1. An NPC is standing at location with a forward direction of .
   1. How can the dot product be used to determine whether the point is in front of or behind the NPC?
   2. Let and . For each of the following points , determine whether is in front of or behind the NPC:
2. Extending the concept from question 3, consider the case where the NPC has a limited field of view (FOV). If the total FOV angle is , then the NPC can see to the left or the right of its forward direction by a maximum angle of .
   1. How can the dot product be used to determine whether the point is visible to the NPC?
   2. For each of the points in question 3b, determine whether is visible to the NPC if its FOV is 90°.
   3. Suppose that the NPC’s viewing distance is also limited to a maximum distance of 7 units. Which points are visible to the NPC then?
3. A bus travels along a straight road, heading east-north-east through the origin, observed by Alex, who is standing two units east and one unit south of the origin.  
   If the -axis points east and the -axis points north:
   1. Write the direction of the bus as a unit vector (magnitude 1).  
      Hint: *(proof* [*here*](https://www.math-only-math.com/exact-value-of-tan-22-and-half-degree.html)*)*
   2. Write the displacement of Alex from the origin as a vector .
   3. Use the dot product to determine how far from the origin the bus has travelled when it is closest to Alex.

Exercises may include some modified questions from

*3D Math Primer for Graphics and Game Development*,

Fletcher Dunn and Ian Parberry, CRC Press