



COMP702: Classical Artificial Intelligence

## **7: Navigation**

# Paper Club

For next week's session:

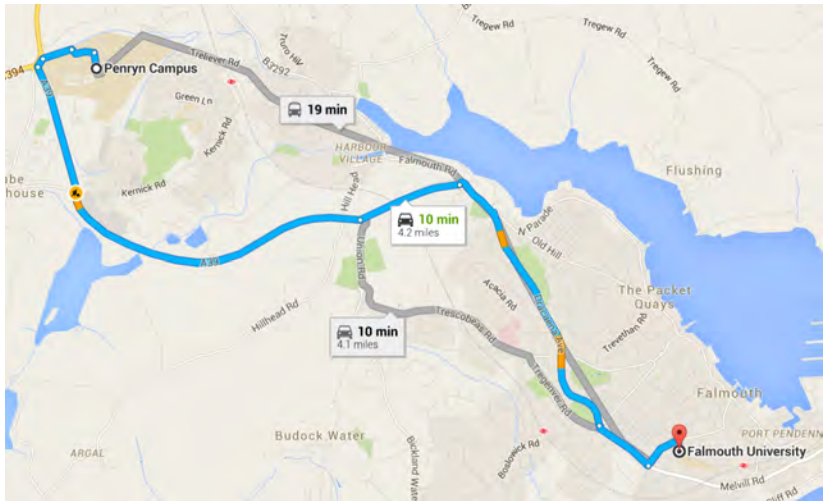
Nathan R. Sturtevant, Devon Sigurdson, Bjorn Taylor, Tim Gibson. Pathfinding and Abstraction with Dynamic Terrain Costs. Proceedings of AIIDE Conference, 2019.  
(PDF link on LearningSpace)

# Pathfinding

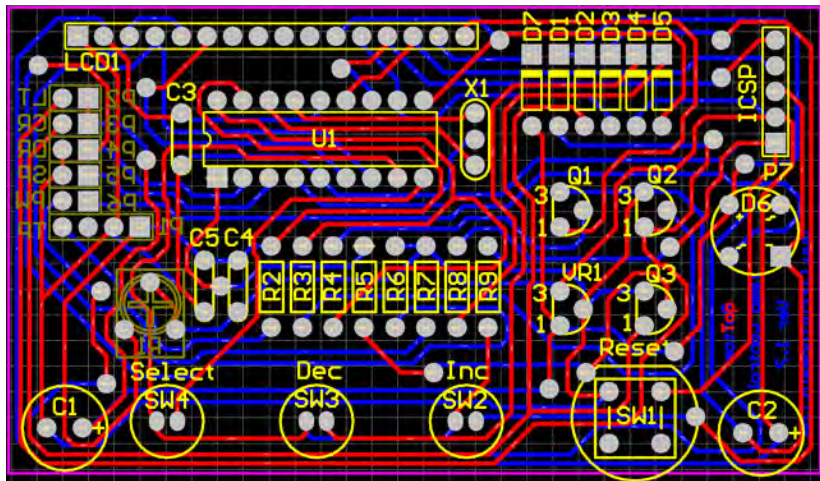
# The problem

- ▶ We have a **graph**
  - ▶ **Nodes** (points)
  - ▶ **Edges** (lines between points, each with a **length**)
- ▶ E.g. a road map
  - ▶ Nodes = addresses
  - ▶ Edges = roads
- ▶ E.g. a tile-based 2D game
  - ▶ Nodes = grid squares
  - ▶ Edges = connections between adjacent squares
- ▶ Given two nodes *A* and *B*, find the **shortest path** from *A* to *B*
  - ▶ “Shortest” in terms of edge lengths — could be distance, time, fuel cost, ...

# Applications of pathfinding



# Applications of pathfinding



# Applications of pathfinding



# Applications of pathfinding





# Applications of pathfinding



# Pathfinding as search

- ▶ Basic idea: build a **spanning tree** for the graph
- ▶ Root node is  $A$  (the start node)
- ▶ Edges in the tree are a **subset** of edges of the graph
- ▶ Once the tree includes  $B$ , we can read off the path from  $A$  to  $B$
- ▶ Need to keep track of two sets of nodes:
  - ▶ **Open set**: nodes within 1 edge of the tree, which could be added next
  - ▶ **Closed set**: nodes which have been added to the tree, and shouldn't be revisited (otherwise we could get stuck in an infinite loop)

# Graph traversal

- ▶ **Depth-first** or **breadth-first**
- ▶ Can be implemented with the open set as a **stack** or a **queue** respectively
- ▶ Inefficient — generally has to explore the **entire map**
- ▶ Finds a path, but probably not the **shortest**
- ▶ Third type of traversal: **best-first**
  - ▶ “Best” according to some heuristic evaluation
  - ▶ Often implemented with the open set as a **priority queue** — a data structure optimised for finding the **highest priority** item

# Greedy search

- ▶ Always try to move **closer** to the goal
- ▶ Visit the node whose **distance to the goal** is **minimal**
- ▶ E.g. **Euclidean** distance (straight line distance — Pythagoras' Theorem)
- ▶ Doesn't handle **dead ends** well
- ▶ Not guaranteed to find the **shortest** path

# Dijkstra's algorithm

- ▶ Let  $g(x)$  be the sum of edge weights of the path found from the start to  $x$
- ▶ Choose a node that minimises  $g(x)$
- ▶ Needs to handle cases where a shorter path to a node is discovered later in the search
- ▶ **Is** guaranteed to find the shortest path
- ▶ ... but is not the most efficient algorithm for doing so

# A\* search

- ▶ Let  $h(x)$  be an estimate of the distance from  $x$  to the goal (as in greedy search)
- ▶ Let  $g(x)$  be the distance of the path found from the start to  $x$  (as in Dijkstra's algorithm)
- ▶ Choose a node that minimises  $g(x) + h(x)$

# Properties of A\* search

- ▶ A\* is **guaranteed** to find the shortest path if the distance estimate  $h(x)$  is **admissible**
- ▶ Essentially, **admissible** means it must be an **underestimate**
  - ▶ E.g. straight line Euclidean distance is clearly an underestimate for actual travel distance
- ▶ The more accurate  $h(x)$  is, the more efficient the search
  - ▶ E.g.  $h(x) = 0$  is admissible (and gives Dijkstra's algorithm), but not very helpful
- ▶  $h(x)$  is a **heuristic**
  - ▶ In AI, a heuristic is an estimate based on human intuition
  - ▶ Heuristics are often used to prioritise search, i.e. explore the most promising options first

# Tweaking $A^*$

- ▶ Can change how  $g(x)$  is calculated
  - ▶ Increased movement cost for rough terrain, water, lava...
  - ▶ Penalty for changing direction
- ▶ Different  $h(x)$  can lead to different paths (if there are multiple “shortest” paths)



# String pulling

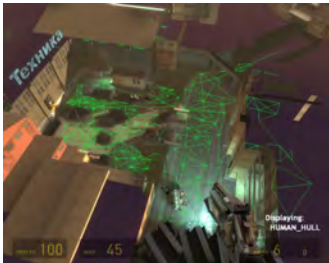
- ▶ Paths restricted to edges can look unnatural
- ▶ Intuition: visualise the path as a string, then pull both ends to make it taut
- ▶ Simple algorithm:
  - ▶ Found path is  $p[0], p[1], \dots, p[n]$
  - ▶ If the line from  $p[i]$  to  $p[i + 2]$  is unobstructed, remove point  $p[i + 1]$
  - ▶ Repeat until there are no more points that can be removed

# Navigation meshes

# Pathfinding in videogames

- ▶ A\* works on any **graph**
- ▶ But what if the game world is not a graph? E.g. complex 3D environments

# Waypoint navigation



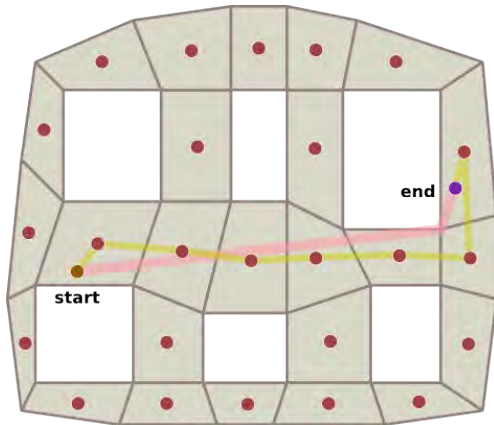
- ▶ Manually place graph nodes in the world
- ▶ Place them at key points, e.g. in doorways, around obstacles
- ▶ Works, but...
  - ▶ More work for level designers
  - ▶ Requires lots of testing and tweaking to get natural-looking results
  - ▶ No good for dynamic environments

# Navigation meshes



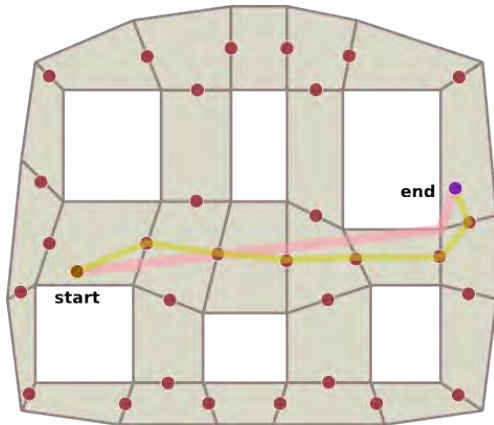
- ▶ Automatically generate navigation graph from level geometry
- ▶ Basic idea:
  - ▶ Filter level geometry to those polygons which are **passable** (i.e. floors, not walls/ceilings/obstacles)
  - ▶ Generate graph from polygons

# Meshes to graphs



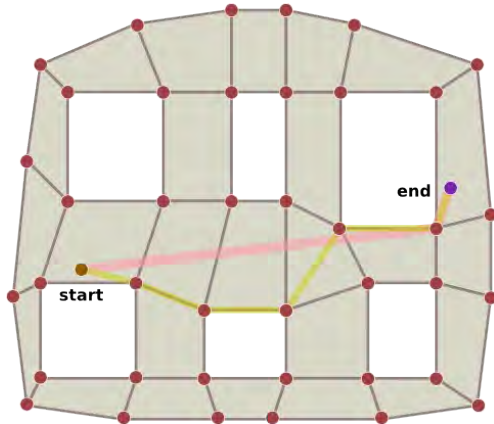
Centres of polygons

# Meshes to graphs



Centres of edges

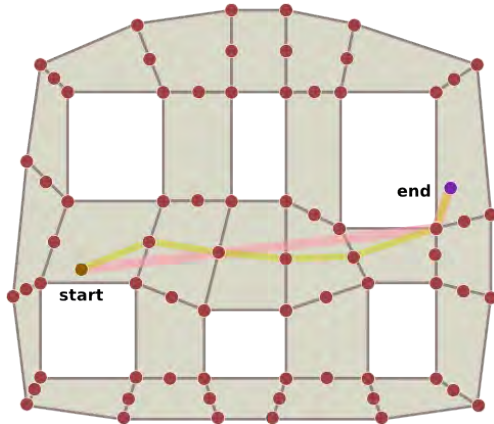
# Meshes to graphs



Vertices of polygons



# Meshes to graphs



Hybrid approach: edges and vertices

# Following the path

- ▶ **Funnelling:** like string pulling but for navigation meshes
  - ▶ <http://digestingduck.blogspot.co.uk/2010/03/simple-stupid-funnel-algorithm.html>
  - ▶ <http://jceipek.com/Olin-Coding-Tutorials/pathing.html>
- ▶ **Steering:** don't have your AI agent follow the path exactly, but instead try to stay close to it
- ▶ **Dynamic environments:** may need to re-run pathfinder if environment changes (e.g. movable obstacles, destructible terrain)