



COMP220: Graphics & Simulation  
**7: Lighting**



# Learning outcomes

By the end of this week, you should be able to:

- ▶ **Explain** the Blinn-Phong illumination model
- ▶ **Describe** how effects such as normal mapping can be used to enhance appearance
- ▶ **Implement** basic lighting effects in your scene

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  - ▶ **Calculate** the colours in a lit scene using the Blinn-Phong model.
- ▶ Workshop (sync):
  - ▶ **Create** a light source and use it to illuminate objects in the scene.
  - ▶ **Recap** and **extend** the use of uniforms to pass data to shaders.

# Vector products



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$$\mathbf{a} \times \mathbf{b} = (|\mathbf{a}||\mathbf{b}| \sin \theta)\mathbf{n}$$

where  $n$  is a unit vector **perpendicular** to both  $a$  and  $b$   
with direction given by the **right-hand rule**

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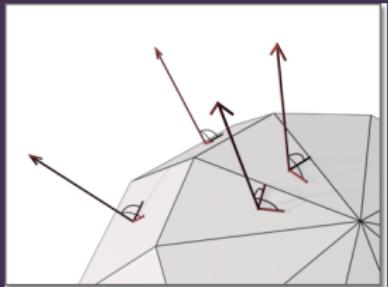
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- ▶ Cross product can be used to find a vector **perpendicular** to two others

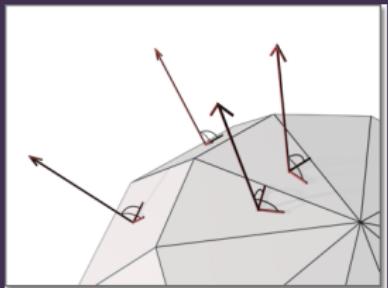
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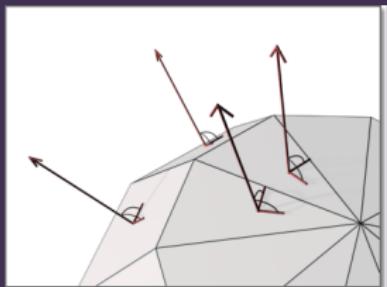


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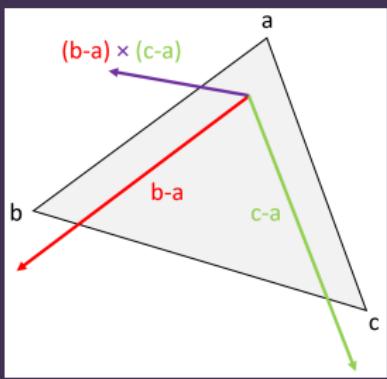


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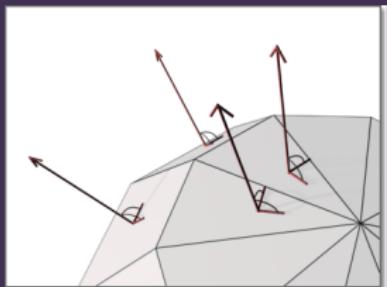
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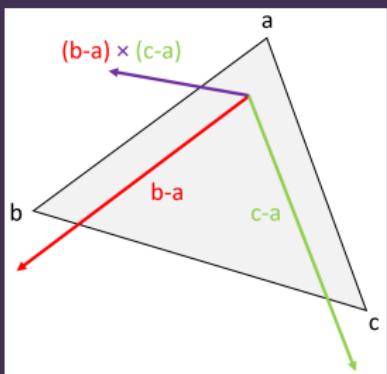
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- ▶ For a triangle with vertices  $a, b, c$ , two such vectors are  $b - a$  and  $c - a$
- ▶ So the normal is
$$\frac{n}{|n|} \quad \text{where} \quad n = (b - a) \times (c - a)$$



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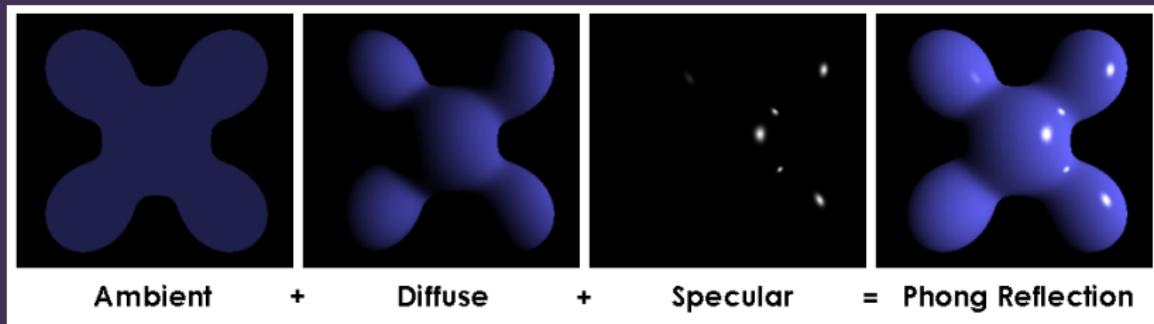
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- ▶ It breaks lighting down into three parts: **ambient**, **diffuse**, and **specular**.

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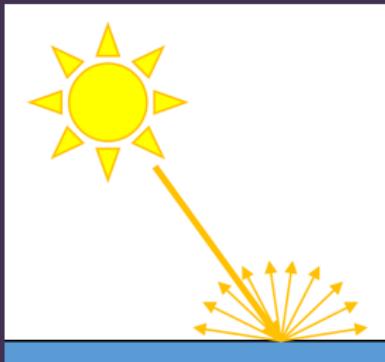
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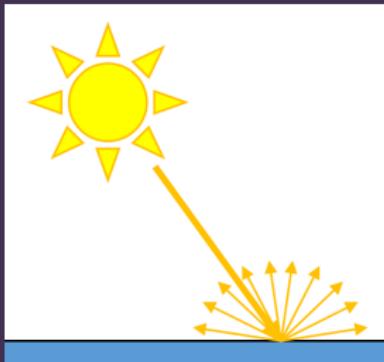
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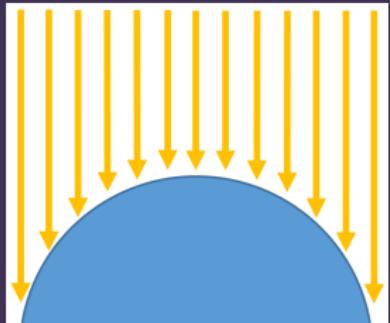
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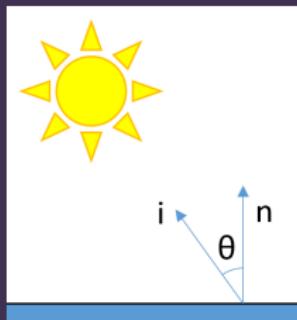


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The amount of light hitting the surface  
depends on the **angle** between the  
surface and the light source

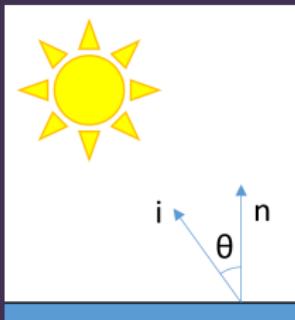


# Diffuse lighting formula



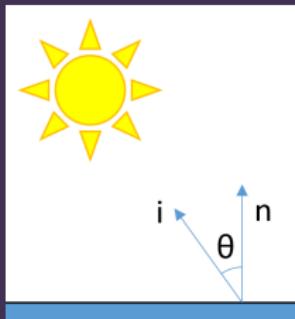
# Diffuse lighting formula

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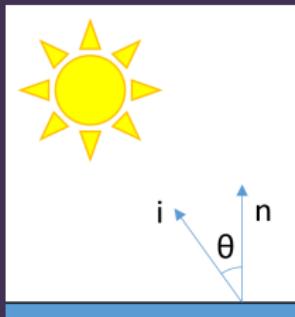
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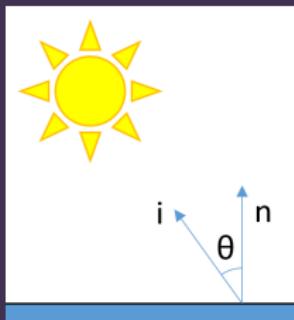


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- ▶ Let  $n$  be the normal, and  $i$  be a unit vector pointing towards the light source
- ▶ Light intensity is proportional to  $\cos \theta = n \cdot i$
- ▶ If the surface is **pointing away** from the light source, we get  $\theta > \frac{\pi}{2}$  so  $\cos \theta < 0$  — in this case we **clamp** the answer to 0

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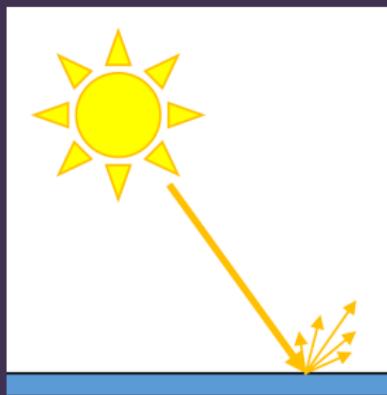
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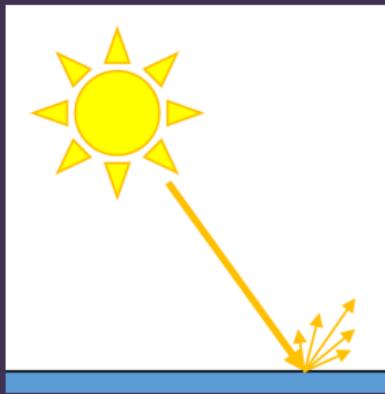
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  - ▶ These are known as **directional** lights
- ▶ For a **point** light source (e.g. a lightbulb):
  - ▶ Direction is calculated by subtracting the fragment position from the light position
  - ▶ Intensity is usually **attenuated**, e.g. using an **inverse square law**: if the distance between the fragment and the light source is  $d$ , then the light intensity is proportional to  $\frac{1}{d^2}$

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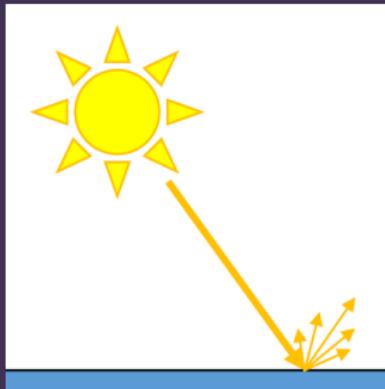


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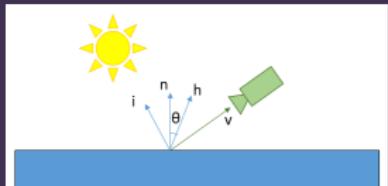
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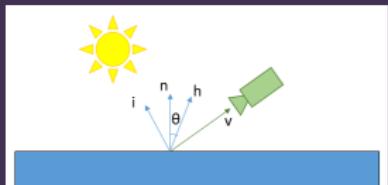


- ▶ When light hits a “smooth” surface, it is **reflected** across a narrow range of angles
- ▶ This creates a **specular highlight**, with intensity dependent on the **view direction** as well as the direction to the light source.

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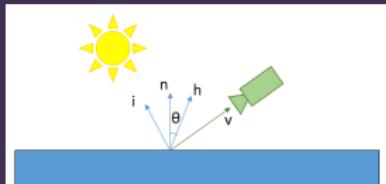


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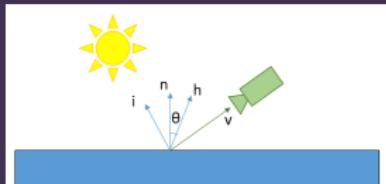
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- ▶ The closer  $h$  is to  $n$ , the higher the specular contribution.
- ▶ Specular light intensity is proportional to

$$\text{clamp}(n \cdot h)^s$$

where  $s$  is a “shininess” parameter, and  $\text{clamp}(x)$  clamps its argument between 0 and 1

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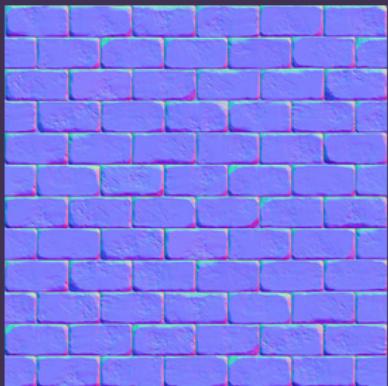
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- ▶ Another option would be to add more light sources...

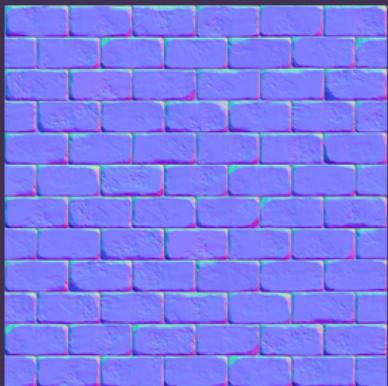
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- ▶ Can be used to add detail to flat, low-poly surfaces
- ▶ Can use textures to change other lighting parameters across a surface, e.g. **specular mapping**

# Next steps

- ▶ **Review** the additional asynchronous material for more background on different lighting models and effects.
- ▶ **Attend** the workshop to practice creating light sources and using them to illuminate the scene.