



FALMOUTH
UNIVERSITY



COMP702: Classical Artificial Intelligence

7: Navigation

Paper Club

For next week's session:

Nathan R. Sturtevant, Devon Sigurdson, Bjorn Taylor, Tim Gibson. Pathfinding and Abstraction with Dynamic Terrain Costs. Proceedings of AIIDE Conference, 2019.
(PDF link on LearningSpace)

Pathfinding



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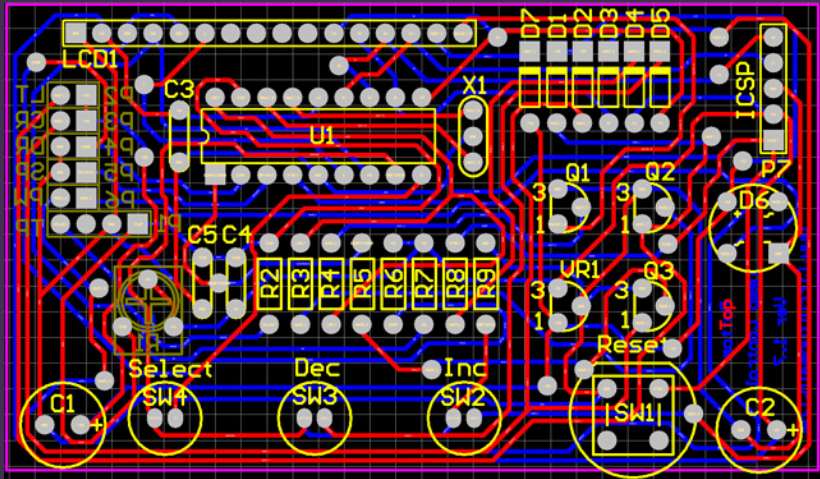
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 - ▶ “Shortest” in terms of edge lengths — could be distance, time, fuel cost, ...

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 - ▶ **Closed set**: nodes which have been added to the tree, and shouldn't be revisited (otherwise we could get stuck in an infinite loop)

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 - ▶ Often implemented with the open set as a **priority queue** — a data structure optimised for finding the **highest priority** item

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- ▶ ... but is not the most efficient algorithm for doing so

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 - ▶ In AI, a heuristic is an estimate based on human intuition
 - ▶ Heuristics are often used to prioritise search, i.e. explore the most promising options first

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- ▶ Different $h(x)$ can lead to different paths (if there are multiple “shortest” paths)

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 - ▶ Repeat until there are no more points that can be removed

Navigation meshes



Pathfinding in videogames

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- ▶ A* works on any **graph**
- ▶ But what if the game world is not a graph? E.g. complex 3D environments

Waypoint navigation



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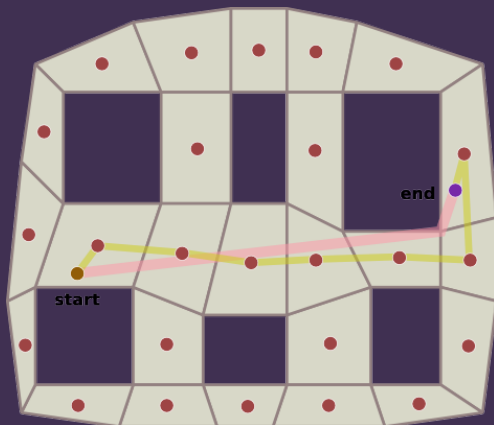
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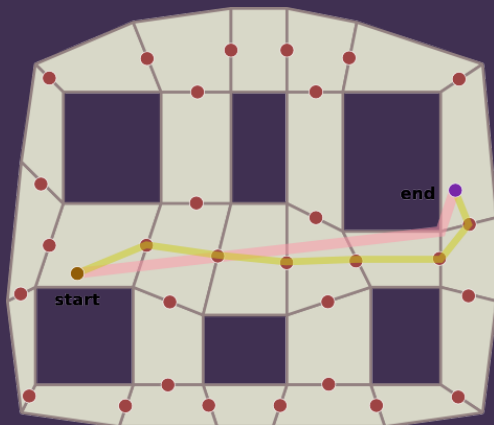
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 - ▶ Generate graph from polygons

Meshes to graphs



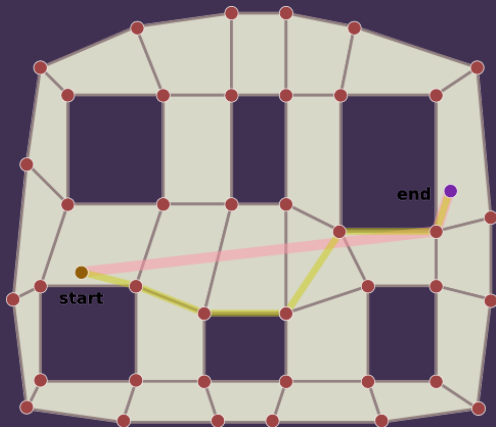
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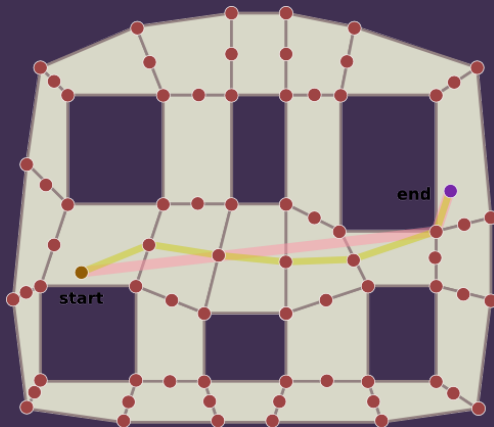
Centres of edges

Meshes to graphs



Vertices of polygons

Meshes to graphs



Hybrid approach: edges and vertices

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- ▶ **Steering:** don't have your AI agent follow the path exactly, but instead try to stay close to it
- ▶ **Dynamic environments:** may need to re-run pathfinder if environment changes (e.g. movable obstacles, destructible terrain)