# FFY\_ROUWENHORST AR1 Shock Discretization Example

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This is the example vignette for function: ffy\_rouwenhorst from the MEconTools Package. See also ffy tauchen function from the MEconTools Package. This function discretize a mean zero AR1 process, uses Rouwenhorst (1995). See AR 1 Example for some details on how the AR1 process works. And See Kopecky and Suen (2010).

#### **Test FFY\_ROUWENHORST Defaults**

Call the function with defaults.

#### ffy\_rouwenhorst(); CONTAINER NAME: mp\_container\_map ND Array (Matrix etc) std numel rowN colN sum mean coefvari ar\_disc\_ar1 2 5 0 0.39528 1 1 0 Inf 5 mt\_disc\_ar1\_trans 2 25 5 5 0.2 0.18246 0.91229 0.0016 11 xxx TABLE:ar\_disc\_ar1 xxxxxxxxxxxxxxxxxxx **c1** r1 -0.5 r2 -0.25 r3 r4 0.25 0.5 xxx TABLE:mt\_disc\_ar1\_trans xxxxxxxxxxxxxxxxxx **c1** c4 с5 c2 **c**3 r1 0.4096 0.4096 0.1536 0.0256 0.0016 r2 0.1024 0.4864 0.3264 0.0784 0.0064 r3 0.0256 0.2176 0.5136 0.2176 0.0256 0.0064 0.0784 0.3264 0.4864 0.1024 r5 0.0016 0.0256 0.1536 0.4096 0.4096

min

-0.5

CONTAINER NAME: mp\_container\_map Scalars 

	1	ıax	varue
	-		
fl_ar1_beg	1	2	-0.5
fl_ar1_end	2	3	0.5
fl_ar1_persistence	3	4	0.6
fl_ar1_step	4	5	0.25
fl_p0	5	6	0.8
f1_q0	6	7	0.8
fl_shk_std	7	8	0.2
fl_sig_ar1	8	9	0.25

### **Test FFY\_ROUWENHORST Specify Parameters**

With a grid of 10 points, the Rwouenhorst bounds on standard deviations are equall to Tauchen bounds of 3. With the not extremely persistent shock process here, the Tauchen and Rouwenhorst Results are very similar.

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
    deal(0.60, 0.10, 10, true);
ffy_rouwenhorst(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);
```

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CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

	i	idx	ndim	numel	rowN	colN	sum	mean	std	coefva
	-									
ar_disc_ar1	1	1	2	10	10	1	5.5511e-17	5.5511e-18	0.2523	4.54516
mt_disc_ar1_trans	2	11	2	100	10	10	10	0.1	0.11724	1.1

xxx TABLE:ar\_disc\_ar1 xxxxxxxxxxxxxxxxxx

**c1** 

r1	-0.375
r2	-0.29167
r3	-0.20833
r4	-0.125
r5	-0.041667
r6	0.041667
r7	0.125
r8	0.20833
r9	0.29167
r10	0.375

xxx TABLE:mt\_disc\_ar1\_trans xxxxxxxxxxxxxxxxx

	c1	c2	<b>c</b> 3	с4	<b>c</b> 5	с6	с7	с8
r1	0.13422	0.30199	0.30199	0.17616	0.06606	0.016515	0.0027525	0.00029491
r2	0.033554	0.20133	0.32716	0.26424	0.12662	0.038535	0.0075694	0.00093389
r3	0.0083886	0.081789	0.26267	0.32755	0.21401	0.082747	0.019741	0.0028677
r4	0.0020972	0.028312	0.14038	0.30946	0.30369	0.15877	0.047989	0.0084603
r5	0.00052429	0.009044	0.061145	0.20246	0.33477	0.25969	0.10585	0.023642
r6	0.00013107	0.0027525	0.023642	0.10585	0.25969	0.33477	0.20246	0.061145
r7	3.2768e-05	0.00081101	0.0084603	0.047989	0.15877	0.30369	0.30946	0.14038
r8	8.192e-06	0.00023347	0.0028677	0.019741	0.082747	0.21401	0.32755	0.26267
r9	2.048e-06	6.6048e-05	0.00093389	0.0075694	0.038535	0.12662	0.26424	0.32716
r10	5.12e-07	1.8432e-05	0.00029491	0.0027525	0.016515	0.06606	0.17616	0.30199

CONTAINER NAME: mp\_container\_map Scalars

	i	idx	value
	-		
fl_ar1_beg	1	2	-0.375
fl_ar1_end	2	3	0.375
fl_ar1_persistence	3	4	0.6
fl ar1 step	4	5	0.083333

```
5 6
6 7
7 8
8 9
fl_p0
                                    0.8
fl_p0
fl_q0
fl_shk_std
fl_sig_ar1
                                    0.8
                                    0.1
                                 0.125
it_std_bound 9 10
```

# Test FFY\_ROUWENHORST High Persistence, Low SD

[fl\_ar1\_persistence, fl\_shk\_std, it\_disc\_points, bl\_verbose] = ... deal(0.99, 0.01, 7, true); ffy\_rouwenhorst(fl\_ar1\_persistence, fl\_shk\_std, it\_disc\_points, bl\_verbose);

CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

	i	idx	ndim	numel	rowN	colN	sum	mean	std	coefvari	mi
	-										
ar_disc_ar1	1	1	2	7	7	1	0	0	0.12503	Inf	-0.
mt_disc_ar1_trans	2	11	2	49	7	7	7	0.14286	0.34148	2.3904	1.562

xxx TABLE:ar\_disc\_ar1 xxxxxxxxxxxxxxxxxx

r1	-0.17364
r2	-0.11576
r3	-0.05788
r4	0
r5	0.05788
r6	0.11576
r7	0.17364

xxx TABLE:mt\_disc\_ar1\_trans xxxxxxxxxxxxxxxxxx

<b>c1</b>	c2	<b>c</b> 3	c4	c5	с6	c7
0.97037	0.029257	0.00036756	2.4627e-06	9.2815e-09	1.8656e-11	1.5625e-14
0.0048762	0.9705	0.024382	0.00024504	1.2314e-06	3.0938e-09	3.1094e-12
2.4504e-05	0.009753	0.97057	0.019506	0.00014703	4.9254e-07	6.1877e-10
1.2313e-07	7.3513e-05	0.01463	0.97059	0.01463	7.3513e-05	1.2313e-07
6.1877e-10	4.9254e-07	0.00014703	0.019506	0.97057	0.009753	2.4504e-05
3.1094e-12	3.0938e-09	1.2314e-06	0.00024504	0.024382	0.9705	0.0048762
1.5625e-14	1.8656e-11	9.2815e-09	2.4627e-06	0.00036756	0.029257	0.97037
	0.97037 0.0048762 2.4504e-05 1.2313e-07 6.1877e-10 3.1094e-12	0.97037 0.029257 0.0048762 0.9705 2.4504e-05 0.009753 1.2313e-07 7.3513e-05 6.1877e-10 4.9254e-07 3.1094e-12 3.0938e-09	0.97037       0.029257       0.00036756         0.0048762       0.9705       0.024382         2.4504e-05       0.009753       0.97057         1.2313e-07       7.3513e-05       0.01463         6.1877e-10       4.9254e-07       0.00014703         3.1094e-12       3.0938e-09       1.2314e-06	0.97037       0.029257       0.00036756       2.4627e-06         0.0048762       0.9705       0.024382       0.00024504         2.4504e-05       0.009753       0.97057       0.019506         1.2313e-07       7.3513e-05       0.01463       0.97059         6.1877e-10       4.9254e-07       0.00014703       0.019506         3.1094e-12       3.0938e-09       1.2314e-06       0.00024504	0.97037       0.029257       0.00036756       2.4627e-06       9.2815e-09         0.0048762       0.9705       0.024382       0.00024504       1.2314e-06         2.4504e-05       0.009753       0.97057       0.019506       0.00014703         1.2313e-07       7.3513e-05       0.01463       0.97059       0.01463         6.1877e-10       4.9254e-07       0.00014703       0.019506       0.97057         3.1094e-12       3.0938e-09       1.2314e-06       0.00024504       0.024382	0.97037       0.029257       0.00036756       2.4627e-06       9.2815e-09       1.8656e-11         0.0048762       0.9705       0.024382       0.00024504       1.2314e-06       3.0938e-09         2.4504e-05       0.009753       0.97057       0.019506       0.00014703       4.9254e-07         1.2313e-07       7.3513e-05       0.01463       0.97059       0.01463       7.3513e-05         6.1877e-10       4.9254e-07       0.00014703       0.019506       0.97057       0.009753         3.1094e-12       3.0938e-09       1.2314e-06       0.00024504       0.024382       0.9705

CONTAINER NAME: mp\_container\_map Scalars 

	i	idx	value
	-		
fl_ar1_beg	1	2	-0.17364
fl_ar1_end	2	3	0.17364
fl_ar1_persistence	3	4	0.99
fl_ar1_step	4	5	0.05788
fl_p0	5	6	0.995
fl_q0	6	7	0.995
fl_shk_std	7	8	0.01
fl_sig_ar1	8	9	0.070888
it_std_bound	9	10	0

#### Test FFY\_ROUWENHORST Low Persistence, Low SD

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
    deal(0.01, 0.01, 7, true);
ffy_rouwenhorst(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);
```

CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

	i	idx	ndim	numel	rowN	colN	sum	mean	std	coefvari	r
	-										
ar_disc_ar1	1	1	2	7	7	1	0	0	0.017639	Inf	-0.6
mt_disc_ar1_trans	2	11	2	49	7	7	7	0.14286	0.10985	0.76893	0.6

c1

r1	-0.024496
r2	-0.016331
r3	-0.0081654
r4	0
r5	0.0081654
r6	0.016331
r7	0.024496
r5 r6	0.0081654 0.016331

xxx TABLE:mt\_disc\_ar1\_trans xxxxxxxxxxxxxxxxxx

	<b>c1</b>	c2	с3	c4	c5	с6	с7
r1	0.016586	0.097547	0.23904	0.31241	0.22966	0.090047	0.014711
r2	0.016258	0.096266	0.23749	0.31247	0.23124	0.091266	0.015008
r3	0.015936	0.094997	0.23594	0.31251	0.23281	0.092497	0.015311
r4	0.01562	0.093741	0.23438	0.31252	0.23438	0.093741	0.01562
r5	0.015311	0.092497	0.23281	0.31251	0.23594	0.094997	0.015936
r6	0.015008	0.091266	0.23124	0.31247	0.23749	0.096266	0.016258
r7	0.014711	0.090047	0.22966	0.31241	0.23904	0.097547	0.016586

	i	idx	value
	-		
fl_ar1_beg	1	2	-0.024496
fl_ar1_end	2	3	0.024496
fl_ar1_persistence	3	4	0.01
fl_ar1_step	4	5	0.0081654
f1_p0	5	6	0.505
f1_q0	6	7	0.505
fl_shk_std	7	8	0.01
fl_sig_ar1	8	9	0.010001
it_std_bound	9	10	0

# Test FFY\_ROUWENHORST High Persistence, High SD

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
deal(0.99, 0.99, 7, true);
```

#### ffy\_rouwenhorst(fl\_ar1\_persistence, fl\_shk\_std, it\_disc\_points, bl\_verbose);

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CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

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	i	idx	ndim	numel	rowN	colN	sum	mean	std	coefvar
	_									
ar_disc_ar1	1	1	2	7	7	1	3.5527e-15	5.0753e-16	12.378	2.439e+
<pre>mt_disc_ar1_trans</pre>	2	11	2	49	7	7	7	0.14286	0.34148	2.39

xxx TABLE:ar\_disc\_ar1 xxxxxxxxxxxxxxxxxxx

c1

r1	-17.19
r2	-11.46
r3	-5.7301
r4	0
r5	5.7301
r6	11.46
r7	17.19

xxx TABLE:mt\_disc\_ar1\_trans xxxxxxxxxxxxxxxxxx

	c1	c2	c3	c4	c5	c6	c7
r1	0.97037	0.029257	0.00036756	2.4627e-06	9.2815e-09	1.8656e-11	1.5625e-14
r2	0.0048762	0.9705	0.024382	0.00024504	1.2314e-06	3.0938e-09	3.1094e-12
r3	2.4504e-05	0.009753	0.97057	0.019506	0.00014703	4.9254e-07	6.1877e-10
r4	1.2313e-07	7.3513e-05	0.01463	0.97059	0.01463	7.3513e-05	1.2313e-07
r5	6.1877e-10	4.9254e-07	0.00014703	0.019506	0.97057	0.009753	2.4504e-05
r6	3.1094e-12	3.0938e-09	1.2314e-06	0.00024504	0.024382	0.9705	0.0048762
r7	1.5625e-14	1.8656e-11	9.2815e-09	2.4627e-06	0.00036756	0.029257	0.97037

i	idx	value
-		
1	2	-17.19
2	3	17.19
3	4	0.99
4	5	5.7301
5	6	0.995
6	7	0.995
7	8	0.99
8	9	7.0179
9	10	0
	1 2 3 4 5 6 7	1 2 2 3 3 4 4 5 5 6 6 7 7 8 8 9

## Test FFY\_ROUWENHORST Low Persistence, Low SD

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
  deal(0.01, 0.01, 7, true);
ffy_rouwenhorst(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);
```

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CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

i	idx	ndim	numel	rowN	colN	sum	mean	std	coefvari	n
-										
 1 2		2 2	7 49	7 7			0 0.14286	0.017639 0.10985	Inf 0.76893	-0.0 0.0

xxx TABLE:ar\_disc\_ar1 xxxxxxxxxxxxxxxxxx

c1

r1	-0.024496
r2	-0.016331
r3	-0.0081654
r4	0
r5	0.0081654
r6	0.016331
r7	0.024496

xxx TABLE:mt disc ar1 trans xxxxxxxxxxxxxxxxx

	<b>c1</b>	c2	<b>c</b> 3	c4	<b>c</b> 5	c6	с7
r1	0.016586	0.097547	0.23904	0.31241	0.22966	0.090047	0.014711
r2	0.016258	0.096266	0.23749	0.31247	0.23124	0.091266	0.015008
r3	0.015936	0.094997	0.23594	0.31251	0.23281	0.092497	0.015311
r4	0.01562	0.093741	0.23438	0.31252	0.23438	0.093741	0.01562
r5	0.015311	0.092497	0.23281	0.31251	0.23594	0.094997	0.015936
r6	0.015008	0.091266	0.23124	0.31247	0.23749	0.096266	0.016258
r7	0.014711	0.090047	0.22966	0.31241	0.23904	0.097547	0.016586

	i	idx	value
	_		
fl_ar1_beg	1	2	-0.024496
fl_ar1_end	2	3	0.024496
fl_ar1_persistence	3	4	0.01
fl_ar1_step	4	5	0.0081654
fl_p0	5	6	0.505
fl_q0	6	7	0.505
fl_shk_std	7	8	0.01
fl_sig_ar1	8	9	0.010001
it_std_bound	9	10	0