



COMP220: Graphics & Simulation
6: Materials and Lighting

Learning outcomes

- ▶ **Explain** the Blinn-Phong illumination model
- ▶ **Implement** Blinn-Phong illumination in your own programs
- ▶ **Describe** how effects such as normal mapping can be used to render realistic materials

Vector products



Dot and cross product

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$$\mathbf{a} \times \mathbf{b} = (|\mathbf{a}||\mathbf{b}| \sin \theta)\mathbf{n}$$

where n is a unit vector **perpendicular** to both a and b
with direction given by the **right-hand rule**

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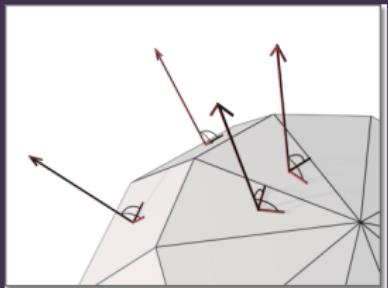
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- ▶ $\text{vector} \cdot \text{vector} = \text{number}$; $\text{vector} \times \text{vector} = \text{vector}$

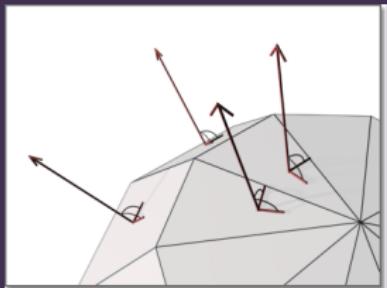
Surface normals

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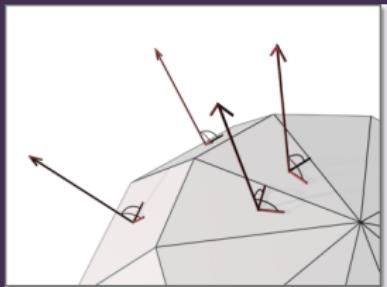


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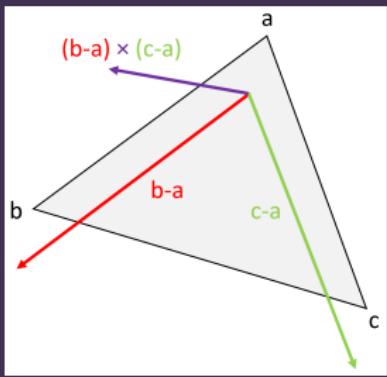


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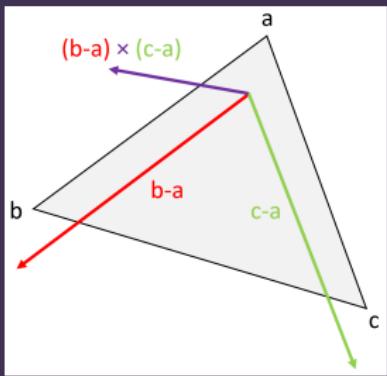
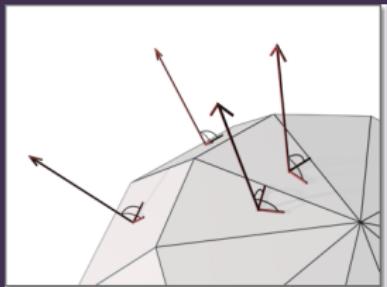
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- ▶ For a triangle with vertices a, b, c , two such vectors are $b - a$ and $c - a$
- ▶ So the normal is
$$\frac{n}{|n|} \quad \text{where} \quad n = (b - a) \times (c - a)$$

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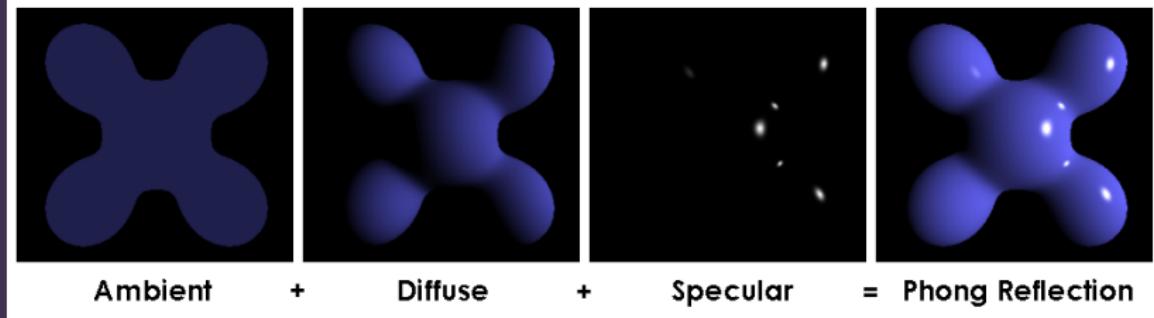
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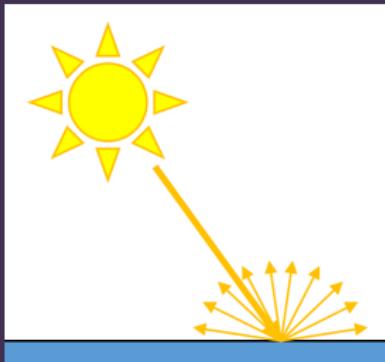
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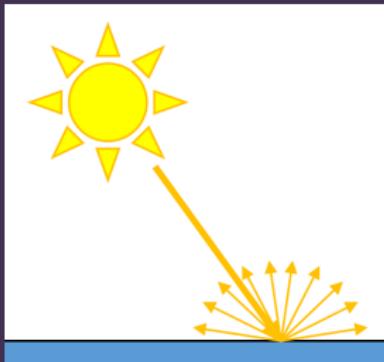
Diffuse lighting

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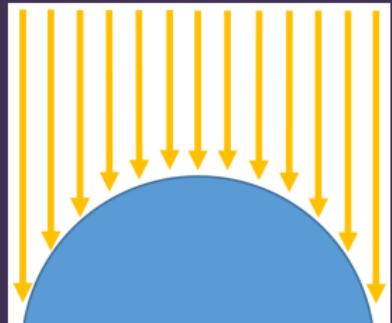
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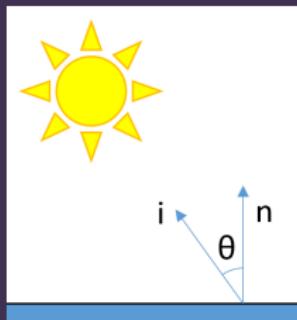


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The amount of light hitting the surface
depends on the **angle** between the
surface and the light source

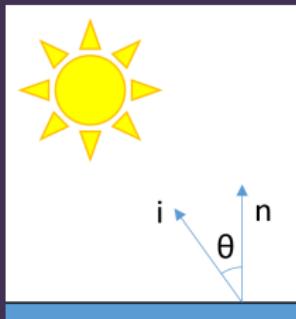


Diffuse lighting formula



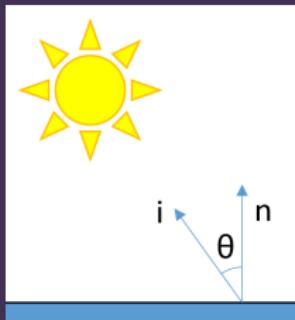
Diffuse lighting formula

- ▶ Light intensity is proportional to the **cosine** of the angle between the **light direction** and the **surface normal**



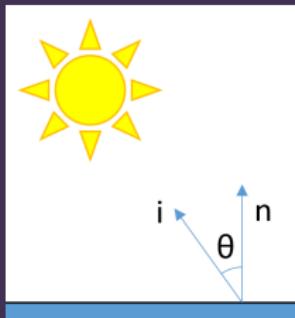
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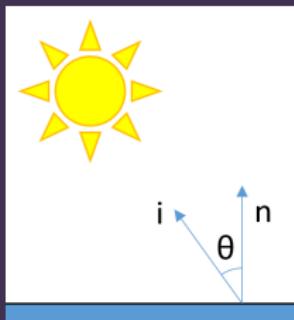


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- ▶ Let n be the normal, and i be a unit vector pointing towards the light source
- ▶ Light intensity is proportional to $\cos \theta = n \cdot i$
- ▶ If the surface is **pointing away** from the light source, we get $\theta > \frac{\pi}{2}$ so $\cos \theta < 0$ — in this case we **clamp** the answer to 0

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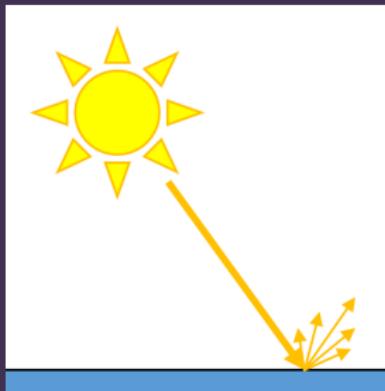
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 - ▶ Direction is calculated by subtracting the light position from the fragment position
 - ▶ Intensity obeys an **inverse square law**: if the distance between the fragment and the light source is d , then the light intensity is $\frac{1}{d^2}$

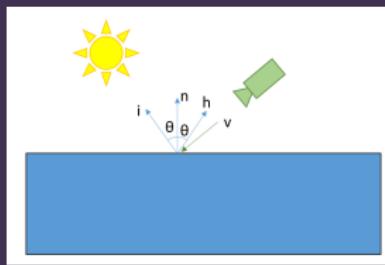
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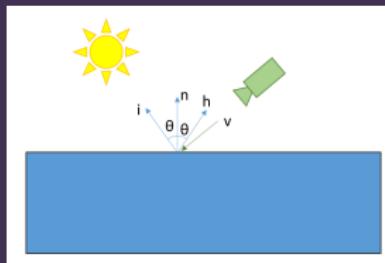


When light hits a “smooth” surface, it is **reflected** across a narrow range of angles

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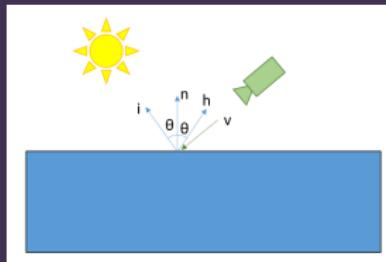


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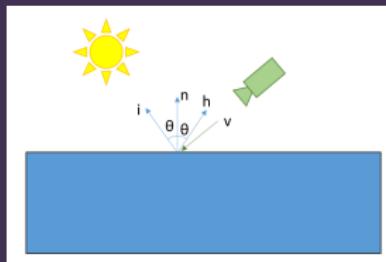
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- ▶ h can be thought of as the surface normal which leads to the maximum reflection in v
- ▶ Specular light intensity is proportional to

$$\text{clamp}(n \cdot h)^s$$

where s is a “shininess” parameter, and $\text{clamp}(x)$ clamps its argument between 0 and 1

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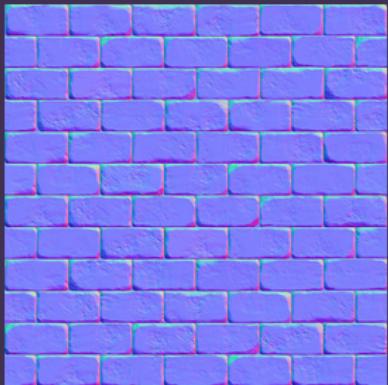
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- ▶ Another option would be to add more light sources...

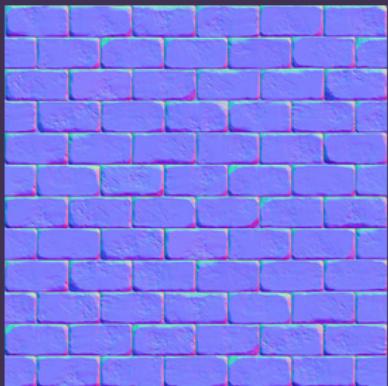
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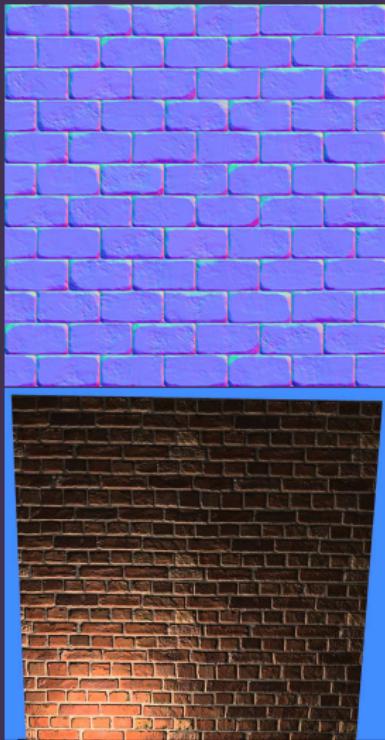
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- ▶ Can be used to add detail to flat, low-poly surfaces
- ▶ Can use textures to change other lighting parameters across a surface, e.g. **specular mapping**