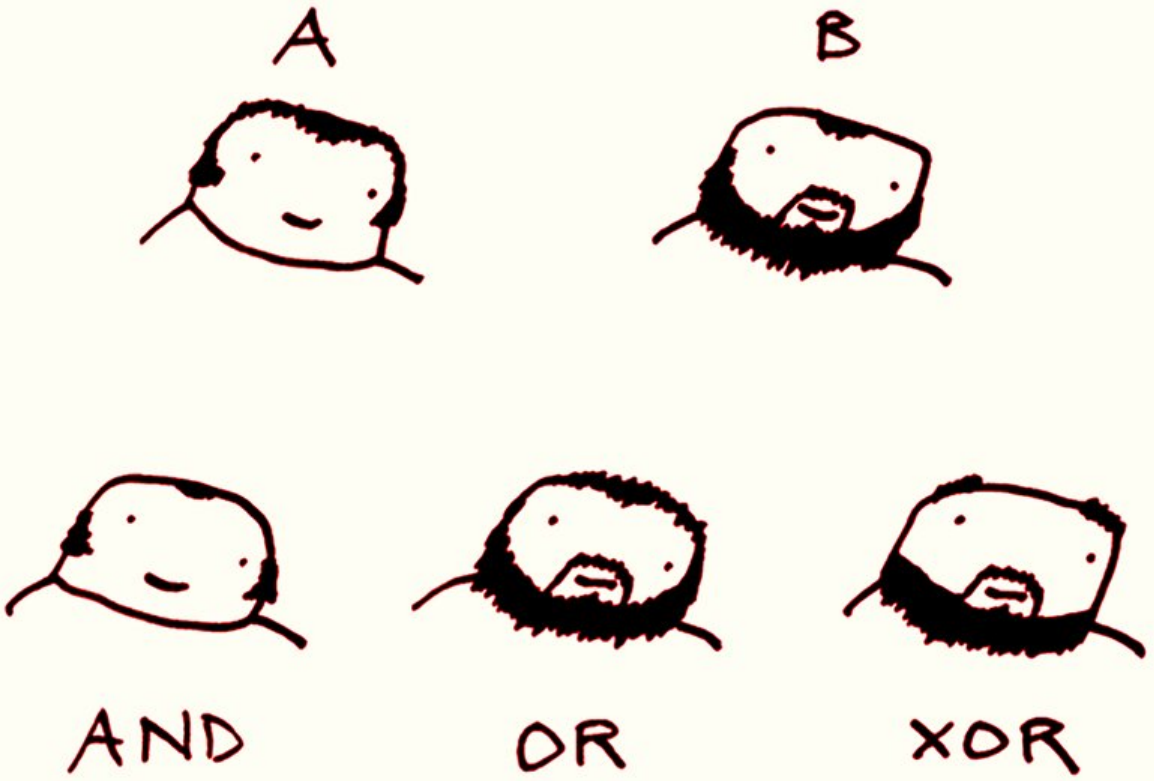
*A* XOR *B* is TRUE
if and only if
**either** *A* **or** *B*, **but not both,** are TRUE

| *A* | *B* | *A* AND *B* |
|---|---|---|
| FALSE | FALSE | FALSE |
| FALSE | TRUE | TRUE |
| TRUE | FALSE | TRUE |
| TRUE | TRUE | FALSE |

# Socrative FALCOMPED

How can *A* XOR *B* be written using the operations AND , OR , NOT ?

# BOOLEAN HAIR LOGIC



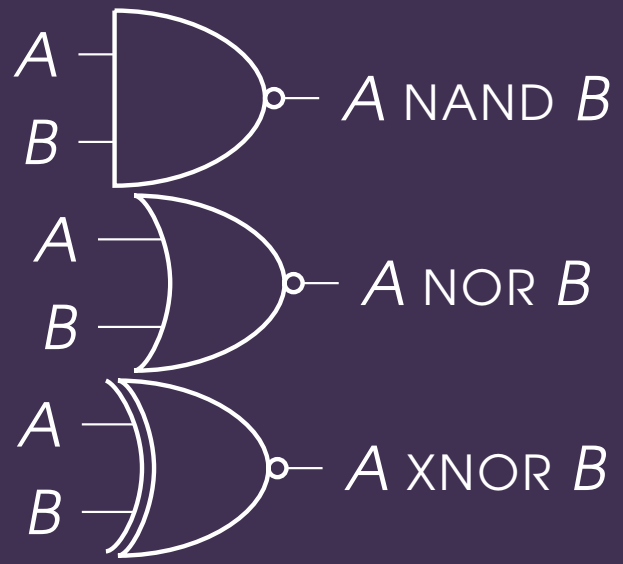
# Negative gates

NAND , NOR , XNOR
are the **negations** of
AND , OR , XOR

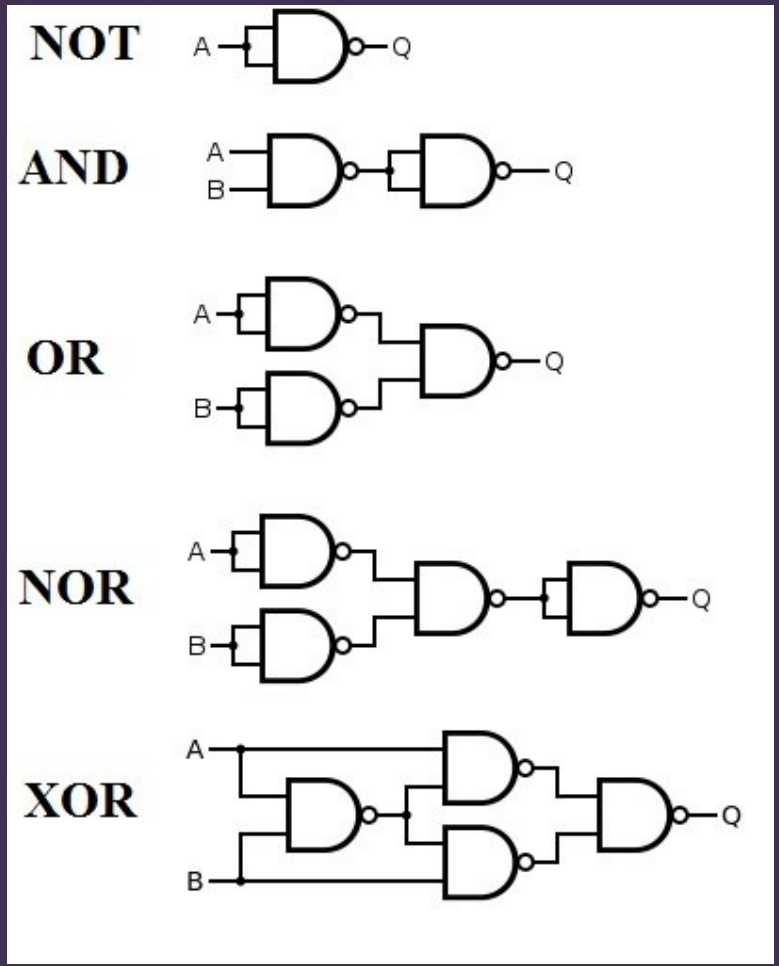
$A \text{ NAND } B = \text{NOT } (A \text{ AND } B)$

$A \text{ NOR } B = \text{NOT } (A \text{ OR } B)$

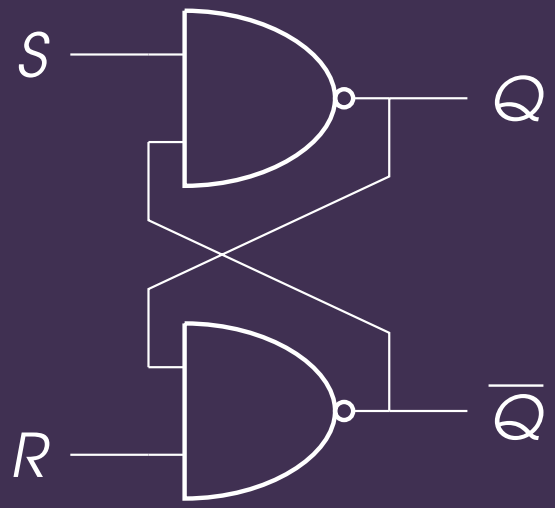
$A \text{ XNOR } B = \text{NOT } (A \text{ XOR } B)$



# Any logic gate can be constructed from NAND gates



# What does this circuit do?




- This is called a **NAND latch**
- It "remembers" a single boolean value
- Put a few billion of these together (along with some control circuitry) and you've got **memory**!

# NAND gates

- All arithmetic and logic operations, as well as memory, can be built from NAND gates
- So an entire computer can be built just from NAND gates!
- Play the game: `http://nandgame.com`
- NAND gate circuits are **Turing complete**
- The same is true of NOR gates

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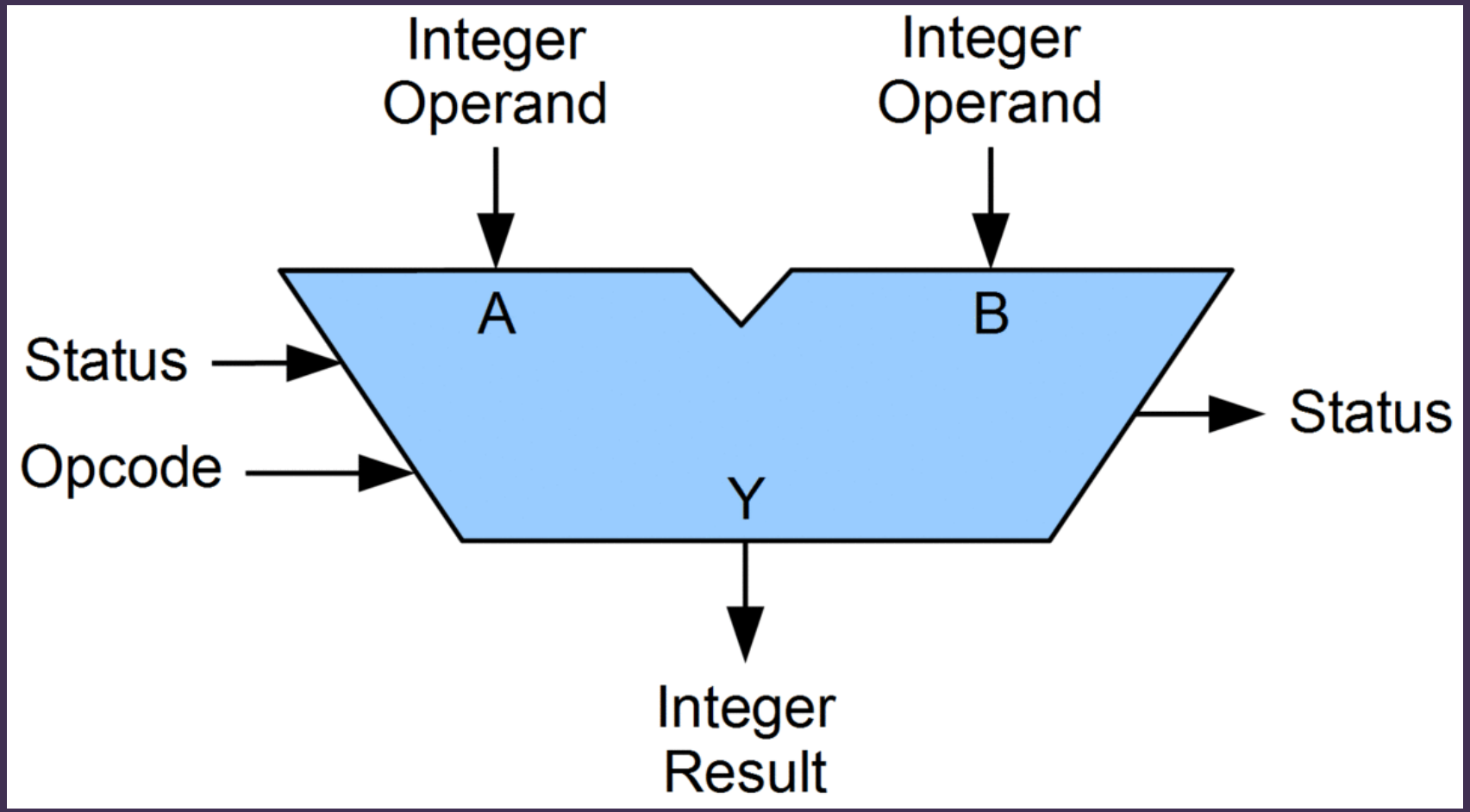
# Arithmetic Logic Unit

# Arithmetic Logic Unit



# Arithmetic Logic Unit

- Important part of the CPU
- Inputs:
  - **Operand** words *A*, *B*
  - **Opcode**
  - **Status** bits
- Outputs:
  - **Result** word *Y*
  - **Status** bits
- Opcode specifies how *Y* is calculated based on *A* and *B*

# ALU operations

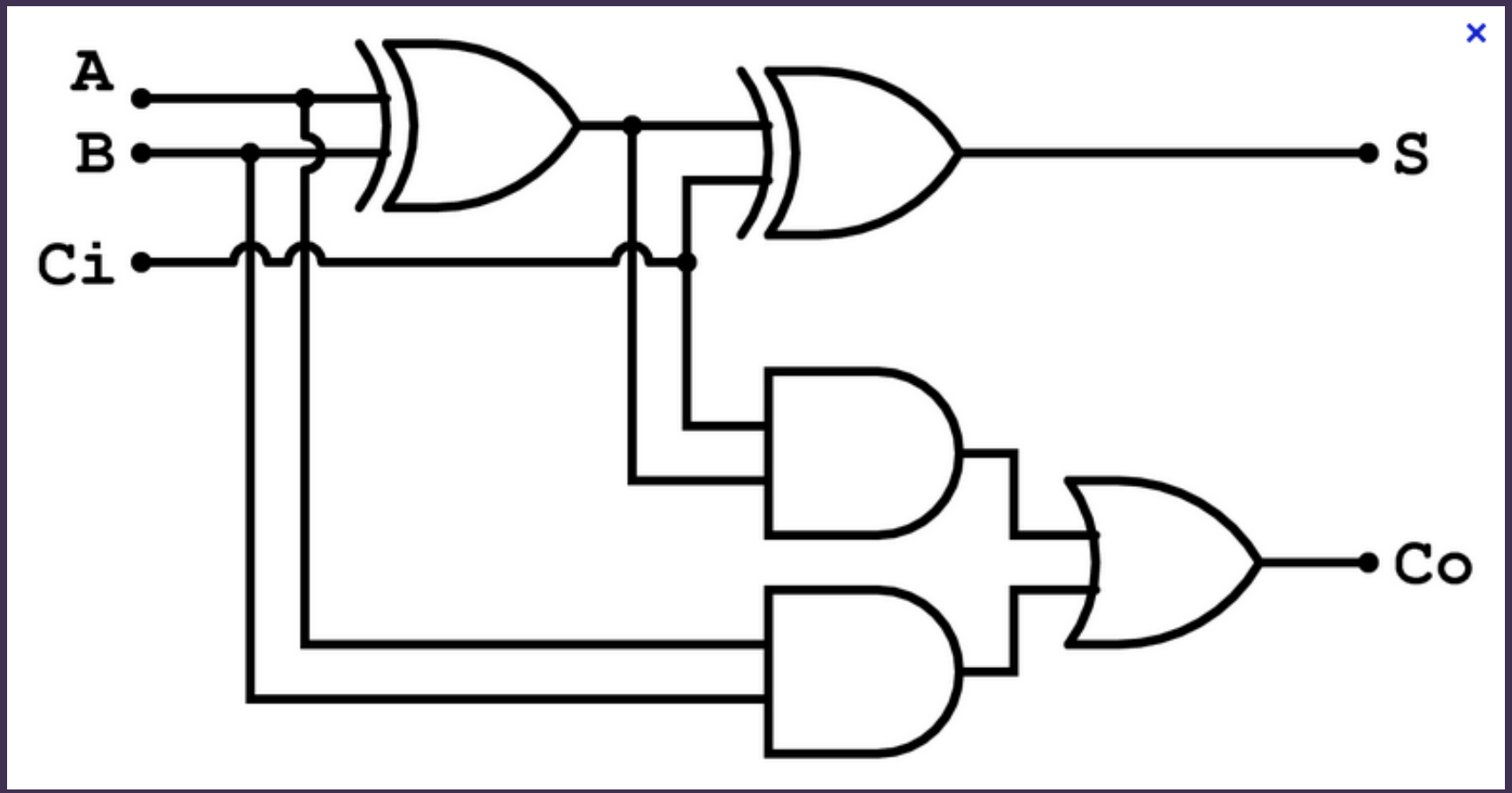
Typically include:

- Add with carry
- Subtract with borrow
- Negate (2's complement)
- Increment, decrement
- Bitwise AND, OR, NOT, ...
- Bit shifts

# Adding 3 bits

| $A$ | $B$ | $C$ | $A+B+C$ |
|---|---|---|---|
| 0 | 0 | 0 | 00 |
| 0 | 0 | 1 | 01 |
| 0 | 1 | 0 | 01 |
| 0 | 1 | 1 | 10 |
| 1 | 0 | 0 | 01 |
| 1 | 0 | 1 | 10 |
| 1 | 1 | 0 | 10 |
| 1 | 1 | 1 | 11 |

# 1-bit adder



# How does the 1-bit adder work?

Exercise:

- Write down the boolean expressions for *S* and *Co*
- Draw a truth table for these
- Compare the truth table to the addition table on a previous slide

# *n*-bit adder