



COMP110: Principles of Computing

11: Session title here

Learning outcomes

- ▶ Outcome 1
- ▶ Outcome 2
- ▶ Outcome 3

Modular arithmetic



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- ▶ This is because $20 = 6 \times 3 + 2$

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- ▶ E.g. $20 \div 5$ leaves a remainder of 0, but $14 \div 5$ leaves a remainder of 4, so

$$20 \not\equiv 14 \pmod{5}$$

Representing numbers



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This also works in Python and many other programming languages