

Contents

Pı	reface	5
1	Savings Dynamic Programming 1.1 FF_VFI_AZ_LOOP Dynamic Savings Problem Loop Common Grid 1.2 FF_VFI_AZ_VEC Dynamic Savings Problem Vectorized Common Grid 1.3 FF_VFI_AZ_BISEC_LOOP Dynamic Savings Problem Loop Continuous Choice 1.4 FF_VFI_AZ_BISEC_VEC Dynamic Savings Problem Vectorized Continuous Exact	29
2		51 51
3	Distributional Analysis3.1FF_SIMU_STATS Examples3.2FF_DISC_RAND_VAR_STATS Examples3.3FF_DISC_RAND_VAR_MASS2OUTCOMES Examples3.4FF_DISC_RAND_VAR_MASS2COVCOR Examples	67
4	Graphs 4.1 FF_GRAPH_GRID Examples: X, Y and Color Line Plots	75
5	Data Structures 5.1 FF_SAVEBORR_GRID Example for Generating Asset Grid	83
6	Common Functions 6.1 FFY_TAUCHEN AR1 Shock Discretization Example	
7	Support Tools 7.1 FF_CONTAINER_MAP_DISPLAY Examples	1 05 105
A	A.1 Savings Dynamic Programming links	
	A.2 Summarize Policy and Value links	112
	A.4 Graphs links A.5 Data Structures links A.6 Common Functions links A.7 Support Tools links	112 112

4 CONTENTS

Preface

This is a work-in-progress Matlab package consisting of functions that facilitate Dynamic Programming and Related Tasks. Materials gathered from various projects in which Matlab code is used. Some of the solutions/algorithms are research outputs developed for specific research papers, other algorithms and methods are commonly-used. Files are the MEconTools repository. Matlab files are linked below by section with livescript files. Tested with Matlab 2019a (The MathWorks Inc, 2019).

Download and install the Matlab toolbox: MEconTools.mltbx

This bookdown file is a collection of mlx based vignettes for functions that are available from MEconTools. Each Vignette file contains various examples for invoking each function. The goal of this repository is to make it easier to find/re-use codes produced for various projects.

From other repositories: For dynamic borrowing and savings problems, see Dynamic Asset Repository; For code examples, see also R Example Code, Matlab Example Code, and Stata Example Code; For intro stat with R, see Intro Statistics for Undergraduates, and intro Math with Matlab, see Intro Mathematics for Economists. See here for all of Fan's public repositories.

The site is built using Bookdown (Xie, 2020).

Please contact FanWangEcon for issues or problems.

6 CONTENTS

Chapter 1

Savings Dynamic Programming

1.1 FF_VFI_AZ_LOOP Dynamic Savings Problem Loop Common Grid

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: **ff_vfi_az_loop** from the **MEconTools Package.** This function solves the dynamic programming problem for a (a,z) model. Households can save a, and face AR(1) shock z. The problem is solved over the infinite horizon. This is the looped code, it is slow for larger state-space problems. The code uses common grid, with the same state space and choice space grids.

Links to Four Code:

Four Core Savings/Borrowing Dynamic Programming Solution Functions that are functions in the **MEconTools Package.**:

- Common Choice and States Grid: ff_vfi_az_loop, slow should use for testing new models
- Common Choice and States Grid: ff_vfi_az_vec, fast good for many purposes
- States Grid + Continuous Exact Savings as Share of Cash-on-Hand :ff_vfi_az_bisec_loop, high precision even with small grid
- States Grid + Continuous Exact Savings as Share of Cash-on-Hand : **ff_vfi_az_bisec_vec**, precision and speed

The four sample codes are written for the standard dynamic savings problem with AR(1) shock that is one of the core problems introduced in first sessions of graduate Economics courses. The code can be easily adapted to accommand multiple assets, savings and borrowing, discrete and continuous choice, etc. A large proportion of dynamic economic models are based on the underlying structure of solving a model with endogenous states and exogenous shocks, and that is what the (a,z) model does. In general, one should write looped code first to make sure the economics is correct, then vectorized code can be adopted to increase speed.

1.1.1 Test FF VFI AZ LOOP Defaults

Call the function with defaults. By default, shows the asset policy function summary. Model parameters can be changed by the mp_params.

```
%mp_params
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('fl_crra') = 1.5;
mp_params('fl_beta') = 0.94;
% call function
ff_vfi_az_loop(mp_params);
```

Elapsed time is 1.291175 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	XXXXXXXXXXXXXXX

	i	idx	ndim	numel	rowN	colN	sum	mean	std	coefvari	min
	-										
ap	1	1	2	700	100	7	16864	24.091	14.08	0.58446	0

xxx TABLE:ap xxxxxxxxxxxxxxxx

	c1	c2	c3	c4	с5	с6	с7
r1	0	0	0	0	0	0.50505	2.0202
r2	0	0	0	0.50505	0.50505	1.0101	2.5253
r3	0.50505	0.50505	0.50505	0.50505	1.0101	1.5152	3.0303
r4	1.0101	1.0101	1.0101	1.0101	1.5152	2.0202	3.5354
r5	1.5152	1.5152	1.5152	1.5152	2.0202	2.5253	4.0404
r96	45.455	45.455	45.96	45.96	45.96	46.97	48.485
r97	45.96	45.96	45.96	46.465	46.465	47.475	48.99
r98	46.465	46.465	46.465	46.97	46.97	47.98	48.99
r99	46.97	46.97	46.97	47.475	47.475	48.485	49.495
r100	47.475	47.475	47.475	47.98	47.98	48.99	50

1.1.2 Test FF_VFI_AZ_LOOP Speed Tests

Call the function with different a and z grid size, print out speed:

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_timer') = true;
mp_support('ls_ffcmd') = {};
A grid 50, shock grid 5:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 50;
mp_params('it_z_n') = 5;
ff_vfi_az_loop(mp_params, mp_support);
Elapsed time is 0.223217 seconds.
A grid 100, shock grid 7:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 100;
```

Elapsed time is 1.284511 seconds.

ff_vfi_az_loop(mp_params, mp_support);

A grid 200, shock grid 9:

mp_params('it_z_n') = 7;

```
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 200;
mp_params('it_z_n') = 9;
ff_vfi_az_loop(mp_params, mp_support);
```

Elapsed time is 6.325330 seconds.

27.

Test FF_VFI_AZ_LOOP Control Outputs

Run the function first without any outputs;

```
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 50;
mp_params('it_z_n') = 5;
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_timer') = false;
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
```

Run the function and show policy function for savings choice. For ls_ffcmd, ls_ffsna, ls_ffgrh, can include these: 'v', 'ap', 'c', 'y', 'coh', 'savefraccoh'. These are value, aprime savings choice, consumption, income, cash on hand, and savings fraction as cash-on-hand.

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
% ls_ffcmd: summary print which outcomes
mp_support('ls_ffcmd') = {};
% ls_ffsna: detail print which outcomes
mp_support('ls_ffsna') = {'ap'};
% ls_ffgrh: graphical print which outcomes
mp_support('ls_ffgrh') = {'ap'};
ff_vfi_az_loop(mp_params, mp_support);
```

Elapsed time is 0.313830 seconds.

28

27.551

25.51

xxx ff vfi

xx ff_vf	i_az_vec, o	outcome=ap xxxxxxx	XXXXXXXXXXXXXXXXX	XXX		
group	a	mean_z_0_54195	mean_z_0_66401	mean_z_0_88162	mean_z_1_3095	mean_z
1	0	0	0	0	0	1.0
2	1.0204	0	0	1.0204	1.0204	2.0
3	2.0408	1.0204	1.0204	2.0408	2.0408	3.0
4	3.0612	2.0408	2.0408	2.0408	3.0612	4.0
5	4.0816	3.0612	3.0612	3.0612	4.0816	5.
6	5.102	4.0816	4.0816	4.0816	5.102	6.1
7	6.1224	5.102	5.102	5.102	6.1224	7.1
8	7.1429	6.1224	6.1224	6.1224	7.1429	8.1
9	8.1633	7.1429	7.1429	7.1429	8.1633	9.1
10	9.1837	8.1633	8.1633	8.1633	9.1837	10.
11	10.204	9.1837	9.1837	9.1837	10.204	11.
12	11.224	10.204	10.204	10.204	11.224	12.
13	12.245	11.224	11.224	11.224	12.245	13.
14	13.265	12.245	12.245	12.245	12.245	14.
15	14.286	13.265	13.265	13.265	13.265	15.
16	15.306	14.286	14.286	14.286	14.286	15.
17	16.327	15.306	15.306	15.306	15.306	16.
18	17.347	16.327	16.327	16.327	16.327	17.
19	18.367	17.347	17.347	17.347	17.347	18.
20	19.388	18.367	18.367	18.367	18.367	19.
21	20.408	19.388	19.388	19.388	19.388	20.
22	21.429	19.388	20.408	20.408	20.408	21.
23	22.449	20.408	21.429	21.429	21.429	22.
24	23.469	21.429	22.449	22.449	22.449	23.
25	24.49	22.449	22.449	23.469	23.469	24
26	25.51	23.469	23.469	24.49	24.49	25
27	26.531	24.49	24.49	25.51	25.51	26.

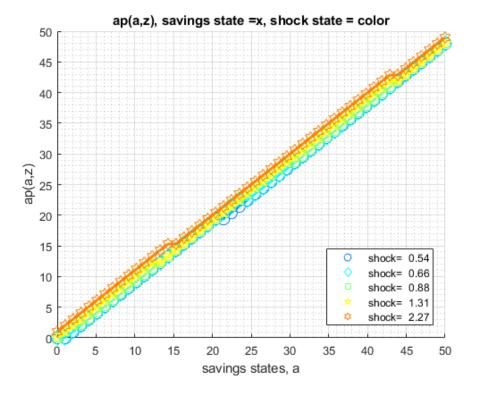
25.51

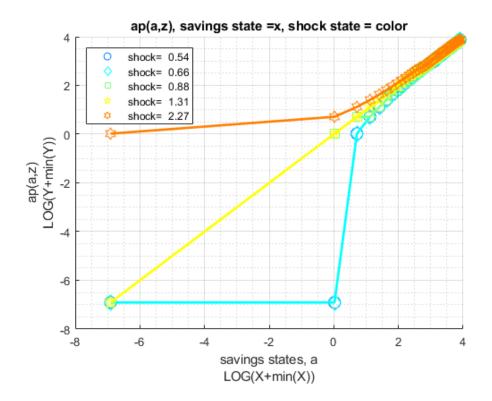
26.531

26.531

28. 29. 30. 31. 32. 33. 34. 35. 36. 37. 38. 39. 40. 41. 42. 42. 43. 44. 45. 46. 47. 48

| 29 | 28.571 | 26.531 | 26.531 | 27.551 | 27.551 | |
|----|--------|--------|--------|--------|--------|--|
| 30 | 29.592 | 27.551 | 27.551 | 28.571 | 28.571 | |
| 31 | 30.612 | 28.571 | 28.571 | 28.571 | 29.592 | |
| 32 | 31.633 | 29.592 | 29.592 | 29.592 | 30.612 | |
| 33 | 32.653 | 30.612 | 30.612 | 30.612 | 31.633 | |
| 34 | 33.673 | 31.633 | 31.633 | 31.633 | 32.653 | |
| 35 | 34.694 | 32.653 | 32.653 | 32.653 | 33.673 | |
| 36 | 35.714 | 33.673 | 33.673 | 33.673 | 34.694 | |
| 37 | 36.735 | 34.694 | 34.694 | 34.694 | 35.714 | |
| 38 | 37.755 | 35.714 | 35.714 | 35.714 | 36.735 | |
| 39 | 38.776 | 36.735 | 36.735 | 36.735 | 37.755 | |
| 40 | 39.796 | 37.755 | 37.755 | 37.755 | 38.776 | |
| 41 | 40.816 | 38.776 | 38.776 | 38.776 | 39.796 | |
| 42 | 41.837 | 39.796 | 39.796 | 39.796 | 40.816 | |
| 43 | 42.857 | 40.816 | 40.816 | 40.816 | 41.837 | |
| 44 | 43.878 | 41.837 | 41.837 | 41.837 | 41.837 | |
| 45 | 44.898 | 42.857 | 42.857 | 42.857 | 42.857 | |
| 46 | 45.918 | 43.878 | 43.878 | 43.878 | 43.878 | |
| 47 | 46.939 | 44.898 | 44.898 | 44.898 | 44.898 | |
| 48 | 47.959 | 45.918 | 45.918 | 45.918 | 45.918 | |
| 49 | 48.98 | 46.939 | 46.939 | 46.939 | 46.939 | |
| 50 | 50 | 47.959 | 47.959 | 47.959 | 47.959 | |
| | | | | | | |





Run the function and show summaries for savings and fraction of coh saved:

```
mp_params('it_a_n') = 100;
mp_params('it_z_n') = 9;
mp_support('ls_ffcmd') = {'ap', 'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
mp_support('bl_vfi_store_all') = true; % store c(a,z), y(a,z)
ff_vfi_az_loop(mp_params, mp_support);
```

Elapsed time is 1.867278 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | 1 | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-------------------|-------|--------|------|-------|------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| ap | 1 | 1 | 2 | 900 | 100 | 9 | 21825 | 24.25 | 14.089 | 0. |
| savefraccoh | 2 | 2 | 2 | 900 | 100 | 9 | 752.38 | 0.83597 | 0.13497 | 0.16 |
| xxx TABLE:ap xxxx | xxxxx | xxxxxx | xx | | | | | | | |
| c1 | | c2 | C | :3 | c4 | с5 | с6 | с7 | с8 | |

| xx TABLE:ap | xxxxxxx | XXXXXXXXX | | | | | | | |
|-------------|---------|-----------|---------|---------|---------|---------|---------|--------|--|
| | c1 | c2 | c3 | c4 | c5 | c6 | c7 | c8 | |
| | | | | | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0 | 0 | 0.50505 | 1.5152 | |
| r2 | 0 | 0 | 0 | 0 | 0.50505 | 0.50505 | 1.0101 | 1.5152 | |
| r3 | 0.50505 | 0.50505 | 0.50505 | 0.50505 | 0.50505 | 1.0101 | 1.5152 | 2.0202 | |
| r4 | 1.0101 | 1.0101 | 1.0101 | 1.0101 | 1.0101 | 1.5152 | 2.0202 | 2.5253 | |
| r5 | 1.5152 | 1.5152 | 1.5152 | 1.5152 | 1.5152 | 2.0202 | 2.5253 | 3.0303 | |
| r96 | 45.455 | 45.455 | 45.455 | 45.96 | 45.96 | 45.96 | 46.465 | 47.475 | |
| r97 | 45.96 | 45.96 | 45.96 | 46.465 | 46.465 | 46.465 | 46.97 | 47.98 | |
| r98 | 46.465 | 46.465 | 46.465 | 46.465 | 46.97 | 46.97 | 47.475 | 48.485 | |
| r99 | 46.97 | 46.97 | 46.97 | 46.97 | 47.475 | 47.475 | 47.98 | 48.99 | |

| r100 | 47.475 | 47.475 | 47.475 | 47.475 | 47.98 | 47.98 | 48.485 | 49.495 | | | | | | |
|---|---------|---------|---------|---------|---------|---------|---------|---------|--|--|--|--|--|--|
| xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx | | | | | | | | | | | | | | |
| | c1 | c2 | c3 | c4 | c5 | с6 | c7 | c8 | | | | | | |
| | | | | | | | | | | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0 | 0 | 0.24587 | 0.48182 | | | | | | |
| r2 | 0 | 0 | 0 | 0 | 0.3075 | 0.25444 | 0.39276 | 0.41371 | | | | | | |
| r3 | 0.30679 | 0.29486 | 0.27938 | 0.25939 | 0.2338 | 0.40362 | 0.49043 | 0.4833 | | | | | | |
| r4 | 0.4668 | 0.45285 | 0.43438 | 0.40981 | 0.37721 | 0.50166 | 0.56006 | 0.53755 | | | | | | |
| r5 | 0.56502 | 0.55132 | 0.53293 | 0.50802 | 0.47415 | 0.57101 | 0.61221 | 0.58103 | | | | | | |
| r96 | 0.91292 | 0.9117 | 0.90997 | 0.91752 | 0.91364 | 0.90746 | 0.90692 | 0.90732 | | | | | | |
| r97 | 0.91357 | 0.91236 | 0.91064 | 0.91812 | 0.91427 | 0.90815 | 0.90761 | 0.90799 | | | | | | |
| r98 | 0.9142 | 0.913 | 0.9113 | 0.90882 | 0.91489 | 0.90882 | 0.90828 | 0.90865 | | | | | | |
| r99 | 0.91482 | 0.91363 | 0.91195 | 0.90949 | 0.91549 | 0.90949 | 0.90894 | 0.90929 | | | | | | |
| r100 | 0.91543 | 0.91425 | 0.91258 | 0.91014 | 0.91609 | 0.91013 | 0.90959 | 0.90992 | | | | | | |

1.1.4 Test FF_VFI_AZ_LOOP Change Interest Rate and Discount

Show only save fraction of cash on hand:

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 50;
mp_params('it_z_n') = 5;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
Solve the model with several different interest rates and discount factor:
% Lower Savings Incentives
mp_params('fl_beta') = 0.80;
mp_params('fl_r') = 0.01;
ff_vfi_az_loop(mp_params, mp_support);
```

Elapsed time is 0.113265 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coefv |
|-------------|---|-----|------|-------|------|------|--------|---------|--------|-------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 250 | 50 | 5 | 118.68 | 0.47472 | 0.2843 | 0.598 |

xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxxx

| | c1 | c2 | c3 | c4 | c5 |
|-----|---------|---------|---------|---------|---------|
| | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0.10642 |
| r2 | 0 | 0 | 0 | 0 | 0.1064 |
| r3 | 0 | 0 | 0 | 0 | 0.10629 |
| r4 | 0 | 0 | 0 | 0 | 0.106 |
| r5 | 0 | 0 | 0 | 0 | 0.10543 |
| r46 | 0.79096 | 0.78787 | 0.78241 | 0.77191 | 0.74922 |

```
0.79553 0.79262 0.78747 0.77755
                                    0.75606
r47
r48
     0.7999 0.79715 0.79229 0.7829 0.76254
r49 0.80407 0.80147 0.79687 0.78799 0.76868
r50 0.80805 0.80559 0.80125 0.79284 0.7745
```

% Higher Savings Incentives mp_params('fl_beta') = 0.95; $mp_params('fl_r') = 0.04;$ ff_vfi_az_loop(mp_params, mp_support);

Elapsed time is 0.327279 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-------------|---|-----|------|-------|------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 250 | 50 | 5 | 160.99 | 0.64394 | 0.29947 | 0.46 |

xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx

| | c1 | c2 | с3 | c4 | с5 |
|-----|---------|---------|----------|---------|---------|
| | | | | | |
| r1 | 0 | 0 | 0.024103 | 0.18484 | 0.40057 |
| r2 | 0 | 0 | 0.024094 | 0.1848 | 0.40051 |
| r3 | 0 | 0 | 0.024028 | 0.18446 | 0.40008 |
| r4 | 0 | 0 | 0.046583 | 0.18354 | 0.39894 |
| r5 | 0 | 0 | 0.045925 | 0.24935 | 0.39672 |
| r46 | 0.94526 | 0.94167 | 0.93533 | 0.92312 | 0.89672 |
| r47 | 0.94628 | 0.94291 | 0.93696 | 0.92548 | 0.90059 |
| r48 | 0.94722 | 0.94405 | 0.93846 | 0.92766 | 0.90418 |
| r49 | 0.94808 | 0.94511 | 0.93984 | 0.92966 | 0.90749 |
| r50 | 0.94888 | 0.94608 | 0.94111 | 0.93151 | 0.91056 |

Test FF_VFI_AZ_LOOP Changing Risk Aversion

Here, again, show fraction of coh saved in summary tabular form, but also show it graphically.

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp support('ls ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {'savefraccoh'};
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 100;
mp_params('it_z_n') = 5;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
Solve the model with different risk aversion levels, higher preferences for risk:
% Lower Risk Aversion
mp_params('fl_crra') = 0.5;
ff_vfi_az_loop(mp_params, mp_support);
Elapsed time is 0.581794 seconds.
```

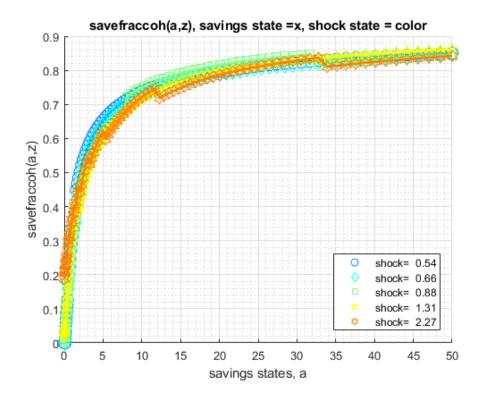
${\tt CONTAINER~NAME:~mp_ffcmd~ND~Array~(Matrix~etc)}$

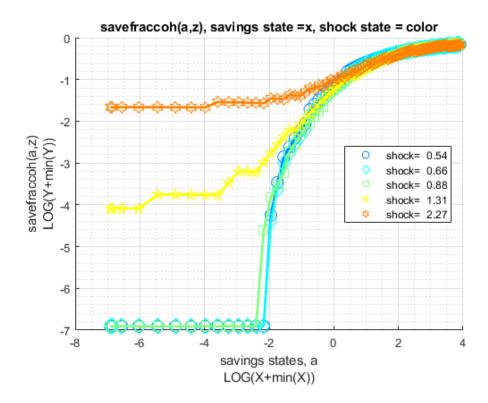
| ********** | XXXXXXXXX |
|------------|-----------|

| | 1 | ıdx | ndım | numel | rowN | COTN | sum | mean | std | coei |
|-------------|---|-----|------|-------|------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 500 | 100 | 5 | 268.82 | 0.53764 | 0.29852 | 0.55 |

xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx

| | Davorracoon | | | | |
|------|-------------|---------|---------|----------|---------|
| | c1 | c2 | c3 | c4 | c5 |
| | | | | | |
| r1 | 0 | 0 | 0 | 0.015741 | 0.18847 |
| r2 | 0 | 0 | 0 | 0.01574 | 0.18847 |
| r3 | 0 | 0 | 0 | 0.015737 | 0.18844 |
| r4 | 0 | 0 | 0 | 0.015728 | 0.18838 |
| r5 | 0 | 0 | 0 | 0.022367 | 0.18825 |
| r96 | 0.84455 | 0.84169 | 0.83664 | 0.85445 | 0.83255 |
| r97 | 0.84611 | 0.84333 | 0.83842 | 0.85626 | 0.83496 |
| r98 | 0.84763 | 0.84493 | 0.84016 | 0.85803 | 0.83729 |
| r99 | 0.84911 | 0.84648 | 0.84185 | 0.85974 | 0.83956 |
| r100 | 0.85055 | 0.848 | 0.84349 | 0.86141 | 0.84176 |
| | | | | | |





When risk aversion increases, at every state-space point, the household wants to save more.

```
% Higher Risk Aversion
mp_params('fl_crra') = 5;
ff_vfi_az_loop(mp_params, mp_support);
```

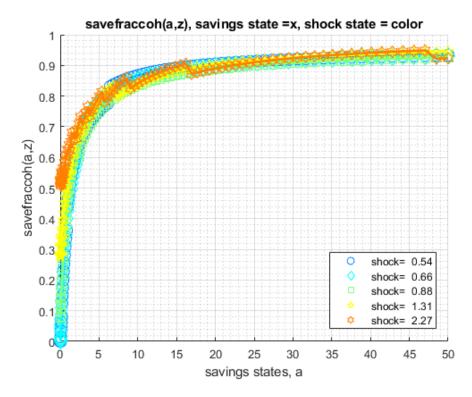
Elapsed time is 0.937495 seconds.

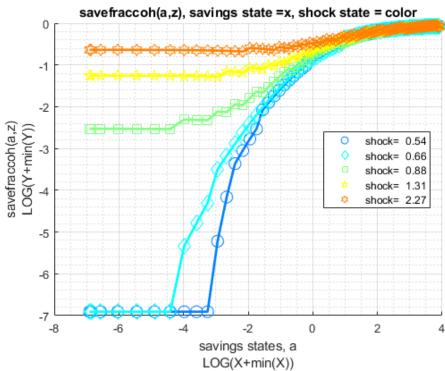
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-------------|---|-----|------|-------|------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 500 | 100 | 5 | 335.64 | 0.67129 | 0.28688 | 0.42 |

xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxxx

| | | c1 | c2 | c3 | c4 | с5 |
|---|-----|---------|---------|----------|---------|---------|
| | | | | | | |
| r | 1 | 0 | 0 | 0.078907 | 0.28472 | 0.52731 |
| r | 2 | 0 | 0 | 0.078904 | 0.28471 | 0.5273 |
| r | 3 | 0 | 0 | 0.078878 | 0.28465 | 0.52723 |
| r | 4 | 0 | 0 | 0.078808 | 0.28448 | 0.52705 |
| r | 5 | 0 | 0 | 0.078672 | 0.28415 | 0.52669 |
| r | 96 | 0.93086 | 0.92771 | 0.92215 | 0.94079 | 0.94593 |
| r | 97 | 0.93161 | 0.92855 | 0.92315 | 0.94183 | 0.94739 |
| r | 98 | 0.93233 | 0.92936 | 0.92411 | 0.94283 | 0.9488 |
| r | 99 | 0.93303 | 0.93015 | 0.92505 | 0.94379 | 0.92164 |
| r | 100 | 0.93371 | 0.93091 | 0.92595 | 0.94471 | 0.92317 |
| | | | | | | |





1.1.6 Test FF_VFI_AZ_LOOP with Higher Uncertainty

Increase the standard deviation of the Shock.

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
```

coefva

0.5454

std

0.32083

```
1.1. FF VFI AZ LOOP DYNAMIC SAVINGS PROBLEM LOOP COMMON GRID
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 100;
mp_params('it_z_n') = 5;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
Lower standard deviation of shock:
% Lower Risk Aversion
mp_params('fl_shk_std') = 0.10;
ff_vfi_az_loop(mp_params, mp_support);
Elapsed time is 0.957457 seconds.
_____
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
idx ndim numel
                                    rowN colN sum mean
                                                ----
                                    100 5 294.1 0.5882
                 1 2 500
   savefraccoh
              1
xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx
```

| | c1 | c2 | c3 | c4 | с5 |
|------|---------|---------|---------|----------|---------|
| | | | | | |
| r1 | 0 | 0 | 0 | 0.034556 | 0.11424 |
| r2 | 0 | 0 | 0 | 0.034555 | 0.11424 |
| r3 | 0 | 0 | 0 | 0.034546 | 0.11422 |
| r4 | 0 | 0 | 0 | 0.034523 | 0.11416 |
| r5 | 0 | 0 | 0 | 0.034478 | 0.11404 |
| r96 | 0.89673 | 0.89421 | 0.91986 | 0.91499 | 0.90808 |
| r97 | 0.89789 | 0.89545 | 0.92093 | 0.9162 | 0.90948 |
| r98 | 0.89903 | 0.89665 | 0.92196 | 0.91737 | 0.91084 |
| r99 | 0.90013 | 0.89782 | 0.92295 | 0.9185 | 0.91215 |
| r100 | 0.90119 | 0.89896 | 0.92392 | 0.91959 | 0.91342 |

Higher shock standard deviation: low shock high asset save more, high shock more asset save less, high shock low asset save more:

```
% Higher Risk Aversion
mp_params('fl_shk_std') = 0.40;
ff_vfi_az_loop(mp_params, mp_support);
```

Elapsed time is 0.923630 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-------------|---|-----|------|-------|------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 500 | 100 | 5 | 350.37 | 0.70073 | 0.26741 | 0.38 |

xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx

| | c1 | c2 | c3 | c4 | c5 |
|----|----|----|----------|---------|---------|
| | | | | | |
| r1 | 0 | 0 | 0.030722 | 0.36969 | 0.77072 |
| r2 | 0 | 0 | 0.03072 | 0.36967 | 0.77071 |

| r3 | 0 | 0 | 0.0307 | 0.36958 | 0.77068 |
|------|---------|---------|----------|---------|---------|
| r4 | 0 | 0 | 0.030646 | 0.36933 | 0.7706 |
| r5 | 0 | 0 | 0.030543 | 0.36885 | 0.77044 |
| r96 | 0.90975 | 0.90819 | 0.9038 | 0.91513 | 0.88687 |
| r97 | 0.91053 | 0.90902 | 0.90476 | 0.91633 | 0.89076 |
| r98 | 0.91129 | 0.90982 | 0.90569 | 0.9175 | 0.86794 |
| r99 | 0.91204 | 0.91061 | 0.9066 | 0.91862 | 0.84583 |
| r100 | 0.91276 | 0.91138 | 0.90748 | 0.91971 | 0.82439 |

1.2 FF_VFI_AZ_VEC Dynamic Savings Problem Vectorized Common Grid

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: **ff_vfi_az_vec** from the **MEconTools Package.** This function solves (vectorized) the dynamic programming problem for a (a,z) model. Households can save a, and face AR(1) shock z. The problem is solved over the infinite horizon.

The code uses common grid, with the same state space and choice space grids. **ff_vfi_az_bisec_vec** from the **MEconTools Package** solves the same problem but using continuous exact percentage asset choices, which is more precise than the solution here, and perhaps a little bit slower.

This is the vectorized code, its speed is much faster than the looped code. The function is designed to have small memory footprint and requires low computing resources, yet is fast.

Links to Four Code:

Four Core Savings/Borrowing Dynamic Programming Solution Functions that are functions in the **MEconTools Package.**:

- Common Choice and States Grid: ff_vfi_az_loop, slow should use for testing new models
- Common Choice and States Grid: ff_vfi_az_vec, fast good for many purposes
- States Grid + Continuous Exact Savings as Share of Cash-on-Hand :ff_vfi_az_bisec_loop, high precision even with small grid
- States Grid + Continuous Exact Savings as Share of Cash-on-Hand : **ff_vfi_az_bisec_vec**, precision and speed

1.2.1 Test FF VFI AZ VEC Defaults

Call the function with defaults. By default, shows the asset policy function summary. Model parameters can be changed by the mp_params.

| AAAAAA | i | idx | ndim | numel | rowN | colN | sum | mean | std | coefvari | min |
|--------|---|-----|------|-------|------|------|-------|--------|-------|----------|-----|
| | - | | | | | | | | | | |
| ap | 1 | 1 | 2 | 700 | 100 | 7 | 16864 | 24.091 | 14.08 | 0.58446 | 0 |

| xxx TABLE: | ар хххххххх | xxxxxxxxx | | | | | |
|------------|-------------|-----------|---------|---------|---------|---------|--------|
| | c1 | c2 | c3 | c4 | c5 | с6 | с7 |
| | | | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0 | 0.50505 | 2.0202 |
| r2 | 0 | 0 | 0 | 0.50505 | 0.50505 | 1.0101 | 2.5253 |
| r3 | 0.50505 | 0.50505 | 0.50505 | 0.50505 | 1.0101 | 1.5152 | 3.0303 |
| r4 | 1.0101 | 1.0101 | 1.0101 | 1.0101 | 1.5152 | 2.0202 | 3.5354 |
| r5 | 1.5152 | 1.5152 | 1.5152 | 1.5152 | 2.0202 | 2.5253 | 4.0404 |
| r96 | 45.455 | 45.455 | 45.96 | 45.96 | 45.96 | 46.97 | 48.485 |
| r97 | 45.96 | 45.96 | 45.96 | 46.465 | 46.465 | 47.475 | 48.99 |
| r98 | 46.465 | 46.465 | 46.465 | 46.97 | 46.97 | 47.98 | 48.99 |
| r99 | 46.97 | 46.97 | 46.97 | 47.475 | 47.475 | 48.485 | 49.495 |
| r100 | 47.475 | 47.475 | 47.475 | 47.98 | 47.98 | 48.99 | 50 |

1.2.2 Test FF_VFI_AZ_BISEC_VEC Speed Tests

Call the function with different a and z grid size, print out speed:

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_timer') = true;
mp_support('ls_ffcmd') = {};
A grid 200, shock grid 9:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 200;
mp_params('it_z_n') = 9;
ff_vfi_az_vec(mp_params, mp_support);
Elapsed time is 0.220867 seconds.
A grid 750, shock grid 15:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 750;
mp_params('it_z_n') = 15;
ff_vfi_az_vec(mp_params, mp_support);
Elapsed time is 3.573648 seconds.
A grid 600, shock grid 45:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 600;
mp_params('it_z_n') = 45;
ff_vfi_az_vec(mp_params, mp_support);
```

1.2.3 Test FF VFI AZ VEC Control Outputs

Run the function first without any outputs;

Elapsed time is 8.398580 seconds.

```
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 50;
mp_params('it_z_n') = 5;
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_timer') = false;
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
```

0.9

0.9

Run the function and show policy function for savings choice. For ls_ffcmd, ls_ffsna, ls_ffgrh, can include these: 'v', 'ap', 'c', 'y', 'coh', 'savefraccoh'. These are value, aprime savings choice, consumption, income, cash on hand, and savings fraction as cash-on-hand.

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
% ls_ffcmd: summary print which outcomes
mp_support('ls_ffcmd') = {};
% ls_ffsna: detail print which outcomes
mp_support('ls_ffsna') = {'savefraccoh'};
% ls_ffgrh: graphical print which outcomes
mp_support('ls_ffgrh') = {'savefraccoh'};
ff_vfi_az_vec(mp_params, mp_support);
```

38

39

37.755

38.776

0.90662

0.90841

| _ | | outcome=savefraccoh | | | 1 300F | |
|-------|--------|---------------------|----------------|----------------|---------------|------|
| group | a
 | mean_z_0_54195 | mean_z_0_66401 | mean_z_0_88162 | mean_z_1_3095 | mear |
| 1 | 0 | 0 | 0 | 0 | 0 | |
| 2 | 1.0204 | 0 | 0 | 0.46928 | 0.37487 | (|
| 3 | 2.0408 | 0.36632 | 0.34687 | 0.63373 | 0.54163 | (|
| 4 | 3.0612 | 0.53265 | 0.51178 | 0.47837 | 0.63592 | |
| 5 | 4.0816 | 0.62764 | 0.60816 | 0.57627 | 0.69655 | |
| 6 | 5.102 | 0.68908 | 0.67137 | 0.64196 | 0.73882 | |
| 7 | 6.1224 | 0.73208 | 0.71603 | 0.68909 | 0.76996 | |
| 8 | 7.1429 | 0.76386 | 0.74926 | 0.72456 | 0.79387 | |
| 9 | 8.1633 | 0.7883 | 0.77494 | 0.75221 | 0.81279 | |
| 10 | 9.1837 | 0.80769 | 0.79539 | 0.77438 | 0.82815 | |
| 11 | 10.204 | 0.82343 | 0.81206 | 0.79254 | 0.84086 | |
| 12 | 11.224 | 0.83648 | 0.82591 | 0.8077 | 0.85155 | |
| 13 | 12.245 | 0.84747 | 0.83759 | 0.82053 | 0.86067 | |
| 14 | 13.265 | 0.85685 | 0.84758 | 0.83155 | 0.80173 | |
| 15 | 14.286 | 0.86495 | 0.85622 | 0.8411 | 0.81288 | |
| 16 | 15.306 | 0.87201 | 0.86377 | 0.84947 | 0.82268 | |
| 17 | 16.327 | 0.87823 | 0.87043 | 0.85685 | 0.83137 | |
| 18 | 17.347 | 0.88374 | 0.87633 | 0.86342 | 0.83912 | |
| 19 | 18.367 | 0.88866 | 0.88161 | 0.8693 | 0.84608 | |
| 20 | 19.388 | 0.89309 | 0.88635 | 0.8746 | 0.85237 | |
| 21 | 20.408 | 0.89708 | 0.89064 | 0.87939 | 0.85807 | |
| 22 | 21.429 | 0.85567 | 0.89454 | 0.88375 | 0.86327 | |
| 23 | 22.449 | 0.86096 | 0.89809 | 0.88773 | 0.86803 | |
| 24 | 23.469 | 0.86581 | 0.90135 | 0.89138 | 0.87241 | |
| 25 | 24.49 | 0.87026 | 0.86502 | 0.89474 | 0.87644 | |
| 26 | 25.51 | 0.87436 | 0.8693 | 0.89784 | 0.88017 | |
| 27 | 26.531 | 0.87816 | 0.87327 | 0.90071 | 0.88362 | |
| 28 | 27.551 | 0.88168 | 0.87695 | 0.90338 | 0.88684 | |
| 29 | 28.571 | 0.88496 | 0.88037 | 0.90586 | 0.88984 | |
| 30 | 29.592 | 0.88802 | 0.88357 | 0.90818 | 0.89264 | |
| 31 | 30.612 | 0.89087 | 0.88655 | 0.87896 | 0.89527 | |
| 32 | 31.633 | 0.89355 | 0.88935 | 0.88197 | 0.89773 | |
| 33 | 32.653 | 0.89606 | 0.89198 | 0.8848 | 0.90005 | |
| 34 | 33.673 | 0.89843 | 0.89446 | 0.88747 | 0.90223 | |
| 35 | 34.694 | 0.90065 | 0.89679 | 0.88998 | 0.90429 | |
| 36 | 35.714 | 0.90275 | 0.89899 | 0.89235 | 0.90624 | |
| 37 | 36.735 | 0.90474 | 0.90107 | 0.8946 | 0.90809 | |

0.90304

0.90491

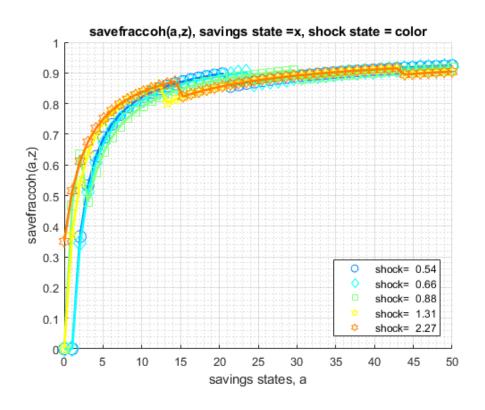
0.89673

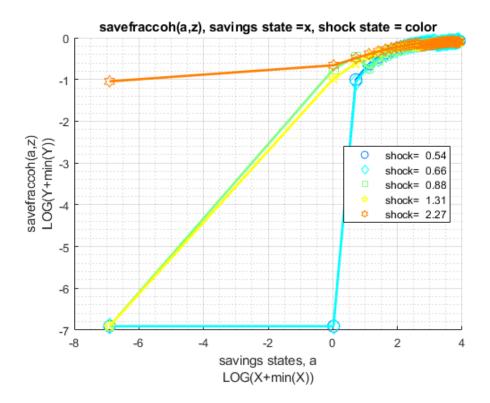
0.89874

0.90984

0.9115

| 40 | 39.796 | 0.9101 | 0.90669 | 0.90066 | 0.91308 | 0.9 |
|----|--------|---------|---------|---------|---------|-----|
| 41 | 40.816 | 0.91171 | 0.90838 | 0.90249 | 0.91458 | 0.9 |
| 42 | 41.837 | 0.91325 | 0.90998 | 0.90422 | 0.91601 | 0.9 |
| 43 | 42.857 | 0.91471 | 0.91152 | 0.90588 | 0.91738 | 0.9 |
| 44 | 43.878 | 0.9161 | 0.91298 | 0.90746 | 0.89681 | 0.8 |
| 45 | 44.898 | 0.91743 | 0.91438 | 0.90897 | 0.89854 | 0.8 |
| 46 | 45.918 | 0.91871 | 0.91571 | 0.91042 | 0.90019 | 0.8 |
| 47 | 46.939 | 0.91993 | 0.91699 | 0.91181 | 0.90178 | 0.8 |
| 48 | 47.959 | 0.9211 | 0.91822 | 0.91313 | 0.9033 | 0.9 |
| 49 | 48.98 | 0.92222 | 0.91939 | 0.91441 | 0.90475 | 0.9 |
| 50 | 50 | 0.92329 | 0.92052 | 0.91563 | 0.90615 | 0.9 |
| | | | | | | |





Run the function and show summaries for savings and fraction of coh saved:

```
mp_params('it_a_n') = 100;
mp_params('it_z_n') = 9;
mp_support('ls_ffcmd') = {'ap', 'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
mp_support('bl_vfi_store_all') = true; % store c(a,z), y(a,z)
ff_vfi_az_vec(mp_params, mp_support);
```

Elapsed time is 0.127807 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | 1 | ıax | naim | numer | LOMIN | COIN | sum | mean | sta | coei |
|-------------------|-------|--------|------|-------|-------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| ap | 1 | 1 | 2 | 900 | 100 | 9 | 21825 | 24.25 | 14.089 | 0. |
| savefraccoh | 2 | 2 | 2 | 900 | 100 | 9 | 752.38 | 0.83597 | 0.13497 | 0.16 |
| xxx TABLE:ap xxxx | xxxxx | xxxxxx | xx | | | | | | | |

| | c1 | c2 | c3 | c4 | c5 | с6 | c7 | c8 |
|----|---------|---------|---------|---------|---------|---------|---------|--------|
| | | | | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0 | 0 | 0.50505 | 1.5152 |
| r2 | 0 | 0 | 0 | 0 | 0.50505 | 0.50505 | 1.0101 | 1.5152 |
| r3 | 0.50505 | 0.50505 | 0.50505 | 0.50505 | 0.50505 | 1.0101 | 1.5152 | 2.0202 |
| r4 | 1.0101 | 1.0101 | 1.0101 | 1.0101 | 1.0101 | 1.5152 | 2.0202 | 2.5253 |

3

| r2 | U | U | U | U | 0.50505 | 0.50505 | 1.0101 | 1.5152 | |
|-----|---------|---------|---------|---------|---------|---------|--------|--------|--|
| r3 | 0.50505 | 0.50505 | 0.50505 | 0.50505 | 0.50505 | 1.0101 | 1.5152 | 2.0202 | |
| r4 | 1.0101 | 1.0101 | 1.0101 | 1.0101 | 1.0101 | 1.5152 | 2.0202 | 2.5253 | |
| r5 | 1.5152 | 1.5152 | 1.5152 | 1.5152 | 1.5152 | 2.0202 | 2.5253 | 3.0303 | |
| r96 | 45.455 | 45.455 | 45.455 | 45.96 | 45.96 | 45.96 | 46.465 | 47.475 | |
| r97 | 45.96 | 45.96 | 45.96 | 46.465 | 46.465 | 46.465 | 46.97 | 47.98 | |
| r98 | 46.465 | 46.465 | 46.465 | 46.465 | 46.97 | 46.97 | 47.475 | 48.485 | |
| r99 | 46.97 | 46.97 | 46.97 | 46.97 | 47.475 | 47.475 | 47.98 | 48.99 | |
| | | | | | | | | | |

| | r100 | 47.475 | 47.475 | 47.475 | 47.475 | 47.98 | 47.98 | 48.485 | 49.495 |
|-----|--------|-------------|-----------|---------|---------|---------|---------|---------|---------|
| xxx | TABLE: | savefraccoh | xxxxxxxxx | xxxxxxx | | | | | |
| | | c1 | c2 | c3 | c4 | c5 | с6 | c7 | c8 |
| | | | | | | | | | |
| | r1 | 0 | 0 | 0 | 0 | 0 | 0 | 0.24587 | 0.48182 |
| | r2 | 0 | 0 | 0 | 0 | 0.3075 | 0.25444 | 0.39276 | 0.41371 |
| | r3 | 0.30679 | 0.29486 | 0.27938 | 0.25939 | 0.2338 | 0.40362 | 0.49043 | 0.4833 |
| | r4 | 0.4668 | 0.45285 | 0.43438 | 0.40981 | 0.37721 | 0.50166 | 0.56006 | 0.53755 |
| | r5 | 0.56502 | 0.55132 | 0.53293 | 0.50802 | 0.47415 | 0.57101 | 0.61221 | 0.58103 |
| | r96 | 0.91292 | 0.9117 | 0.90997 | 0.91752 | 0.91364 | 0.90746 | 0.90692 | 0.90732 |
| | r97 | 0.91357 | 0.91236 | 0.91064 | 0.91812 | 0.91427 | 0.90815 | 0.90761 | 0.90799 |
| | r98 | 0.9142 | 0.913 | 0.9113 | 0.90882 | 0.91489 | 0.90882 | 0.90828 | 0.90865 |
| | r99 | 0.91482 | 0.91363 | 0.91195 | 0.90949 | 0.91549 | 0.90949 | 0.90894 | 0.90929 |
| | r100 | 0.91543 | 0.91425 | 0.91258 | 0.91014 | 0.91609 | 0.91013 | 0.90959 | 0.90992 |

1.2.4 Test FF_VFI_AZ_VEC Change Interest Rate and Discount

Show only save fraction of cash on hand:

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 750;
mp_params('it_z_n') = 9;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
Solve the model with several different interest rates and discount factor:
% Lower Savings Incentives
mp_params('fl_beta') = 0.80;
mp_params('fl_r') = 0.01;
ff_vfi_az_vec(mp_params, mp_support);
```

Elapsed time is 0.771613 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| - | | | | | | | | | |
|---|-----|------|-------|------|------|-----|------|-----|------|
| i | idx | ndim | numel | rowN | colN | sum | mean | std | coef |

| : | savefraccoh | 1 | 1 | 2 6750 | 750 | 9 | 3318.8 | 0.49167 | 0.27768 0.56 |
|-------|---------------|------|----------|---------|-----|----|--------|-----------|--------------|
| xxx ' | TABLE:savefra | ccoh | xxxxxxxx | xxxxxxx | | | | | |
| | c1 | | c2 | c3 | c4 | с5 | с6 | c7 | c8 |
| | | | | | | | | | |
| : | r1 | 0 | 0 | 0 | 0 | 0 | | 0 0.02347 | 75 0.13289 |
| | r2 | 0 | 0 | 0 | 0 | 0 | | 0.02347 | 75 0.13289 |

| r1 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023475 | 0.13289 |
|------|--------|---------|---------|---------|---------|---------|----------|---------|
| r2 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023475 | 0.13289 |
| r3 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023475 | 0.13289 |
| r4 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023475 | 0.13289 |
| r5 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023475 | 0.13289 |
| r746 | 0.8044 | 0.80333 | 0.80182 | 0.79961 | 0.79626 | 0.79093 | 0.7887 | 0.7824 |

```
      r747
      0.80465
      0.80359
      0.80209
      0.79989
      0.79655
      0.79124
      0.78903
      0.78277

      r748
      0.80491
      0.80385
      0.80235
      0.80016
      0.79683
      0.79154
      0.78936
      0.78315

      r749
      0.80517
      0.80411
      0.80262
      0.80043
      0.79712
      0.79185
      0.78969
      0.78352

      r750
      0.80542
      0.80437
      0.80288
      0.80071
      0.7974
      0.79215
      0.79002
      0.78389
```

```
% Higher Savings Incentives
mp_params('fl_beta') = 0.95;
mp_params('fl_r') = 0.04;
ff_vfi_az_vec(mp_params, mp_support);
```

Elapsed time is 2.484993 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-------------|---|-----|------|-------|------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 6750 | 750 | 9 | 4491.9 | 0.66547 | 0.28771 | 0.43 |

| xxx | TABLE: savefraccoh | xxxxxxxxxxxxxxx |
|-----|--------------------|-----------------|
| | | |

| | c1 | c2 | c3 | c4 | с5 | с6 | c7 | c8 |
|------|---------|---------|---------|---------|----------|---------|---------|---------|
| | | | | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0.031818 | 0.14726 | 0.31047 | 0.48484 |
| r2 | 0 | 0 | 0 | 0 | 0.031818 | 0.14726 | 0.31047 | 0.48484 |
| r3 | 0 | 0 | 0 | 0 | 0.031818 | 0.14726 | 0.31047 | 0.48484 |
| r4 | 0 | 0 | 0 | 0 | 0.031818 | 0.14726 | 0.31047 | 0.48484 |
| r5 | 0 | 0 | 0 | 0 | 0.031818 | 0.14726 | 0.31047 | 0.48484 |
| r746 | 0.92742 | 0.93 | 0.9283 | 0.92581 | 0.92578 | 0.92349 | 0.92443 | 0.91686 |
| r747 | 0.9275 | 0.93007 | 0.92838 | 0.9259 | 0.92588 | 0.92361 | 0.92457 | 0.91706 |
| r748 | 0.92757 | 0.93014 | 0.92846 | 0.92599 | 0.92598 | 0.92373 | 0.92472 | 0.91359 |
| r749 | 0.92764 | 0.93022 | 0.92854 | 0.92608 | 0.92608 | 0.92384 | 0.92115 | 0.91014 |
| r750 | 0.92772 | 0.93029 | 0.92862 | 0.92617 | 0.92618 | 0.92396 | 0.9213 | 0.90671 |

1.2.5 Test FF_VFI_AZ_VEC Changing Risk Aversion

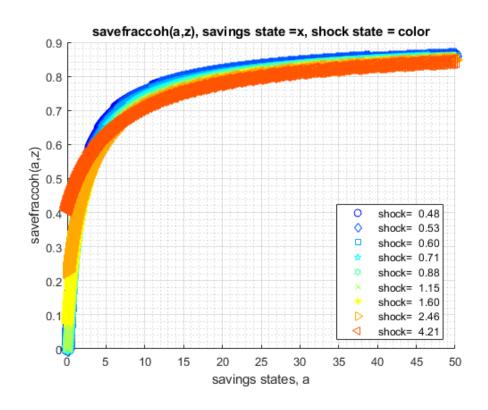
Here, again, show fraction of coh saved in summary tabular form, but also show it graphically.

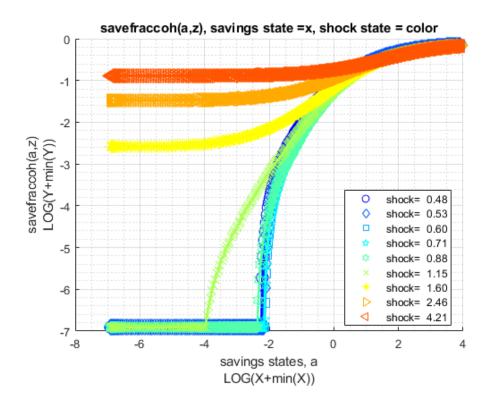
```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp support('ls ffcmd') = {'savefraccoh'};
mp support('ls ffsna') = {};
mp_support('ls_ffgrh') = {'savefraccoh'};
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 750;
mp_params('it_z_n') = 9;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
Solve the model with different risk aversion levels, higher preferences for risk:
% Lower Risk Aversion
mp_params('fl_crra') = 0.5;
ff_vfi_az_vec(mp_params, mp_support);
Elapsed time is 1.991475 seconds.
```

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| XXXXXXXXXXXXXXXX | XXXXX | XXXXXXX | XXXXXXXX. | .XXX | | | | | | |
|------------------|-------|---------|-----------|-------|------|------|--------|---------|--------|-------|
| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coefv |
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 6750 | 750 | 9 | 3735.9 | 0.55347 | 0.2897 | 0.523 |

| xxx TABLE:savefraccoh xxxxxxxxxxxxxxx | | | | | | | | | | | |
|---------------------------------------|---------|---------|---------|---------|---------|---------|----------|---------|--|--|--|
| | c1 | c2 | c3 | c4 | c5 | c6 | с7 | c8 | | | |
| | | | | | | | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0 | 0 | 0.075021 | 0.22812 | | | |
| r2 | 0 | 0 | 0 | 0 | 0 | 0 | 0.075021 | 0.22812 | | | |
| r3 | 0 | 0 | 0 | 0 | 0 | 0 | 0.075021 | 0.22812 | | | |
| r4 | 0 | 0 | 0 | 0 | 0 | 0 | 0.075021 | 0.22812 | | | |
| r5 | 0 | 0 | 0 | 0 | 0 | 0 | 0.075021 | 0.22812 | | | |
| r746 | 0.85928 | 0.85816 | 0.85657 | 0.85425 | 0.85428 | 0.8522 | 0.84972 | 0.84635 | | | |
| r747 | 0.85946 | 0.85834 | 0.85676 | 0.85444 | 0.85449 | 0.85242 | 0.84997 | 0.84665 | | | |
| r748 | 0.85963 | 0.85852 | 0.85694 | 0.85464 | 0.85469 | 0.85264 | 0.85021 | 0.84694 | | | |
| r749 | 0.85981 | 0.8587 | 0.85713 | 0.85483 | 0.85489 | 0.85286 | 0.85046 | 0.84723 | | | |
| r750 | 0.85998 | 0.85888 | 0.85731 | 0.85502 | 0.85509 | 0.85307 | 0.8507 | 0.84752 | | | |





When risk aversion increases, at every state-space point, the household wants to save more.

```
% Higher Risk Aversion
mp_params('fl_crra') = 5;
ff_vfi_az_vec(mp_params, mp_support);
```

Elapsed time is 2.026442 seconds.

r750

0.94113

0.93993

0.942

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX | X |
|---|---|
| | |

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coefv |
|-------------|---|-----|------|-------|------|------|--------|--------|---------|-------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 6750 | 750 | 9 | 4639.3 | 0.6873 | 0.28204 | 0.410 |

| xxx TABLE: | savefraccoh | xxxxxxxxx | xxxxxxx | | | | | |
|------------|-------------|-----------|---------|-----------|----------|---------|---------|---------|
| | c1 | c2 | с3 | c4 | с5 | с6 | c7 | c8 |
| | | | | | | | | |
| r1 | 0 | 0 | 0 | 0.008995 | 0.085095 | 0.21314 | 0.37277 | 0.53628 |
| r2 | 0 | 0 | 0 | 0.008995 | 0.085095 | 0.21314 | 0.37277 | 0.53628 |
| r3 | 0 | 0 | 0 | 0.008995 | 0.085095 | 0.21314 | 0.37277 | 0.53628 |
| r4 | 0 | 0 | 0 | 0.008995 | 0.085095 | 0.21314 | 0.37277 | 0.53628 |
| r5 | 0 | 0 | 0 | 0.0089949 | 0.085094 | 0.21314 | 0.37277 | 0.53628 |
| r746 | 0.94083 | 0.9396 | 0.94168 | 0.93912 | 0.93904 | 0.94041 | 0.93743 | 0.92949 |
| r747 | 0.94091 | 0.93969 | 0.94176 | 0.93921 | 0.93914 | 0.93674 | 0.93758 | 0.92969 |
| r748 | 0.94098 | 0.93977 | 0.94184 | 0.93931 | 0.93924 | 0.93686 | 0.93772 | 0.92618 |
| r749 | 0.94106 | 0.93985 | 0.94192 | 0.9394 | 0.93934 | 0.93699 | 0.93787 | 0.92269 |

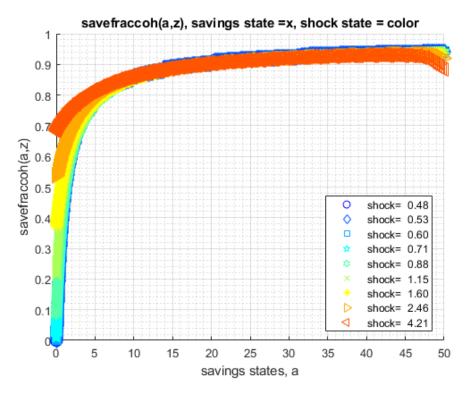
0.93949

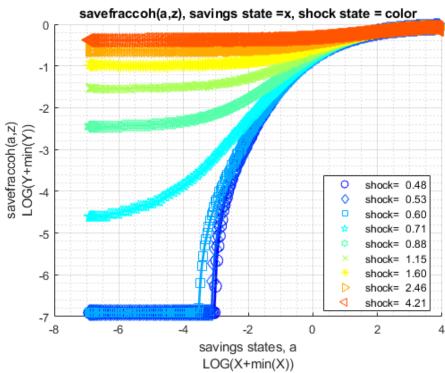
0.93944

0.93711

0.93801

0.91921





1.2.6 Test FF_VFI_AZ_VEC with Higher Uncertainty

Increase the standard deviation of the Shock.

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
```

r1

r2

0

0

0

0

0

0

```
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 750;
mp_params('it_z_n') = 9;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
Lower standard deviation of shock:
% Lower Risk Aversion
mp_params('fl_shk_std') = 0.10;
ff_vfi_az_vec(mp_params, mp_support);
Elapsed time is 2.065989 seconds.
-----
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
idx
                           ndim
                                   numel
                                           rowN
                                                   colN
                                                          \operatorname{\mathtt{sum}}
                                                                  mean
                                                                             std
                                                                                     coefva
   savefraccoh
                      1
                             2
                                   6750
                                           750
                                                   9
                                                          4026
                                                                 0.59644
                                                                           0.31533
                                                                                     0.5286
                 1
xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx
            c1
                      c2
                                          c4
                                                    с5
                                                               с6
                                                                          с7
                                                                                    с8
                                                             _____
   r1
                0
                          0
                                    0
                                              0
                                                        0
                                                             0.012569
                                                                       0.062884
                                                                                  0.13754
   r2
                0
                          0
                                    0
                                              0
                                                        0
                                                             0.012569
                                                                       0.062884
                                                                                  0.13754
                0
                          0
                                    0
                                              0
                                                        0
                                                            0.012569
                                                                       0.062884
   r3
                                                                                  0.13754
                0
                                    0
                          0
                                              0
                                                        0
                                                            0.012569
                                                                       0.062884
                                                                                  0.13754
   r4
   r5
                0
                          0
                                    0
                                              0
                                                        0
                                                            0.012569
                                                                       0.062884
                                                                                  0.13754
   r746
          0.91375
                    0.91251
                              0.91101 0.91289
                                                0.91057
                                                             0.91138
                                                                        0.91136
                                                                                  0.91021
   r747
          0.91387
                    0.91264
                              0.91114
                                        0.91302
                                                  0.91072
                                                             0.91153
                                                                        0.91152
                                                                                  0.91039
   r748
          0.91399
                    0.91277
                               0.91127
                                        0.91315
                                                   0.91086
                                                             0.91168
                                                                        0.91168
                                                                                  0.91056
   r749
          0.91411
                    0.91289
                               0.9114
                                        0.91329
                                                    0.911
                                                             0.91183
                                                                        0.91183
                                                                                  0.91073
   r750
          0.91423
                    0.91302
                              0.91153
                                        0.91342
                                                   0.91114
                                                             0.91197
                                                                        0.91199
                                                                                   0.9109
Higher shock standard deviation: low shock high asset save more, high shock more asset save less, high
shock low asset save more:
% Higher Risk Aversion
mp_params('fl_shk_std') = 0.40;
ff_vfi_az_vec(mp_params, mp_support);
Elapsed time is 2.184888 seconds.
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
i
                     idx
                            ndim
                                   numel
                                           rowN
                                                   colN
                                                                               std
                                                                                       coef
                                                           sum
                                                                    mean
                            ____
                                           ----
                                                   ----
                                                                   -----
                                                          -----
                                                                             -----
                             2
                                   6750
                                           750
                                                          4687.4
                     1
                                                   9
                                                                   0.69442
                                                                             0.27109
                                                                                       0.39
   savefraccoh
                 1
xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx
            c1
                      c2
                                c3
                                          c4
                                                     c5
                                                               с6
                                                                         с7
                                                                                    с8
```

0.030619

0.030619

0

0

0.24561

0.24561

0.80189

0.80189

0.55369

0.55369

| r3 | 0 | 0 | 0 | 0 | 0.030619 | 0.2456 | 0.55369 | 0.80189 |
|------|---------|---------|---------|---------|----------|---------|---------|---------|
| r4 | 0 | 0 | 0 | 0 | 0.030619 | 0.2456 | 0.55369 | 0.80189 |
| r5 | 0 | 0 | 0 | 0 | 0.030618 | 0.2456 | 0.55369 | 0.80189 |
| r746 | 0.93365 | 0.93335 | 0.9328 | 0.93173 | 0.92941 | 0.92713 | 0.92079 | 0.8402 |
| r747 | 0.93371 | 0.93341 | 0.93286 | 0.9318 | 0.92949 | 0.92723 | 0.92095 | 0.83734 |
| r748 | 0.93378 | 0.93348 | 0.93293 | 0.93187 | 0.92957 | 0.92733 | 0.92111 | 0.83449 |
| r749 | 0.93384 | 0.93354 | 0.933 | 0.93194 | 0.92965 | 0.92743 | 0.92127 | 0.83166 |
| r750 | 0.9339 | 0.9336 | 0.93306 | 0.93201 | 0.92973 | 0.92753 | 0.92143 | 0.82883 |

1.3 FF_VFI_AZ_BISEC_LOOP Dynamic Savings Problem Loop Continuous Choice

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: ff_vfi_az_bisec_loop from the MEconTools Package. This function solves the dynamic programming problem for a (a,z) model. Households can save a, and face AR(1) shock z. The problem is solved over the infinite horizon. This is the looped code, it is slow for larger state-space problems. The code uses continuous choices, solved with bisection. The state-space is on a grid, but choice grids are in terms of percentage of resources to save and solved exactly.

Links to Four Code:

Four Core Savings/Borrowing Dynamic Programming Solution Functions that are functions in the **MEconTools Package.**:

- Common Choice and States Grid : ff_vfi_az_loop, slow should use for testing new models
- Common Choice and States Grid: ff_vfi_az_vec, fast good for many purposes
- States Grid + Continuous Exact Savings as Share of Cash-on-Hand :ff_vfi_az_bisec_loop,
 high precision even with small grid
- States Grid + Continuous Exact Savings as Share of Cash-on-Hand : **ff_vfi_az_bisec_vec**, precision and speed

1.3.1 Test FF VFI AZ BISEC LOOP Defaults

Call the function with defaults. By default, shows the asset policy function summary. Model parameters can be changed by the mp_params.

```
%mp_params
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('fl_crra') = 1.5;
mp params('fl beta') = 0.94;
% call function
ff_vfi_az_bisec_loop(mp_params);
Elapsed time is 31.520504 seconds.
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
i
            idx
                 ndim
                         numel
                                 rowN
                                        colN
                                               sum
                                                       mean
                                                                std
                                                                       coefvari
                                                                                  min
                   2
                          700
                                 100
                                        7
                                              16866
                                                      24.094
                                                               14.071
                                                                       0.58399
                                                                                  0
   ap
xxx TABLE:ap xxxxxxxxxxxxxxxxx
           c1
                    c2
                              сЗ
                                        c4
                                                 с5
                                                          с6
                                                                    с7
          -----
                   -----
                             -----
                                      -----
                                                -----
                                                         -----
```

| r1 | 0 | 0 | 0 | 0 | 0.13188 | 0.66203 | 1.9859 |
|------|---------|---------|---------|---------|---------|---------|--------|
| r2 | 0.25914 | 0.26426 | 0.29511 | 0.39221 | 0.57697 | 1.1208 | 2.4569 |
| r3 | 0.65371 | 0.66543 | 0.70966 | 0.82502 | 1.029 | 1.582 | 2.9298 |
| r4 | 1.0748 | 1.0921 | 1.1447 | 1.2698 | 1.5151 | 2.0481 | 3.4046 |
| r5 | 1.5152 | 1.5319 | 1.5903 | 1.721 | 2.0011 | 2.5252 | 3.8802 |
| r96 | 45.561 | 45.615 | 45.712 | 45.887 | 46.192 | 46.835 | 48.252 |
| r97 | 46.049 | 46.104 | 46.201 | 46.377 | 46.681 | 47.325 | 48.743 |
| r98 | 46.54 | 46.593 | 46.69 | 46.866 | 47.171 | 47.815 | 49.235 |
| r99 | 47.029 | 47.082 | 47.179 | 47.356 | 47.661 | 48.304 | 49.734 |
| r100 | 47.518 | 47.572 | 47.67 | 47.845 | 48.15 | 48.793 | 50.252 |

1.3.2 Test FF_VFI_AZ_BISEC_LOOP Speed Tests

Call the function with different a and z grid size, print out speed:

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_timer') = true;
mp_support('ls_ffcmd') = {};
A grid 50, shock grid 5:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 50;
mp_params('it_z_n') = 5;
ff_vfi_az_bisec_loop(mp_params, mp_support);
Elapsed time is 9.142315 seconds.
A grid 100, shock grid 7:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 100;
mp_params('it_z_n') = 7;
ff_vfi_az_bisec_loop(mp_params, mp_support);
Elapsed time is 26.910198 seconds.
A grid 200, shock grid 9:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 200;
mp_params('it_z_n') = 9;
ff_vfi_az_bisec_loop(mp_params, mp_support);
```

Run the function first without any outputs;

Elapsed time is 74.127079 seconds.

```
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 50;
mp_params('it_z_n') = 5;
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_timer') = false;
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
```

Test FF VFI AZ BISEC LOOP Control Outputs

Run the function and show policy function for savings choice. For ls_ffcmd, ls_ffsna, ls_ffgrh, can include these: 'v', 'ap', 'c', 'y', 'coh', 'savefraccoh'. These are value, aprime savings choice, consumption, income, cash on hand, and savings fraction as cash-on-hand.

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
% ls_{ffcmd}: summary print which outcomes
mp_support('ls_ffcmd') = {};
\% ls_ffsna: detail print which outcomes
mp_support('ls_ffsna') = {'ap'};
% ls_ffgrh: graphical print which outcomes
mp_support('ls_ffgrh') = {'ap'};
ff_vfi_az_bisec_loop(mp_params, mp_support);
```

Elapsed time is 9.221215 seconds.

42

41.837

39.663

| group | a | mean_z_0_54195 | mean_z_0_66401 | mean_z_0_88162 | mean_z_1_3095 | mean_ |
|-------|--------|----------------|----------------|----------------|---------------|-------|
| | | | | | | |
| 1 | 0 | 0 | 0 | 0 | 0.17037 | 1. |
| 2 | 1.0204 | 0.69295 | 0.72405 | 0.84423 | 1.099 | 2. |
| 3 | 2.0408 | 1.5665 | 1.6143 | 1.7589 | 2.0408 | 3. |
| 4 | 3.0612 | 2.4757 | 2.534 | 2.6903 | 3.0612 | 4. |
| 5 | 4.0816 | 3.4036 | 3.4686 | 3.6319 | 4.0274 | 4. |
| 6 | 5.102 | 4.3431 | 4.4131 | 4.5822 | 4.9848 | 5. |
| 7 | 6.1224 | 5.2908 | 5.3648 | 5.5384 | 5.9466 | 6. |
| 8 | 7.1429 | 6.2445 | 6.3216 | 6.4989 | 6.9116 | 7. |
| 9 | 8.1633 | 7.2029 | 7.2827 | 7.463 | 7.8793 | 8. |
| 10 | 9.1837 | 8.1651 | 8.2469 | 8.4301 | 8.8495 | 9. |
| 11 | 10.204 | 9.1837 | 9.2139 | 9.3992 | 9.8212 | 10 |
| 12 | 11.224 | 10.175 | 10.204 | 10.37 | 10.795 | 11 |
| 13 | 12.245 | 11.141 | 11.225 | 11.343 | 11.769 | 12 |
| 14 | 13.265 | 12.109 | 12.198 | 12.316 | 12.745 | 13 |
| 15 | 14.286 | 13.079 | 13.169 | 13.291 | 13.721 | 1 |
| 16 | 15.306 | 14.051 | 14.142 | 14.286 | 14.699 | |
| 17 | 16.327 | 15.026 | 15.117 | 15.306 | 15.677 | 1 |
| 18 | 17.347 | 16.001 | 16.093 | 16.289 | 16.655 | 1 |
| 19 | 18.367 | 16.978 | 17.069 | 17.265 | 17.634 | 18 |
| 20 | 19.388 | 17.955 | 18.048 | 18.243 | 18.614 | 19 |
| 21 | 20.408 | 18.934 | 19.026 | 19.223 | 19.595 | 20 |
| 22 | 21.429 | 19.913 | 20.006 | 20.203 | 20.577 | 21 |
| 23 | 22.449 | 20.894 | 20.986 | 21.184 | 21.559 | 22 |
| 24 | 23.469 | 21.875 | 21.968 | 22.166 | 22.542 | 23 |
| 25 | 24.49 | 22.856 | 22.95 | 23.148 | 23.525 | 24 |
| 26 | 25.51 | 23.838 | 23.932 | 24.131 | 24.509 | 25 |
| 27 | 26.531 | 24.821 | 24.915 | 25.114 | 25.51 | 26 |
| 28 | 27.551 | 25.804 | 25.899 | 26.098 | 26.531 | 27 |
| 29 | 28.571 | 26.788 | 26.883 | 27.082 | 27.524 | 28 |
| 30 | 29.592 | 27.772 | 27.867 | 28.067 | 28.507 | 29 |
| 31 | 30.612 | 28.757 | 28.852 | 29.052 | 29.492 | 30 |
| 32 | 31.633 | 29.742 | 29.837 | 30.037 | 30.477 | 31 |
| 33 | 32.653 | 30.727 | 30.822 | 31.023 | 31.463 | 32 |
| 34 | 33.673 | 31.712 | 31.808 | 32.009 | 32.449 | 3 |
| 35 | 34.694 | 32.698 | 32.795 | 32.995 | 33.435 | 34 |
| 36 | 35.714 | 33.685 | 33.781 | 33.982 | 34.422 | 35 |
| 37 | 36.735 | 34.694 | 34.768 | 34.969 | 35.41 | 36 |
| 38 | 37.755 | 35.714 | 35.755 | 35.955 | 36.397 | 37 |
| 39 | 38.776 | 36.703 | 36.741 | 36.942 | 37.385 | 38 |
| 40 | 39.796 | 37.689 | 37.755 | 37.93 | 38.372 | 39 |
| 41 | 40.816 | 38.676 | 38.774 | 38.918 | 39.361 | 40 |
| 42 | 41 837 | 39 663 | 39 761 | 39 906 | 40 349 | 41 |

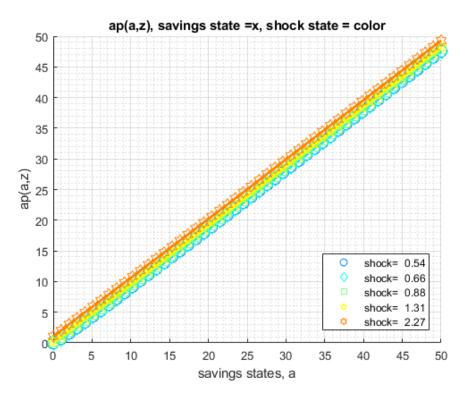
39.761

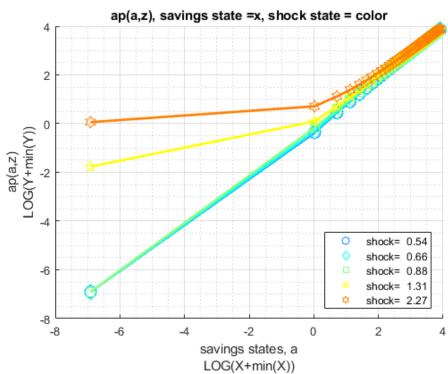
39.906

40.349

41.

| 43 | 42.857 | 40.65 | 40.749 | 40.894 | 41.337 | 42. |
|----|--------|--------|--------|--------|--------|-----|
| 44 | 43.878 | 41.637 | 41.736 | 41.881 | 42.326 | 43. |
| 45 | 44.898 | 42.624 | 42.724 | 42.87 | 43.314 | 44. |
| 46 | 45.918 | 43.612 | 43.711 | 43.877 | 44.303 | 45. |
| 47 | 46.939 | 44.6 | 44.7 | 44.898 | 45.293 | 46. |
| 48 | 47.959 | 45.589 | 45.688 | 45.893 | 46.281 | 47. |
| 49 | 48.98 | 46.577 | 46.676 | 46.881 | 47.27 | 4 |
| 50 | 50 | 47.566 | 47.664 | 47.87 | 48.259 | 49. |
| | | | | | | |





Run the function and show summaries for savings and fraction of coh saved:

```
mp_params('it_z_n') = 9;
mp_support('ls_ffcmd') = {'ap', 'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
mp_support('bl_vfi_store_all') = true; % store c(a,z), y(a,z)
ff_vfi_az_bisec_loop(mp_params, mp_support);
Elapsed time is 35.765637 seconds.
_____
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
std
                 i
                     idx
                           ndim
                                  numel
                                          rowN
                                                  colN
                                                          sum
                                                                   mean
                                                                                     coefv
                      1
                            2
                                   900
                                           100
                                                   9
                                                          21835
                                                                   24.261
                                                                            14.095
                                                                                     0.580
                 1
                 2
                      2
                            2
                                   900
                                           100
                                                   9
                                                         754.27
                                                                  0.83808
                                                                            0.1259
                                                                                     0.150
   savefraccoh
xxx TABLE:ap xxxxxxxxxxxxxxxxx
                                                              с6
                                                                        с7
                     c2
                                сЗ
                                          c4
                                                    c5
                                                                                  с8
            с1
                    -----
                              -----
                                        -----
                                                  -----
                                                            -----
   r1
                0
                         0
                                   0
                                             0
                                                       0
                                                            0.082559
                                                                      0.50504
                                                                                1.2988
                    0.25936
   r2
          0.26067
                              0.26888
                                        0.30308
                                                  0.39296
                                                           0.52492
                                                                      0.96211
                                                                                1.7672
   r3
          0.65383
                    0.65589
                            0.67297
                                        0.71974
                                                  0.82473
                                                            1.0101
                                                                      1.4185
                                                                                2.2377
          1.0734
                    1.0789
                             1.1015
                                       1.1556
                                                 1.2679
                                                            1.4909
                                                                      1.8821
                                                                                2.7095
   r4
           1.5151
                    1.5159
                              1.5427
                                        1.6019
                                                    1.72
                                                             1.9489
                                                                        2.349
                                                                                3.1825
   r5
                                                             46.134
   r96
           45.547
                     45.58
                              45.636
                                         45.73
                                                   45.888
                                                                       46.603
                                                                                 47.52
   r97
           46.036
                     46.069
                               46.126
                                         46.22
                                                   46.377
                                                             46.622
                                                                       47.092
                                                                                48.009
   r98
           46.525
                     46.559
                               46.615
                                         46.71
                                                   46.867
                                                             47.112
                                                                       47.583
                                                                                48.501
   r99
           47.014
                     47.049
                               47.104
                                         47.198
                                                   47.357
                                                             47.601
                                                                       48.072
                                                                                48.992
           47.503
                               47.593
                                                   47.845
                                                             48.091
   r100
                     47.537
                                         47.687
                                                                       48.561
                                                                                49.495
xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxxx
                                                                                  с8
            c1
                     c2
                               сЗ
                                         c4
                                                    с5
                                                              с6
                                                                        с7
          -----
                    -----
                              -----
                                        -----
                                                  -----
                                                            -----
                                                            0.056268
                                                                      0.24587
   r1
                0
                         Ω
                                   Ω
                                             0
                                                       0
                                                                                0.41301
                            0.20843
   r2
          0.23098
                                        0.21203
                                                  0.23925
                     0.217
                                                          0.26445
                                                                      0.3741
                                                                                0.48253
                                                  0.38179
   r3
          0.39717
                    0.38292 0.37227
                                        0.36965
                                                            0.40361
                                                                      0.45915
                                                                                0.53532
   r4
          0.49605
                    0.48369 0.47368 0.46883
                                                  0.47347
                                                            0.49364
                                                                      0.52177
                                                                                0.57677
   r5
          0.56502
                    0.55159 0.54262 0.53709
                                                  0.53825
                                                            0.55086
                                                                      0.56947
                                                                                0.61021
          0.91477
                    0.91422
                              0.91361
                                       0.91294
                                                  0.91221
                                                             0.9109
                                                                      0.90961
                                                                                0.90818
   r96
   r97
          0.91508
                    0.91453
                              0.91395
                                        0.91328
                                                  0.91254
                                                            0.91123
                                                                      0.90998
                                                                                0.90855
   r98
          0.91538
                    0.91486
                              0.91425
                                        0.91361
                                                  0.91288
                                                            0.91157
                                                                      0.91035
                                                                                0.90894
   r99
          0.91569
                    0.91517
                              0.91456
                                        0.91392
                                                  0.91322
                                                             0.9119
                                                                      0.91068
                                                                                0.90934
          0.91596
                    0.91544
                              0.91486
                                        0.91422
                                                  0.91352
                                                             0.91224
                                                                      0.91102
                                                                                0.90992
   r100
```

1.3.4 Test FF_VFI_AZ_BISEC_LOOP Change Interest Rate and Discount

Show only save fraction of cash on hand:

 $mp_params('it_a_n') = 100;$

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
```

r2

0

0

0.029535

0.21258

0.4539

```
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 50;
mp_params('it_z_n') = 5;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
Solve the model with several different interest rates and discount factor:
% Lower Savings Incentives
mp_params('fl_beta') = 0.80;
mp_params('fl_r') = 0.01;
ff_vfi_az_bisec_loop(mp_params, mp_support);
Elapsed time is 2.672239 seconds.
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
ndim numel
                                      rowN colN
                                                                      std
                                                                             coef
                  idx
                                                   sum
                                                            mean
                         ----
                               ----
                                             ----
                                                           -----
                                      ----
                                                   ----
                                                                    -----
                   1
                         2
                                250
                                       50
                                             5
                                                  119.77
                                                           0.47907
                                                                    0.28808
                                                                             0.60
   savefraccoh
               1
xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxxx
          c1 c2 c3
                                     c4
                                              с5
                 -----
                          -----
   r1
             0
                      0
                               0
                                        0
                                            0.10641
   r2
             0
                      0
                               0
                                        0
                                            0.10641
   r3
             0
                      0
                               0
                                        0
                                            0.10629
                      0
                               0
   r4
             0
                                        0
                                           0.10601
   r5
             0
                      0
                               0
                                          0.10793
                                        0
   r46
      0.79096  0.78788  0.78242  0.77293  0.76768
   r47
        0.79554  0.79261  0.78749  0.77754  0.77168
        0.79991 0.79716 0.79228
                                   0.78291
                                            0.7754
   r48
   r49
        0.80406
                 0.80146 0.79688
                                    0.788
                                            0.77891
                                   0.79283
        0.80699
                 0.80396
                          0.8003
                                            0.78218
   r50
% Higher Savings Incentives
mp_params('fl_beta') = 0.95;
mp_params('fl_r') = 0.04;
ff_vfi_az_bisec_loop(mp_params, mp_support);
Elapsed time is 11.445094 seconds.
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
i
                   idx
                       \mathtt{ndim}
                               numel
                                      rowN
                                             colN
                                                    sum
                                                            mean
                                                                      std
                                                                             coef
                         ----
                               ----
                                      ----
                                             ----
                                                   ____
                                                           -----
                                                                    -----
                         2
                                250
                                       50
                                              5
                                                  162.74
                                                           0.65097
                                                                    0.29744
                                                                             0.45
   savefraccoh
               1
                   1
c1 c2 c3
                                     c4
                                              с5
                 -----
                          -----
                      0
                          0.029138
                                    0.21236
                                             0.45384
   r1
             0
```

| r3 | 0 | 0 | 0.03219 | 0.21401 | 0.45448 |
|-----|---------|---------|----------|---------|---------|
| r4 | 0 | 0 | 0.039301 | 0.21795 | 0.45607 |
| r5 | 0 | 0 | 0.045923 | 0.22542 | 0.45909 |
| r46 | 0.9221 | 0.92124 | 0.92029 | 0.91929 | 0.91587 |
| r47 | 0.92408 | 0.92329 | 0.92237 | 0.92142 | 0.91816 |
| r48 | 0.92591 | 0.92518 | 0.92432 | 0.92344 | 0.92057 |
| r49 | 0.92762 | 0.92692 | 0.92612 | 0.92536 | 0.92347 |
| r50 | 0.92924 | 0.9286 | 0.92792 | 0.92737 | 0.92783 |

1.3.5 Test FF_VFI_AZ_BISEC_LOOP Changing Risk Aversion

Here, again, show fraction of coh saved in summary tabular form, but also show it graphically.

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {'savefraccoh'};
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 100;
mp_params('it_z_n') = 5;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
```

Solve the model with different risk aversion levels, higher preferences for risk:

```
% Lower Risk Aversion
mp_params('fl_crra') = 0.5;
ff_vfi_az_bisec_loop(mp_params, mp_support);
```

Elapsed time is 20.016228 seconds.

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

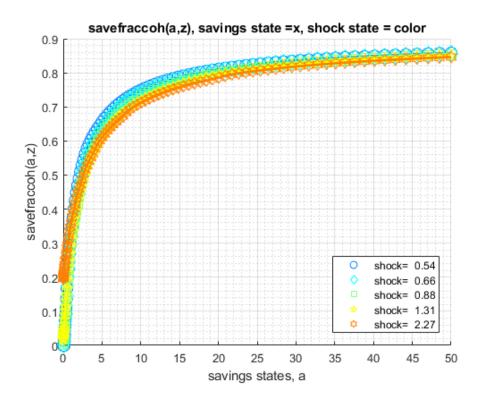
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

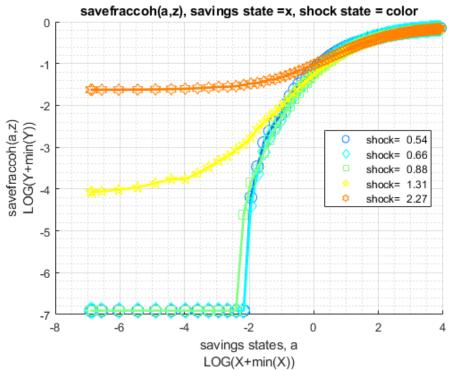
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | 1 | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-------------|---|-----|------|-------|------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 500 | 100 | 5 | 270.24 | 0.54048 | 0.30018 | 0.5 |

xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxxx

| | c1 | c2 | сЗ | c4 | с5 |
|------|---------|---------|---------|----------|---------|
| | | | | | |
| r1 | 0 | 0 | 0 | 0.016108 | 0.19552 |
| r2 | 0 | 0 | 0 | 0.016138 | 0.19555 |
| r3 | 0 | 0 | 0 | 0.016352 | 0.19564 |
| r4 | 0 | 0 | 0 | 0.016962 | 0.19591 |
| r5 | 0 | 0 | 0 | 0.018091 | 0.19646 |
| r96 | 0.85334 | 0.85127 | 0.84879 | 0.84602 | 0.84037 |
| r97 | 0.85456 | 0.85255 | 0.85017 | 0.84748 | 0.8419 |
| r98 | 0.85578 | 0.85383 | 0.85151 | 0.84889 | 0.84339 |
| r99 | 0.85694 | 0.85502 | 0.85279 | 0.85023 | 0.84483 |
| r100 | 0.85804 | 0.85621 | 0.85404 | 0.85154 | 0.84623 |
| | | | | | |





When risk aversion increases, at every state-space point, the household wants to save more.

$1.3.\ \ FF_VFI_AZ_BISEC_LOOP\ DYNAMIC\ SAVINGS\ PROBLEM\ LOOP\ CONTINUOUS\ CHOICE37$

| xxxxxxxxx | xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx | | | | | | | | | | | | |
|------------|---------------------------------|------------|--------|--------|---------|--------|--------|---------|---------|---|--|--|--|
| | | i idx | ndim | numel | rowN | colN | sum | mean | std | | | | |
| | | | | | | | | | | | | | |
| savefr | raccoh | 1 1 | 2 | 500 | 100 | 5 | 337.39 | 0.67477 | 0.28798 | (| | | |
| xxx TABLE: | savefraco | oh xxxxxxx | xxxxxx | xxxx | | | | | | | | | |
| | c1 | c2 | | c3 | c4 | с5 | | | | | | | |
| | | | | | | | | | | | | | |
| r1 | C | | 0 0. | 082635 | 0.2781 | 0.50 | 78 | | | | | | |
| r2 | C | | 0 0. | 082665 | 0.27813 | 0.50 | 78 | | | | | | |
| r3 | C | | 0 0 | .08297 | 0.27828 | 0.5078 | 36 | | | | | | |
| r4 | C | | 0 0. | 083794 | 0.27871 | 0.5080 | 01 | | | | | | |
| r5 | C | | 0 0. | 085381 | 0.27956 | 0.5083 | 35 | | | | | | |
| r96 | 0.93751 | 0.9369 | 9 0 | .93641 | 0.93586 | 0.9348 | 32 | | | | | | |

0.9368

0.93775

0.93867

0.93961

0.93586

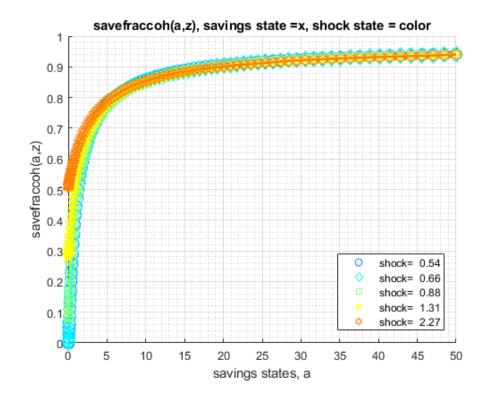
0.93702

0.93839

0.94013

coef

0.42



r97

r98

r99 r100 0.93839

0.93925

0.9401

0.94089

0.9379

0.93876

0.93961

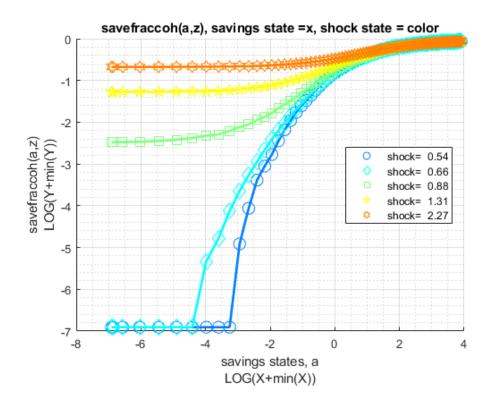
0.94044

0.93732

0.93824

0.93909

0.93998



1.3.6 Test FF_VFI_AZ_BISEC_LOOP with Higher Uncertainty

mp_support = containers.Map('KeyType','char', 'ValueType','any');

Increase the standard deviation of the Shock.

```
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 100;
mp_params('it_z_n') = 5;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
Lower standard deviation of shock:
% Lower Risk Aversion
mp_params('fl_shk_std') = 0.10;
ff_vfi_az_bisec_loop(mp_params, mp_support);
Elapsed time is 19.744605 seconds.
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
                                                     colN
                                                                                   std
                                                                                            coef
                       idx
                             ndim
                                     numel
                                              rowN
                                                              sum
                                                                       mean
                              2
                                      500
                                                      5
                                                             295.24
                                                                       0.59048
    savefraccoh
                                              100
                                                                                 0.32213
                                                                                            0.54
xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx
             c1
                       c2
                                  сЗ
                                              c4
                                                        c5
                      _____
           -----
                                -----
                                                      -----
```

| r1 | 0 | 0 | 0 | 0.030451 | 0.12142 |
|------|---------|---------|---------|----------|---------|
| r2 | 0 | 0 | 0 | 0.030481 | 0.12145 |
| r3 | 0 | 0 | 0 | 0.030725 | 0.12164 |
| r4 | 0 | 0 | 0 | 0.031366 | 0.12209 |
| r5 | 0 | 0 | 0 | 0.032648 | 0.12304 |
| r96 | 0.90824 | 0.90775 | 0.90726 | 0.90675 | 0.90629 |
| r97 | 0.90943 | 0.90894 | 0.90845 | 0.90797 | 0.90751 |
| r98 | 0.91056 | 0.9101 | 0.90961 | 0.90916 | 0.9087 |
| r99 | 0.91166 | 0.9112 | 0.91074 | 0.91029 | 0.90983 |
| r100 | 0.9127 | 0.91227 | 0.91184 | 0.91138 | 0.91096 |

Higher shock standard deviation: low shock high asset save more, high shock more asset save less, high shock low asset save more:

```
% Higher Risk Aversion
mp_params('fl_shk_std') = 0.40;
ff_vfi_az_bisec_loop(mp_params, mp_support);
```

Elapsed time is 17.556461 seconds.

0.92689

r100

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

0.9257

| ******* | XXXXX | XXXXXXX | XXXXXXXX | XXX | | | | | | |
|-------------|-------|---------|----------|-------|------|------|--------|---------|---------|-----|
| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coe |
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 500 | 100 | 5 | 354.06 | 0.70811 | 0.27055 | 0.3 |

0.92103

0.92811

0.38

| xxx | xx TABLE:savefraccoh xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx | | | | | | | | | | | |
|-----|--|---------|---------|----------|---------|---------|--|--|--|--|--|--|
| | | c1 | c2 | с3 | c4 | с5 | | | | | | |
| | | | | | | | | | | | | |
| | r1 | 0 | 0 | 0.030725 | 0.36968 | 0.77064 | | | | | | |
| | r2 | 0 | 0 | 0.030725 | 0.36968 | 0.77064 | | | | | | |
| | r3 | 0 | 0 | 0.030695 | 0.36959 | 0.77064 | | | | | | |
| | r4 | 0 | 0 | 0.030634 | 0.36934 | 0.77061 | | | | | | |
| | r5 | 0 | 0 | 0.030542 | 0.36885 | 0.77043 | | | | | | |
| | r96 | 0.92429 | 0.92289 | 0.92091 | 0.91688 | 0.92026 | | | | | | |
| | r97 | 0.92496 | 0.92362 | 0.92173 | 0.91795 | 0.92231 | | | | | | |
| | r98 | 0.92564 | 0.92432 | 0.92252 | 0.91898 | 0.92429 | | | | | | |
| | r99 | 0.92628 | 0.92503 | 0.92332 | 0.91999 | 0.92625 | | | | | | |

FF_VFI_AZ_BISEC_VEC Dynamic Savings Problem Vectorized Continuous Exact

0.92408

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: ff_vfi_az_bisec_vec from the MEconTools Package. This function solves the dynamic programming problem for a (a,z) model. Households can save a, and face AR(1) shock z. The problem is solved over the infinite horizon. This is a vectorized code, it is much faster for larger state-space problems then looped code.

The code uses continuous choices, solved with bi(multi)section. The state-space is on a grid, but choice grids are in terms of percentage of resources available, which is individual specific, to save and solved exactly up to $((1/(2)^{1}6)*100=0.001525878)$ percentage of cash on hand. THe ff_vfi_az_vec from the MEconTools Package solves the same problem using vectorized common grid code where the choice set and state space share the same grid.

This is the vectorized code, its speed is much faster than the looped code. The function is designed to have small memory footprint and requires low computing resources, yet is fast.

Links to Four Code:

Four Core Savings/Borrowing Dynamic Programming Solution Functions that are functions in the **MEconTools Package.**:

- Common Choice and States Grid: ff_vfi_az_loop, slow should use for testing new models
- Common Choice and States Grid: ff vfi az vec, fast good for many purposes
- States Grid + Continuous Exact Savings as Share of Cash-on-Hand :ff_vfi_az_bisec_loop, high precision even with small grid
- States Grid + Continuous Exact Savings as Share of Cash-on-Hand : **ff_vfi_az_bisec_vec**, precision and speed

1.4.1 Test FF_VFI_AZ_BISEC_VEC Defaults

Call the function with defaults. By default, shows the asset policy function summary. Model parameters can be changed by the mp_params.

```
%mp_params
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('fl_crra') = 1.5;
mp_params('fl_beta') = 0.94;
% call function
ff_vfi_az_bisec_vec(mp_params);
```

Elapsed time is 0.668798 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coefvari | min |
|----|---|-----|------|-------|------|------|-------|--------|--------|----------|-----|
| | - | | | | | | | | | | |
| ap | 1 | 1 | 2 | 700 | 100 | 7 | 16866 | 24.094 | 14.071 | 0.58399 | 0 |

xxx TABLE:ap xxxxxxxxxxxxxxxxx

| | c1 | c2 | c3 | c4 | с5 | с6 | c7 |
|------|---------|---------|---------|---------|---------|---------|--------|
| | | | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0.13188 | 0.66203 | 1.9859 |
| r2 | 0.25914 | 0.26426 | 0.29511 | 0.39221 | 0.57697 | 1.1208 | 2.4569 |
| r3 | 0.65371 | 0.66543 | 0.70966 | 0.82502 | 1.029 | 1.582 | 2.9298 |
| r4 | 1.0748 | 1.0921 | 1.1447 | 1.2698 | 1.5151 | 2.0481 | 3.4046 |
| r5 | 1.5152 | 1.5319 | 1.5903 | 1.721 | 2.0011 | 2.5252 | 3.8802 |
| r96 | 45.561 | 45.615 | 45.712 | 45.887 | 46.192 | 46.835 | 48.252 |
| r97 | 46.049 | 46.104 | 46.201 | 46.377 | 46.681 | 47.325 | 48.743 |
| r98 | 46.54 | 46.593 | 46.69 | 46.866 | 47.171 | 47.815 | 49.235 |
| r99 | 47.029 | 47.082 | 47.179 | 47.356 | 47.661 | 48.304 | 49.734 |
| r100 | 47.518 | 47.572 | 47.67 | 47.845 | 48.15 | 48.793 | 50.252 |

1.4.2 Test FF_VFI_AZ_BISEC_VEC Speed Tests

Call the function with defaults. By default, shows the asset policy function summary. Model parameters can be changed by the mp_params.

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
```

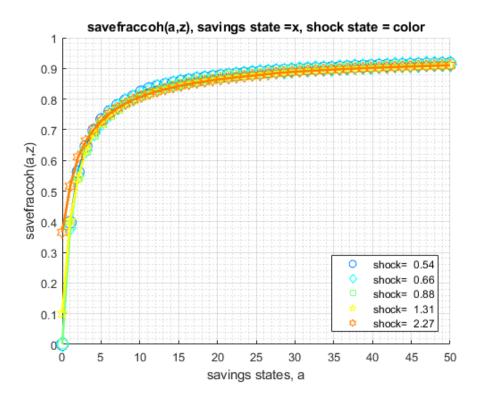
```
mp_support('bl_timer') = true;
mp_support('ls_ffcmd') = {};
A grid 50, shock grid 5:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 50;
mp_params('it_z_n') = 5;
ff_vfi_az_bisec_vec(mp_params, mp_support);
Elapsed time is 0.336083 seconds.
A grid 750, shock grid 15:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 750;
mp_params('it_z_n') = 15;
ff_vfi_az_bisec_vec(mp_params, mp_support);
Elapsed time is 23.612756 seconds.
A grid 600, shock grid 45:
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 600;
mp_params('it_z_n') = 45;
ff_vfi_az_bisec_vec(mp_params, mp_support);
Elapsed time is 46.281741 seconds.
      Test FF_VFI_AZ_BISEC_VEC Control Outputs
Run the function first without any outputs;
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 50;
mp_params('it_z_n') = 5;
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_timer') = false;
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
Run the function and show policy function for savings choice. For ls_ffcmd, ls_ffsma, ls_ffgrh, can
include these: 'v', 'ap', 'c', 'y', 'coh', 'savefraccoh'. These are value, aprime savings choice, consumption,
income, cash on hand, and savings fraction as cash-on-hand.
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
% ls_ffcmd: summary print which outcomes
mp_support('ls_ffcmd') = {};
% ls_ffsna: detail print which outcomes
mp_support('ls_ffsna') = {'savefraccoh'};
% ls_ffgrh: graphical print which outcomes
mp_support('ls_ffgrh') = {'savefraccoh'};
ff_vfi_az_bisec_vec(mp_params, mp_support);
Elapsed time is 0.470134 seconds.
group a mean_z_0_54195 mean_z_0_66401 mean_z_0_88162 mean_z_1_3095
                    -----
                                                                           -----
                 0
                               0
                                                0
                                                                  0
                                                                              0.10165
```

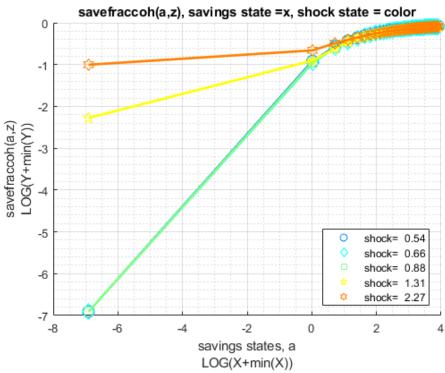
mean_z

0.3

0.5 0.6 0.6 0.7 0. 0.7 0.7 0.7 0.7 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0. 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.8 0.9 0. 0.9 0.9 0.9 0.9 0. 0.9 0.9 0.9 0.9 0.9

| 2 | 1.0204 | 0.39833 | 0.38191 | 0.38826 | 0.40373 |
|----|--------|---------|---------|---------|---------|
| 3 | 2.0408 | 0.56236 | 0.54875 | 0.54619 | 0.54161 |
| 4 | 3.0612 | 0.64616 | 0.63545 | 0.6306 | 0.63591 |
| 5 | 4.0816 | 0.69783 | 0.6891 | 0.6837 | 0.6873 |
| 6 | 5.102 | 0.73323 | 0.7259 | 0.72068 | 0.72184 |
| 7 | 6.1224 | 0.75917 | 0.75291 | 0.74803 | 0.74784 |
| 8 | 7.1429 | 0.77909 | 0.77363 | 0.76911 | 0.76817 |
| 9 | 8.1633 | 0.79493 | 0.79011 | 0.78593 | 0.78452 |
| 10 | 9.1837 | 0.80787 | 0.80354 | 0.79969 | 0.79801 |
| 11 | 10.204 | 0.82343 | 0.81474 | 0.81114 | 0.8093 |
| 12 | 11.224 | 0.83412 | 0.82591 | 0.82084 | 0.81895 |
| 13 | 12.245 | 0.84116 | 0.83759 | 0.82917 | 0.82725 |
| 14 | 13.265 | 0.84733 | 0.84434 | 0.83637 | 0.83448 |
| 15 | 14.286 | 0.85282 | 0.84998 | 0.84272 | 0.84083 |
| 16 | 15.306 | 0.8577 | 0.85508 | 0.84947 | 0.84647 |
| 17 | 16.327 | 0.86213 | 0.85966 | 0.85685 | 0.85151 |
| 18 | 17.347 | 0.86613 | 0.86378 | 0.86143 | 0.856 |
| 19 | 18.367 | 0.86976 | 0.8675 | 0.86521 | 0.86008 |
| 20 | 19.388 | 0.87305 | 0.87092 | 0.86869 | 0.86384 |
| 21 | 20.408 | 0.87608 | 0.87403 | 0.8719 | 0.86726 |
| 22 | 21.429 | 0.87885 | 0.8769 | 0.87486 | 0.8704 |
| 23 | 22.449 | 0.88145 | 0.87955 | 0.8776 | 0.87333 |
| 24 | 23.469 | 0.88383 | 0.88203 | 0.88013 | 0.87601 |
| 25 | 24.49 | 0.88602 | 0.88432 | 0.88248 | 0.87852 |
| 26 | 25.51 | 0.8881 | 0.88645 | 0.88468 | 0.88087 |
| 27 | 26.531 | 0.89002 | 0.88844 | 0.88673 | 0.88361 |
| 28 | 27.551 | 0.89185 | 0.89033 | 0.88865 | 0.88685 |
| 29 | 28.571 | 0.89353 | 0.89207 | 0.89045 | 0.88895 |
| 30 | 29.592 | 0.89515 | 0.89371 | 0.89216 | 0.89063 |
| 31 | 30.612 | 0.89664 | 0.89527 | 0.89375 | 0.89225 |
| 32 | 31.633 | 0.89808 | 0.89674 | 0.89524 | 0.89378 |
| 33 | 32.653 | 0.89942 | 0.89811 | 0.89667 | 0.89521 |
| 34 | 33.673 | 0.90067 | 0.89942 | 0.89802 | 0.89658 |
| 35 | 34.694 | 0.90189 | 0.90067 | 0.8993 | 0.8979 |
| 36 | 35.714 | 0.90305 | 0.90186 | 0.90052 | 0.89915 |
| 37 | 36.735 | 0.90473 | 0.90299 | 0.90168 | 0.90034 |
| 38 | 37.755 | 0.90662 | 0.90406 | 0.90278 | 0.90147 |
| 39 | 38.776 | 0.90763 | 0.90507 | 0.90382 | 0.90256 |
| 40 | 39.796 | 0.90852 | 0.90668 | 0.90482 | 0.90357 |
| 41 | 40.816 | 0.90937 | 0.90833 | 0.9058 | 0.90458 |
| 42 | 41.837 | 0.91019 | 0.90919 | 0.90671 | 0.90552 |
| 43 | 42.857 | 0.91099 | 0.91001 | 0.9076 | 0.90641 |
| 44 | 43.878 | 0.91172 | 0.91077 | 0.90842 | 0.90729 |
| 45 | 44.898 | 0.91245 | 0.91154 | 0.90925 | 0.90812 |
| 46 | 45.918 | 0.91315 | 0.91224 | 0.91041 | 0.90891 |
| 47 | 46.939 | 0.91383 | 0.91294 | 0.91181 | 0.90971 |
| 48 | 47.959 | 0.9145 | 0.91361 | 0.91264 | 0.91044 |
| 49 | 48.98 | 0.91511 | 0.91425 | 0.91328 | 0.91114 |
| 50 | 50 | 0.91572 | 0.91486 | 0.91392 | 0.91181 |
| | | | | | |
| | | | | | |





Run the function and show summaries for savings and fraction of coh saved:

```
mp_params('it_a_n') = 100;
mp_params('it_z_n') = 9;
mp_support('ls_ffcmd') = {'ap', 'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
mp_support('bl_vfi_store_all') = true; % store c(a,z), y(a,z)
ff_vfi_az_bisec_vec(mp_params, mp_support);
```

Elapsed time is 0.716025 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| xxxxxxxxx | xxxxxxxx | XXXX | xxxxxxxx | XXXXXX | XXXX | | | | | | | |
|-----------|-----------|------|----------|--------|--------|---------|---------|--------|---------|------|--------|-------|
| | | i | idx | ndim | numel | rowN | colN | sum | mean | sto | d d | coefv |
| | | - | | | | | | | | | | |
| ap | | 1 | 1 | 2 | 900 | 100 | 9 | 21835 | 24.261 | 14.0 | 095 (| 0.580 |
| savef | raccoh | 2 | 2 | 2 | 900 | 100 | 9 | 754.27 | 0.83808 | 0.1 | 259 (| 0.150 |
| xxx TABLE | :ap xxxxx | xxxx | xxxxxxxx | x | | | | | | | | |
| | c1 | | c2 | | c3
 | c4 | c5 | c6 | c | 7 | c8 | _ |
| r1 | | 0 | C |) | 0 | 0 | 0 | 0.0825 | 559 0.5 | 0504 | 1.2988 | 3 |
| r2 | 0.2606 | 67 | 0.25936 | 0.: | 26888 | 0.30308 | 0.39296 | 0.524 | 92 0.9 | 6211 | 1.7672 | 2 |
| r3 | 0.6538 | | 0.65589 | 0.0 | 67297 | 0.71974 | 0.82473 | 1.01 | | 4185 | 2.2377 | |
| r4 | 1.073 | 34 | 1.0789 | 1 | .1015 | 1.1556 | 1.2679 | 1.49 | 009 1. | 8821 | 2.709 | 5 |
| r5 | 1.515 | 51 | 1.5159 | 1 | .5427 | 1.6019 | 1.72 | 1.94 | 89 2 | .349 | 3.182 | 5 |
| r96 | 45.54 | 47 | 45.58 | 3 4 | 5.636 | 45.73 | 45.888 | 46.1 | .34 46 | .603 | 47.52 | 2 |
| r97 | 46.03 | 36 | 46.069 | 4 | 6.126 | 46.22 | 46.377 | 46.6 | 322 47 | .092 | 48.009 | 9 |
| r98 | 46.52 | 25 | 46.559 | 4 | 6.615 | 46.71 | 46.867 | 47.1 | .12 47 | .583 | 48.50 | 1 |
| r99 | 47.03 | 14 | 47.049 | 4 | 7.104 | 47.198 | 47.357 | 47.6 | 301 48 | .072 | 48.992 | 2 |
| r100 | 47.50 | 03 | 47.537 | 4 | 7.593 | 47.687 | 47.845 | 48.0 | 91 48 | .561 | 49.49 | 5 |
| xxx TABLE | :savefrac | ccoh | xxxxxxx | xxxxxx | xxxx | | | | | | | |
| | c1 | | c2 | | с3 | c4 | c5 | c6 | С | 7 | c8 | |
| | | | | | | | | | | | | |
| r1 | | 0 | C |) | 0 | 0 | 0 | 0.0562 | 268 0.2 | 4587 | 0.4130 | 01 |
| r2 | 0.2309 | 98 | 0.217 | 0.1 | 20843 | 0.21203 | 0.23925 | 0.264 | 45 0. | 3741 | 0.482 | 53 |
| r3 | 0.397 | 17 | 0.38292 | 0.3 | 37227 | 0.36965 | 0.38179 | 0.403 | 0.4 | 5915 | 0.5353 | 32 |
| r4 | 0.4960 | 05 | 0.48369 | 0.4 | 47368 | 0.46883 | 0.47347 | 0.493 | 364 0.5 | 2177 | 0.5767 | 77 |
| r5 | 0.5650 | 02 | 0.55159 | 0. | 54262 | 0.53709 | 0.53825 | 0.550 | 0.5 | 6947 | 0.6102 | 21 |
| r96 | 0.9147 | 77 | 0.91422 | 0.9 | 91361 | 0.91294 | 0.91221 | 0.91 | .09 0.9 | 0961 | 0.9083 | 18 |
| r97 | 0.9150 | 80 | 0.91453 | 0.9 | 91395 | 0.91328 | 0.91254 | 0.911 | .23 0.9 | 0998 | 0.908 | 55 |
| r98 | 0.9153 | 38 | 0.91486 | 0. | 91425 | 0.91361 | 0.91288 | 0.911 | .57 0.9 | 1035 | 0.9089 | 94 |
| r99 | 0.9156 | 69 | 0.91517 | 0. | 91456 | 0.91392 | 0.91322 | 0.91 | .19 0.9 | 1068 | 0.9093 | 34 |
| r100 | 0.9159 | 96 | 0.91544 | 0.9 | 91486 | 0.91422 | 0.91352 | 0.912 | 224 0.9 | 1102 | 0.9099 | 92 |
| | | | | | | | | | | | | |

1.4.4 Test FF_VFI_AZ_BISEC_VEC Change Interest Rate and Discount

Show only save fraction of cash on hand:

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 750;
mp_params('it_z_n') = 9;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
```

Solve the model with several different interest rates and discount factor:

% Lower Savings Incentives

1.4. FF VFI AZ BISEC VEC DYNAMIC SAVINGS PROBLEM VECTORIZED CONTINUOUS EXACT45

mp_params('fl_beta') = 0.80;
mp_params('fl_r') = 0.01;
ff_vfi_az_bisec_vec(mp_params, mp_support);

Elapsed time is 4.541023 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | | i | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-----|--------------|------|-----------------|-------------------|-------|------|------|--------|---------|---------|------|
| | | - | | | | | | | | | |
| | savefraccoh | 1 | 1 | 2 | 6750 | 750 | 9 | 3318.4 | 0.49162 | 0.27766 | 0.56 |
| vvv | TARIFICATION | ccoh | VVVVVV V | VVVVVVV VV | vvv | | | | | | |

xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx

| | c1 | c2 | сЗ | c4 | с5 | с6 | с7 | c8 |
|------|---------|---------|---------|---------|---------|---------|----------|---------|
| | | | | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023584 | 0.1329 |
| r2 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023584 | 0.1329 |
| r3 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023584 | 0.1329 |
| r4 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023584 | 0.1329 |
| r5 | 0 | 0 | 0 | 0 | 0 | 0 | 0.023584 | 0.1329 |
| r746 | 0.80439 | 0.80299 | 0.80094 | 0.79856 | 0.79588 | 0.79222 | 0.78825 | 0.78263 |
| r747 | 0.80467 | 0.80314 | 0.8011 | 0.79875 | 0.79606 | 0.7924 | 0.78846 | 0.78285 |
| r748 | 0.80491 | 0.80329 | 0.80125 | 0.7989 | 0.79621 | 0.79255 | 0.78864 | 0.78315 |
| r749 | 0.80515 | 0.80341 | 0.80137 | 0.79905 | 0.7964 | 0.79273 | 0.78883 | 0.78352 |
| r750 | 0.80534 | 0.80357 | 0.80152 | 0.7992 | 0.79655 | 0.79292 | 0.78904 | 0.78388 |

% Higher Savings Incentives

mp_params('fl_beta') = 0.95;

 $mp_params('fl_r') = 0.04;$

ff_vfi_az_bisec_vec(mp_params, mp_support);

Elapsed time is 17.994960 seconds.

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-------------|---|-----|------|-------|------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 6750 | 750 | 9 | 4493.5 | 0.66571 | 0.28784 | 0.43 |

xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx

| | c1 | c2 | c3 | c4 | с5 | с6 | c7 | c8 |
|------|---------|---------|---------|---------|----------|---------|---------|---------|
| | | | | | | | | |
| r1 | 0 | 0 | 0 | 0 | 0.032007 | 0.15008 | 0.31087 | 0.48467 |
| r2 | 0 | 0 | 0 | 0 | 0.032007 | 0.15008 | 0.31087 | 0.48467 |
| r3 | 0 | 0 | 0 | 0 | 0.032007 | 0.15008 | 0.31087 | 0.48467 |
| r4 | 0 | 0 | 0 | 0 | 0.032007 | 0.15008 | 0.31087 | 0.48467 |
| r5 | 0 | 0 | 0 | 0 | 0.032007 | 0.15008 | 0.31087 | 0.48467 |
| r746 | 0.9289 | 0.9285 | 0.92805 | 0.92734 | 0.92664 | 0.92594 | 0.92515 | 0.92545 |
| r747 | 0.92902 | 0.9286 | 0.92814 | 0.92747 | 0.92673 | 0.92606 | 0.9253 | 0.92573 |
| r748 | 0.92911 | 0.92869 | 0.92826 | 0.92756 | 0.92686 | 0.92618 | 0.92545 | 0.926 |
| r749 | 0.92921 | 0.92881 | 0.92835 | 0.92768 | 0.92698 | 0.92631 | 0.92564 | 0.92631 |
| r750 | 0.9293 | 0.9289 | 0.92844 | 0.92777 | 0.92707 | 0.92643 | 0.92591 | 0.92658 |

1.4.5 Test FF_VFI_AZ_BISEC_VEC Changing Risk Aversion

Here, again, show fraction of coh saved in summary tabular form, but also show it graphically.

```
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {'savefraccoh'};
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 750;
mp_params('it_z_n') = 9;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
```

Solve the model with different risk aversion levels, higher preferences for risk:

0.85828

0

0

0

0

0

0.85859 0.85734

0.85871 0.85749

0.85889 0.85761

0

0

0

0

0

0.85844 0.85719 0.85575 0.85413

0.85703

0

0

0

0

0

0.85941

0.85957

0.85969

0.85984

0.85999

r1 r2

r3 r4

r5

r746

r747

r748

r749

r750

```
% Lower Risk Aversion
mp_params('fl_crra') = 0.5;
ff_vfi_az_bisec_vec(mp_params, mp_support);
Elapsed time is 13.815578 seconds.
_____
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
               i
                   idx
                       ndim
                             numel
                                       rowN
                                             colN
                                                    sum
                                                             mean
                                                                       std
                                                                              coef
   savefraccoh
               1
                    1
                          2
                               6750
                                       750
                                              9
                                                    3735.7
                                                            0.55343
                                                                     0.28972
                                                                               0.5
xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx
                   c2
                            сЗ
                                      c4
                                               c5
                                                        с6
                                                                  с7
                                                                           с8
           c1
```

0

0

0

0

0

0.8559 0.85429

0.8556

0.85606

0.85621

0

0

0

0

0

0.85398

0.85447

0.85462

0

0

0

0

0

0.85178

0.85212

0.85227

0.85246

0.85194

0.074609

0.074609

0.074609

0.074609

0.074609

0.84907

0.84925

0.84943

0.84962

0.84977

0.22661

0.22661

0.22661

0.22661

0.22664

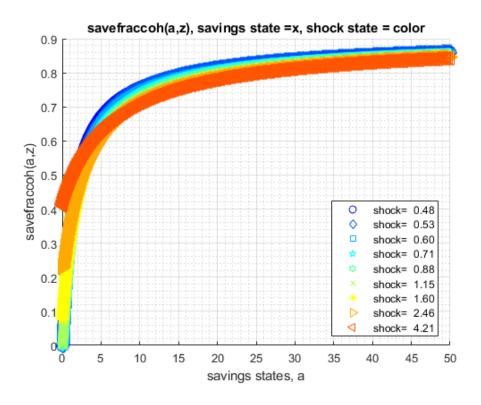
0.84583

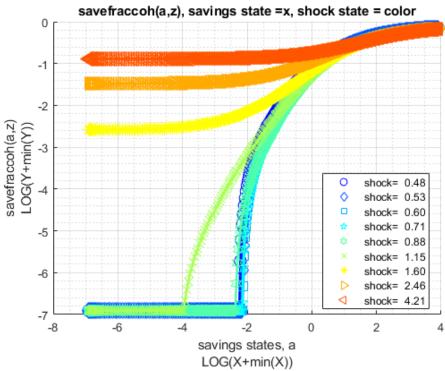
0.84602

0.8462

0.84638

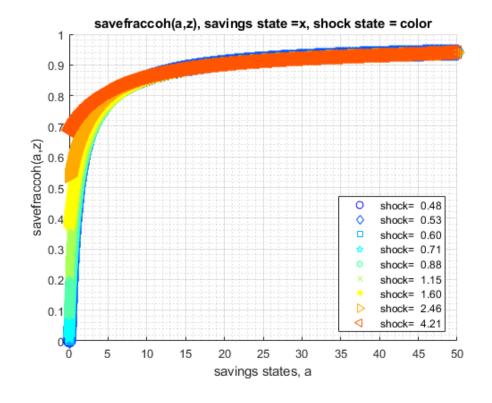
0.84657

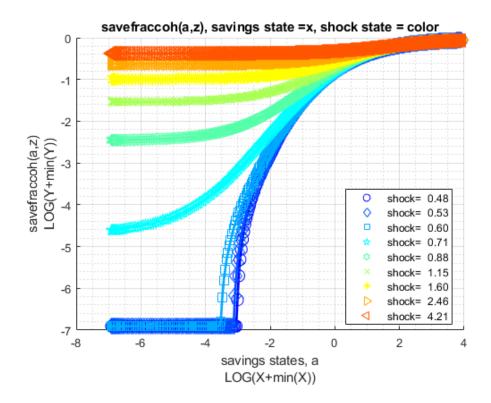




When risk aversion increases, at every state-space point, the household wants to save more.

| xxx | XXXXXXX | xxxxxxx | xxxx | xxxxxxxx | XXXXXX | XXXX | | | | | | |
|-----|---------|---------|------|----------|--------|-------|-----------|------|-------|---------|---------|---------|
| | | | i | idx | ndim | numel | rowN | colN | sum | mean | std | coefvar |
| | | | _ | | | | | | | | | |
| | savefr | accoh | 1 | 1 | 2 | 6750 | 750 | 9 | 4640 | 0.68741 | 0.2821 | 0.41039 |
| xxx | TABLE: | savefra | ccoh | xxxxxxx | xxxxxx | xxx | | | | | | |
| | | c1 | | c2 | C | :3 | c4 | | c5 | с6 | c7 | с8 |
| | | | | | | | | | | | | |
| | r1 | | 0 | 0 | | 0 | 0.0089972 | 0.0 | 85107 | 0.21343 | 0.37139 | 0.53578 |
| | r2 | | 0 | 0 | | 0 | 0.0089972 | 0.0 | 85107 | 0.21343 | 0.37139 | 0.53578 |
| | r3 | | 0 | 0 | | 0 | 0.0089972 | 0.0 | 85107 | 0.21343 | 0.37139 | 0.53578 |
| | r4 | | 0 | 0 | | 0 | 0.0089972 | 0.0 | 85107 | 0.21343 | 0.37139 | 0.53578 |
| | r5 | | 0 | 0 | | 0 | 0.0089972 | 0.0 | 85107 | 0.21343 | 0.37139 | 0.53578 |
| | r746 | 0.941 | .05 | 0.94074 | 0.9 | 94041 | 0.93992 | 0. | 93943 | 0.93897 | 0.93848 | 0.93885 |
| | r747 | 0.941 | 14 | 0.94083 | 0.9 | 94053 | 0.94004 | 0. | 93955 | 0.93909 | 0.93864 | 0.93909 |
| | r748 | 0.941 | 26 | 0.94095 | 0.9 | 94062 | 0.94016 | 0. | 93964 | 0.93922 | 0.93879 | 0.93931 |
| | r749 | 0.941 | 35 | 0.94105 | 0.9 | 94074 | 0.94025 | 0. | 93976 | 0.93934 | 0.93894 | 0.93955 |
| | r750 | 0.941 | 44 | 0.94117 | 0.9 | 94083 | 0.94038 | 0. | 93989 | 0.93946 | 0.93915 | 0.93976 |





1.4.6 Test FF_VFI_AZ_BISEC_VEC with Higher Uncertainty

mp_support = containers.Map('KeyType','char', 'ValueType','any');

Increase the standard deviation of the Shock.

```
mp_support('bl_print_params') = false;
mp_support('bl_print_iterinfo') = false;
mp_support('ls_ffcmd') = {'savefraccoh'};
mp_support('ls_ffsna') = {};
mp_support('ls_ffgrh') = {};
mp_params = containers.Map('KeyType','char', 'ValueType','any');
mp_params('it_a_n') = 750;
mp_params('it_z_n') = 9;
mp_params('fl_a_max') = 50;
mp_params('st_grid_type') = 'grid_powerspace';
Lower standard deviation of shock:
% Lower Risk Aversion
mp_params('fl_shk_std') = 0.10;
ff_vfi_az_bisec_vec(mp_params, mp_support);
Elapsed time is 14.533433 seconds.
CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
                                                                                  std
                                                                                           coefv
                       idx
                             ndim
                                     numel
                                              rowN
                                                      colN
                                                              sum
                                                                        mean
                              2
                                                             4025.4
                                                                       0.59636
    savefraccoh
                                     6750
                                              750
                                                      9
                                                                                 0.3153
                                                                                            0.52
xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx
             c1
                       c2
                                  сЗ
                                             c4
                                                       с5
                                                                   с6
                                                                              с7
                                                                                         с8
           -----
                      -----
                                -----
                                           -----
```

| r1 | 0 | 0 | 0 | 0 | 0 | 0.012568 | 0.063073 | 0.13604 |
|------|---------|---------|---------|---------|---------|----------|----------|---------|
| r2 | 0 | 0 | 0 | 0 | 0 | 0.012568 | 0.063073 | 0.13604 |
| r3 | 0 | 0 | 0 | 0 | 0 | 0.012598 | 0.063073 | 0.13604 |
| r4 | 0 | 0 | 0 | 0 | 0 | 0.012598 | 0.063073 | 0.13604 |
| r5 | 0 | 0 | 0 | 0 | 0 | 0.012598 | 0.063073 | 0.13604 |
| r746 | 0.91276 | 0.91248 | 0.91196 | 0.91163 | 0.91111 | 0.91077 | 0.91025 | 0.90977 |
| r747 | 0.91291 | 0.9126 | 0.91209 | 0.91178 | 0.91126 | 0.91093 | 0.91041 | 0.90992 |
| r748 | 0.91303 | 0.91276 | 0.91224 | 0.91193 | 0.91138 | 0.91108 | 0.91056 | 0.91004 |
| r749 | 0.91318 | 0.91288 | 0.91236 | 0.91206 | 0.91154 | 0.9112 | 0.91068 | 0.91019 |
| r750 | 0.91331 | 0.913 | 0.91251 | 0.91221 | 0.91169 | 0.91135 | 0.91083 | 0.91035 |

Higher shock standard deviation: low shock high asset save more, high shock more asset save less, high shock low asset save more:

% Higher Risk Aversion

mp_params('fl_shk_std') = 0.40;

ff_vfi_az_bisec_vec(mp_params, mp_support);

Elapsed time is 14.829381 seconds.

CONTAINER NAME: mp_ffcmd ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-------------|---|-----|------|-------|------|------|--------|---------|---------|------|
| | - | | | | | | | | | |
| savefraccoh | 1 | 1 | 2 | 6750 | 750 | 9 | 5105.2 | 0.75633 | 0.26373 | 0.3 |

xxx TABLE:savefraccoh xxxxxxxxxxxxxxxxx c1 c2 сЗ c4 c5 с6 с7 с8 0 0 0 0 0.80573 0.031641 0.2456 0.55455 r1 0 0 0.80573 r2 0 0 0.031641 0.2456 0.55455 r3 0 0 0 0 0.031641 0.2456 0.55455 0.80573 r4 0 0 0 0 0.031671 0.2456 0.55455 0.80573 r5 0 0 0 0 0.031671 0.2456 0.55455 0.80573 r746 0.93336 0.93287 0.93226 0.93149 0.9303 0.9289 0.92725 0.93293 0.93232 0.93342 0.93293 0.93159 0.9304 0.92899 0.92737 0.93317 r747 r748 0.93348 0.93299 0.93241 0.93165 0.93046 0.92905 0.93339 0.9275 0.93354 0.93305 0.93247 0.93171 0.93055 0.92914 0.93363 r749 0.92762 r750 0.9336 0.93311 0.93253 0.93177 0.93061 0.92924 0.92771 0.93384

Chapter 2

Summarize Policy and Value

2.1 FF SUMM ND ARRAY Examples

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: ff_summ_nd_array from the MEconTools Package. This function summarizes policy and value functions over states.

2.1.1 Test FF_SUMM_ND_ARRAY Defaults

Call the function with defaults.

ff_summ_nd_array();

| xxx | Summ | over (a,z), | condi | age as cols, ki | .ds/marriage as | rows xxxxxxxxx | xxxxxxxxxxxxxx |
|-----|-------|-------------|-------|-----------------|-----------------|----------------|----------------|
| | group | marry | kids | mean_age_18 | mean_age_19 | mean_age_20 | mean_age_21 |
| | | | | | | | |
| | 1 | 0 | 1 | 0.52456 | 0.51689 | 0.48412 | 0.54526 |
| | 2 | 1 | 1 | 0.49355 | 0.52906 | 0.5583 | 0.47342 |
| | 3 | 0 | 2 | 0.49085 | 0.51315 | 0.45158 | 0.43201 |
| | 4 | 1 | 2 | 0.58096 | 0.50596 | 0.47985 | 0.58791 |
| | 5 | 0 | 3 | 0.57811 | 0.6068 | 0.55221 | 0.50677 |
| | 6 | 1 | 3 | 0.53023 | 0.49258 | 0.48728 | 0.43352 |
| | 7 | 0 | 4 | 0.50339 | 0.48449 | 0.53618 | 0.45993 |
| | 8 | 1 | 4 | 0.44418 | 0.5223 | 0.55657 | 0.48583 |

2.1.2 Test FF_SUMM_ND_ARRAY with Random 2 Dimensional Matrix

Summarize over 6 dimensional array, iteratively change how many dimensions to group over.

First, generate matrix:

```
      0.6965
      0.4231
      0.3432
      0.7380

      0.2861
      0.9808
      0.7290
      0.1825

      0.2269
      0.6848
      0.4386
      0.1755

      0.5513
      0.4809
      0.0597
      0.5316

      0.7195
      0.3921
      0.3980
      0.5318
```

Second, show the entire matrix (no labels):

```
it_aggd = 0;
bl_row = 1;
```

ff_summ_nd_array(st_title, mn_polval, bl_print_table, ar_st_stats, it_aggd, bl_row);

| group | vardim2 | mean_vardim1_1 | mean_vardim1_2 | mean_vardim1_3 | ${\tt mean_vardim1_4}$ | mean |
|-------|---------|----------------|----------------|----------------|--------------------------|------|
| | | | | | | |
| 1 | 1 | 0.69647 | 0.28614 | 0.22685 | 0.55131 | 0 |
| 2 | 2 | 0.42311 | 0.98076 | 0.68483 | 0.48093 | 0 |
| 3 | 3 | 0.34318 | 0.72905 | 0.43857 | 0.059678 | 0 |
| 4 | 4 | 0.738 | 0.18249 | 0.17545 | 0.53155 | 0 |
| | | | | | | |

Third, rotate row and column, and now with labels:

```
it_aggd = 0;
bl_row = 1;
ar_permute = [2,1];
ff_summ_nd_array(st_title, mn_polval, bl_print_table, ar_st_stats, it_aggd, bl_row, ...
    cl_mp_datasetdesc, ar_permute);
```

| xxx | Random | 2D dime | nsional Array | Testing Summarizing | XXXXXXXXXXXXXX | XXXXXXXXXXX |
|-----|--------|---------|---------------|---------------------|----------------|-------------|
| | group | a | $mean_z_1$ | mean_z0_33333 | mean_z_0_33333 | $mean_z_1$ |
| | | | | | | |
| | 1 | 0 | 0.69647 | 0.42311 | 0.34318 | 0.738 |
| | 2 | 0.25 | 0.28614 | 0.98076 | 0.72905 | 0.18249 |
| | 3 | 0.5 | 0.22685 | 0.68483 | 0.43857 | 0.17545 |
| | 4 | 0.75 | 0.55131 | 0.48093 | 0.059678 | 0.53155 |
| | 5 | 1 | 0.71947 | 0.39212 | 0.39804 | 0.53183 |

Fourth, dimension one as columns, average over dim 2:

```
it_aggd = 1;
bl_row = 1;
```

group

Fifth, dimension one as rows, average over dim 2:

sum

z

std

coefvari min

max

mean

| 1 | -1 | 2.4802 | 0.49605 | 0.22895 | 2.1666 | 0.22685 | 0.71947 |
|---|----------|--------|---------|---------|--------|----------|---------|
| 2 | -0.33333 | 2.9617 | 0.59235 | 0.24524 | 2.4154 | 0.39212 | 0.98076 |
| 3 | 0.33333 | 1.9685 | 0.3937 | 0.23907 | 1.6468 | 0.059678 | 0.72905 |
| 4 | 1 | 2.1593 | 0.43186 | 0.24575 | 1.7573 | 0.17545 | 0.738 |

Sixth, dimension two as rows, average over dim 1:

| xxx | Random | 2D dime | ensional <i>A</i> | Array Testing | Summarizing | xxxxxxxx | xxxxxxxxxx | xxxxx |
|-----|--------|---------|-------------------|---------------|-------------|----------|------------|---------|
| | group | a | sum | mean | std | coefvari | min | max |
| | | | | | | | | |
| | 1 | 0 | 2.2007 | 0.55019 | 0.19636 | 2.8019 | 0.34318 | 0.738 |
| | 2 | 0.25 | 2.1784 | 0.54461 | 0.37514 | 1.4518 | 0.18249 | 0.98076 |
| | 3 | 0.5 | 1.5257 | 0.38143 | 0.23212 | 1.6432 | 0.17545 | 0.68483 |
| | 4 | 0.75 | 1.6235 | 0.40587 | 0.23269 | 1.7443 | 0.059678 | 0.55131 |
| | 5 | 1 | 2.0415 | 0.51036 | 0.15361 | 3.3226 | 0.39212 | 0.71947 |

2.1.3 Test FF_SUMM_ND_ARRAY with Random 6 Dimensional Matrix

Summarize over 6 dimensional array, iteratively change how many dimensions to group over.

First, generate matrix:

```
st_title = "Random ND dimensional Array Testing Summarizing";
rng(123)
mn_polval = rand(8,7,6,5,4,3);
bl_print_table = true;
ar_st_stats = ["mean"];
```

Second, summarize over the first four dimensions, row group others:

```
it_aggd = 4;
bl_row = 0;
ff_summ_nd_array(st_title, mn_polval, bl_print_table, ar_st_stats, it_aggd, bl_row);
```

| XXX | Random | ND dimensi | ional Array | Testing St | ummarizing | XXXXXXXXXX | xxxxxxxxxxx | XXXXX | |
|-----|--------|------------|-------------|------------|------------|------------|-------------|------------|---------|
| | group | vardim5 | vardim6 | sum | mean | std | coefvari | min | max |
| | | | | | | | | | |
| | 1 | 1 | 1 | 836.78 | 0.49808 | 0.29255 | 1.7026 | 8.1888e-05 | 0.99964 |
| | 2 | 2 | 1 | 842.15 | 0.50128 | 0.28968 | 1.7305 | 6.7838e-05 | 0.99936 |
| | 3 | 3 | 1 | 831.45 | 0.49491 | 0.28851 | 1.7154 | 0.00091373 | 0.99989 |
| | 4 | 4 | 1 | 843.9 | 0.50232 | 0.28154 | 1.7842 | 0.00012471 | 0.99731 |
| | 5 | 1 | 2 | 838.99 | 0.4994 | 0.2911 | 1.7156 | 0.00029749 | 0.99938 |
| | 6 | 2 | 2 | 830.81 | 0.49453 | 0.28634 | 1.7271 | 0.00027113 | 0.9992 |
| | 7 | 3 | 2 | 832.59 | 0.49559 | 0.28682 | 1.7279 | 0.00035994 | 0.99936 |
| | 8 | 4 | 2 | 820.42 | 0.48835 | 0.29032 | 1.6821 | 0.00096259 | 0.99896 |
| | 9 | 1 | 3 | 870.56 | 0.51819 | 0.29111 | 1.7801 | 0.0010616 | 0.99951 |
| | 10 | 2 | 3 | 854.68 | 0.50874 | 0.28458 | 1.7877 | 0.001884 | 0.99965 |
| | 11 | 3 | 3 | 838.29 | 0.49898 | 0.2891 | 1.726 | 0.0019192 | 0.99945 |
| | 12 | 4 | 3 | 842.83 | 0.50169 | 0.2877 | 1.7438 | 0.00016871 | 0.99963 |

Third, summarize over the first four dimensions, column group 5th, and row group others:

```
it_aggd = 4;
bl_row = 1;
ff_summ_nd_array(st_title, mn_polval, bl_print_table, ["sum"], it_aggd, bl_row);
```

| XXX | Random | ND dimensi | onal Array Testing | Summarizing : | xxxxxxxxxxxxxxx | XXXXXXX |
|-----|--------|------------|--------------------|---------------|-----------------|-----------------|
| | group | vardim6 | sum_vardim5_1 | sum_vardim5_2 | sum_vardim5_3 | $sum_vardim5_4$ |
| | | | | | | |
| | 1 | 1 | 836.78 | 842.15 | 831.45 | 843.9 |
| | 2 | 2 | 838.99 | 830.81 | 832.59 | 820.42 |
| | 3 | 3 | 870.56 | 854.68 | 838.29 | 842.83 |

Fourth, summarize over the first five dimensions, column group 6th, no row groups:

```
it_aggd = 5;
bl_row = 1;
ff_summ_nd_array(st_title, mn_polval, bl_print_table, ["mean", "std"], it_aggd, bl_row);
mean_vardim6_1
  group
                        mean_vardim6_2
                                     mean_vardim6_3
                                                 std_vardim6_1
                                                             std_vardim6
  ----
            -----
                        -----
                                     -----
                                                 -----
              0.49915
                          0.49447
        1
                                        0.5069
                                                    0.28805
                                                               0.28862
```

1.7349

6.7838e-05

0.99989

Fifth, summarize over all six dimensions, summary statistics over the entire dataframe:

1

10083

0.50017

0.28831

2.1.4 Test FF_SUMM_ND_ARRAY with Random 7 Dimensional Matrix with All Parameters

Given a random seven dimensional matrix, average over the 2nd, 4th and 5th dimensionals. Show as row groups the 3, 6 and 7th dimensions, and row groups the 1st dimension. Show Coefficient of Variation only.

```
st_title = "avg VALUE 2+4+5th dims. groups 3+6+7th dims, and row groups the 1st dim.";
rng(123)
mn_polval = rand(3,10,2,10,10,2,3);
ar_permute = [2,4,5,1,3,6,7];
bl_print_table = true;
ar_st_stats = ["coefvari"];
it_aggd = 3; % mean over 3 dims
bl_row = 1; % one var for row group
cl_mp_datasetdesc = {};
cl_mp_datasetdesc{1} = containers.Map({'name', 'labval'}, ...
    {'age', [18, 19, 20]});
cl_mp_datasetdesc{2} = containers.Map({'name', 'labval'}, ...
    {'savings', linspace(0,1,10)});
cl_mp_datasetdesc{3} = containers.Map({'name', 'labval'}, ...
    {'borrsave', [-1,+1]});
cl_mp_datasetdesc{4} = containers.Map({'name', 'labval'}, ...
    {'shocka', linspace(-5,5,10)});
cl_mp_datasetdesc{5} = containers.Map({'name', 'labval'}, ...
```

| group | borrsave | marry | region | cv_age_18 | cv_age_19 | cv_age_20 |
|-------|----------|-------|--------|-----------|-----------|-----------|
| | | | | | | |
| 1 | -1 | 0 | 1 | 1.7607 | 1.7534 | 1.7065 |
| 2 | 1 | 0 | 1 | 1.6566 | 1.7501 | 1.7042 |
| 3 | -1 | 1 | 1 | 1.6608 | 1.7658 | 1.7291 |
| 4 | 1 | 1 | 1 | 1.756 | 1.7479 | 1.7606 |
| 5 | -1 | 0 | 2 | 1.7314 | 1.7506 | 1.786 |
| 6 | 1 | 0 | 2 | 1.7347 | 1.728 | 1.738 |
| 7 | -1 | 1 | 2 | 1.7811 | 1.755 | 1.7568 |
| 8 | 1 | 1 | 2 | 1.7445 | 1.7398 | 1.7746 |
| 9 | -1 | 0 | 3 | 1.7025 | 1.7286 | 1.69 |
| 10 | 1 | 0 | 3 | 1.74 | 1.7549 | 1.7356 |
| 11 | -1 | 1 | 3 | 1.7147 | 1.7287 | 1.7341 |
| 12 | 1 | 1 | 3 | 1.7919 | 1.7313 | 1.7452 |

Chapter 3

Distributional Analysis

3.1 FF_SIMU_STATS Examples

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: **ff_simu_stats** from the **MEconTools Package.** This is a gate-way function that computes mean, percentiles, covariance etc between several variables.

3.1.1 Test FF_SIMU_STATS Defaults

Call the function with defaults.

ff_simu_stats();

xxx tb_outcomes: all stats xxx

| OriginalVariableN | ames | cl_mt_pol_a | cl_mt_pol_c |
|-------------------|-------|-------------|-------------|
| | | | |
| {'mean' | } | -0.11081 | 8.8423 |
| {'sd' | } | 4.1239 | 6.5845 |
| {'coefofvar' | } | -37.215 | 0.74466 |
| {'min' | } | -7 | -6.3772 |
| {'max' | } | 9 | 21.786 |
| {'pYis0' | } | 0.064259 | 0 |
| {'pYls0' | } | 0.54867 | 0.027329 |
| {'pYgr0' | } | 0.38707 | 0.97267 |
| {'pYisMINY' | } | 0.051764 | 0.015232 |
| {'pYisMAXY' | } | 0.027329 | 0.046484 |
| {'p1' | } | -7 | -6.3772 |
| {'p10' | } | -6 | 0.27238 |
| {'p25' | } | -3 | 5.2138 |
| {'p50' | } | -1 | 6.5321 |
| {'p75' | } | 3 | 13.799 |
| {'p90' | } | 5 | 16.887 |
| {'p99' | } | 9 | 21.786 |
| {'fl_cov_cl_mt_po | 1_a'} | 17.007 | -22.084 |
| {'fl_cor_cl_mt_po | 1_a'} | 1 | -0.81327 |
| {'fl_cov_cl_mt_po | 1_c'} | -22.084 | 43.356 |
| {'fl_cor_cl_mt_po | 1_c'} | -0.81327 | 1 |
| {'fracByP1' | } | 3.2699 | -0.010985 |
| {'fracByP10' | } | 5.9889 | -0.013362 |
| {'fracByP25' | } | 14.165 | 0.041007 |
| {'fracByP50' | } | 16.208 | 0.1893 |

```
{'fracByP75' } 12.702 0.59539
{'fracByP90' } 6.6611 0.8307
{'fracByP99' } 1 1
```

3.1.2 Test FF SIMU STATS Four States-Points Matrix

Over some (a,z) states that is 3 by 3, c matrix, generate all stats

```
% Set Parameters
mt_x_of_s = [1, 2, 3.0;...
            3, 1, 1.5;...
             4, 3, 2.0];
mt_y_of_s = [2, -10, 9.0;...
             5, 1.1,3.0;...
             1, 3, -1.5];
mt_z_{of_s} = [1.1, 2, 3.3; ...
             2.3, 1,1.5;...
             4, 2.5,2.0];
mp_cl_mt_xyz_of_s = containers.Map('KeyType','char', 'ValueType','any');
mp_cl_mt_xyz_of_s('cl_mt_x_of_s') = {mt_x_of_s, zeros(1)};
mp_cl_mt_xyz_of_s('cl_mt_y_of_s') = {mt_y_of_s, zeros(1)};
mp_cl_mt_xyz_of_s('cl_mt_z_of_s') = {mt_z_of_s, zeros(1)};
mp_cl_mt_xyz_of_s('ar_st_y_name') = ["cl_mt_x_of_s", "cl_mt_y_of_s", "cl_mt_z_of_s"];
% Mass
rng(123);
mt_f_of_s = rand(size(mt_x_of_s));
mt_f_of_s = mt_f_of_s/sum(mt_f_of_s, 'all');
% Call Function
mp_cl_mt_xyz_of_s_out = ff_simu_stats(mt_f_of_s, mp_cl_mt_xyz_of_s);
xxx tb_outcomes: all stats xxx
     {\tt Original Variable Names} \qquad {\tt cl\_mt\_x\_of\_s} \qquad {\tt cl\_mt\_y\_of\_s} \qquad {\tt cl\_mt\_z\_of\_s}
    -----
                                                 -----
                                                                  -----
                          }
    {'mean'
                                   2.0763
                                                    1.9323
                                                                     2.0668
                     } 2.0763
} 0.9071
} 0.43688
} 1
} 4
} 00
} 00
} 1
} 0.28039
} 0.044922
} 1
                                                                     0.9042
    {'sd'
                                                    5.2239
    {'coefofvar'
                                                    2.7034
                                                                    0.43749
    {'min'
                                                     -10
                                                                           1
                                                         9
    {'max'
                                                 0
0.20441
    {'pYis0'
                                                                            0
                                                                            0
    {'pYls0'
    {'pYgr0'
                                                   0.79559
    {'pYisMINY'
                                                   0.10917
                                                                    0.14247
                                                   0.19422
    {'pYisMAXY'
                                                                    0.044922
    {'p1'
                           }
                                       1
                                                      -10
                                                                          1
    {'p10'
                                          1
                                                        -10
                                                                            1
    {'p25'
                                          1
                                                         1.1
                                                                          1.1
    {'p50'
                          }
                                                         2
                                          2
                                                                          2
    {'p75'
                                          3
                                                          5
                                                                          2.5
    {'p90'
                                          3
                                                          9
                                                                          3.3
    {'p99'
                                         4
                                                          9
                                                                           4
                                 0.82282
                                                     1.589
                                                                    0.78646
    {'fl_cov_cl_mt_x_of_s'}
    {'fl_cor_cl_mt_x_of_s'}
                                                   0.33534
                                   1
                                                                     0.95887
                                                    27.289
    {'fl_cov_cl_mt_y_of_s'}
                                     1.589
                                                                      1.8353
    {'fl_cov_cl_mt_y_of_s'} 1.589 27.289

{'fl_cor_cl_mt_y_of_s'} 0.33534 1

{'fl_cov_cl_mt_z_of_s'} 0.78646 1.8353

{'fl_cor_cl_mt_z_of_s'} 0.95887 0.38856

{'fracByP1' } 0.13504 -0.56498

{'fracByP10' } 0.13504 -0.56498
                                                                     0.38856
                                                                    0.81758
                                                                      1
                                                                     0.068934
                                                                     0.068934
```

| {'fracByP25' | } | 0.13504 | -0.53456 | 0.14234 |
|--------------|---|---------|----------|---------|
| {'fracByP50' | } | 0.42991 | -0.39181 | 0.43856 |
| {'fracByP75' | } | 0.91346 | 0.095425 | 0.60296 |
| {'fracByP90' | } | 0.91346 | 1 | 0.91306 |
| {'fracByP99' | } | 1 | 1 | 1 |

3.1.3 Test FF_SIMU_STATS Four States-Points Matrix Single Column Inputs

Same as before, but now inputs are single column, should have identical results:

```
% Array Inputs
mp_cl_ar_xyz_of_s = containers.Map('KeyType','char', 'ValueType','any');
mp_cl_mt_xyz_of_s('cl_mt_x_of_s') = {mt_x_of_s(:), zeros(1)};
mp_cl_mt_xyz_of_s('cl_mt_y_of_s') = {mt_y_of_s(:), zeros(1)};
mp_cl_mt_xyz_of_s('cl_mt_z_of_s') = {mt_z_of_s(:), zeros(1)};
mp_cl_mt_xyz_of_s('ar_st_y_name') = ["cl_mt_x_of_s", "cl_mt_y_of_s", "cl_mt_z_of_s"];
% Call Function
mp_cl_mt_xyz_of_s_out = ff_simu_stats(mt_f_of_s(:), mp_cl_mt_xyz_of_s);
xxx tb_outcomes: all stats xxx
     OriginalVariableNames cl_mt_x_of_s
                                                cl_mt_y_of_s
                         }
    {'mean'
                                  2.0763
                                                   1.9323
                                                                    2.0668
                       } 0.9071
} 0.43688
} 1
    {'sd'
                                  0.9071
                                                   5.2239
                                                                    0.9042
    {'coefofvar'
                                                   2.7034
                                                                   0.43749
    {'min'
                                                    -10
                                                        9
    {'max'
                         }
                                         4
                                                                          4
                        {'pYis0'
                                                         0
                                                                          0
    {'pYls0'
                                                 0.20441
                                                                          0
    {'pYgr0'
                                                  0.79559
    {'pYisMINY'
                                                  0.10917
                                                                   0.14247
    {'pYisMAXY'
                                                  0.19422
                                                                   0.044922
    {'p1'
                                       1
                                                     -10
                                                       -10
    {'p10'
                                         1
                                                                          1
    {'p25'
                                                        1.1
                                         1
                                                                        1.1
                                         2
    {'p50'
                                                        2
                                                                         2
    {'p75'
                                         3
                                                         5
                                                                        2.5
    {'p90'
                                                         9
                                                                        3.3
                            3
4
0.82282
    {'p99'
                                                         9
                                                    1.589
                                                                   0.78646
    {'fl_cov_cl_mt_x_of_s'}
    {'fl_cor_cl_mt_x_of_s'}
                                                  0.33534
                                                                    0.95887
    {'fl_cov_cl_mt_y_of_s'}
                                    1.589
                                                   27.289
                                                                     1.8353
                        1.569
[s'] 0.33534
[s'] 0.78646
[s'] 0.95887
[s'] 0.13504
[s'] 0.13504
[s'] 0.1346
[s'] 0.91346
[s'] 0.91346
[s'] 0.91346
   __cor_cr_mt_y_of_s'}
{'fl_cov_cl_mt_z_of_s'}
{'fl_cor_cl_mt_z_of_s'}
{'fracByP1' }
{'fracBvP10'
                                                        1
                                                                    0.38856
                                                                    0.81758
                                                   1.8353
                                                  0.38856
                                                 -0.56498
                                                                   0.068934
                                                 -0.56498
    {'fracByP10'
                                                                   0.068934
                                                 -0.53456
    {'fracByP25'
                                                                    0.14234
    {'fracByP50'
                                                  -0.39181
                                                                    0.43856
                                                                   0.60296
    {'fracByP75'
                                                0.095425
                                                        1
    {'fracByP90'
                                   0.91346
                                                                   0.91306
    {'fracByP99'
                                         1
                                                          1
                                                                           1
```

3.1.4 Test FF_SIMU_STATS Print Many Details

The Same As before, but now control which percentiles and other details to display.

```
% Array Inputs
mp_cl_ar_xyz_of_s = containers.Map('KeyType','char', 'ValueType','any');
mp_cl_ar_xyz_of_s('cl_ar_x_of_s') = {mt_x_of_s(:), zeros(1)};
mp_cl_ar_xyz_of_s('cl_ar_z_of_s') = {mt_z_of_s(:), zeros(1)};
mp_cl_ar_xyz_of_s('ar_st_y_name') = ["cl_ar_x_of_s", "cl_ar_z_of_s"];
% controls
mp_support = containers.Map('KeyType','char', 'ValueType','any');
mp_support('bl_display_detail') = false;
mp_support('bl_display_final') = true;
mp_support('bl_display_drvm2outcomes') = false;
mp_support('ar_fl_percentiles') = [25 50 75];
mp_support('bl_display_drvstats') = true;
mp_support('bl_display_drvm2covcor') = false;
% Call Function
mp_cl_mt_xyz_of_s_out = ff_simu_stats(mt_f_of_s(:), mp_cl_ar_xyz_of_s, mp_support);
Summary Statistics for: cl_ar_x_of_s
fl_choice_mean
   2.0763
fl choice sd
   0.9071
fl_choice_coefofvar
   0.4369
fl_choice_prob_zero
fl_choice_prob_below_zero
fl_choice_prob_above_zero
fl_choice_prob_max
   0.0449
tb_disc_cumu
   cl_ar_x_of_sDiscreteVal cl_ar_x_of_sDiscreteValProbMass
                                                          CDF
                                                                 cumsumFrac
                          _____
                                                         ----
   _____
                                                                  -----
                                     0.28039
                                                        28.039 0.13504
             1
            1.5
                                     0.13561
                                                          41.6 0.23301
                                                        62.041 0.42991
              2
                                     0.20441
                                                         95.508
              3
                                     0.33466
                                                                   0.91346
                                    0.044922
                                                          100
                                                                        1
   cl_ar_x_of_sDiscreteVal cl_ar_x_of_sDiscreteValProbMass
                                                         CDF cumsumFrac
                                                                  -----
                                     0.28039
                                                         28.039
                                                                 0.13504
```

| 1.5
2
3
4 | | 0.13561
0.20441
0.33466
0.044922 | 41.6
62.041
95.508
100 | 0.23301
0.42991
0.91346
1 |
|--|-------------------------------|---|---------------------------------|------------------------------------|
| tb_prob_drv percentiles | cl_ar_x_of_ | _sDiscreteValPercentileValues | fracOfSumHe | ldBelowThisPercentile |
| 25
50
75 | | 1
2
3 | | 0.13504
0.42991
0.91346 |
| xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx | s for: cl_ar_
xxxxxxxxxxxx | z_of_s
xxxxxxxxxx | | |
| fl_choice_mean 2.0668 | | | | |
| fl_choice_sd
0.9042 | | | | |
| fl_choice_coefofv
0.4375 | ar | | | |
| fl_choice_prob_ze | ro | | | |
| fl_choice_prob_be | low_zero | | | |
| fl_choice_prob_ab | ove_zero | | | |
| fl_choice_prob_max
0.0449 | x | | | |
| tb_disc_cumu
cl_ar_z_of_sD | iscreteVal | cl_ar_z_of_sDiscreteValProb | Mass CDF | cumsumFrac |
| 4 | | 0.14047 | 14.247 | 0.000034 |
| 1 1.1 | | 0.14247
0.13792 | 28.039 | 0.068934
0.14234 |
| 1.5 | | 0.13792 | 41.6 | 0.24076 |
| 2 | | 0.20441 | 62.041 | 0.43856 |
| 2.3 | | 0.056663 | 67.708 | 0.50162 |
| 2.5 | | 0.083786 | 76.086 | 0.60296 |
| 3.3 | | 0.19422 | 95.508 | 0.91306 |
| 4 | | 0.19422 | 100 | 1 |
| cl_ar_z_of_sD | iscreteVal | cl_ar_z_of_sDiscreteValProb | Mass CDF | cumsumFrac |
| | | | | |
| 1 | | 0.14247 | 14.247 | 0.068934 |
| 1.1 | | 0.13792 | 28.039 | 0.14234 |
| 1.5 | | 0.13561 | 41.6 | 0.24076 |
| | | | | |

| 2
2.3
2.5
3.3
4 | | 0.0
0.0
0. | 20441
56663
83786
19422
44922 | 62.041
67.708
76.086
95.508
100 | 0.43856
0.50162
0.60296
0.91306 | |
|----------------------------------|--------------------------|-------------------|---|---|--|---|
| tb_prob_drv percentiles | cl_ar_z_of | _sDiscreteValPer | centileValues | fracOfSumHeld | BelowThisPercentile |) |
| 25
50
75 | | 1.1
2
2.5 | | 0 | .14234
.43856
.60296 | |
| xxx tb_outcomes: a OriginalVaria | | x
cl_ar_x_of_s | cl_ar_z_of_s | | | |
| <pre>{'mean'</pre> | <pre>} } } } } } }</pre> | 0.9071 | 2.0668
0.9042
0.43749
1
4
0
0
1
0.14247
0.044922
1.1
2
2.5
0.78646 | | | |

FF DISC RAND VAR STATS Examples

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: ff_disc_rand_var_stats from the MEconTools Package. This function summarizes statistics of matrixes stored in a container map, as well as scalar, string, function and other values stored in container maps.

Test FF_DISC_RAND_VAR_STATS Defaults

Call the function with defaults.

ff_disc_rand_var_stats();

Summary Statistics for: binom

- fl_choice_mean -1.0000
- fl_choice_sd 2.5100
- fl_choice_coefofvar
 -2.5100
- fl_choice_prob_zero
 0.1416
- fl_choice_prob_below_zero
 0.5888
- fl_choice_prob_above_zero
 0.2696
- fl_choice_prob_max
 2.0589e-16

| tb | disc | cumu |
|----|------|------|

| binomDiscreteVal | ${\tt binomDiscreteValProbMass}$ | CDF | ${\tt cumsumFrac}$ |
|------------------|----------------------------------|-----------|--------------------|
| | | | |
| -10 | 2.2539e-05 | 0.0022539 | 0.00022539 |
| -9 | 0.00028979 | 0.031233 | 0.0028335 |
| -8 | 0.0018008 | 0.21132 | 0.01724 |
| -7 | 0.0072034 | 0.93166 | 0.067664 |
| -6 | 0.020838 | 3.0155 | 0.19269 |
| -5 | 0.04644 | 7.6595 | 0.42489 |
| -4 | 0.082928 | 15.952 | 0.75661 |
| -3 | 0.12185 | 28.138 | 1.1222 |
| -2 | 0.15014 | 43.152 | 1.4224 |
| -1 | 0.15729 | 58.881 | 1.5797 |
| | | | |

| binomDiscreteVal | binomDiscreteValProbMass | CDF | cumsumFrac |
|------------------|--------------------------|-----|------------|
| | | | |
| 11 | 6.0392e-06 | 100 | 1 |
| 12 | 1.0588e-06 | 100 | 1 |
| 13 | 1.5784e-07 | 100 | 1 |
| 14 | 1.973e-08 | 100 | 1 |
| 15 | 2.0293e-09 | 100 | 1 |
| 16 | 1.6725e-10 | 100 | 1 |
| 17 | 1.0619e-11 | 100 | 1 |
| 18 | 4.8762e-13 | 100 | 1 |
| 19 | 1.4412e-14 | 100 | 1 |
| 20 | 2.0589e-16 | 100 | 1 |

tb_prob_drv

| percentiles | binomDiscreteValPercentileValues | <pre>fracOfSumHeldBelowThisPercentile</pre> |
|-------------|----------------------------------|---|
| | | |
| 0.1 | -8 | 0.01724 |
| 1 | -6 | 0.19269 |
| 5 | -5 | 0.42489 |
| 10 | -4 | 0.75661 |
| | | |

| 15 | -4 | 0.75661 |
|------|----|---------|
| 20 | -3 | 1.1222 |
| 25 | -3 | 1.1222 |
| 35 | -2 | 1.4224 |
| 50 | -1 | 1.5797 |
| 65 | 0 | 1.5797 |
| 75 | 1 | 1.4694 |
| 80 | 1 | 1.4694 |
| 85 | 2 | 1.3197 |
| 90 | 2 | 1.3197 |
| 95 | 3 | 1.1865 |
| 99 | 5 | 1.0412 |
| 99.9 | 7 | 1.0052 |

3.2.2 Test FF_DISC_RAND_VAR_STATS 0 and 1 Random Variable

The simplest discrete random variable has two values, zero or one. The probability of zero is 30 percent, and 70 percent is the probability of one.

```
% Parameters
% 1. specify the random variable
st_var_name = 'bernoulli';
ar_choice_unique_sorted = [0, 1];
ar_choice_prob = [0.3, 0.7];
% 2. percentiles of interest
ar_fl_percentiles = [0.1 5 25 50 75 95 99.9];
% 3. print resutls
bl_display_drvstats = true;
% Call Function
[ds_stats_map] = ff_disc_rand_var_stats(st_var_name, ...
   ar_choice_unique_sorted, ar_choice_prob, ...
   ar_fl_percentiles, bl_display_drvstats);
Summary Statistics for: bernoulli
_____
fl_choice_mean
   0.7000
fl_choice_sd
   0.4583
fl_choice_coefofvar
   0.6547
fl_choice_prob_zero
   0.3000
fl_choice_prob_below_zero
fl_choice_prob_above_zero
   0.7000
fl_choice_prob_max
   0.7000
```

| tb_disc_cumu | | | | |
|---------------------|----------------------------------|---------------------------------------|------------|------------|
| bernoulliDiscreteVa | l bernoulliDiscreteValProbMass | CDF | cumsumFrac | |
| | | | | |
| 0 | 0.3 | 30 | 0 | |
| 1 | 0.7 | 100 1 | | |
| bernoulliDiscreteVa | l bernoulliDiscreteValProbMass | CDF | cumsumFrac | |
| 0 | 0.3 | 30 | 0 | |
| 1 | 0.7 | 100 1 | | |
| tb_prob_drv | | | | |
| percentiles berr | oulliDiscreteValPercentileValues | ${\tt fracOfSumHeldBelowThisPercent}$ | | Percentile |
| | | | | |
| 0.1 | 0 | | 0 | |
| 5 | 0 | | 0 | |
| 25 | 0 | | 0 | |
| 50 | 1 | | 1 | |
| 75 | 1 | | 1 | |
| 95 | 1 | | 1 | |
| 99.9 | 1 | _
1 | | |

3.2.3 Test FF_DISC_RAND_VAR_STATS with Poisson

Poisson random variable, with mean equals to ten, summarize over umsymmetric percentiles. Note that the poisson random variable has no upper bound.

```
% Parameters
% 1. specify the random variable
st_var_name = 'poisson';
mu = 10;
ar_choice_unique_sorted = 0:1:50;
ar_choice_prob = poisspdf(ar_choice_unique_sorted, mu);
% 2. percentiles of interest, unsymmetric
ar_fl_percentiles = [0.1 5 10 25 50 90 95 99 99.9 99.99 99.999 99.9999];
% 3. print resutls
bl_display_drvstats = true;
% Call Function
[ds_stats_map] = ff_disc_rand_var_stats(st_var_name, ...
   ar_choice_unique_sorted, ar_choice_prob, ...
   ar_fl_percentiles, bl_display_drvstats);
Summary Statistics for: poisson
fl\_choice\_mean
   10
fl choice sd
   3.1623
fl_choice_coefofvar
   0.3162
```

- fl_choice_prob_zero 4.5400e-05
- fl_choice_prob_below_zero
- fl_choice_prob_above_zero 1.0000
- fl_choice_prob_max 1.4927e-19

| tb_ | _disc_ | cumu |
|-----|--------|------|
| | | |

| poissonDiscreteVal | ${\tt poissonDiscreteValProbMass}$ | CDF | cumsumFrac |
|----------------------------|------------------------------------|-------|-------------|
| | | | |
| 0 | 4.54e-05 | 0.004 | .54 0 |
| 1 | 0.000454 | 0.049 | 94 4.54e-05 |
| 2 | 0.00227 | 0.276 | 0.0004994 |
| 3 | 0.0075667 | 1.03 | 0.0027694 |
| 4 | 0.018917 | 2.92 | 0.010336 |
| 5 | 0.037833 | 6.70 | 0.029253 |
| 6 | 0.063055 | 13.0 | 0.067086 |
| 7 | 0.090079 | 22.0 | 0.13014 |
| 8 | 0.1126 | 33.2 | 0.22022 |
| 9 | 0.12511 | 45.7 | 93 0.33282 |
| ${\tt poissonDiscreteVal}$ | poissonDiscreteValProbMass | CDF | cumsumFrac |
| | | | |
| 41 | 1.3571e-13 | 100 | 1 |
| 42 | 3.2313e-14 | 100 | 1 |
| 43 | 7.5146e-15 | 100 | 1 |
| 44 | 1.7079e-15 | 100 | 1 |
| 45 | 3.7953e-16 | 100 | 1 |
| 46 | 8.2506e-17 | 100 | 1 |
| 47 | 1.7554e-17 | 100 | 1 |
| 48 | 3.6572e-18 | 100 | 1 |
| 49 | 7.4636e-19 | 100 | 1 |
| 50 | 1.4927e-19 | 100 | 1 |
| | | | |

| tb | prob | drv |
|----|------|-----|
| | | |

| prob_drv
percentiles | poissonDiscreteValPercentileValues | fracOfSumHeldBelowThisPercentile |
|-------------------------|------------------------------------|----------------------------------|
| 0.1 | 2 | 0.0004994 |
| 5 | 5 | 0.029253 |
| 10 | 6 | 0.067086 |
| 25 | 8 | 0.22022 |
| 50 | 10 | 0.45793 |
| 90 | 14 | 0.86446 |
| 95 | 15 | 0.91654 |
| 99 | 18 | 0.98572 |
| 99.9 | 21 | 0.99841 |
| 99.99 | 24 | 0.99988 |
| 99.999 | 26 | 0.99998 |
| 100 | 28 | 1 |

coe

0.6 0.5 0.6

 $\mbox{\ensuremath{\mbox{\%}}}$ Print out full Stored Matrix

 $\mbox{\ensuremath{\mbox{\%}}}$ Note that the outputs are single row arrays.

ff_container_map_display(ds_stats_map, 100, 100)

CONTAINER NAME: ds_stats_map ND Array (Matrix etc)

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| AAA | AAAAA | · AAAAA | AAAAAA | **** | AAAAAA. | ***** | | | | | | | | | | |
|-----|-------|---------|--------|--------|---------|---------|-------|-------|-------|--------|-----|---------|---------|-----|-------|-----|
| | | | | | i | idx | n n | dim | numel | rowl | N | colN | mean | st | :d | C |
| | | | | | - | | - | | | | - | | | | | - |
| | ar_cl | noice_ | perc_f | rachel | d 1 | 1 | : | 2 | 12 | 1 | | 12 | 0.62833 | 0. | . 435 | C |
| | ar_cl | noice_ | percen | tiles | 2 | 2 | | 2 | 12 | 1 | | 12 | 14.75 | 8.7 | 7399 | C |
| | _ | _ | entile | | 3 | 3 | : | 2 | 12 | 1 | | 12 | 64.499 | 42. | .887 | C |
| xxx | TABLE | E:ar c | hoice | perc f | rachel | d xxxxx | xxxxx | xxxxx | ххх | | | | | | | |
| | | c | | _ | c2 | | :3 | | c4 | с5 | | с6 | c7 | | с8 | ; |
| | | | | | | | | | | | | | | | | |
| | r1 | 0.00 | 04994 | 0.0 | 29253 | 0.06 | 7086 | 0.2 | 22022 | 0.4579 | 93 | 0.86446 | 0.91 | 654 | 0.98 | 572 |
| xxx | TABLE | E:ar_c | hoice_ | percen | tiles : | xxxxxx | xxxxx | xxxxx | K | | | | | | | |
| | | c1 | c2 | c3 | c4 | с5 | с6 | c7 | c8 | с9 | c10 | c11 | c12 | | | |
| | | | | | | | | | | | | | | | | |
| | r1 | 2 | 5 | 6 | 8 | 10 | 14 | 15 | 18 | 21 | 24 | 26 | 28 | | | |
| xxx | TABLE | E:ar_f | l_perc | entile | s xxxx | xxxxxx | xxxxx | xx | | | | | | | | |
| | | c1 | c2 | сЗ | c4 | с5 | с6 | с7 | c8 | с9 | | c10 | c11 | c12 | | |
| | | | | | | | | | | | | | | | | |
| | r1 | 0.1 | 5 | 10 | 25 | 50 | 90 | 95 | 99 | 99.9 | 9 | 99.99 | 99.999 | 100 | | |

| | i | idx | value |
|--------------------------|------|-----|------------|
| | | | |
| fl_choice_coefofvar | 1 | 4 | 0.31623 |
| fl_choice_max | 2 | 5 | 50 |
| fl_choice_mean | 3 | 6 | 10 |
| fl_choice_min | 4 | 7 | 0 |
| fl_choice_prob_above_zer | ro 5 | 8 | 0.99995 |
| fl_choice_prob_below_zer | ro 6 | 9 | 0 |
| fl_choice_prob_max | 7 | 10 | 1.4927e-19 |
| fl_choice_prob_min | 8 | 11 | 4.54e-05 |
| fl_choice_prob_zero | 9 | 12 | 4.54e-05 |
| fl_choice_sd | 10 | 13 | 3.1623 |
| | | | |

3.3 FF_DISC_RAND_VAR_MASS2OUTCOMES Examples

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: ff_disc_rand_var_mass2outcomes from the MEcon-Tools Package. This function generates sorted discrete random variable from state-space joint distri-

bution.

3.3.1 Test FF_DISC_RAND_VAR_MASS2OUTCOMES Defaults

Call the function with defaults.

0

0

0

0

0.2109

0.0717

0

0

0

0

0

0

```
ff_disc_rand_var_mass2outcomes();
INPUT f(a,z): mt_dist_bystates
   0.0289 0.0465 0.0228
                                0.0036
                                          0.0001
   0.0241
            0.0930
                      0.0857
                                0.0241
                                          0.0015
   0.0080
           0.0744
                      0.1285
                                0.0643
                                          0.0074
   0.0013
           0.0297
                      0.0964
                                0.0857
                                          0.0186
             0.0059
   0.0001
                      0.0361
                                0.0571
                                          0.0232
   0.0000
             0.0005
                      0.0054
                                0.0152
                                          0.0116
INPUT y(a,z): mt_choice_bystates
                   -4
   -5
         -4
               -5
   -3
         -2
               -3
                     -2
                          -3
   -1
         -1
               -1
                     0
                           0
                     3
    1
               2
                           1
          1
                           3
    4
          3
               3
                     4
    5
          6
                5
                      6
                           6
OUTPUT f(y): ar_choice_prob_byY
   0.0518
   0.0502
   0.1113
   0.1171
   0.2109
   0.0717
   0.0497
   0.0964
   0.1510
   0.0572
   0.0054
   0.0273
OUTPUT f(y,z): mt_choice_prob_byYZ
   0.0289
              0 0.0228
                                     0
                                              0
             0.0465
                                0.0036
                                          0.0001
        0
                      0
                                          0.0015
   0.0241
                 0
                      0.0857
                                     0
             0.0930
                                0.0241
        0
                      0
                                              0
   0.0080
             0.0744
                                              0
                      0.1285
                                     0
                 0
                           0
                                0.0643
                                          0.0074
   0.0013
             0.0297
                           0
                                     0
                                          0.0186
                 0
                      0.0964
        0
                                     0
                                              0
        0
             0.0059
                      0.0361
                                0.0857
                                          0.0232
                                0.0571
   0.0001
                0
                          0
                                              0
   0.0000
                  0
                       0.0054
                                              0
             0.0005
                           0
                                0.0152
                                          0.0116
        0
OUTPUT f(y,a): mt_choice_prob_byYA
   0.0518
                 0
                      0
                                     0
                                              0
                                                        0
   0.0502
                 0
                           0
                                     0
                                              0
                                                        0
        0
             0.1113
                           0
                                     0
                                              0
                                                        0
             0.1171
                                              0
                                                        0
        0
                           0
                                     0
```

| 0 | 0 | 0 | 0.0497 | 0 | 0 |
|---|---|---|--------|--------|--------|
| 0 | 0 | 0 | 0.0964 | 0 | 0 |
| 0 | 0 | 0 | 0.0857 | 0.0653 | 0 |
| 0 | 0 | 0 | 0 | 0.0572 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0.0054 |
| 0 | 0 | 0 | 0 | 0 | 0.0273 |

OUTPUT f(y) and y in table: tb_choice_drv_cur_byY binomtestOutcomes probMassFunction

| -5 | 0.051764 |
|----|-----------|
| -4 | 0.050217 |
| -3 | 0.11126 |
| -2 | 0.11706 |
| -1 | 0.21092 |
| 0 | 0.071696 |
| 1 | 0.049682 |
| 2 | 0.096388 |
| 3 | 0.15102 |
| 4 | 0.057231 |
| 5 | 0.0054256 |
| 6 | 0.027329 |

0.2990

3.0000

3.3.2 Test FF_DISC_RAND_VAR_MASS2OUTCOMES Four States-Points

Over some (a,z) states that is 2 by 2, matrix or vectorized inputs identical results.

```
% Set Parameters
st_y_name = 'consumption';
% consumption matrix: c(a,z)
mt_c_of_s = [1,2;3,1];
% stationary mass over assets adn shocks: f(a,z)
mt_f_of_s = rand(size(mt_c_of_s));
mt_f_of_s = mt_f_of_s/sum(mt_f_of_s, 'all');
% Call Function
[ar_f_of_y, ar_y_unique_sorted] = ...
    ff_disc_rand_var_mass2outcomes(st_y_name, mt_c_of_s, mt_f_of_s);
% print
disp([ar_f_of_y ar_y_unique_sorted]);
    0.4039
              1.0000
              2.0000
    0.2971
    0.2990
              3.0000
Same as before, but now inputs are single column:
% Call Function
[ar_f_of_y, ar_y_unique_sorted] = ...
    ff_disc_rand_var_mass2outcomes(st_y_name, mt_c_of_s(:), mt_f_of_s);
disp([ar_f_of_y ar_y_unique_sorted]);
    0.4039
            1.0000
    0.2971
            2.0000
```


Same inputs as before, but now, also output additional conditional statistis, f(y, a), where a is the row state variable for f(a,z). For conditional statistics, must provide matrix based inputs.

```
% Set Parameters
st_y_name = 'consumption';
% consumption matrix: c(a,z)
mt_c_of_s = [1,2,0.5;
             3,1,2.0];
% stationary mass over assets adn shocks: f(a,z)
mt_f_of_s = rand(size(mt_c_of_s));
mt_f_of_s = mt_f_of_s/sum(mt_f_of_s, 'all');
% Call Function
[ar_f_of_y, ar_y_unique_sorted, mt_f_of_y_srow, mt_f_of_y_scol] = ...
    ff_disc_rand_var_mass2outcomes(st_y_name, mt_c_of_s, mt_f_of_s);
% print
disp([ar_f_of_y ar_y_unique_sorted]);
    0.2695
              0.5000
    0.3765
              1.0000
              2.0000
    0.2649
    0.0891
              3.0000
disp(mt_f_of_y_srow);
    0.2695
                   0
              0.2550
    0.1215
    0.1217
              0.1432
         0
              0.0891
disp(mt_f_of_y_scol);
         0
                   0
                        0.2695
    0.1215
              0.2550
                             0
         0
              0.1217
                        0.1432
    0.0891
                   0
                             0
```

3.4 FF_DISC_RAND_VAR_MASS2COVCOR Examples

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: **ff_disc_rand_var_mass2covcor** from the **MEconTools Package.** This function calculates covariance and correlation based for two discrete random variables.

3.4.1 Test FF DISC RAND VAR MASS2COVCOR Defaults

Call the function with defaults.

```
ff_disc_rand_var_mass2covcor();
CONTAINER NAME: covvar_input_map ND Array (Matrix etc)
i
              idx
                   ndim
                                    colN
                                                   std
                                                          coefvari
                        numel
                               rowN
                                           mean
              ---
                   ----
                         ----
                               ----
                                    ----
                                          -----
                                                  -----
                                                          -----
```

3.

| mt_f | _of_s | 1 | 5 | 2 | | 30 6 | 5 | 0.033333 | 0.035743 | 1.0723 |
|--|---|---|--|--|---|---|--|-----------|----------|---------|
| mt_x | _of_s | 2 | 6 | 2 | | 30 6 | 5 | 0.83333 | 5.3051 | 6.3661 |
| mt_y | _of_s | 3 | 7 | 2 | | 30 6 | 5 | 8.3259 | 7.1913 | 0.86373 |
| x TABL | E:mt_f | _of_s | xxxxxx | (XXXX | xxxxxx | | | | | |
| | | :1 | | c2 | | | c4 | с5 | | |
| | | | | | | | | | | |
| r1 | 0 (| 128917 | | 0.0464 | 184 | 0.022848 | 0 0036146 | 0.000119 | | |
| | | | | | | | 0.024097 | | | |
| | 0.00 | | | | | 0.12852 | | 0.0074374 | | |
| | | | | | | 0.096388 | | 0.018593 | | |
| | | | | | | 0.036146 | | 0.023242 | | |
| | | | 0.0 | | | 0.0054218 | | 0.011621 | | |
| x TABL | E:mt x | of s | xxxxxx | (XXXX | xxxxxx | : | | | | |
| | | | сЗ | | c5 | • | | | | |
| | | | | | | | | | | |
| r1 | -7 | -6 | -7 | -6 | -6 | | | | | |
| r2 | -5 | -3 | -5 | -3 | -4 | | | | | |
| r3 | -2 | -1 | -1 | 0 | -1 | | | | | |
| | 2 | 2 | 3 | 4 | 2 | | | | | |
| r5 | 6 | 5 | 5 | 6 | 5 | | | | | |
| | | | | | | | | | | |
| r6 | 8 | 9 | 7 | 9 | 9 | | | | | |
| | | | 7 | 9 | 9 | : | | | | |
| | | _of_s | 7
xxxxxxx
c2 | 9 | 9 | | c5 | | | |
| | E:mt_y_ | _of_s | 7
xxxxxx | 9 | 9 | | c5
 | | | |
| x TABL | E:mt_y
c1 | _of_s
 | 7
xxxxxxx
c2
 | 9
xxxxx:
 | 9
xxxxxxx
c3
 | c4
 | | | | |
| x TABL | E:mt_y
c1
 | _of_s

31 | 7 xxxxxxx c2 | 9
************************************ | 9
xxxxxxx
c3

18.136 | c4

3 19.3 | 5 13.901 | | | |
| x TABL
r1
r2 | E:mt_y_c1

13.23
9.94 | _of_s

31
46 | 7 xxxxxxx c2 21.78 16.88 | 9 | 9
xxxxxxx
c3

18.136
9.6914 | c4

3 19.3
4 15.7 | 13.901
1 8.6906 | | | |
| x TABL r1 r2 r3 | E:mt_y
c1
 | _of_s

31
46
55 | 7 xxxxxxx c2 21.78 16.88 6.216 | 9
************************************ | 9
xxxxxxx
c3

18.136
9.6914
13.799 | c4

5 19.3
15.7
5.213 | | | | |
| x TABL r1 r2 r3 | E:mt_y_c1

13.23
9.94
16.28 | _of_s

31
46
55
28 | 7 xxxxxxx c2 21.78 16.88 6.216 | 9
36
37
36
25 | 9
xxxxxxx
c3

18.136
9.6914
13.799 | c4 5 19.3 - 15.7 5 5.213 0.2723 | 5 13.901
1 8.6906
8 11.641
18 13.357 | | | |
| r1
r2
r3
r4 | E:mt_y_c1 13.23 9.94 16.28 12.62 5.884 | _of_s

31
46
55
28
44 | 7 xxxxxxx c2 21.78 16.88 6.216 2.752 | 9
33
36
37
36
36
25
32 | 9 xxxxxxx c3 18.136 9.6914 13.799 6.5321 6.05 | c4 3 19.3 15.7 5.213 0.2723 0.1410 | 13.901
1 8.6906
18 11.641
18 13.357
12 0.50318 | | | |
| r1
r2
r3
r4
r5 | E:mt_y_c1 13.23 9.94 16.28 12.62 5.884 | _of_s

31
46
55
28
44 | 7 xxxxxxx c2 21.78 16.88 6.216 2.752 4.035 | 9
33
36
37
36
36
25
32 | 9 xxxxxxx c3 18.136 9.6914 13.799 6.5321 6.05 | c4 3 19.3 15.7 5.213 0.2723 0.1410 | 13.901
1 8.6906
18 11.641
18 13.357
12 0.50318 | | | |
| r1
r2
r3
r4
r5
r6 | E:mt_y_c1 13.23 9.94 16.29 12.62 5.884 3.563 | _of_s 31 46 55 28 44 17 | 7 xxxxxxx c2 21.78 16.88 6.216 2.752 4.035 -0.7209 | 9 XXXXXX 36 37 36 25 21 | 9 xxxxxxx c3 18.136 9.6914 13.799 6.5321 6.05 5.1855 | c4 | 13.901
1 8.6906
18 11.641
18 13.357
12 0.50318 | | | |
| r1 r2 r3 r4 r5 r6 | E:mt_y_c1 13.23 9.94 16.25 12.62 5.884 3.563 | _of_s 31 46 55 28 44 17 xxxxxx : covv | 7 xxxxxxx c2 21.78 16.88 6.216 2.752 4.035 -0.7209 | 9 36 37 36 35 30 31 31 31 31 31 31 31 31 31 31 31 31 31 | 9 xxxxxxx c3 18.136 9.6914 13.799 6.5321 6.05 5.1855 | c4 5 19.3 15.7 5.213 0.2723 0.1410 -6.377 | 13.901
1 8.6906
18 11.641
18 13.357
12 0.50318 | | | |
| r1 r2 r3 r4 r5 r6 | E:mt_y_c1 13.23 9.94 16.25 12.62 5.884 3.563 | _of_s 31 46 55 28 44 17 xxxxxx : covv | 7 xxxxxxx c2 21.78 16.88 6.216 2.752 4.035 -0.7209 | 9 xxxxx 36 37 36 25 32 91 xxxxx it_maj xxxxx | 9 xxxxxxx c3 18.136 9.6914 13.799 6.5321 6.05 5.1855 | c4 5 19.3 15.7 5.213 0.2723 0.1410 -6.377 | 13.901
1 8.6906
18 11.641
18 13.357
12 0.50318 | | | |
| r1 r2 r3 r4 r5 r6 | E:mt_y_c1 13.23 9.94 16.25 12.62 5.884 3.563 | _of_s 31 46 55 28 44 17 xxxxxx : covv | 7 xxxxxxx c2 21.78 16.88 6.216 2.752 4.035 -0.7209 | 9 xxxxx 36 37 36 25 32 91 xxxxx it_maj xxxxx | 9 xxxxxxx c3 18.136 9.6914 13.799 6.5321 6.05 5.1855 xxxxxxx p Scala | c4 5 19.3 15.7 5.213 0.2723 0.1410 -6.377 | 13.901
1 8.6906
18 11.641
18 13.357
12 0.50318 | | | |
| r1 r2 r3 r4 r5 r6 | E:mt_y_c1 13.23 9.94 16.29 12.62 5.884 3.56: xxxxxxx | _of_s 31 46 55 28 44 17 xxxxxx : covv | 7 xxxxxxx c2 21.78 16.88 6.216 2.752 4.035 -0.7209 xxxxxxx car_input xxxxxxx idx | 9 XXXXX 366 37 366 25 31 XXXXX XXX VX | 9 xxxxxxx c3 18.136 9.6914 13.799 6.5321 6.05 5.1855 xxxxxxx p Scala | c4 5 19.3 15.7 5.213 0.2723 0.1410 -6.377 | 13.901
1 8.6906
18 11.641
18 13.357
12 0.50318 | | | |
| r1 r2 r3 r4 r5 r6 xxxxx NTAINE xxxxxx | E:mt_y_c1 13.23 9.94 16.29 12.62 5.884 3.563 xxxxxxx R NAME | _of_s 31 46 55 28 44 17 xxxxxx i - 1 | 7 xxxxxxx c2 21.78 16.88 6.216 2.752 4.035 -0.7209 xxxxxxx xar_inpu xxxxxxx idx 1 | 9 XXXXX 36 37 36 25 21 XXXXX v: v: -0 | 9 xxxxxxx c3 18.136 9.6914 13.799 6.5321 6.05 5.1855 xxxxxxx p Scala xxxxxxx alue | c4 5 19.3 15.7 5.213 0.2723 0.1410 -6.377 | 13.901
1 8.6906
18 11.641
18 13.357
12 0.50318 | | | |
| r1 r2 r3 r4 r5 r6 xxxxxx NTAINE xxxxxx | E:mt_y_c1 13.23 9.94 16.29 12.62 5.884 3.563 xxxxxxx R NAME | _of_s 31 46 55 28 44 17 xxxxxx : covv | 7 xxxxxxx c2 21.78 16.88 6.216 2.752 4.035 -0.7209 xxxxxxx xar_inpu xxxxxxx idx 1 | 9 36 37 66 25 91 3xxxx: v: v: -0 | 9 xxxxxxx c3 18.136 9.6914 13.799 6.5321 6.05 5.1855 xxxxxxx p Scala xxxxxxx alue11081 | c4 5 19.3 15.7 5.213 0.2723 0.1410 -6.377 | 13.901
1 8.6906
18 11.641
18 13.357
12 0.50318 | | | |

CONTAINER NAME: covvar_output_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | mean | std |
|---------------------------|---|-----|------|-------|------|------|----------|--------|
| | - | | | | | | | |
| mt_cov_component_weighted | 1 | 1 | 2 | 30 | 6 | 5 | -0.73612 | 1.0404 |

0.94415

-31.321 -0.51644 5.3051 36.564

7.1913

| | mt_x_y | levi_from_mer_multiply | | 2 | 2 3 | 2 2 | 30
30 | 6 | 5
5 | | |
|-----|---|------------------------|------------|---------|-------|----------|-----------|-----|----------|--|--|
| | mt_y_d | levi_from_me | ean | 4 | 4 | 2 | 30 | 6 | 5 | | |
| xxx | TABLE: | mt_cov_com | ponent_wei | ghted x | xxxxx | xxxxxxx | xxxx | | | | |
| | | c1 | c2 | 2 | c: | 3 | c4 | | c5 | | |
| | | | | | | | | | | | |
| | r1 | -0.87434 | 4 -3. | 5432 | -1.4 | 1628 | -0.22368 | -0. | 0035451 | | |
| | r2 | -0.13003 | 3 -2. | 1607 | -0.3 | 5565 | -0.47814 | 0.0 | 00087767 | | |
| | r3 | -0.11248 | 3 0.1 | 7365 | -0.5 | 6642 · | -0.025838 | -0 | 0.018507 | | |
| | r4 | 0.01069 | | 88241 | -0.69 | 9273 | -3.0184 | | 0.17717 | | |
| | | -0.002016 | | | -0.5 | | -3.0371 | | 0.99056 | | |
| | r6 | -0.00015927 | 7 -0.04 | 1473 | -0.1 | 1098 | -2.1121 | | -1.4106 | | |
| xxx | xxx TABLE:mt_x_devi_from_mean xxxxxxxxxxxxxxxxxxx | | | | | | | | | | |
| | | c1 | c2 | C | :3 | c4 | c5 | | | | |
| | | | | | | | | | | | |
| | r1 | -6.8892 | -5.8892 | -6. | 8892 | -5.889 | 92 -5.8 | 892 | | | |
| | r2 | -4.8892 | -2.8892 | -4. | 8892 | -2.889 | 92 -3.8 | 892 | | | |
| | r3 | -1.8892 | -0.88919 | -0.8 | 8919 | 0.1108 | 31 -0.88 | 919 | | | |
| | r4 | 2.1108 | 2.1108 | 3. | 1108 | 4.110 | 08 2.1 | 108 | | | |
| | r5 | 6.1108 | 5.1108 | 5. | 1108 | 6.110 | 08 5.1 | 108 | | | |
| | r6 | 8.1108 | 9.1108 | 7. | 1108 | 9.110 | 9.1 | 108 | | | |
| xxx | TABLE: | mt_x_y_mul | tiplv xxxx | xxxxxx | xxxxx | xx | | | | | |
| | | c1 | c2 | с3 | | c4 | с5 | | | | |
| | | | | | | | | - | | | |
| | r1 | -30.237 | -76.225 | -64.0 | 23 | -61.88 | 2 -29.79 | 2 | | | |
| | r2 | -5.396 | -23.242 | -4.1 | | -19.84 | | 4 | | | |
| | r3 | -14.003 | 2.3348 | -4.40 | 73 | -0.40209 | 9 -2.488 | 4 | | | |
| | r4 | 7.9905 | -12.854 | -7.18 | 68 | -35.23 | 9.528 | 7 | | | |
| | r5 | -18.075 | -24.568 | -14.2 | 71 | -53.17 | 2 -42.6 | 2 | | | |
| | r6 | -42.83 | -87.129 | -26.0 | 03 | -138.6 | 5 -121.3 | 8 | | | |
| xxx | TABLE: | mt_y_devi_ | from mean | xxxxxxx | xxxxx | xxxxx | | | | | |
| | | c1 | c2 | c3 | | c4 | с5 | | | | |
| | | | | | | | | _ | | | |
| | r1 | 4.389 | 12.943 | 9.29 | 33 | 10.508 | 5.058 | 7 | | | |
| | r2 | 1.1037 | 8.0444 | 0.849 | | 6.8677 | -0.1517 | | | | |
| | r3 | 7.4123 | -2.6258 | 4.95 | | -3.6286 | 2.798 | | | | |
| | r4 | 3.7855 | -6.0898 | -2.31 | | -8.57 | 4.514 | | | | |
| | | -2.9579 | -4.8071 | -2.79 | | -8.7013 | -8.339 | | | | |
| | r6 | -5.2806 | -9.5633 | -3.65 | | -15.22 | -13.32 | | | | |
| | | | | | | | | | | | |

fl_cov -22.0835

$3.4.2 \quad Test \ FF_DISC_RAND_VAR_MASS2COVCOR \ Four \ States-Points$

Over some (a,z) states that is 2 by 2, c matrix, and y matrix, find correlation. Positively related.

% Set Parameters

fl_cor -0.8133

```
mt_c_of_s = [1,2;3,1];
mt_y_of_s = [2,10;5,1.1];
rng(123);
mt_f_of_s = rand(size(mt_c_of_s));
mt_f_of_s = mt_f_of_s/sum(mt_f_of_s, 'all');
bl_display_drvm2covcor = false;
% Call Function
[fl_cov_xy, fl_cor_xy] = ff_disc_rand_var_mass2covcor(...
    mt_c_of_s, mt_y_of_s, mt_f_of_s, bl_display_drvm2covcor);
display(['cov=' num2str(fl_cov_xy) ',cor=', num2str(fl_cor_xy)]);
cov=1.4446,cor=0.65723
Same as before, but now inputs are single column:
% Call Function
[fl_cov_xy, fl_cor_xy] = ff_disc_rand_var_mass2covcor(...
    mt_c_of_s(:), mt_y_of_s(:), mt_f_of_s(:), bl_display_drvm2covcor);
display(['cov=' num2str(fl_cov_xy) ',cor=', num2str(fl_cor_xy)]);
cov=1.4446,cor=0.65723
```

3.4.3 Test FF_DISC_RAND_VAR_MASS2COVCOR Two Random Vectors

Generate two random vectors, with random or even mass, correlation should be zero:

3.4.4 Test FF_DISC_RAND_VAR_MASS2COVCOR Provide Mean and SD

Same as above, but now provide means and sd for x andy directly. The results are the same as when mean and sd are calculated inside the function.

```
% Set Parameters
rng(4567);
mt_c_of_s = rand([20,1])*100;
mt_y_of_s = rand([20,1])*100;
mt_f_of_s = rand(size(mt_c_of_s));
mt_f_of_s = mt_f_of_s/sum(mt_f_of_s, 'all');
fl_c_mean = sum(mt_f_of_s.*mt_c_of_s);
fl_c_sd = sqrt(sum(mt_f_of_s.*(mt_c_of_s-fl_c_mean).^2));
fl_y_mean = sum(mt_f_of_s.*mt_y_of_s);
fl_y_sd = sqrt(sum(mt_f_of_s.*(mt_y_of_s-fl_y_mean).^2));
bl_display_drvm2covcor = false;
% Call Function
[fl_cov_xy, fl_cor_xy] = ff_disc_rand_var_mass2covcor(...
```

```
mt_c_of_s, mt_y_of_s, mt_f_of_s, ...
fl_c_mean, fl_c_sd, ...
fl_y_mean, fl_y_sd, bl_display_drvm2covcor);
display(['cov=' num2str(fl_cov_xy) ',cor=', num2str(fl_cor_xy)]);
cov=-57.6533,cor=-0.062023
```

Chapter 4

Graphs

4.1 FF_GRAPH_GRID Examples: X, Y and Color Line Plots

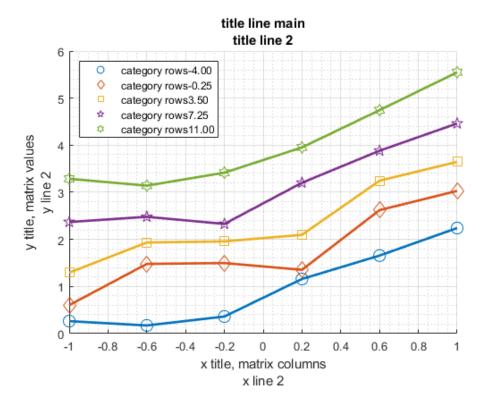
Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: **ff_graph_grid** from the **MEconTools Package.** This function can graph out value and policy functions given one state vector (x-axis), conditional on other states (line groups). Can handle a few lines (scatter + lines), or many groups (jet spectrum).

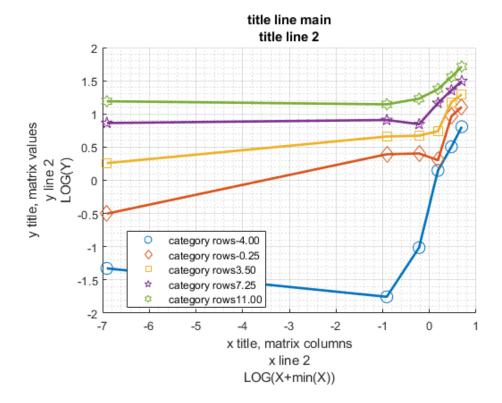
4.1.1 Test FF_GRAPH_GRID Defaults

Call the function with defaults.

ff_graph_grid();

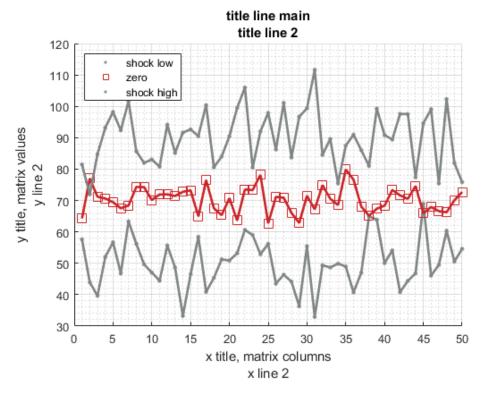


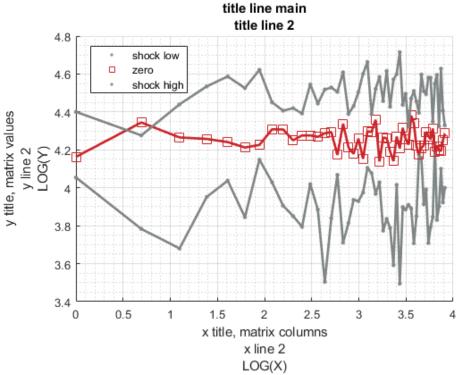
76 CHAPTER 4. GRAPHS



4.1.2 Test FF_GRAPH_GRID Random Matrix Pick Markers and Colors

Call the function with defaults.



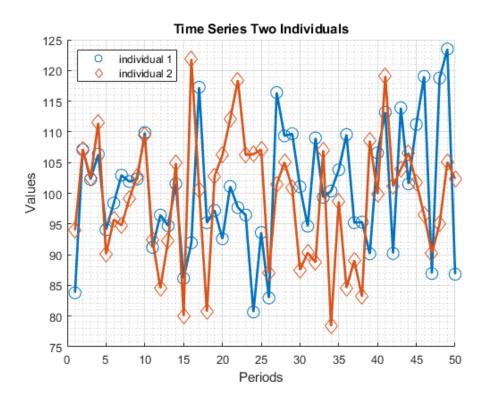


4.1.3 Test FF_GRAPH_GRID Two Random Normal Lines and Labels

There are two autoregressive time series, plot out the time two time series.

```
% Generate the two time series
rng(456);
mt_value = normrnd(100,10,[2, 50]);
ar_row_grid = ["individual 1", "individual 2"];
ar_col_grid = 1:50;
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
```

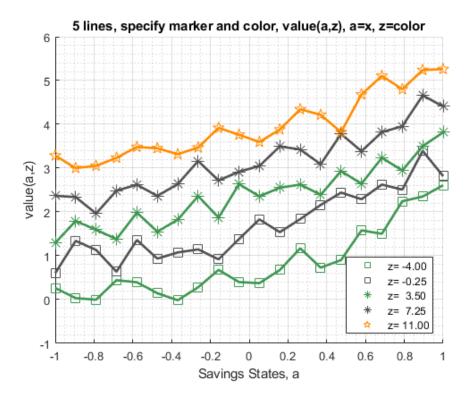
```
mp_support_graph('cl_st_graph_title') = {'Time Series Two Individuals'};
mp_support_graph('cl_st_ytitle') = {'Values'};
mp_support_graph('cl_st_xtitle') = {'Periods'};
mp_support_graph('bl_graph_logy') = false; % do not log
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```



4.1.4 Test FF GRAPH GRID 6 Lines Pick Marker and Colors

Plot many lines, with auto legend.

```
% Generate some Data
rng(456);
ar_row_grid = linspace(-4, 11, 5);
ar_col_grid = linspace(-1, 1, 20);
rng(123);
mt_value = 0.2*ar_row_grid' + exp(ar_col_grid) + rand([length(ar_row_grid), length(ar_col_grid)]);
% container map settings
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_graph_title') = {'5 lines, specify marker and color, value(a,z), a=x, z=colo
mp_support_graph('cl_st_ytitle') = {'value(a,z)'};
mp_support_graph('cl_st_xtitle') = {'Savings States, a'};
mp_support_graph('st_legend_loc') = 'southeast';
mp_support_graph('bl_graph_logy') = false; % do not log
mp_support_graph('st_rowvar_name') = 'z=';
mp_support_graph('it_legend_select') = 3; % how many shock legends to show
mp_support_graph('st_rounding') = '6.2f'; % format shock legend
mp_support_graph('cl_scatter_shapes') = {'s', 's', '*', '*', 'p'};
mp_support_graph('cl_colors') = {'green', 'black', 'green', 'black', 'orange'};
% Call function
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```

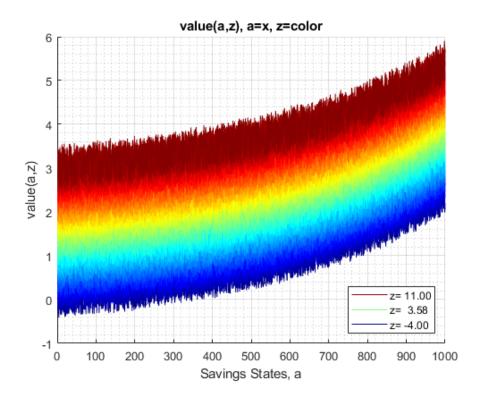


4.1.5 Test FF_GRAPH_GRID Many Lines

Plot many lines, with auto legend.

```
% Generate some Data
rng(456);
ar_row_grid = linspace(-4, 11, 100);
ar_col_grid = linspace(-1, 1, 1000);
rng(123);
mt_value = 0.2*ar_row_grid' + exp(ar_col_grid) + rand([length(ar_row_grid), length(ar_col_grid)]);
% container map settings
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_graph_title') = {'value(a,z), a=x, z=color'};
mp_support_graph('cl_st_ytitle') = {'value(a,z)'};
mp_support_graph('cl_st_xtitle') = {'Savings States, a'};
mp_support_graph('st_legend_loc') = 'southeast';
mp_support_graph('bl_graph_logy') = false; % do not log
mp_support_graph('st_rowvar_name') = 'z=';
mp_support_graph('it_legend_select') = 3; % how many shock legends to show
mp_support_graph('st_rounding') = '6.2f'; % format shock legend
mp_support_graph('cl_colors') = 'jet'; % any predefined matlab colormap
% Call function
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```

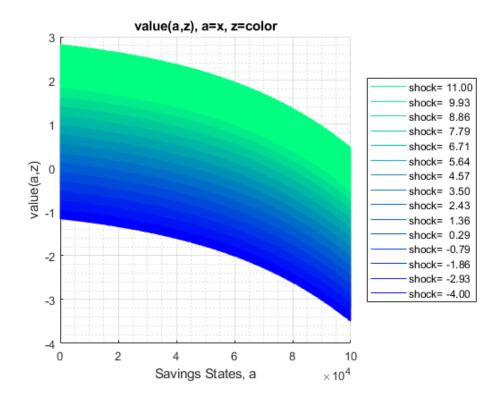
80 CHAPTER 4. GRAPHS



4.1.6 Test FF_GRAPH_GRID Many Lines Legend Exogenous

Plot many lines, exogenously set legend

```
% Generate the two time series
rng(456);
ar_row_grid = linspace(-4, 11, 15);
ar_col_grid = linspace(-1, 1, 100000);
rng(123);
mt_value = 0.2*ar_row_grid' - exp(ar_col_grid) + rand([length(ar_row_grid), length(ar_col_grid)]);
% setting shock vector name exogenously here
ar_row_grid = string(num2str(ar_row_grid', "shock=%6.2f"));
% container map settings
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_graph_title') = {'value(a,z), a=x, z=color'};
mp_support_graph('cl_st_ytitle') = {'value(a,z)'};
mp_support_graph('cl_st_xtitle') = {'Savings States, a'};
mp_support_graph('st_legend_loc') = 'eastoutside';
mp_support_graph('bl_graph_logy') = false; % do not log
mp_support_graph('it_legend_select') = 15;
mp_support_graph('cl_colors') = 'winter'; % any predefined matlab colormap
% Call function
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```



Chapter 5

Data Structures

FF_SAVEBORR_GRID Example for Generating Asset Grid

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: ff_saveborr_grid from the MEconTools Package. This function generates variously spaced savings/borrowing states/choices grid.

Test FF_SAVEBORR_GRID Defaults

Call the function with defaults.

ff_saveborr_grid();

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coefv |
|----------------|---|-----|------|-------|------|------|-------|-------|--------|-------|
| | - | | | | | | | | | |
| ar_fl_saveborr | 1 | 1 | 2 | 25 | 25 | 1 | 216.7 | 8.668 | 13.363 | 1.54 |

xxx TABLE:ar_fl_saveborr xxxxxxxxxxxxxxxx c1

| r1 | 0 |
|-----|----------|
| r2 | 0.029558 |
| r3 | 0.067855 |
| r4 | 0.11748 |
| r5 | 0.18177 |
| r6 | 0.26507 |
| r7 | 0.37301 |
| r8 | 0.51286 |
| r9 | 0.69407 |
| r10 | 0.92885 |
| r11 | 1.2331 |
| r12 | 1.6272 |
| r13 | 2.1379 |
| r14 | 2.7996 |

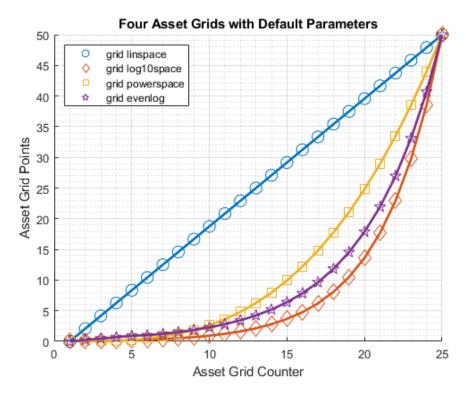
```
r15
        3.657
r16
       4.7679
      6.2072
r17
r18
      8.0722
r19
      10.489
r20
        13.62
      17.676
r21
r22
        22.932
r23
       29.743
r24
        38.567
r25
           50
```

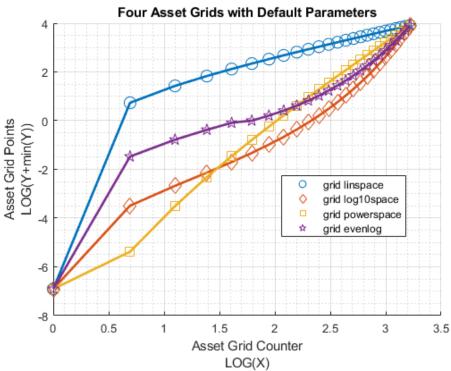
| | 1 | ıax | value |
|-------------------------------|---|-----|-------|
| | - | | |
| grid_evenlog_threshold | 1 | 2 | 1 |
| <pre>grid_log10space_x1</pre> | 2 | 3 | 0.3 |
| <pre>grid_log10space_x2</pre> | 3 | 4 | 3 |
| grid powerspace power | 4 | 5 | 3 |

5.1.2 Test FF_SAVEBORR_GRID Default Linear Grid, Log Grid, Power Grid, Threshold Grid

Call the function with defaults.

```
% Same min and max and grid points
[fl_a_min, fl_a_max, it_a_points] = deal(0,50,25);
% Four types of grid points
st_grid_type = 'grid_linspace';
[ar_fl_saveborr_linspace] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type);
st_grid_type = 'grid_log10space';
[ar_fl_saveborr_log10space] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type);
st_grid_type = 'grid_powerspace';
[ar_fl_saveborr_powerspace] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type);
st_grid_type = 'grid_evenlog';
[ar_fl_saveborr_evenlog] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type);
% draw four types of lines jointly
mt_value = [ar_fl_saveborr_linspace'; ar_fl_saveborr_log10space'; ...
    ar_fl_saveborr_powerspace'; ar_fl_saveborr_evenlog'];
ar_row_grid = ["grid linspace", "grid log10space", "grid powerspace", "grid evenlog"];
ar_col_grid = 1:it_a_points;
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_graph_title') = {'Four Asset Grids with Default Parameters'};
mp_support_graph('cl_st_ytitle') = {'Asset Grid Points'};
mp_support_graph('cl_st_xtitle') = {'Asset Grid Counter'};
mp_support_graph('bl_graph_logy') = true; % do not log
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```



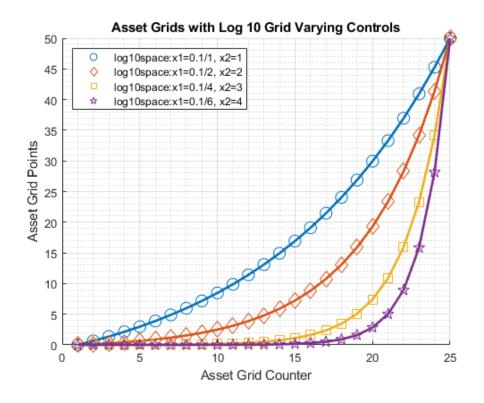


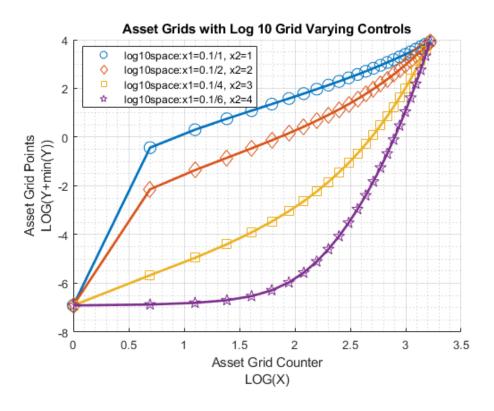
5.1.3 Test FF_SAVEBORR_GRID Log Grid Changing Parameters

Log grid, same min and max, change log X1 and X2 points

```
% Same min and max and grid points
[fl_a_min, fl_a_max, it_a_points] = deal(0,50,25);
st_grid_type = 'grid_log10space';
% Four types of grid points
mp_grid_control = containers.Map('KeyType','char', 'ValueType','any');
mp_grid_control('grid_log10space_x1') = 0.1;
```

```
mp_grid_control('grid_log10space_x2') = 1;
[ar\_fl\_log10space\_a] = ff\_saveborr\_grid(fl\_a\_min, fl\_a\_max, it\_a\_points, st\_grid\_type, mp\_grid\_contractions for the standard of the standard
mp_grid_control('grid_log10space_x1') = 0.1/2;
mp_grid_control('grid_log10space_x2') = 1*2;
[ar_fl_log10space_b] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_contr
mp_grid_control('grid_log10space_x1') = 0.1/4;
mp_grid_control('grid_log10space_x2') = 1*4;
[ar_fl_log10space_c] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_contr
mp_grid_control('grid_log10space_x1') = 0.1/6;
mp_grid_control('grid_log10space_x2') = 1*6;
[ar_fl_log10space_d] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_contr
% draw four types of lines jointly
mt_value = [ar_fl_log10space_a'; ar_fl_log10space_b'; ...
          ar_fl_log10space_c'; ar_fl_log10space_d'];
ar_row_grid = [...
          "log10space:x1=0.1/1, x2=1", ...
          "log10space:x1=0.1/2, x2=2", ...
          "log10space:x1=0.1/4, x2=3", ...
          "log10space:x1=0.1/6, x2=4"];
ar_col_grid = 1:it_a_points;
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_graph_title') = {'Asset Grids with Log 10 Grid Varying Controls'};
mp_support_graph('cl_st_ytitle') = {'Asset Grid Points'};
mp_support_graph('cl_st_xtitle') = {'Asset Grid Counter'};
mp_support_graph('bl_graph_logy') = true; % do not log
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```

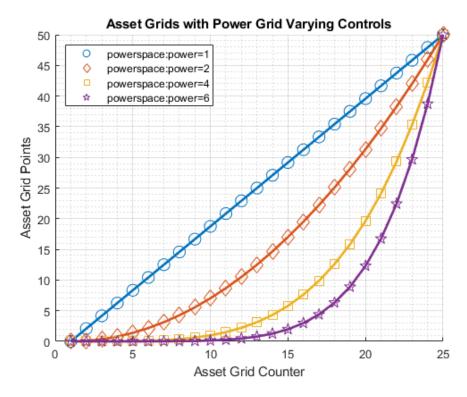


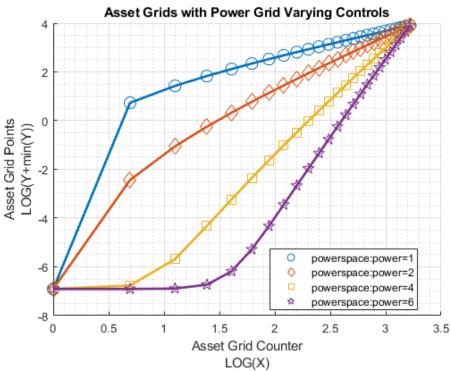


5.1.4 Test FF_SAVEBORR_GRID Power Grid Changing Parameters

Log grid, same min and max, change log X1 and X2 points

```
\% Same min and max and grid points
[fl_a_min, fl_a_max, it_a_points] = deal(0,50,25);
st_grid_type = 'grid_powerspace';
% Four types of grid points
mp_grid_control = containers.Map('KeyType','char', 'ValueType','any');
mp_grid_control('grid_powerspace_power') = 1;
[ar_fl_powerspace_a] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_contr
mp_grid_control('grid_powerspace_power') = 2;
[ar_fl_powerspace_b] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_contr
mp_grid_control('grid_powerspace_power') = 4;
[ar_fl_powerspace_c] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_contr
mp_grid_control('grid_powerspace_power') = 6;
[ar_fl_powerspace_d] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_contr
% draw four types of lines jointly
mt_value = [ar_fl_powerspace_a'; ar_fl_powerspace_b'; ...
    ar_fl_powerspace_c'; ar_fl_powerspace_d'];
ar_row_grid = [...
    "powerspace:power=1", ...
    "powerspace:power=2", ...
    "powerspace:power=4", ...
    "powerspace:power=6"];
ar_col_grid = 1:it_a_points;
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_graph_title') = {'Asset Grids with Power Grid Varying Controls'};
mp_support_graph('cl_st_ytitle') = {'Asset Grid Points'};
mp_support_graph('cl_st_xtitle') = {'Asset Grid Counter'};
mp_support_graph('bl_graph_logy') = true; % do not log
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```



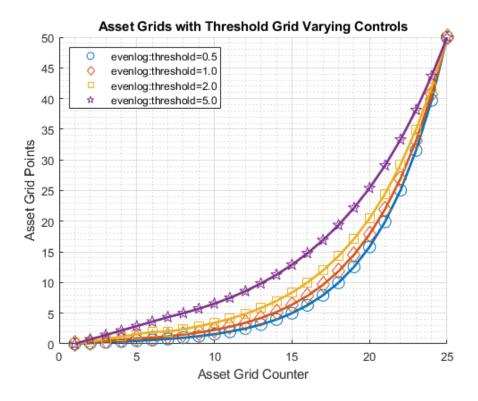


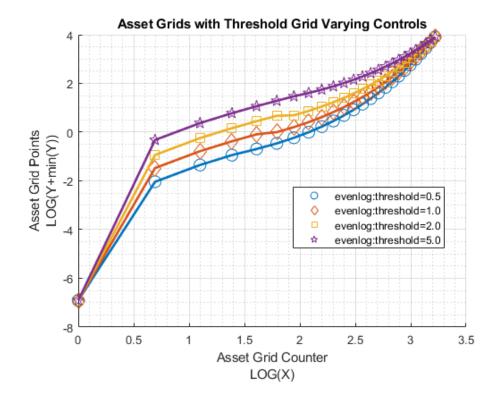
5.1.5 Test FF_SAVEBORR_GRID Threshold Grid Changing Parameters

Threshold Grid, Changing Threshold Levels. Initial segments below threshold are linspace, then logspace.

```
% Same min and max and grid points
[fl_a_min, fl_a_max, it_a_points] = deal(0,50,25);
st_grid_type = 'grid_evenlog';
% Four types of grid points
mp_grid_control = containers.Map('KeyType','char', 'ValueType','any');
mp_grid_control('grid_evenlog_threshold') = 0.50;
```

```
[ar_fl_evenlog_a] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_control)
mp_grid_control('grid_evenlog_threshold') = 1.00;
[ar_fl_evenlog_b] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_control)
mp_grid_control('grid_evenlog_threshold') = 2;
[ar_fl_evenlog_c] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_control)
mp_grid_control('grid_evenlog_threshold') = 5;
[ar_fl_evenlog_d] = ff_saveborr_grid(fl_a_min, fl_a_max, it_a_points, st_grid_type, mp_grid_control)
% draw four types of lines jointly
mt_value = [ar_fl_evenlog_a'; ar_fl_evenlog_b'; ...
    ar_fl_evenlog_c'; ar_fl_evenlog_d'];
ar_row_grid = [...
    "evenlog:threshold=0.5", ...
    "evenlog:threshold=1.0", ...
    "evenlog:threshold=2.0", ...
    "evenlog:threshold=5.0"];
ar_col_grid = 1:it_a_points;
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_graph_title') = {'Asset Grids with Threshold Grid Varying Controls'};
mp_support_graph('cl_st_ytitle') = {'Asset Grid Points'};
mp_support_graph('cl_st_xtitle') = {'Asset Grid Counter'};
mp_support_graph('bl_graph_logy') = true; % do not log
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```





Chapter 6

Common Functions

6.1 FFY TAUCHEN AR1 Shock Discretization Example

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: **ffy_tauchen** from the **MEconTools Package.**: See also the **ffy_rouwenhorst** function from the **MEconTools Package.** This function discretize a mean zero AR1 process, uses Tauchen (1986). See AR 1 Example for some details on how the AR1 process works. And See Kopecky and Suen (2010).

6.1.1 Test FFY_TAUCHEN Defaults

Call the function with defaults. Default sd bounds are plus and minus 4. This is used in the following examples, unless otherwise specified as the 5th parameter.

ffy_tauchen();

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coe |
|------------------------------|---|-----|------|-------|------|------|-----|------|---------|-----|
| | - | | | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 5 | 5 | 1 | 0 | 0 | 0.79057 | |
| <pre>mt_disc_ar1_trans</pre> | 2 | 6 | 2 | 25 | 5 | 5 | 5 | 0.2 | 0.27623 | 1. |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxx

c1 ----

r1 -1

r2 -0.5

r3 0 r4 0.5

r5 1

xxx TABLE:mt_disc_ar1_trans xxxxxxxxxxxxxxxxx

| | | c2 | c3 | c4 | с5 |
|----|----------|---------|----------|------------|------------|
| | | | | | |
| r1 | 0.22663 | 0.73331 | 0.040048 | 1.0689e-05 | 7.3923e-12 |
| r2 | 0.012224 | 0.58648 | 0.39831 | 0.0029797 | 7.605e-08 |

| r3 | 8.8417e-05 | 0.10556 | 0.7887 | 0.10556 | 8.8417e-05 |
|----|------------|------------|----------|---------|------------|
| r4 | 7.605e-08 | 0.0029797 | 0.39831 | 0.58648 | 0.012224 |
| r5 | 7.3923e-12 | 1.0689e-05 | 0.040048 | 0.73331 | 0.22663 |

| | i | idx | value |
|--------------------|---|-----|-------|
| | - | | |
| fl_ar1_persistence | 1 | 2 | 0.6 |
| fl_ar1_step | 2 | 3 | 0.5 |
| fl_shk_std | 3 | 4 | 0.2 |
| it std bound | 4 | 5 | 4 |

6.1.2 Test FFY_TAUCHEN Specify Parameters

With a grid of 10 points, the sd bounds on Tauchen and Rouwenhorst are identical. With the not extremely persistent shock process here, the Tauchen and Rouwenhorst Results are very similar.

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose, it_std_bound] = ...
    deal(0.60, 0.10, 10, true, 3);
ffy_tauchen(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose, it_std_bound);
```

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean |
|------------------------------|---|-----|------|-------|------|------|-------------|-------------|
| | - | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 10 | 10 | 1 | -7.2164e-16 | -7.2164e-17 |
| <pre>mt_disc_ar1_trans</pre> | 2 | 6 | 2 | 100 | 10 | 10 | 10 | 0.1 |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxxx

r1 -0.375

с1

r2 -0.29167 r3 -0.20833 r4 -0.125 r5 -0.041667 r6 0.041667 r7 0.125

r8 0.20833 r9 0.29167

0.375

r10

| | c1 | c2 | c3 | c4 | c5 | с6 | с7 |
|----|-----------|----------|----------|---------|----------|----------|-----------|
| | | | | | | | |
| r1 | 0.13933 | 0.26196 | 0.31887 | 0.20154 | 0.066066 | 0.011201 | 0.0009785 |
| r2 | 0.056673 | 0.16995 | 0.30658 | 0.28713 | 0.1396 | 0.035167 | 0.004575 |
| r3 | 0.01861 | 0.087039 | 0.23281 | 0.32308 | 0.23281 | 0.087039 | 0.01684 |
| r4 | 0.0048925 | 0.035167 | 0.1396 | 0.28713 | 0.30658 | 0.16995 | 0.04884 |
| r5 | 0.0010235 | 0.011201 | 0.066066 | 0.20154 | 0.31887 | 0.26196 | 0.1116 |

| r6 | 0.00016962 | 0.0028101 | 0.02466 | 0.11169 | 0.26196 | 0.31887 | 0.2015 |
|-----|------------|------------|------------|------------|----------|----------|--------|
| r7 | 2.2197e-05 | 0.00055483 | 0.0072547 | 0.048841 | 0.16995 | 0.30658 | 0.2871 |
| r8 | 2.2881e-06 | 8.6129e-05 | 0.0016806 | 0.016841 | 0.087039 | 0.23281 | 0.3230 |
| r9 | 1.8543e-07 | 1.0503e-05 | 0.00030628 | 0.0045756 | 0.035167 | 0.1396 | 0.2871 |
| r10 | 1.1798e-08 | 1.0053e-06 | 4.3874e-05 | 0.00097859 | 0.011201 | 0.066066 | 0.2015 |

| | i | idx | value |
|--------------------|---|-----|----------|
| | - | | |
| fl_ar1_persistence | 1 | 2 | 0.6 |
| fl_ar1_step | 2 | 3 | 0.083333 |
| fl_shk_std | 3 | 4 | 0.1 |
| it_std_bound | 4 | 5 | 3 |

6.1.3 Test FFY_TAUCHEN High Persistence, Low SD

[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
 deal(0.99, 0.01, 7, true);

ffy_tauchen(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean |
|------------------------------|---|-----|------|-------|------|------|-------------|-------------|
| | - | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 7 | 7 | 1 | -5.5511e-17 | -7.9302e-18 |
| ${\tt mt_disc_ar1_trans}$ | 2 | 6 | 2 | 49 | 7 | 7 | 7 | 0.14286 |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxxx

c1

| r1 | -0.28355 |
|----|-------------|
| r2 | -0.18903 |
| r3 | -0.094517 |
| r4 | -2.7756e-17 |
| r5 | 0.094517 |
| r6 | 0.18903 |
| r7 | 0.28355 |

 $\verb|xxx TABLE:mt_disc_ar1_trans | \verb|xxxxxxxxxxxxxxxxxxxxx| \\$

| | c1 | c2 | c3 | c4 | C5 | C6 | |
|----|-------------|-------------|-------------|-------------|------------|------------|----|
| | | | | | | | |
| r1 | 1 | 4.4497e-06 | 0 | 0 | 0 | 0 | |
| r2 | 4.4412e-07 | 1 | 2.8552e-06 | 0 | 0 | 0 | |
| r3 | 1.632e-46 | 7.1638e-07 | 1 | 1.8164e-06 | 0 | 0 | |
| r4 | 9.6185e-124 | 6.3021e-46 | 1.1456e-06 | 1 | 1.1456e-06 | 0 | |
| r5 | 6.3206e-239 | 8.9712e-123 | 2.4121e-45 | 1.8164e-06 | 1 | 7.1638e-07 | |
| r6 | 0 | 1.426e-237 | 8.2932e-122 | 9.1503e-45 | 2.8552e-06 | 1 | 4. |
| r7 | 0 | 0 | 3.1885e-236 | 7.5984e-121 | 3.4405e-44 | 4.4497e-06 | |
| | | | | | | | |

| | i | idx | value |
|--------------------|---|-----|----------|
| | - | | |
| fl_ar1_persistence | 1 | 2 | 0.99 |
| fl_ar1_step | 2 | 3 | 0.094517 |
| fl_shk_std | 3 | 4 | 0.01 |
| it_std_bound | 4 | 5 | 4 |

6.1.4 Test FFY_TAUCHEN Low Persistence, Low SD

[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
 deal(0.01, 0.01, 7, true);
ffy_tauchen(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | i | idx | ndim | numel | rowN | colN | sum | mean | std |
|------------------------------|---|-----|------|-------|------|------|-----|---------|----------|
| | - | | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 7 | 7 | 1 | 0 | 0 | 0.028805 |
| <pre>mt_disc_ar1_trans</pre> | 2 | 6 | 2 | 49 | 7 | 7 | 7 | 0.14286 | 0.17448 |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxxx

c1

r1 -0.040002 r2 -0.026668 r3 -0.013334 r4 0 r5 0.013334

r6 0.026668 r7 0.040002

xxx TABLE:mt_disc_ar1_trans xxxxxxxxxxxxxxxxxx

| | c1 | c2 | c3 | c4 | с5 | с6 | c7 |
|----|------------|----------|---------|---------|---------|----------|------------|
| | | | | | | | |
| r1 | 0.00049475 | 0.024497 | 0.24044 | 0.4947 | 0.21921 | 0.020299 | 0.00037109 |
| r2 | 0.00047179 | 0.023751 | 0.23685 | 0.49488 | 0.2227 | 0.020954 | 0.00038948 |
| r3 | 0.00044982 | 0.023024 | 0.23329 | 0.495 | 0.22621 | 0.021626 | 0.0004087 |
| r4 | 0.0004288 | 0.022316 | 0.22974 | 0.49504 | 0.22974 | 0.022316 | 0.0004288 |
| r5 | 0.0004087 | 0.021626 | 0.22621 | 0.495 | 0.23329 | 0.023024 | 0.00044982 |
| r6 | 0.00038948 | 0.020954 | 0.2227 | 0.49488 | 0.23685 | 0.023751 | 0.00047179 |
| r7 | 0.00037109 | 0.020299 | 0.21921 | 0.4947 | 0.24044 | 0.024497 | 0.00049475 |
| | | | | | | | |

i idx value

- ---

| fl_ar1_persistence | 1 | 2 | 0.01 |
|--------------------|---|---|----------|
| fl_ar1_step | 2 | 3 | 0.013334 |
| fl_shk_std | 3 | 4 | 0.01 |
| it std bound | 4 | 5 | 4 |

6.1.5 Test FFY_TAUCHEN High Persistence, High SD

[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
 deal(0.99, 0.99, 7, true);

ffy_tauchen(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean |
|-------------------|---|-----|------|-------|------|------|-------------|-------------|
| | - | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 7 | 7 | 1 | -3.5527e-15 | -5.0753e-16 |
| mt disc ar1 trans | 2 | 6 | 2 | 49 | 7 | 7 | 7 | 0.14286 |

c1

r1 -28.072 r2 -18.714 r3 -9.3572 r4 0 r5 9.3572 r6 18.714 r7 28.072

xxx TABLE:mt_disc_ar1_trans xxxxxxxxxxxxxxxxx

| | c1 | c2 | c3 | c4 | с5 | c6 | |
|----|-------------|-------------|-------------|-------------|------------|------------|---|
| | | | | | | | |
| r1 | 1 | 4.4497e-06 | 0 | 0 | 0 | 0 | |
| r2 | 4.4412e-07 | 1 | 2.8552e-06 | 0 | 0 | 0 | |
| r3 | 1.632e-46 | 7.1638e-07 | 1 | 1.8164e-06 | 0 | 0 | |
| r4 | 9.6185e-124 | 6.3021e-46 | 1.1456e-06 | 1 | 1.1456e-06 | 0 | |
| r5 | 6.3206e-239 | 8.9712e-123 | 2.4121e-45 | 1.8164e-06 | 1 | 7.1638e-07 | |
| r6 | 0 | 1.426e-237 | 8.2932e-122 | 9.1503e-45 | 2.8552e-06 | 1 | 4 |
| r7 | 0 | 0 | 3.1885e-236 | 7.5984e-121 | 3.4405e-44 | 4.4497e-06 | |

| | 1 | idx | value |
|--------------------|---|-----|--------|
| | - | | |
| fl_ar1_persistence | 1 | 2 | 0.99 |
| fl_ar1_step | 2 | 3 | 9.3572 |
| fl_shk_std | 3 | 4 | 0.99 |
| it std bound | 4 | 5 | 4 |

6.1.6 Test FFY_TAUCHEN Low Persistence, Low SD

[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
 deal(0.01, 0.01, 7, true);
ffy_tauchen(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std |
|------------------------------|---|-----|------|-------|------|------|-----|---------|----------|
| | - | | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 7 | 7 | 1 | 0 | 0 | 0.028805 |
| ${\tt mt_disc_ar1_trans}$ | 2 | 6 | 2 | 49 | 7 | 7 | 7 | 0.14286 | 0.17448 |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxxx

c1

r1 -0.040002

r2 -0.026668

r3 -0.013334

r4 0 r5 0.013334

r6 0.026668

r7 0.040002

xxx TABLE:mt_disc_ar1_trans xxxxxxxxxxxxxxxxx

| | c1 | c2 | сЗ | c4 | c5 | с6 | c7 |
|----|------------|----------|---------|---------|---------|----------|------------|
| | | | | | | | |
| r1 | 0.00049475 | 0.024497 | 0.24044 | 0.4947 | 0.21921 | 0.020299 | 0.00037109 |
| r2 | 0.00047179 | 0.023751 | 0.23685 | 0.49488 | 0.2227 | 0.020954 | 0.00038948 |
| r3 | 0.00044982 | 0.023024 | 0.23329 | 0.495 | 0.22621 | 0.021626 | 0.0004087 |
| r4 | 0.0004288 | 0.022316 | 0.22974 | 0.49504 | 0.22974 | 0.022316 | 0.0004288 |
| r5 | 0.0004087 | 0.021626 | 0.22621 | 0.495 | 0.23329 | 0.023024 | 0.00044982 |
| r6 | 0.00038948 | 0.020954 | 0.2227 | 0.49488 | 0.23685 | 0.023751 | 0.00047179 |
| r7 | 0.00037109 | 0.020299 | 0.21921 | 0.4947 | 0.24044 | 0.024497 | 0.00049475 |
| | | | | | | | |

| | 1 | ıdx | value |
|--------------------|---|-----|----------|
| | - | | |
| fl_ar1_persistence | 1 | 2 | 0.01 |
| fl_ar1_step | 2 | 3 | 0.013334 |
| fl_shk_std | 3 | 4 | 0.01 |
| it_std_bound | 4 | 5 | 4 |

6.2 FFY_ROUWENHORST AR1 Shock Discretization Example

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: ffy_rouwenhorst from the MEconTools Package. See also ffy_tauchen function from the MEconTools Package. This function discretize a mean zero AR1 process, uses Rouwenhorst (1995). See AR 1 Example for some details on how the AR1 process works. And See Kopecky and Suen (2010).

6.2.1 Test FFY_ROUWENHORST Defaults

Call the function with defaults.

ffy_rouwenhorst();

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coef |
|-------------------|---|-----|------|-------|------|------|-----|------|---------|------|
| | - | | | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 5 | 5 | 1 | 0 | 0 | 0.39528 | |
| mt disc ar1 trans | 2 | 11 | 2 | 25 | 5 | 5 | 5 | 0.2 | 0.18246 | 0.91 |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxxx

c1

r1 -0.5

r2 -0.25 r3 0

r4 0.25

r5 0.5

xxx TABLE:mt_disc_ar1_trans xxxxxxxxxxxxxxxxx

| | c1 | -
c2 | с3 | c4 | с5 |
|----|--------|---------|--------|--------|--------|
| | | | | | |
| r1 | 0.4096 | 0.4096 | 0.1536 | 0.0256 | 0.0016 |
| r2 | 0.1024 | 0.4864 | 0.3264 | 0.0784 | 0.0064 |
| r3 | 0.0256 | 0.2176 | 0.5136 | 0.2176 | 0.0256 |
| r4 | 0.0064 | 0.0784 | 0.3264 | 0.4864 | 0.1024 |
| r5 | 0.0016 | 0.0256 | 0.1536 | 0.4096 | 0.4096 |
| | | | | | |

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | i | idx | value |
|--------------------|---|-----|-------|
| | - | | |
| fl_ar1_beg | 1 | 2 | -0.5 |
| fl_ar1_end | 2 | 3 | 0.5 |
| fl_ar1_persistence | 3 | 4 | 0.6 |
| fl_ar1_step | 4 | 5 | 0.25 |
| fl_p0 | 5 | 6 | 0.8 |
| fl_q0 | 6 | 7 | 0.8 |
| fl_shk_std | 7 | 8 | 0.2 |
| fl_sig_ar1 | 8 | 9 | 0.25 |
| it_std_bound | 9 | 10 | 0 |
| | | | |

6.2.2 Test FFY_ROUWENHORST Specify Parameters

With a grid of 10 points, the Rwouenhorst bounds on standard deviations are equall to Tauchen bounds of 3. With the not extremely persistent shock process here, the Tauchen and Rouwenhorst Results are very similar.

```
[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
    deal(0.60, 0.10, 10, true);
ffy_rouwenhorst(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);
```

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | | |
|-------------------|---|-----|------|-------|------|------|------------|------------|----|--|
| | - | | | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 10 | 10 | 1 | 5.5511e-17 | 5.5511e-18 | 0 | |
| mt disc ar1 trans | 2 | 11 | 2 | 100 | 10 | 10 | 10 | 0.1 | 0. | |

r1 -0.375 r2 -0.29167 r3 -0.20833 r4 -0.125 r5 -0.041667 r6 0.041667

с1

r7 0.125 r8 0.20833 r9 0.29167

0.375

r10

| | c1 | c2 | с3 | c4 | с5 | с6 | с7 |
|-----|------------|------------|------------|-----------|----------|----------|-----------|
| | | | | | | | |
| r1 | 0.13422 | 0.30199 | 0.30199 | 0.17616 | 0.06606 | 0.016515 | 0.0027525 |
| r2 | 0.033554 | 0.20133 | 0.32716 | 0.26424 | 0.12662 | 0.038535 | 0.0075694 |
| r3 | 0.0083886 | 0.081789 | 0.26267 | 0.32755 | 0.21401 | 0.082747 | 0.019741 |
| r4 | 0.0020972 | 0.028312 | 0.14038 | 0.30946 | 0.30369 | 0.15877 | 0.047989 |
| r5 | 0.00052429 | 0.009044 | 0.061145 | 0.20246 | 0.33477 | 0.25969 | 0.10585 |
| r6 | 0.00013107 | 0.0027525 | 0.023642 | 0.10585 | 0.25969 | 0.33477 | 0.20246 |
| r7 | 3.2768e-05 | 0.00081101 | 0.0084603 | 0.047989 | 0.15877 | 0.30369 | 0.30946 |
| r8 | 8.192e-06 | 0.00023347 | 0.0028677 | 0.019741 | 0.082747 | 0.21401 | 0.32755 |
| r9 | 2.048e-06 | 6.6048e-05 | 0.00093389 | 0.0075694 | 0.038535 | 0.12662 | 0.26424 |
| r10 | 5.12e-07 | 1.8432e-05 | 0.00029491 | 0.0027525 | 0.016515 | 0.06606 | 0.17616 |

| | i | idx | value |
|------------|---|-----|--------|
| | - | | |
| fl_ar1_beg | 1 | 2 | -0.375 |
| fl_ar1_end | 2 | 3 | 0.375 |

| fl_ar1_persistence | 3 | 4 | 0.6 |
|--------------------|---|----|----------|
| fl_ar1_step | 4 | 5 | 0.083333 |
| fl_p0 | 5 | 6 | 0.8 |
| fl_q0 | 6 | 7 | 0.8 |
| fl_shk_std | 7 | 8 | 0.1 |
| fl_sig_ar1 | 8 | 9 | 0.125 |
| it_std_bound | 9 | 10 | 0 |

6.2.3 Test FFY_ROUWENHORST High Persistence, Low SD

[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
deal(0.99, 0.01, 7, true);

ffy_rouwenhorst(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | |
|-------------------|---|-----|------|-------|------|------|-----|---------|---------|--|
| | - | | | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 7 | 7 | 1 | 0 | 0 | 0.12503 | |
| mt_disc_ar1_trans | 2 | 11 | 2 | 49 | 7 | 7 | 7 | 0.14286 | 0.34148 | |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxxx

c1

r1 -0.17364 r2 -0.11576 r3 -0.05788 r4 0 r5 0.05788 r6 0.11576 r7 0.17364

xxx TABLE:mt_disc_ar1_trans xxxxxxxxxxxxxxxxx

| | c1 | c2 | c3 | c4 | c5 | с6 | c7 |
|----|------------|------------|------------|------------|------------|------------|--------|
| | | | | | | | |
| r1 | 0.97037 | 0.029257 | 0.00036756 | 2.4627e-06 | 9.2815e-09 | 1.8656e-11 | 1.5625 |
| r2 | 0.0048762 | 0.9705 | 0.024382 | 0.00024504 | 1.2314e-06 | 3.0938e-09 | 3.1094 |
| r3 | 2.4504e-05 | 0.009753 | 0.97057 | 0.019506 | 0.00014703 | 4.9254e-07 | 6.1877 |
| r4 | 1.2313e-07 | 7.3513e-05 | 0.01463 | 0.97059 | 0.01463 | 7.3513e-05 | 1.2313 |
| r5 | 6.1877e-10 | 4.9254e-07 | 0.00014703 | 0.019506 | 0.97057 | 0.009753 | 2.4504 |
| r6 | 3.1094e-12 | 3.0938e-09 | 1.2314e-06 | 0.00024504 | 0.024382 | 0.9705 | 0.004 |
| r7 | 1.5625e-14 | 1.8656e-11 | 9.2815e-09 | 2.4627e-06 | 0.00036756 | 0.029257 | 0.9 |

| 1 | ıdx | value |
|---|-----|------------|
| - | | |
| 1 | 2 | -0.17364 |
| 2 | 3 | 0.17364 |
| 3 | 4 | 0.99 |
| | 2 | 1 2
2 3 |

| fl_ar1_step | 4 | 5 | 0.05788 |
|--------------|---|----|----------|
| fl_p0 | 5 | 6 | 0.995 |
| fl_q0 | 6 | 7 | 0.995 |
| fl_shk_std | 7 | 8 | 0.01 |
| fl_sig_ar1 | 8 | 9 | 0.070888 |
| it std bound | 9 | 10 | 0 |

6.2.4 Test FFY_ROUWENHORST Low Persistence, Low SD

[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
 deal(0.01, 0.01, 7, true);

ffy_rouwenhorst(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std |
|------------------------------|---|-----|------|-------|------|------|-----|---------|----------|
| | - | | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 7 | 7 | 1 | 0 | 0 | 0.017639 |
| <pre>mt_disc_ar1_trans</pre> | 2 | 11 | 2 | 49 | 7 | 7 | 7 | 0.14286 | 0.10985 |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxxx

c1

r1 -0.024496 r2 -0.016331 r3 -0.0081654 r4 0 r5 0.0081654 r6 0.016331 r7 0.024496

xxx TABLE:mt_disc_ar1_trans xxxxxxxxxxxxxxxxx

| | c1 | -
c2 | c3 | c4 | с5 | с6 | c7 |
|----|----------|----------|---------|---------|---------|----------|----------|
| | | | | | | | |
| r1 | 0.016586 | 0.097547 | 0.23904 | 0.31241 | 0.22966 | 0.090047 | 0.014711 |
| r2 | 0.016258 | 0.096266 | 0.23749 | 0.31247 | 0.23124 | 0.091266 | 0.015008 |
| r3 | 0.015936 | 0.094997 | 0.23594 | 0.31251 | 0.23281 | 0.092497 | 0.015311 |
| r4 | 0.01562 | 0.093741 | 0.23438 | 0.31252 | 0.23438 | 0.093741 | 0.01562 |
| r5 | 0.015311 | 0.092497 | 0.23281 | 0.31251 | 0.23594 | 0.094997 | 0.015936 |
| r6 | 0.015008 | 0.091266 | 0.23124 | 0.31247 | 0.23749 | 0.096266 | 0.016258 |
| r7 | 0.014711 | 0.090047 | 0.22966 | 0.31241 | 0.23904 | 0.097547 | 0.016586 |

| | i | idx | value |
|--------------------|---|-----|-----------|
| | - | | |
| fl_ar1_beg | 1 | 2 | -0.024496 |
| fl_ar1_end | 2 | 3 | 0.024496 |
| fl_ar1_persistence | 3 | 4 | 0.01 |
| fl_ar1_step | 4 | 5 | 0.0081654 |
| | | | |

| fl_p0 | 5 | 6 | 0.505 |
|--------------|---|----|----------|
| fl_q0 | 6 | 7 | 0.505 |
| fl_shk_std | 7 | 8 | 0.01 |
| fl_sig_ar1 | 8 | 9 | 0.010001 |
| it std bound | 9 | 10 | 0 |

6.2.5 Test FFY_ROUWENHORST High Persistence, High SD

[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
 deal(0.99, 0.99, 7, true);

ffy_rouwenhorst(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | |
|------------------------------|---|-----|------|-------|------|------|------------|------------|----|
| | - | | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 7 | 7 | 1 | 3.5527e-15 | 5.0753e-16 | 1 |
| <pre>mt_disc_ar1_trans</pre> | 2 | 11 | 2 | 49 | 7 | 7 | 7 | 0.14286 | 0. |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxxx

c1

r1 -17.19 r2 -11.46 r3 -5.7301 r4 0 r5 5.7301 r6 11.46 r7 17.19

| | c1 | c2 | c3 | c4 | c5 | с6 | c7 |
|----|------------|------------|------------|------------|------------|------------|--------|
| | | | | | | | |
| r1 | 0.97037 | 0.029257 | 0.00036756 | 2.4627e-06 | 9.2815e-09 | 1.8656e-11 | 1.5625 |
| r2 | 0.0048762 | 0.9705 | 0.024382 | 0.00024504 | 1.2314e-06 | 3.0938e-09 | 3.1094 |
| r3 | 2.4504e-05 | 0.009753 | 0.97057 | 0.019506 | 0.00014703 | 4.9254e-07 | 6.1877 |
| r4 | 1.2313e-07 | 7.3513e-05 | 0.01463 | 0.97059 | 0.01463 | 7.3513e-05 | 1.2313 |
| r5 | 6.1877e-10 | 4.9254e-07 | 0.00014703 | 0.019506 | 0.97057 | 0.009753 | 2.4504 |
| r6 | 3.1094e-12 | 3.0938e-09 | 1.2314e-06 | 0.00024504 | 0.024382 | 0.9705 | 0.004 |
| r7 | 1.5625e-14 | 1.8656e-11 | 9.2815e-09 | 2.4627e-06 | 0.00036756 | 0.029257 | 0.9 |

| | i | idx | value |
|--------------------|---|-----|--------|
| | - | | |
| fl_ar1_beg | 1 | 2 | -17.19 |
| fl_ar1_end | 2 | 3 | 17.19 |
| fl_ar1_persistence | 3 | 4 | 0.99 |
| fl_ar1_step | 4 | 5 | 5.7301 |
| fl_p0 | 5 | 6 | 0.995 |
| | | | |

| fl_q0 | 6 | 7 | 0.995 |
|--------------|---|----|--------|
| fl_shk_std | 7 | 8 | 0.99 |
| fl_sig_ar1 | 8 | 9 | 7.0179 |
| it std bound | 9 | 10 | 0 |

6.2.6 Test FFY_ROUWENHORST Low Persistence, Low SD

[fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose] = ...
 deal(0.01, 0.01, 7, true);

ffy_rouwenhorst(fl_ar1_persistence, fl_shk_std, it_disc_points, bl_verbose);

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std |
|------------------------------|---|-----|------|-------|------|------|-----|---------|----------|
| | - | | | | | | | | |
| ar_disc_ar1 | 1 | 1 | 2 | 7 | 7 | 1 | 0 | 0 | 0.017639 |
| <pre>mt_disc_ar1_trans</pre> | 2 | 11 | 2 | 49 | 7 | 7 | 7 | 0.14286 | 0.10985 |

xxx TABLE:ar_disc_ar1 xxxxxxxxxxxxxxxxxx

c1

r1 -0.024496 r2 -0.016331 r3 -0.0081654 r4 0 r5 0.0081654 r6 0.016331 r7 0.024496

xxx TABLE:mt_disc_ar1_trans xxxxxxxxxxxxxxxxx

| | c1 | c2 | c3 | c4 | с5 | с6 | c7 |
|----|----------|----------|---------|---------|---------|----------|----------|
| | | | | | | | |
| r1 | 0.016586 | 0.097547 | 0.23904 | 0.31241 | 0.22966 | 0.090047 | 0.014711 |
| r2 | 0.016258 | 0.096266 | 0.23749 | 0.31247 | 0.23124 | 0.091266 | 0.015008 |
| r3 | 0.015936 | 0.094997 | 0.23594 | 0.31251 | 0.23281 | 0.092497 | 0.015311 |
| r4 | 0.01562 | 0.093741 | 0.23438 | 0.31252 | 0.23438 | 0.093741 | 0.01562 |
| r5 | 0.015311 | 0.092497 | 0.23281 | 0.31251 | 0.23594 | 0.094997 | 0.015936 |
| r6 | 0.015008 | 0.091266 | 0.23124 | 0.31247 | 0.23749 | 0.096266 | 0.016258 |
| r7 | 0.014711 | 0.090047 | 0.22966 | 0.31241 | 0.23904 | 0.097547 | 0.016586 |

| | i | idx | value |
|--------------------|---|-----|-----------|
| | - | | |
| fl_ar1_beg | 1 | 2 | -0.024496 |
| fl_ar1_end | 2 | 3 | 0.024496 |
| fl_ar1_persistence | 3 | 4 | 0.01 |
| fl_ar1_step | 4 | 5 | 0.0081654 |
| fl_p0 | 5 | 6 | 0.505 |
| fl_q0 | 6 | 7 | 0.505 |
| | | | |

| fl_shk_std | 7 | 8 | 0.01 |
|--------------|---|----|----------|
| fl_sig_ar1 | 8 | 9 | 0.010001 |
| it std bound | 9 | 10 | 0 |

Chapter 7

Support Tools

7.1 FF_CONTAINER_MAP_DISPLAY Examples

Go back to fan's MEconTools Toolbox (bookdown), Matlab Code Examples Repository (bookdown), or Math for Econ with Matlab Repository (bookdown).

This is the example vignette for function: **ff_container_map_display** from the **MEconTools Package.** This function summarizes statistics of matrixes stored in a container map, as well as scalar, string, function and other values stored in container maps.

7.1.1 Test FF_CONTAINER_MAP_DISPLAY Defaults

Call the function with defaults.

ff_container_map_display();

| xxxxxxxxx | xxxxxxxx | xxxxxxxxxxxxxxxxxx |
|-----------|----------|--------------------|
| ND Array | (Matrix | etc) |

| XXXXXXXXXXXXXXXXXXX | XXXXXX | XXXXXXX | XXXXXXX | | | | | | |
|---------------------|--------|---------|---------|-------|------|------|--------|---------|---------|
| | i | idx | ndim | numel | rowN | colN | sum | mean | std |
| | | | | | | | | | |
| mat_1 | 1 | 7 | 2 | 12 | 3 | 4 | 6.5142 | 0.54285 | 0.2232 |
| mat_2 | 2 | 8 | 2 | 2650 | 50 | 53 | 1313.3 | 0.49559 | 0.29232 |
| mat_2_boolean | 3 | 9 | 2 | 2650 | 50 | 53 | 1361 | 0.51358 | 0.49991 |
| mat_3 | 4 | 10 | 2 | 4 | 2 | 2 | 1.8111 | 0.45277 | 0.45111 |
| tensor_1 | 5 | 15 | 3 | 16 | 2 | 8 | 7.3043 | 0.45652 | 0.27787 |
| tensor_2 | 6 | 16 | 3 | 75 | 3 | 25 | 40.195 | 0.53593 | 0.29044 |
| tensor_3 | 7 | 17 | 2 | 4 | 1 | 4 | 1.6926 | 0.42315 | 0.37389 |
| tesseract_1 | 8 | 18 | 4 | 72 | 3 | 24 | 34.321 | 0.47669 | 0.26374 |
| tesseract_2 | 9 | 19 | 4 | 20 | 2 | 10 | 8.4191 | 0.42096 | 0.28981 |
| tesseract_bl_3 | 10 | 20 | 4 | 10 | 1 | 10 | 3 | 0.3 | 0.48305 |

| | c1 | c2 | c3 | c4 | | |
|----|---------|---------|---------|---------|--|--|
| | | | | | | |
| r1 | 0.69647 | 0.55131 | 0.98076 | 0.39212 | | |
| r2 | 0.28614 | 0.71947 | 0.68483 | 0.34318 | | |
| r3 | 0.22685 | 0.42311 | 0.48093 | 0.72905 | | |

| r1 | 0.43857 | 0.62 | 49 (| 0.17108 | 0.56564 | 0.072 | 152 0 | .67855 | 0.6166 | 67 0.540 |
|----------|-------------|------------|--------|---------|----------|---------|--------|--------|---------|----------|
| r2 | 0.059678 | | | 0.82911 | 0.084904 | | 289 0 | .27236 | 0.3252 | |
| r3 | 0.39804 | | | 0.33867 | 0.58267 | | | .44513 | 0.07504 | |
| r4 | 0.738 | | | 0.55237 | 0.81484 | | | .11117 | 0.5953 | |
| r5 | 0.18249 | | | 0.57855 | 0.33707 | | | 028681 | 0.743 | |
| | | | | | | | | | | |
| r46 | 0.6813 | | | 0.88786 | 0.69983 | | | .16382 | 0.7419 | |
| r47 | 0.87546 | | | 0.69631 | 0.66117 | | | .79092 | 0.4246 | |
| r48 | 0.51042 | | | 0.44033 | 0.049097 | | | .33302 | 0.2440 | |
| r49 | 0.66931 | | 79 (| 0.43821 | 0.7923 | 0.12 | 979 0 | .75311 | 0.7946 | |
| r50 | 0.58594 | 0.354 | 26 | 0.7651 | 0.51872 | 0.86 | 415 0 | .58281 | 0.8479 | 95 0.45 |
| xxx TABL | E:mat_2_boo | lean xxxxx | xxxxxx | xxxxxx | | | | | | |
| | c1 | c2 | c3 | c4 | c50 | c51 | c52 | c53 | | |
| | | | | | | | | | | |
| r1 | true | false | false | true | true | false | true | true | | |
| r2 | true | | true | true | false | false | true | true | | |
| r3 | false | | false | true | false | true | false | true | | |
| r4 | false | | false | false | | true | true | true | | |
| r5 | true | | true | false | | false | false | true | | |
| | | | | | | | | | | |
| r46 | false | | true | false | | true | true | true | | |
| r47 | true | | true | true | true | true | false | false | | |
| r48 | true | | false | false | | true | false | true | | |
| r49 | true | | false | true | true | true | false | false | | |
| r50 | false | false | false | false | false | false | false | false | | |
| xxx TABL | E:mat_3 xxx | xxxxxxxx | xxxxx | | | | | | | |
| | c1 | c2 | | | | | | | | |
| | | | | | | | | | | |
| r1 | 0.0001247 | | | | | | | | | |
| r2 | 0.8861 | 5 0.792 | 26 | | | | | | | |
| xxx TABL | E:tensor_1 | xxxxxxxx | xxxxxx | xx | | | | | | |
| | c1 | c2 | | c3 | c4 | с5 | с6 | c' | 7 | c8 |
| | | | | | | | | | | |
| r1 | 0 019363 | 0 3/1971 | 0 1 | 52167 | 0.53703 | 0 75756 | 0 6883 | a 0.8° | 3/15 0 | 26597 |
| r2 | | | | | 0.33703 | | | | | |
| 12 | 0.018091 | 0.33355 | 0. | 11738 | 0.77857 | 0.81933 | 0.2004 | 4 0.6 | 157 | 0.308 |
| xxx TABL | E:tensor_2 | | | | _ | | | | | |
| | c1 | c2 | • | с3 | c4 | c22 | c23 | | c24 | c25 |
| | | | | | | | | | | |
| r1 | 0.51866 | 0.40495 | 0.4 | 48278 | 0.99731 | 0.46584 | 0.6297 | 6 0.0 | 035924 | 0.10505 |
| | | | | | 0.35201 | | | | | |
| | | | | | 0.15315 | | | | | |
| 15 | 0.07333 | 0.13401 | 0.0 | 30212 | 0.10010 | 0.11003 | 0.5000 | , | 0.2001 | 0.0000 |
| xxx TABL | E:tensor_3 | | | | | | | | | |
| | c1 | c2 | сЗ | | c4 | | | | | |
| | | | | | | | | | | |
| r1 | 0.1219 | 0.5119 | 0.915 | 53 0. | 14329 | | | | | |
| TADE | P. E. | 4 - | | | | | | | | |
| XXX TABL | E:tesseract | _ | | | - 4 | . 04 | 22 | | 00 | -04 |
| | c1 | c2 | c | 3 | c4 | c21 | c22 | C. | 23 | C24 |

| r1 0.64531 0.59299 0.32115 0.67653 0.90328 0.56911 0.52562 0.12014 r2 0.74558 0.5007 0.46142 0.21384 0.35564 0.13732 0.155 0.23786 r3 0.91137 0.46403 0.18118 0.049919 0.46246 0.46842 0.75348 0.64547 XXX TABLE: tesseract_2 XXXXXXXXXXXXXXXXXX |
|--|
| r2 0.74558 0.5007 0.46142 0.21384 0.35564 0.13732 0.155 0.23786 r3 0.91137 0.46403 0.18118 0.049919 0.46246 0.46842 0.75348 0.64547 XXX TABLE: tesseract_2 XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX |
| XXX TABLE:tesseract_2 XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX |
| TABLE:tesseract_2 xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx |
| c1 c2 c3 c4 c7 c8 c9 c10 1 0.28898 0.48211 0.44359 0.97146 0.61782 0.65121 0.80715 0.11605 1 0.094493 0.34941 0.17595 0.14192 0.16754 0.57097 0.043114 0.70518 XXX TABLE: tesseract_bl_3 XXXXXXXXXXXXXXXXX 1 c2 c3 c4 c7 c8 c9 c10 11 false false true true false true false false |
| r1 |
| r1 0.28898 0.48211 0.44359 0.97146 0.61782 0.65121 0.80715 0.11605 r2 0.094493 0.34941 0.17595 0.14192 0.16754 0.57097 0.043114 0.70518 XXX TABLE:tesseract_bl_3 xxxxxxxxxxxxxxxx |
| r2 0.094493 0.34941 0.17595 0.14192 0.16754 0.57097 0.043114 0.70518 xxx TABLE:tesseract_bl_3 xxxxxxxxxxxxxxxx |
| r2 0.094493 0.34941 0.17595 0.14192 0.16754 0.57097 0.043114 0.70518 xxx TABLE:tesseract_bl_3 xxxxxxxxxxxxxxxx |
| xxx TABLE:tesseract_bl_3 xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx |
| c1 c2 c3 c4 c7 c8 c9 c10 r1 false false true true false true false false |
| r1 false false true true false true false false |
| <pre>xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx</pre> |
| <pre>xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx</pre> |
| <pre>xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx</pre> |
| Scalars xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx |
| Scalars xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx |
| i idx value boolean_1 1 1 1 1 empty 2 2 NaN mat_4 3 11 0.74898 string_float_1 4 13 1021.1 string_int_1 5 14 1021 |
| i idx value boolean_1 |
| boolean_1 |
| <pre>empty</pre> |
| <pre>empty</pre> |
| <pre>empty</pre> |
| mat_4 |
| <pre>string_float_1</pre> |
| string_int_1 5 14 1021 |
| |
| String xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx |
| String xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx |
| <pre>xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx</pre> |
| <pre>i idx string list_string_1 "1" "5" "col1;col2;col3;col4" list_string_2 "2" "6" "row1;row2;row3;row4"</pre> |
| list_string_1 "1" "5" "col1;col2;col3;col4" list_string_2 "2" "6" "row1;row2;row4" |
| list_string_1 "1" "5" "col1;col2;col3;col4" list_string_2 "2" "6" "row1;row2;row3;row4" |
| list_string_2 "2" "6" "row1;row2;row3;row4" |
| list_string_2 "2" "6" "row1;row2;row3;row4" |
| |
| string_1 "3" "12" "Table Name" |
| |
| |
| XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX |
| Functions |
| xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx |
| |
| |
| func1 "1" "3" "@(x)1+2+x" |
| func2 "2" "4" "@(x,y)x*1+sqrt(y)" |

$7.1.2 \quad Test \ FF_CONTAINER_MAP_DISPLAY \ summarize \ Matrix \ Only$

Three large matrixes, show summaries

% Create Container

mp_container_map = containers.Map('KeyType','char', 'ValueType','any');

СО

0.

0.

1

СО

0.

0.

0.

c1

c2

c52

c53

```
rng(123);
mp_container_map('mat_1') = rand(100,100);
mp_container_map('mat_2') = rand(100,100)*2 + 1;
mp_container_map('mat_2_boolean') = (rand(100,100) > 0.5);
% Will only print
ff_container_map_display(mp_container_map);
_____
CONTAINER NAME: mp_container_map ND Array (Matrix etc)
i
                       idx
                             ndim
                                    numel
                                            rowN
                                                   colN
                                                           sum
                                                                    mean
                                                                               std
                       ___
                             ____
                                    ----
                                            ----
                                                   ----
                                                          ----
                                                                   -----
                                                                             -----
                              2
   mat_1
                  1
                       1
                                    10000
                                            100
                                                   100
                                                          4982.3
                                                                   0.49823
                                                                             0.28829
   mat_2
                  2
                        2
                              2
                                    10000
                                            100
                                                   100
                                                           20029
                                                                    2.0029
                                                                             0.57632
                  3
                        3
                              2
                                    10000
                                            100
                                                   100
                                                            4995
                                                                    0.4995
                                                                             0.50002
   mat_2_boolean
7.1.3 Test FF_CONTAINER_MAP_DISPLAY Show Matrix Subset
A container map with three small matrixes, print only only 2 rows and 3 columns.
% Create Container
mp_container_map = containers.Map('KeyType','char', 'ValueType','any');
rng(789);
mp_container_map('mat_1') = rand(3,4);
mp_container_map('mat_2') = rand(50,53);
mp_container_map('mat_2_boolean') = (rand(50,53) > 0.5);
% Will only print
ff_container_map_display(mp_container_map, 2, 3);
CONTAINER NAME: mp_container_map ND Array (Matrix etc)
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
                  i
                       idx
                             ndim
                                            rowN
                                                                               std
                                    numel
                                                   colN
                                                           SIIM
                                                                    mean
                                                   ----
                                                           ----
                                                                   -----
                                                                             _____
   mat_1
                  1
                       1
                              2
                                     12
                                              3
                                                     4
                                                          4.9876
                                                                   0.41564
                                                                             0.33586
   mat_2
                  2
                       2
                              2
                                    2650
                                             50
                                                    53
                                                          1324.3
                                                                   0.49973
                                                                             0.28834
   mat_2_boolean
                  3
                       3
                              2
                                    2650
                                             50
                                                    53
                                                            1350
                                                                   0.50943
                                                                             0.50001
xxx TABLE:mat 1 xxxxxxxxxxxxxxxxx
          c1
                    c2
                              сЗ
                                        c4
                            0.01062
   r1
        0.32333
                  0.62442
                                      0.53815
   r3
        0.79378
                  0.75889
                            0.11104
                                      0.55157
xxx TABLE:mat_2 xxxxxxxxxxxxxxxxxx
                               c52
                                         c53
           c1
                     c2
          _____
                   _____
                             -----
                                       _____
   r1
         0.72837
                   0.20976
                             0.74583
                                       0.22321
   r50
         0.52812
                    0.545
                             0.49521
                                       0.29826
xxx TABLE:mat_2_boolean xxxxxxxxxxxxxxxxx
```

r1 false true true true r50 true false false true

Appendix A

Index and Code Links

A.1 Savings Dynamic Programming links

- 1. Looped Grid Infinite Horizon Dynamic Savings Problem: mlx | m | pdf | html
 - Common grid looped solution
 - Slow, but easy to modify, useful for developing new models
 - \bullet Given preferences, some AR(1) shock process, solve the infinite horizon household savings dynamic programming problem. The state-space and choice-space share the same asset grid.
 - MEconTools: ff_vfi_az_loop()
- 2. Vectorized Grid Infinite Horizon Dynamic Savings Problem: mlx | m | pdf | html
 - Common grid vectorized solution
 - Fast, sufficiently approximate value(a,z), but c(a,z) not precise
 - Given preferences, some AR(1) shock process, solve the infinite horizon household savings dynamic programming problem. The state-space and choice-space share the same asset grid.
 - MEconTools: ff_vfi_az_vec()
- 3. Looped Exact Infinite Horizon Dynamic Savings Problem: mlx | m | pdf | html
 - Exact choice looped solution
 - Slow, but high precision at low grid size (given value grid, accurate up to 0.001525878 percent of individual-specific cash-on-hand)
 - Given preferences, some AR(1) shock process, solve the infinite horizon household savings dynamic programming problem. The state-space is on a grid. The choice space are continuous percentages of cash-on-hand.
 - MEconTools: ff_vfi_az_bisec_loop()
- 4. Vectorized Exact Infinite Horizon Dynamic Savings Problem: mlx | m | pdf | html
 - Exact choice vectorized solution
 - $\bullet\,$ Fast, approximates choices with higher precision (given value grid, accurate up to 0.001525878 percent of individual-specific cash-on-hand)
 - Given preferences, some AR(1) shock process, solve the infinite horizon household savings dynamic programming problem. The state-space is on a grid. The choice space are continuous percentages of cash-on-hand.
 - MEconTools: ff_vfi_az_bisec_vec()

A.2 Summarize Policy and Value links

- 1. Summarize ND Array Policy and Value Functions: mlx | m | pdf | html
 - Given an NDarray matrix with N1, N2, ..., ND dimensions. Generate average and standard deviation for the 3rd dimension, grouping by the other dimensions.
 - For example, show the 5th dimension as the column groups, and the other variables generate combinations shown as rows.
 - The resulting summary statistics table contains mean and standard deviation among other statistics over the policy or value contained in the ND array.
 - MEconTools: ff_summ_nd_array()

A.3 Distributional Analysis links

- 1. Gateway Joint Probability Mass Statistics: mlx | m | pdf | html
 - Given probability mass function f(s), and information y(s), x(s), z(s) at each element of the state-space, compute statistics for each variable, y, x, z, which are all discrete random variables.
 - Compute their correlation and covariance.
 - MEconTools: ff_simu_stats()
- 2. Discrete Random Variable Distributional Statistics: mlx | m | pdf | html
 - Model simulation generates discrete random variables, calculate mean, standard deviation, min, max, percentiles, and proportion of outcomes held by x percentiles, etc.
 - MEconTools: ff_disc_rand_var_stats()
- 3. Generate Discrete Random Variable: mlx | m | pdf | html
 - Given mass at state space points, and y, c, a, z and other outcomes or other information at each corresponding state space points, generate discrete random variable, with unique sorted values, and mass for each unique sorted values.
 - Generate additional joint distributions: if initial distribution is over f(a,z), generate joint distribution of f(y,a) or f(y,z).
 - MEconTools: ff_disc_rand_var_mass2outcomes()
- 4. Discrete Random Variable Correlation and Covariance: mlx | m | pdf | html
 - Given probability mass function f(s), X(s), and Y(s), compute the covariance and correlation betwee X and Y.
 - MEconTools: ff_disc_rand_var_mass2covcor()

A.4 Graphs links

- 1. Multiple Line Graph Function: mlx | m | pdf | html
 - Grid based Graph, x-axis one param, color another param, over outcomes.
 - MEconTools: ff_graph_grid()

A.5 Data Structures links

- 1. Log and Power Spaced Asset and Choice Grids: mlx | m | pdf | html
 - Generate linear, log-space, power-space, or threshold-cut asset or choice grids.
 - MEconTools: ff_saveborr_grid()

A.6 Common Functions links

- 1. Discretize AR1 Normal Shock Tauchen (1986): mlx | m | pdf | html
 - Mean zero AR(1) shock discretize following Tauchen (1986).
 - **MEconTools**: *ffy_tauchen()*
- 2. Discretize AR1 Normal Shock Rouwenhorst (1995): mlx | m | pdf | html
 - Mean zero AR(1) shock discretize following Rouwenhorst (1995).
 - **MEconTools**: *ffy_rouwenhorst()*

A.7 Support Tools links

- 1. Organizes and Prints Container Map Key and Values: $\mathbf{mlx} \mid \mathbf{m} \mid \mathbf{pdf} \mid \mathbf{html}$
 - Summarizes the contents of a map container by data types. Includes, scalar, array, matrix, string, functions, tensors (3-tuples), tesseracts (4-tuples).
 - MEconTools: ff_container_map_display()

Bibliography

The Math Works Inc (2019). MATLAB. Matlab package version 2019b.

Xie, Y. (2020). bookdown: Authoring Books and Technical Documents with R Markdown. R package version 0.18.