COMP110: Principles of Computing

8: Data Structures

Learning outcomes

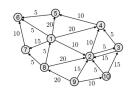
- Define the key concepts of graph theory
- Distinguish advanced data structures such as trees,
 DAGs and graphs
- Determine the complexity of accessing and manipulating data in these data structures
- ► Choose the correct data structure for a given task

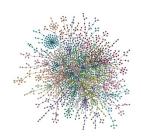
Exercise Sheet iii

Due **tomorrow**

Graphs

Graphs





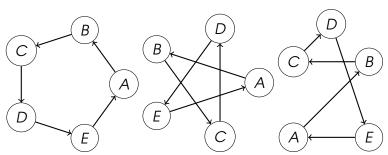
- A graph is defined by:
 - A collection of nodes or vertices (points)
 - A collection of edges or arcs (lines or arrows between points)
- Often used to model networks (e.g. social networks, transport networks, game levels, automata, ...)
- ▶ Directed graph: edges are arrows
- Undirected graph: edges are lines

Implementing graphs

- A graph has a set of nodes and a set of edges
- Each edge has exactly two nodes associated with it (e.g. "from" and "to")

Drawing graphs

- ▶ A graph does not necessarily specify the physical positions of its nodes
- ► E.g. these are technically the same graph:

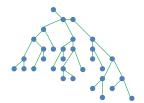


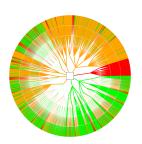
Planar graphs

- A graph is planar if it can be drawn with no overlapping edges
- ► A region enclosed by edges is called a faces
- ► A connected planar graph obeys **Euler's formula**:

$$n_{\text{nodes}} - n_{\text{edges}} + n_{\text{faces}} = 2$$

Trees





- ▶ A tree is a special type of directed graph where:
 - One node (the root) has no incoming edges
 - All other nodes have exactly 1 incoming edge
- Edges go from parent to child
 - All nodes except the root have exactly one parent
 - Nodes can have 0, 1 or many children
- Used to model hierarchies (e.g. file systems, object inheritance, scene graphs, state-action trees, ...)

Implementing trees

- A graph has a root node
- ► Each node has a collection of children
- Each node other than the root has a single parent

Stacks and queues

Stacks and queues





- A stack is a last-in first-out (LIFO) data structure
- Items can be pushed to the top of the stack
- Items can be popped from the top of the stack
- A queue is a first-in first-out (LIFO) data structure
- Items can be enqueued to the back of the queue
- Items can be dequeued from the front of the queue

Lists in Python

- ► Implemented as a (variable-sized) array
- ► Appending is O(1)
- ▶ Inserting is O(n)
- ▶ Deleting is O(n)

Stacks in Python

- Stacks can be implemented efficiently as lists
- append method adds an element to the end of the list
 - What is the time complexity?
- pop method removes and returns the last element of the list
 - What is the time complexity?

Queues in Python

- Queues can be implemented as lists, but not efficiently
- ► Could use append(item) to enqueue and pop(0) to dequeue
 - ▶ What is the time complexity of pop(0)?
- ► Could use insert (0, item) to enqueue and pop() to dequeue
 - What is the time complexity of insert (0, item)?
- deque (from the collections module) implements an efficient double-ended queue
- ► Provides methods append, appendleft, pop, popleft
 - All of which are O(1)

Stacks and function calls

- Stacks are used to implement nested function calls
- ► Each invocation of a function has a **stack frame**
- ► This specifies information like local variable values and return address
- ► Calling a function **pushes** a new frame onto the stack
- Returning from a function pops the top frame off the stack

Graph traversal

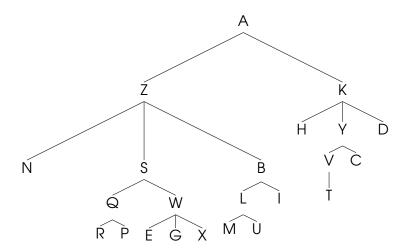
Tree traversal

- ▶ Traversal: visiting all the nodes of the tree
- ► Two main types
 - Depth first
 - Breadth first

Tree traversal

```
procedure DepthFirstSearch
   let S be a stack
   push root node onto S
   while S is not empty do
      pop n from S
      print n
      push children of n onto S
   end while
end procedure
procedure BreadthFirstSearch
   let Q be a queue
   enqueue root node into Q
   while Q is not empty do
      dequeue n from Q
      print n
      enqueue children of n into Q
   end while
end procedure
```

Tree traversal example



Recursive depth first search

```
procedure DEPTHFIRSTSEARCH(n)
print n
for each child c of n do
DEPTHFIRSTSEARCH(c)
end for
end procedure
```

Compare to the pseudocode on the previous slide. Where is the stack?

Linked lists

Linked list

- Composed of a number of nodes
- ► Each node contains:
 - An item the actual data to be stored
 - A pointer or reference to the **next node** in the list (null for the last item)



Linked lists vs arrays

Operation	Array	Linked list
Append	<i>O</i> (1)	O(1) 1
Pop	<i>O</i> (1)	O(1) 1
Index lookup	<i>O</i> (1)	O(n)
Count elements	<i>O</i> (1)	O(n)
Insert	O(n)	O(1) ²
Delete	O(n)	O(1) ²

¹If we already have a reference to the last node

²If we already have a reference to the relevant node

Implementing a linked list