# FFY\_TAUCHEN AR1 Shock Discretization Example

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This is the example vignette for function: ffy\_tauchen from the MEconTools Package. : See also the ffy\_rouwenhorst function from the MEconTools Package. This function discretize a mean zero AR1 process, uses Tauchen (1986). See AR 1 Example for some details on how the AR1 process works. And See Kopecky and Suen (2010).

#### **Test FFY\_TAUCHEN Defaults**

Call the function with defaults. Default sd bounds arer plus and minus 4. This is used in the following examples,

ffy_tau	uchen();									
	xxxxxxxxxxxx									
	R NAME: mp_con			rix etc)						
*********		i idx		umel rowN	colN	sum	mean	std	coefvari	min
ar_d	isc_ar1	1 1	2	5 5	1	0	0	0.79057	Inf	
	isc_ar1_trans	2 6		25 5	5	5	0.2	0.27623	1.3812	7.3923
r4 r5	0.5 1									
xxx TABL	E:mt_disc_ar1_ <b>c1</b>	trans xxxxxxx c2	c3	c4	c5					
r1	0.22663	0.73331	0.040048	1.0689e-05	7.3923	e-12				
r2	0.012224	0.58648			7.605					
r5	7.3923e-12									
r1 r2 r3 r4	0.22663 0.012224 8.8417e-05 7.605e-08	<b>c2</b> 	0.040048 0.39831 0.7887	1.0689e-05 0.0029797 0.10556 0.58648	7.3923 7.605 8.8417 0.01	e-12 e-08 e-05				

	1	Iux	value
	_		
fl_ar1_persistence	1	2	0.6
fl_ar1_step	2	3	0.5
fl_shk_std	3	4	0.2
it_std_bound	4	5	4

## **Test FFY\_TAUCHEN Specify Parameters**

With a grid of 10 points, the sd bounds on Tauchen and Rouwenhorst are identical. With the not extremely persistent shock process here, the Tauchen and Rouwenhorst Results are very similar.

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose, it_std_bound] = ...
    deal(0.60, 0.10, 10, true, 3);
ffy_tauchen(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose, it_std_bound);
```

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CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

	i	idx	ndim	numel	rowN	colN	sum	mean	std	coef
	-									
ar_disc_ar1	1	1	2	10	10	1	-7.2164e-16	-7.2164e-17	0.2523	-3.49
<pre>mt_disc_ar1_trans</pre>	2	6	2	100	10	10	10	0.1	0.11456	

xxx TABLE:ar\_disc\_ar1 xxxxxxxxxxxxxxxxxx

r1	-0.375
r2	-0.29167
r3	-0.20833
r4	-0.125

**c1** 

r4 -0.125 r5 -0.041667 r6 0.041667 r7 0.125

r8 0.20833 r9 0.29167 r10 0.375

xxx TABLE:mt disc ar1 trans xxxxxxxxxxxxxxxxxx

	c1	c2	<b>c</b> 3	c4	<b>c</b> 5	с6	с7	c8
r1	0.13933	0.26196	0.31887	0.20154	0.066066	0.011201	0.00097859	4.3874e-05
r2	0.056673	0.16995	0.30658	0.28713	0.1396	0.035167	0.0045756	0.00030628
r3	0.01861	0.087039	0.23281	0.32308	0.23281	0.087039	0.016841	0.0016806
r4	0.0048925	0.035167	0.1396	0.28713	0.30658	0.16995	0.048841	0.0072547
r5	0.0010235	0.011201	0.066066	0.20154	0.31887	0.26196	0.11169	0.02466
r6	0.00016962	0.0028101	0.02466	0.11169	0.26196	0.31887	0.20154	0.066066
r7	2.2197e-05	0.00055483	0.0072547	0.048841	0.16995	0.30658	0.28713	0.1396
r8	2.2881e-06	8.6129e-05	0.0016806	0.016841	0.087039	0.23281	0.32308	0.23281
r9	1.8543e-07	1.0503e-05	0.00030628	0.0045756	0.035167	0.1396	0.28713	0.30658
r10	1.1798e-08	1.0053e-06	4.3874e-05	0.00097859	0.011201	0.066066	0.20154	0.31887

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

 i
 idx
 value

 fl\_ar1\_persistence
 1
 2
 0.6

 fl\_ar1\_step
 2
 3
 0.083333

 fl\_shk\_std
 3
 4
 0.1

 it\_std\_bound
 4
 5
 3

#### Test FFY\_TAUCHEN High Persistence, Low SD

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
    deal(0.99, 0.01, 7, true);
ffy_tauchen(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);
```

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CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

	i	idx	ndim	numel	rowN	colN	sum	mean	std	coefvari	mir
	-										
ar_disc_ar1	1	1	2	7	7	1	0	0	0.15314	Inf	-0.21
mt_disc_ar1_trans	2	6	2	49	7	7	7	0.14286	0.35338	2.4737	

c1

r1	-0.21266
r2	-0.14178
r3	-0.070888
r4	0
r5	0.070888
r6	0.14178
r7	0.21266

xxx TABLE:mt\_disc\_ar1\_trans xxxxxxxxxxxxxxxxxxxxx

	<b>c1</b>	c2	<b>c</b> 3	c4	<b>c</b> 5	с6	c7
r1	0.99957	0.00043152	0	0	0	0	0
r2	0.00011382	0.99955	0.0003337	0	0	0	0
r3	4.8683e-27	0.00015	0.99959	0.00025684	0	0	0
r4	1.4175e-70	1.0439e-26	0.00019675	0.99961	0.00019675	0	0
r5	1.9884e-135	4.986e-70	2.2273e-26	0.00025684	0.99959	0.00015	0
r6	1.2359e-221	1.149e-134	1.7451e-69	4.7287e-26	0.0003337	0.99955	0.00011382
r7	0	1.1738e-220	6.6059e-134	6.077e-69	9.9893e-26	0.00043152	0.99957

	1	idx	value
	_		
fl_ar1_persistence	1	2	0.99
fl_ar1_step	2	3	0.070888
fl_shk_std	3	4	0.01
it std bound	4	5	3

## Test FFY\_TAUCHEN Low Persistence, Low SD

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
  deal(0.01, 0.01, 7, true);
ffy_tauchen(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);
```

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CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

		i -	idx ——	ndim	numel	rowN	colN	sum	mean
20	dica an1	1	1	2	7	7	1	2 46040	10 4 05640 10
	disc_ar1 disc_ar1_trans	1 2	1 6	2 2	7 49	7	1 7	3.4694e-	18 4.9564e-19 7 0.14286
	a13c_a1 1_c1 a113	2	0	2	72	,	,		7 0.14200
XXX TAB	LE:ar_disc_ar1 <b>c1</b>	xxxxxx	xxxxxx	xxxxx					
r1	-0.030002								
r2	-0.020001								
r3	-0.010001								
r4	0								
r5	0.010001								
r6	0.020001								
r7	0.030002								
XXX IAD	LE:mt_disc_ar1_ <b>c1</b> 	c2	<del></del>	c3	.x 		:5	c6	c7 
r1	0.0067533	0.0646	18	0.2484	0.38278	0.2	23505	0.057298	0.0057011
r2	0.0065668	0.062	286	0.24618	0.38287	0.2	23728	0.05838	0.0058656
r3	0.0063849	0.0617	17	0.24396	0.38292	0.	2395	0.059478	0.0060344
r4	0.0062075	0.066	959	0.24173	0.38294		24173	0.06059	0.0062075
r5	0.0060344	0.0594		0.2395	0.38292		4396	0.061717	0.0063849
r6	0.0058656	0.058		0.23728	0.38287		24618	0.06286	0.0065668
r7	0.0057011	0.0572	298	0.23505	0.38278	0.	2484	0.064018	0.0067533
CONTAIN  XXXXXXX  fl_ fl_ fl_ fl_	xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx	tainer_ xxxxxxx i -	_map Sc	alars	1				

std

0.021604

0.13667

coef

4.3588

0.9

## Test FFY\_TAUCHEN High Persistence, High SD

[fl\_ar1\_persistence, fl\_shk\_std, it\_disc\_points, bl\_verbose] = ... deal(0.99, 0.99, 7, true); ffy\_tauchen(fl\_ar1\_persistence, fl\_shk\_std, it\_disc\_points, bl\_verbose);

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CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

	i	idx	ndim	numel	rowN	colN	sum	sum mean		coef
	-									
ar_disc_ar1	1	1	2	7	7	1	-7.1054e-15	-1.0151e-15	15.16	-1.49
<pre>mt_disc_ar1_trans</pre>	2	6	2	49	7	7	7	0.14286	0.35338	

xxx TABLE:ar\_disc\_ar1 xxxxxxxxxxxxxxxxxx

**c1** 

r1 -21.054

r2	-14.036							
r3	-7.0179							
r4	-1.7764e-15							
r5	7.0179							
r6	14.036							
r7	21.054							
xxx TABL	E:mt_disc_ar1_t	rans x	xxxxxxx	xxxxxxxx				
	c1		c2	с3	c4	<b>c</b> 5	с6	с7
r1	0.99957	0.0	0043152	0	0	0	0	0
r2	0.00011382		0.99955	0.0003337	0	0	0	0
r3	4.8683e-27		0.00015	0.99959	0.00025684	0	0	0
r4	1.4175e-70		439e-26	0.00019675	0.99961	0.00019675	0	0
r5	1.9884e-135	4.	986e-70	2.2273e-26	0.00025684	0.99959	0.00015	0
r6	1.2359e-221	1.1	49e-134	1.7451e-69	4.7287e-26	0.0003337	0.99955	0.00011382
r7	0	1.17	38e-220	6.6059e-134	6.077e-69	9.9893e-26	0.00043152	0.99957
	xxxxxxxxxxxx							
	R NAME: mp_cont							
xxxxxxx	xxxxxxxxxxxxx							
		i	idx	value				
		_						
	r1_persistence	1	2	0.99				
	r1_step	2	3	7.0179				
	hk_std	3	4	0.99				
it_s	td_bound	4	5	3				

## Test FFY\_TAUCHEN Low Persistence, Low SD

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
  deal(0.01, 0.01, 7, true);
ffy_tauchen(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);
```

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CONTAINER NAME: mp\_container\_map ND Array (Matrix etc)

	i	idx	ndim	numel	rowN	colN	sum	mean	std	coefv
	_									
ar_disc_ar1	1	1	2	7	7	1	3.4694e-18	4.9564e-19	0.021604	4.358
mt disc ar1 trans	2	6	2	49	7	7	7	0.14286	0.13667	0.

**c1** 

-0.030002
-0.020001
-0.010001
0
0.010001
0.020001
0.030002

xxx TABLE:mt\_disc\_ar1\_trans xxxxxxxxxxxxxxxxxx

c1 c2 c3 c4 c5 c6 c7

r1	0.0067533	0.064018	0.2484	0.38278	0.23505	0.057298	0.0057011
r2	0.0065668	0.06286	0.24618	0.38287	0.23728	0.05838	0.0058656
r3	0.0063849	0.061717	0.24396	0.38292	0.2395	0.059478	0.0060344
r4	0.0062075	0.06059	0.24173	0.38294	0.24173	0.06059	0.0062075
r5	0.0060344	0.059478	0.2395	0.38292	0.24396	0.061717	0.0063849
r6	0.0058656	0.05838	0.23728	0.38287	0.24618	0.06286	0.0065668
r7	0.0057011	0.057298	0.23505	0.38278	0.2484	0.064018	0.0067533

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	i	idx	value
	_		
fl_ar1_persistence	1	2	0.01
fl_ar1_step	2	3	0.010001
fl_shk_std	3	4	0.01
it_std_bound	4	5	3