



FALMOUTH
UNIVERSITY

COMP110: Principles of Computing

4: Logic and memory

Learning outcomes

- ▶ **Distinguish** the basic types of logic gate
- ▶ **Use** logic gates to build simple circuits
- ▶ **Explain** how computer memory works

Quiz B

Due **Friday 27th October**

Logic gates



Boolean logic

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- ▶ Foundation of the **digital computer**: represented in circuits as **on** and **off**
- ▶ Representing as 1 and 0 leads to **binary notation**
- ▶ One boolean value = one **bit** of information
- ▶ Programmers use boolean logic for conditions in **if** and **while** statements

Simulating logic circuits

<http://logic.ly/demo/>

Not

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NOT A is TRUE
if and only if
 A is FALSE

Not

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A	NOT A
FALSE	TRUE
TRUE	FALSE

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And

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A AND B is TRUE
if and only if
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Socratic FALCOMPED

What is the value of

$A \text{ AND } (B \text{ OR } C)$

when

$A = \text{TRUE}$

$B = \text{FALSE}$

$C = \text{TRUE}$

?

Socratic FALCOMPED

What is the value of

$(\text{NOT } A) \text{ AND } (B \text{ OR } C)$

when

$A = \text{TRUE}$

$B = \text{FALSE}$

$C = \text{TRUE}$

?

Socratic FALCOMPED

For what values of A, B, C, D is

$$A \text{ AND NOT } B \text{ AND NOT } (C \text{ OR } D) = \text{TRUE}$$

?

Socratic FALCOMPED

What is the value of

A OR NOT A

?

Socratic FALCOMPED

What is the value of

$A \text{ AND NOT } A$

?

Socratic FALCOMPED

What is the value of

$A \circ A$

?

Socratic FALCOMPED

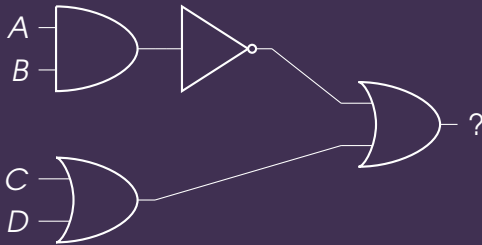
What is the value of

$A \text{ AND } A$

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Socratic FALCOMPED

What expression is equivalent to this circuit?



$\text{not}(A \text{ and } B) \text{ or } (C \text{ or } D)$

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Other operators can be expressed by combining these

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Socratic FALCOMPED

How can $A \text{ XOR } B$ be written using the operations
AND , OR , NOT ?

Negative gates

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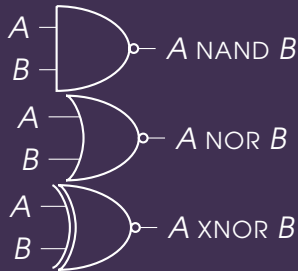
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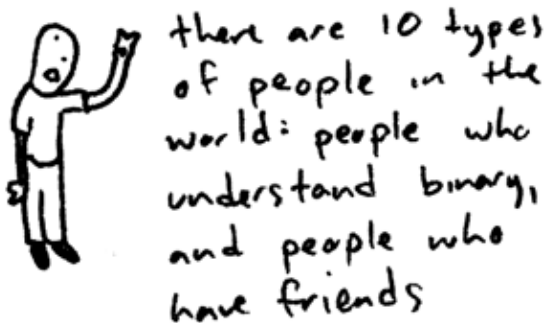


Image credit: <http://www.toothpastefordinner.com>

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 - ▶ $(6 \times 10^3) + (3 \times 10^2) + (9 \times 10^1) + (7 \times 10^0)$

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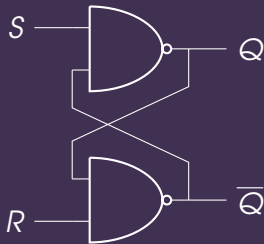
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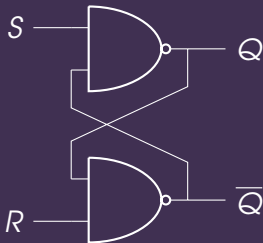
Computer memory



What does this circuit do?

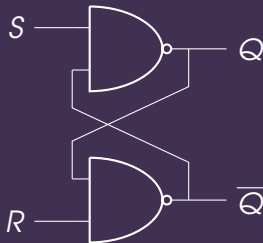


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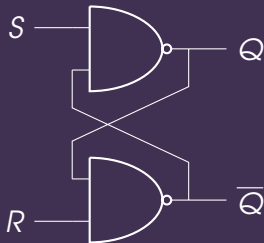
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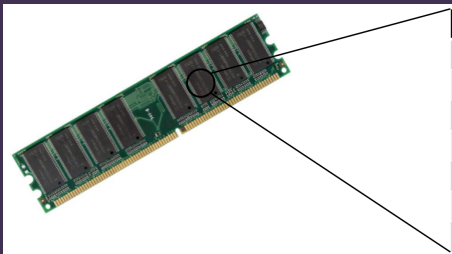
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- ▶ This is called a **NAND latch**
- ▶ It “remembers” a single boolean value
- ▶ Put a few billion of these together (along with some control circuitry) and you’ve got **memory!**

Memory

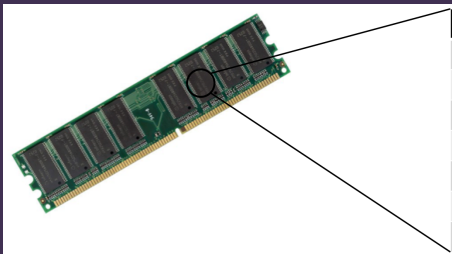
Memory



Address	Data
0	01001000
1	01100101
2	01101100
3	01101100
4	01101111
5	00100001
...	...

- ▶ Memory works like a set of **boxes**

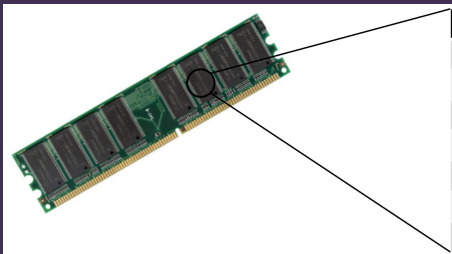
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- ▶ Each box contains a **byte** (8 bits)

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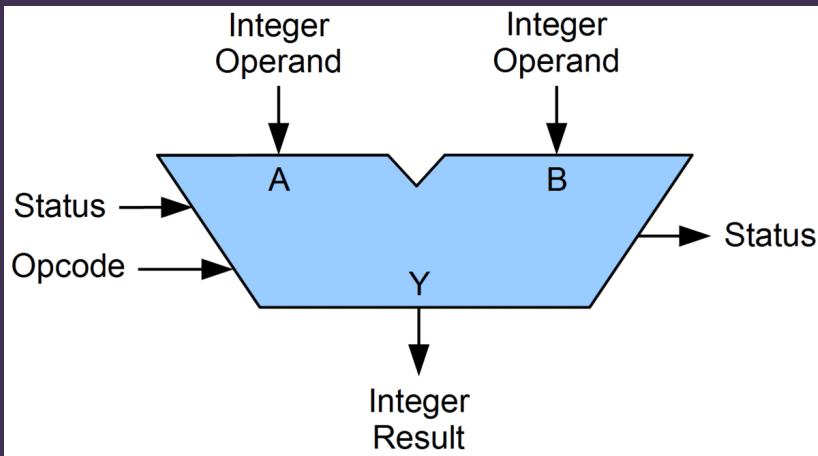
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 - ▶ Executable: sequence of machine code operations

Arithmetic Logic Unit



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- ▶ Opcode specifies how Y is calculated based on A and B

ALU operations

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- ▶ Subtract with borrow
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- ▶ Increment, decrement
- ▶ Bitwise AND, OR, NOT, ...
- ▶ Bit shifts

Addition with carry

In base 10:

$$\begin{array}{r} 1 \\ + 5 \\ \hline \end{array}$$

Addition with carry

In base 10:

$$\begin{array}{rcccc} & 1 & 2 & 3 & 4 \\ + & 5 & 6 & 7_1 & 8 \\ \hline & & & & 2 \end{array}$$

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$$\begin{array}{r} 1 2 3 4 \\ + 5 6_1 7_1 8 \\ \hline 6 9 1 2 \end{array}$$

Addition with carry

In base 2:

$$1 + 1 = 10 \quad 1 + 1 + 1 = 11$$

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+	0	0	1	0 ₁	0 ₁	1 ₁	1	1
				1	0	1	0	1

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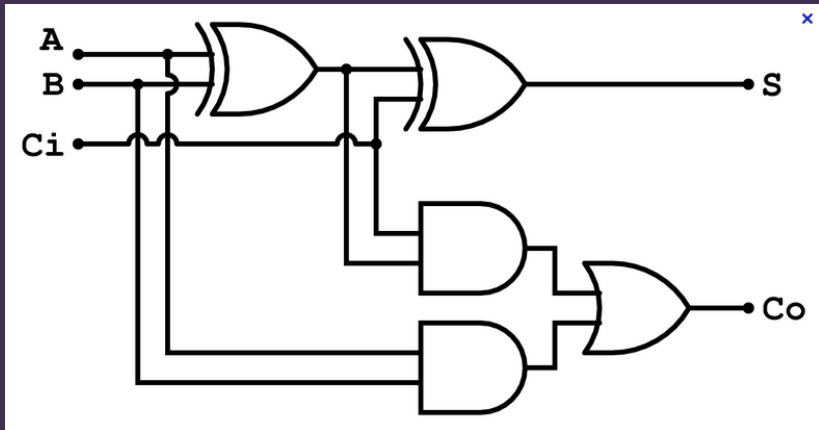
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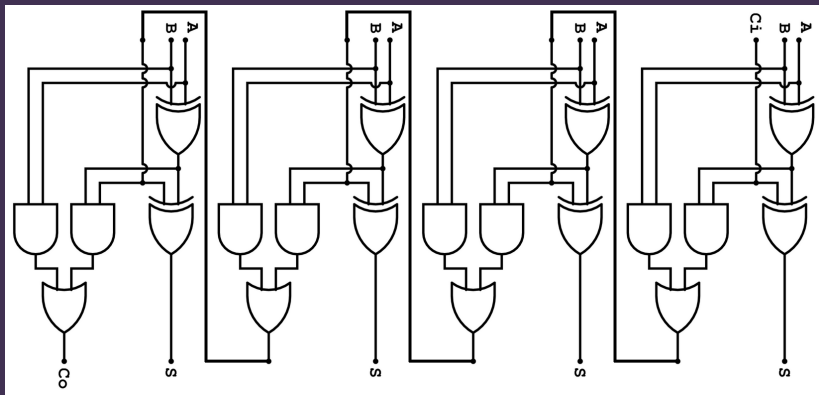
$$1 + 1 = 10 \quad 1 + 1 + 1 = 11$$

$$\begin{array}{r} 0 1 1 0 1 1 1 0 \\ + 0 0 1 0 0 1 1 1 \\ \hline 1 0 0 1 0 1 0 1 \end{array}$$

1-bit adder



n -bit adder



Worksheet B

