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Preface

This is a work-in-progress Matlab package consisting of functions that solve the equilibrium gender labor force participation and wage model in Bhalotra, Fernández and Wang (2022). Tested with Matlab 2021b (The MathWorks Inc, 2021).

All functions are parts of a matlab toolbox that can be installed:

Download and install the Matlab toolbox: PrjLabEquiBFW.mltbx

The Code Companion can also be accessed via the bookdown site and PDF linked below:

bookdown site, bookdown pdf, MathWorks File Exchange

https://www.mathworks.com/matlabcentral/fileexchange/

This bookdown file is a collection of mlx based vignettes for functions that are available from Pr-jLabEquiBFW. Each Vignette file contains various examples for invoking each function.

The package relies on MEconTools, which needs to be installed first. The package does not include allocation functions, only simulation code to generate the value of each stimulus check increments for households.

The site is built using Bookdown (Xie, 2020).

Please contact FanWangEcon for issues or problems.

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Introduction

1.1 Bhalotra, Fernández, and Wang (2022)

In Bhalotra, Fernández, and Wang (2022).

Core Functions

2.1 CES Demand Core Functions

This is the example vignette for function: **bfw_mp_func_demand** from the **PrjLabEquiBFW Package.** This function generates a container map with key CES demand-side equations for a particular sub-nest.

2.1.1 Default Test

| xxxxxxxxxxxxxxxxxxxxxxxxxxxxxx | xxxxxxxx | XXX | |
|--------------------------------|----------|------|--|
| | i | idx | |
| | | | |
| fc_OMEGA | "1" | "1" | "@(p1,p2,rho,beta_1,beta_2)p1.*fc_d1(p1,p2,1,1,rho,be |
| fc_d1 | "2" | "2" | <pre>"@(p1,p2,Y,Z,rho,beta_1,beta_2)(Y/Z).*(beta_1+beta_2.</pre> |
| fc_d2 | "3" | "3" | "@(p1,p2,Y,Z,rho,beta_1,beta_2)(Y/Z).*(beta_1.*((p2./ |
| <pre>fc_lagrange_x1</pre> | "4" | "4" | "@(p1,rho,beta_1,beta_2,x_1,x_2)p1/(((beta_1*x_1^(rho |
| fc_lagrange_x2 | "5" | "5" | "@(p2,rho,beta_1,beta_2,x_1,x_2)p2/(((beta_1*x_1^(rho |
| fc_output_nest | "6" | "6" | "@(q1,q2,rho,beta_1,beta_2)((beta_1)*q1^(rho)+beta_2* |
| fc_p1_foc | "7" | "7" | "@(lagrangem,rho,beta_1,beta_2,x_1,x_2)lagrangem*(((b |
| fc_p2_foc | "8" | "8" | "@(lagrangem,rho,beta_1,beta_2,x_1,x_2)lagrangem*(((b |
| fc_share_given_elas_foc | "9" | "9" | <pre>"@(rho,p1,p2,x1,x2)fc_share_given_elas_foc_Q(rho,p1,p</pre> |
| fc_w1dw2 | "10" | "10" | "@(x_1,x_2,rho,beta_1,beta_2)(x_2/x_1)^(1-rho)*(beta_ |
| fc_yz_ratio | "11" | "11" | "@(p1,p2,q1,q2,rho,beta_1,beta_2)fc_revenue(p1,p2,q1, |

2.2 Multinomial Logit Core Functions

This is the example vignette for function: **bfw_mp_func_supply** from the **PrjLabEquiBFW Package.** This function generates a container map with key multinomial logit supply-side equations.

2.2.1 Test BL LOG WAGE is false

```
Default test
```

bl_log_wage = false;

```
bl_verbose = true;
mp_func_supply = bfw_mp_func_supply(bl_log_wage, bl_verbose);
_____
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
CONTAINER NAME: mp_func Functions
idx
                     "1"
                            "1"
   fc_ar_prob_wrk
                                  "@(arpsi0,psi1,mtwage,probdenom)fc_v_occ(reshape(arpsi0,[1,len
                     "2"
                            "2"
   fc_log_pmdpo_occ
                                  "@(psi0,psi1,arwage,pie1,pie2,pie3,pie4,pie5,pie6,t,prbchd,prb
                     "3"
                            "3"
   fc_prob_denom
                                  "@(arpsi0,psi1,arpie,arwage1,arwage2,arwage3,t,prbchd,prbmar,p
                     "4"
                                  "@(arpie,t,prbchd,prbmar,prbapp,prbjsy,probdenom)fc_v_lei(arpi
                            "4"
   fc_prob_lei
                     "5"
                            "5"
                                  "@(p1,G_1,zeta_1_0,zeta_1_1)G_1./(1+(exp(-zeta_1_0-zeta_1_1.*p
   fc_s1
                     "6"
                            "6"
   fc_s2
                                  "@(p2,G_2,zeta_2_0,zeta_2_1)G_2./(1+(exp(-zeta_2_0-zeta_2_1.*p
                     "7"
                            "7"
                                  "@(potlabor,prob)potlabor.*prob"
   fc_supply
```

2.2.2 Test BL_LOG_WAGE is false

```
Default test
```

```
bl_log_wage = true;
mp_func_supply = bfw_mp_func_supply(bl_log_wage, bl_verbose);
```

CONTAINER NAME: mp_func Functions

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | i | idx | |
|------------------|-----|-----|---|
| | | | |
| fc_ar_prob_wrk | "1" | "1" | "@(arpsi0,psi1,mtwage,probdenom)fc_v_occ(reshape(arpsi0,[1,len |
| fc_log_pmdpo_occ | "2" | "2" | "@(psi0,psi1,arwage,pie1,pie2,pie3,pie4,pie5,pie6,t,prbchd,prb |
| fc_prob_denom | "3" | "3" | "@(arpsi0,psi1,arpie,arwage1,arwage2,arwage3,t,prbchd,prbmar,p |
| fc_prob_lei | "4" | "4" | <pre>"@(arpie,t,prbchd,prbmar,prbapp,prbjsy,probdenom)fc_v_lei(arpi</pre> |
| fc_s1 | "5" | "5" | "@(p1,G_1,zeta_1_0,zeta_1_1)G_1./(1+(exp(-zeta_1_0-zeta_1_1.*p |
| fc_s2 | "6" | "6" | "@(p2,G_2,zeta_2_0,zeta_2_1)G_2./(1+(exp(-zeta_2_0-zeta_2_1.*p |
| fc_supply | "7" | "7" | "@(potlabor,prob)potlabor.*prob" |

2.3 Equilibrium Core Functions

This is the example vignette for function: bfw_mp_func_equi from the PrjLabEquiBFW Package.

2.3.1 Default Test

___ ___

| f_x_root | "1" | "1" | <pre>"@(x,price_ratio,yfz_per_input,rho)(1-x)+(x).*(price_ratio)</pre> |
|---------------------------------|-----|-----|--|
| fc_p1_of_p2 | "2" | "2" | "@(p2,G_2,zeta_2_0,zeta_2_1,Y,Z,rho,beta_1,beta_2)((((((1+ |
| fc_p1_of_p2andSupply | "3" | "3" | <pre>"@(p2,supplyQofP,Y,Z,rho,beta_1,beta_2)((((((Y/Z)./supplyQ</pre> |
| fc_p2_of_p1 | "4" | "4" | "@(p1,G_1,zeta_1_0,zeta_1_1,Y,Z,rho,beta_1,beta_2)((((((1+ |
| <pre>fc_p2_of_p1andSupply</pre> | "5" | "5" | <pre>"@(p1,supplyQofP,Y,Z,rho,beta_1,beta_2)((((((Y/Z)./supplyQ</pre> |

Parameters

3.1 bfw_mp_path

This is the example vignette for function: bfw_mp_path from the PrjLabEquiBFW Package.

3.1.1 Default Map of Path (Fan path)

| | i | idx | string |
|----------------------|------|------|--|
| | | | |
| spt codem | "1" | "1" | "C:\Users\fan\PrjLabEquiBFW\PrjLabEquiBFW\" |
| spt codem data | "2" | "2" | "C:\Users\fan\PrjLabEquiBFW\PrjLabEquiBFW_data\" |
| spt_codem_doc | "3" | "3" | "C:\Users\fan\PrjLabEquiBFW\PrjLabEquiBFW\doc\" |
| spt_output_root | "4" | "4" | "C:\Users\fan\Documents\Dropbox (UH-ECON)\Latex_Bhalotra |
| spt_repo_root | "5" | "5" | "C:\Users\fan\PrjLabEquiBFW\" |
| spt_simu_outputs_log | "6" | "6" | "C:\Users\fan\Documents\Dropbox (UH-ECON)\Latex_Bhalotra |
| spt_simu_outputs_mat | "7" | "7" | "C:\Users\fan\Documents\Dropbox (UH-ECON)\Latex_Bhalotra |
| spt_simu_outputs_prf | "8" | "8" | "C:\Users\fan\Documents\Dropbox (UH-ECON)\Latex_Bhalotra |
| spt_simu_outputs_vig | "9" | "9" | "C:\Users\fan\Documents\Dropbox (UH-ECON)\Latex_Bhalotra |
| spt_simu_results_csv | "10" | "10" | "C:\Users\fan\Documents\Dropbox (UH-ECON)\Latex_Bhalotra |
| spt_simu_results_img | "11" | "11" | "C:\Users\fan\Documents\Dropbox (UH-ECON)\Latex_Bhalotra |
| st_computer | "12" | "12" | "fan" |

3.1.2 Map of Path for Alternative Path Installer

Two directories, one for the repo and one for where outputs go, need to be specified.

| | i | idx | string |
|----------------------|------|------|---|
| | | | |
| spt_codem | "1" | "1" | "~\PrjLabEquiBFW\PrjLabEquiBFW\" |
| spt_codem_data | "2" | "2" | "~\PrjLabEquiBFW\PrjLabEquiBFW_data\" |
| spt_codem_doc | "3" | "3" | "~\PrjLabEquiBFW\PrjLabEquiBFW\doc\" |
| spt_output_root | "4" | "4" | "~\Dropbox\PrjLabEquiBFW" |
| spt_repo_root | "5" | "5" | "~\PrjLabEquiBFW" |
| spt_simu_outputs_log | "6" | "6" | "~\Dropbox\PrjLabEquiBFW\PrjLabEquiBFWOutput\log\" |
| spt_simu_outputs_mat | "7" | "7" | "~\Dropbox\PrjLabEquiBFW\PrjLabEquiBFWOutput\mat\" |
| spt_simu_outputs_prf | "8" | "8" | "~\Dropbox\PrjLabEquiBFW\PrjLabEquiBFWOutput\prof\" |
| spt_simu_outputs_vig | "9" | "9" | "~\Dropbox\PrjLabEquiBFW\PrjLabEquiBFWOutput\vig\" |
| spt_simu_results_csv | "10" | "10" | "~\Dropbox\PrjLabEquiBFW\PrjLabEquiBFWOutput\res\" |
| spt_simu_results_img | "11" | "11" | "~\Dropbox\PrjLabEquiBFW\PrjLabEquiBFWOutput\img\" |

3.2 bfw_mp_control

This is the example vignette for function: bfw_mp_control from the PrjLabEquiBFW Package.

3.2.1 Map of Control Parameters

```
[bl_display_status, bl_display_verbose_status, bl_verbose] = deal(true, true, true);
mp_func_supply = bfw_mp_control(bl_display_status, bl_display_verbose_status, bl_verbose);
pos = 7 ; key = fmin_controls_a
                   Display: 'off'
               MaxFunEvals: 2500
                   MaxIter: 2000
                    TolFun: 1.0000e-05
                      TolX: 1.0000e-05
               FunValCheck: []
                 OutputFcn: []
                  PlotFcns: []
           ActiveConstrTol: []
                 Algorithm: []
    AlwaysHonorConstraints: []
           DerivativeCheck: []
               Diagnostics: []
             DiffMaxChange: []
             DiffMinChange: []
            FinDiffRelStep: []
               FinDiffType: []
         GoalsExactAchieve: []
                GradConstr: []
                   GradObj: []
                   HessFcn: []
                   Hessian: []
                  HessMult: []
               HessPattern: []
                HessUpdate: []
          InitBarrierParam: []
     InitTrustRegionRadius: []
                  Jacobian: []
                 JacobMult: []
              JacobPattern: []
                LargeScale: []
                  MaxNodes: []
                MaxPCGIter: []
```

| ${	t MaxProjCGIter:}$ | [] |
|------------------------------|------|
| MaxSQPIter: | [] |
| MaxTime: | [] |
| MeritFunction: | [] |
| MinAbsMax: | [] |
| | |
| ${\tt NoStopIfFlatInfeas:}$ | |
| ObjectiveLimit: | [] |
| PhaseOneTotalScaling: | [] |
| Preconditioner: | [] |
| PrecondBandWidth: | [] |
| RelLineSrchBnd: | [] |
| | |
| RelLineSrchBndDuration: | [] |
| ScaleProblem: | [] |
| SubproblemAlgorithm: | [] |
| TolCon: | [] |
| TolConSQP: | [] |
| TolGradCon: | [] |
| | |
| TolPCG: | |
| TolProjCG: | [] |
| TolProjCGAbs: | [] |
| TypicalX: | [] |
| UseParallel: | [] |
| | |
| pos = 8 ; key = fmin_control | a h |
| | _ |
| Display: | 'off |
| MaxFunEvals: | [] |
| MaxIter: | [] |
| TolFun: | [] |
| TolX: | [] |
| FunValCheck: | [] |
| OutputFcn: | [] |
| - | |
| PlotFcns: | [] |
| ActiveConstrTol: | [] |
| Algorithm: | [] |
| AlwaysHonorConstraints: | [] |
| DerivativeCheck: | [] |
| Diagnostics: | [] |
| | [] |
| DiffMaxChange: | |
| DiffMinChange: | [] |
| FinDiffRelStep: | [] |
| FinDiffType: | [] |
| GoalsExactAchieve: | [] |
| GradConstr: | [] |
| GradObj: | [] |
| HessFcn: | [] |
| | |
| Hessian: | [] |
| HessMult: | [] |
| HessPattern: | [] |
| HessUpdate: | [] |
| InitBarrierParam: | [] |
| InitTrustRegionRadius: | [] |
| Jacobian: | [] |
| | |
| JacobMult: | [] |
| JacobPattern: | [] |
| LargeScale: | [] |
| MaxNodes: | [] |
| MaxPCGIter: | [] |
| MaxProjCGIter: | [] |
| maxi rojodicer. | LJ |

| MaxSQPIter: | [] |
|-----------------------------|------------|
| MaxTime: | |
| MeritFunction: | |
| MinAbsMax: | |
| NoStopIfFlatInfeas: | |
| ObjectiveLimit: | |
| PhaseOneTotalScaling: | |
| Preconditioner: | |
| PrecondBandWidth: | |
| RelLineSrchBnd: | |
| RelLineSrchBndDuration: | |
| ScaleProblem: | |
| SubproblemAlgorithm: | |
| TolCon: | |
| TolConSQP: | [] |
| TolGradCon: | [] |
| | |
| TolPCG: | |
| TolProjCG: | |
| TolProjCGAbs: | [] |
| TypicalX: | [] |
| UseParallel: | |
| | |
| pos = 9; key = fmin_control | |
| Display: | 'iter' |
| MaxFunEvals: | 750 |
| MaxIter: | 500 |
| TolFun: | 1.0000e-05 |
| TolX: | 1.0000e-05 |
| FunValCheck: | [] |
| OutputFcn: | [] |
| PlotFcns: | [] |
| ActiveConstrTol: | [] |
| Algorithm: | [] |
| AlwaysHonorConstraints: | [] |
| DerivativeCheck: | [] |
| Diagnostics: | [] |
| DiffMaxChange: | [] |
| DiffMinChange: | [] |
| FinDiffRelStep: | [] |
| ${\tt FinDiffType:}$ | [] |
| GoalsExactAchieve: | [] |
| GradConstr: | [] |
| GradObj: | [] |
| HessFcn: | [] |
| Hessian: | [] |
| HessMult: | |
| HessPattern: | |
| HessUpdate: | |
| InitBarrierParam: | |
| InitTrustRegionRadius: | |
| Jacobian: | |
| JacobMult: | |
| JacobPattern: | |
| LargeScale: | [] |
| MaxNodes: | [] |
| MaxPCGIter: | [] |
| | |
| MaxProjCGIter: | [] |
| MaxSQPIter: | |
| | |

```
MaxTime: []
             MeritFunction: []
                 MinAbsMax: []
        NoStopIfFlatInfeas: []
            ObjectiveLimit: []
      PhaseOneTotalScaling: []
            Preconditioner: []
          PrecondBandWidth: []
            RelLineSrchBnd: []
    RelLineSrchBndDuration: []
              ScaleProblem: []
       SubproblemAlgorithm: []
                    TolCon: []
                 TolConSQP: []
                TolGradCon: []
                    TolPCG: []
                 TolProjCG: []
              TolProjCGAbs: []
                  TypicalX: []
               UseParallel: []
pos = 10 ; key = fmin_controls_d
                   Display: 'iter'
               MaxFunEvals: 5000
                   MaxIter: 15
                    TolFun: 1.0000e-06
                      TolX: 1.0000e-06
               FunValCheck: []
                 OutputFcn: []
                  PlotFcns: {@optimplotfval @optimplotx @optimplotstepsize @optimplotfunccount}
           ActiveConstrTol: []
                 Algorithm: []
    AlwaysHonorConstraints: []
           DerivativeCheck: []
               Diagnostics: []
             DiffMaxChange: []
             DiffMinChange: []
            FinDiffRelStep: []
               FinDiffType: []
         GoalsExactAchieve: []
                GradConstr: []
                   GradObj: []
                   HessFcn: []
                   Hessian: []
                  HessMult: []
               HessPattern: []
                HessUpdate: []
          InitBarrierParam: []
     InitTrustRegionRadius: []
                  Jacobian: []
                 JacobMult: []
              JacobPattern: []
                LargeScale: []
                  MaxNodes: []
                MaxPCGIter: []
             MaxProjCGIter: []
                MaxSQPIter: []
                   MaxTime: []
```

```
MeritFunction: []
             MinAbsMax: []
    NoStopIfFlatInfeas: []
        ObjectiveLimit: []
  PhaseOneTotalScaling: []
        Preconditioner: []
      PrecondBandWidth: []
        RelLineSrchBnd: []
RelLineSrchBndDuration: []
          ScaleProblem: []
   SubproblemAlgorithm: []
                TolCon: []
             TolConSQP: []
            TolGradCon: []
                TolPCG: []
             TolProjCG: []
          TolProjCGAbs: []
              TypicalX: []
           UseParallel: []
```

CONTAINER NAME: mp_controls Scalars

| | _ | | |
|--|---|---|---|
| bl_bfw_solveequi_kwfw_display | 1 | 2 | 1 |
| bl_bfw_solveequi_kwfw_display_verbose | 2 | 3 | 1 |
| bl_bfw_solveequi_w2q2w_display | 3 | 4 | 1 |
| bl_bfw_solveequi_w2q2w_display_verbose | 4 | 5 | 1 |
| bl_timer | 5 | 6 | 1 |

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

3.3 bfw_mp_param_esti

This is the example vignette for function: bfw_mp_param_esti from the PrjLabEquiBFW Package.

idx

value

3.3.1 Map of Estimated Parameters

```
bl_log_wage = true;
bl_verbose = true;
mp_func_supply = bfw_mp_param_esti(bl_log_wage, bl_verbose);
pos = 42 ; key = mp_rho_nests
   Map with properties:
```

Count: 11 KeyType: char ValueType: any

pos = 43 ; key = mp_rho_nests_init

Map with properties:

Count: 8 KeyType: char ValueType: any

| | i | idx | ndim | numel | rowN | colN | sum | mean | std |
|-----------------|--------|---------|-------|--------|---------|------|----------|----------|---------|
| | | | | | | | | | |
| ar_alpha_A001 | 1 | 1 | 2 | 4 | 1 | 4 | -0.94699 | -0.23675 | 0.5166 |
| ar_alpha_A002 | 2 | 2 | 2 | 4 | 1 | 4 | -1.4489 | -0.36221 | 0.7982 |
| ar_alpha_A003 | 3 | 3 | 2 | 4 | 1 | 4 | -0.57104 | -0.14276 | 0.3128 |
| ar_alpha_AA01 | 4 | 4 | 2 | 4 | 1 | 4 | -0.67951 | -0.16988 | 0.3633 |
| ar_alpha_AA02 | 5 | 5 | 2 | 4 | 1 | 4 | -0.6718 | -0.16795 | 0.33676 |
| ar_alpha_B001 | 6 | 6 | 2 | 4 | 1 | 4 | -1.2904 | -0.32261 | 0.67446 |
| ar_alpha_B002 | 7 | 7 | 2 | 4 | 1 | 4 | -1.1023 | -0.27558 | 0.57386 |
| ar_alpha_B003 | 8 | 8 | 2 | 4 | 1 | 4 | -0.85037 | -0.21259 | 0.44078 |
| ar_alpha_B101 | 9 | 9 | 2 | 4 | 1 | 4 | -2.7486 | -0.68715 | 1.444 |
| ar_alpha_B102 | 10 | 10 | 2 | 4 | 1 | 4 | -1.3642 | -0.34105 | 0.66492 |
| ar_alpha_B103 | 11 | 11 | 2 | 4 | 1 | 4 | -1.1457 | -0.28641 | 0.5733 |
| arpie_f_s | 12 | 12 | 2 | 6 | 1 | 6 | 4.6479 | 0.77464 | 6.311 |
| arpie_f_u | 13 | 13 | 2 | 6 | 1 | 6 | 8.0344 | 1.3391 | 4.86 |
| arpie_k_s | 14 | 14 | 2 | 6 | 1 | 6 | 1.3887 | 0.23145 | 1.8386 |
| arpie_k_u | 15 | 15 | 2 | 6 | 1 | 6 | 4.7387 | 0.78979 | 1.8849 |
| arpsi0_f_s | 16 | 16 | 2 | 3 | 1 | 3 | 3.3528 | 1.1176 | 1.0974 |
| arpsiO_f_u | 17 | 17 | 2 | 3 | 1 | 3 | 20.22 | 6.74 | 0.5577 |
| arpsi0_k_s | 18 | 18 | 2 | 3 | 1 | 3 | 1.779 | 0.59299 | 0.68939 |
| arpsi0_k_u | 19 | 19 | 2 | 3 | 1 | 3 | 18.003 | 6.0009 | 0.8411 |
| TABLE:ar_alpha_ | A001 x | xxxxxxx | ***** | xx | | | | | |
| c1 | , | c2 | | c3 | c4 | | | | |
| | | | | | | | | | |
| r1 0.0001339 | i.c | 0.00561 | 07 0 | 068567 | -1.0101 | | | | |

| | r1 | 0.00013396 | -0.0056187 | 0.068567 | -1.0101 |
|---|---------|-----------------------|-------------------|----------|---------|
| X | xx TABL | E:ar_alpha_A002 c1 | xxxxxxxxxxx c2 | c3 | c4 |
| | | | | | |
| | r1 | 0.00017171 | -0.0079274 | 0.11544 | -1.5565 |
| X | xx TABL | E:ar_alpha_A003 | xxxxxxxxxx | xxxxx | |
| | | c1 | c2 | c3 | c4 |

r1 6.9362e-05 -0.0031181 0.04301 -0.611

xxx TABLE:ar_alpha_AAO1 xxxxxxxxxxxxxxxxx

c1 c2 c3 c4

| | r1 | 3.3671e-05 | -0.001978 | 0.03661 | -0.71418 | |
|-----|-------|-------------|------------|------------|----------|---------|
| xxx | TABLE | | c2 | c3 | c4 | _ |
| | r1 | 9.8127e-06 | | | | |
| xxx | TABLE | c1 | c2 | c3 | | |
| | r1 | 7.1149e-05 | | | | |
| xxx | TABLE | c1 | c2 | с3 | | |
| | r1 | 7.7753e-05 | -0.0032235 | 0.036755 | -1.1359 | |
| xxx | TABLE | c1 | c2 | с3 | | |
| | r1 | 4.3028e-05 | -0.0018888 | 0.02499 | -0.87352 | |
| xxx | TABLE | c1 | | c3 | | |
| | r1 | -1.7675e-05 | -0.0011106 | 0.10452 | -2.852 | |
| xxx | TABLE | c1 | c2 | c3 | | |
| | r1 | -0.00010096 | 0.0046709 | -0.030629 | -1.3382 | |
| xxx | TABLE | c1 | c2 | c3 | c4 | |
| | r1 | -7.5369e-05 | 0.002346 | -0.0015487 | -1.1464 | |
| xxx | TABLE | | c3 | c4 | c5 | c6 |
| | r1 | 11.145 0 | | | | -1.1508 |
| xxx | TABLE | c1 c2 | | c4 | c5 | c6 |
| | r1 | 11.145 0 | -0.25662 | -0.26519 | -2.0749 | -0.5135 |

| xxx | TABLE | c1 | | c3 | | c4 | | | c6 |
|-----|---|----------------------------|--------|------------------------|-----|------|----------------------|-------|--------------|
| | r1 | | | -0.043896 | | | | | 1.1023 |
| xxx | TABLE | arpie k u | xxxxx | xxxxxxxxx | ХХ | | | | |
| | | c1 | c2 | c3 | (| c4 | | | с6 |
| | | | | | | | | | |
| | r1 | 2.4457 | 0 | -2.2809 | 3.0 | 0169 | 0.845 | 13 | 0.71184 |
| xxx | TABLE | :arpsi0_f_s c1 c2 | 2 | c3 | xxx | | | | |
| | r1 | 0 1.19 | 592 | 2.1936 | | | | | |
| xxx | TABLE | :arpsi0_f_u | ı xxxx | xxxxxxxxx | xxx | | | | |
| | | c1 | c2 | c3 | | | | | |
| | | | | | | | | | |
| | r1 | 7.3697 | 6.542 | 2 6.3081 | | | | | |
| xxx | TABLE | = | | xxxxxxxxx | xxx | | | | |
| | | c1 c2 | 2 | c3 | | | | | |
| | | | | | | | | | |
| | r1 | 0 0.42 | 2958 | 1.3494 | | | | | |
| xxx | TABLE | _ | | xxxxxxxxx | xxx | | | | |
| | | c1 | c2 | c3 | | | | | |
| | | | | | | | | | |
| | r1 | 6.6935 | 6.2443 | 3 5.0649 | | | | | |
| | | | | | | _ | | | |
| | | :XXXXXXXXXXX [_mp: | | xxxxxxxxxxx Scalars | XXX | X | | | |
| | | | | xxxxxxxxx | xxx | | | _ | |
| | | | | | | i | idx | valı | 1e |
| | | | | | | | | | |
| | | g_wage | | | | | 20 | | 1 |
| | _ | _ | | nualroutine | | | 21 | 0.031 | |
| | | o_gen_absti | | | | | 22 | 0.65 | |
| | _ | o_gen_manua o_gen_rout: | | | | | 23 24 | 0.083 | |
| | _ | -0 - | | 12] | | | 2 4 25 | -0.15 | |
| | fl_rho_routine_vs_manual fl_rho_skill_abstract | | | | | | 26 | 0.30 | |
| | _ | o_skill_man | | | | | 27 | 0.73 | |
| | _ | o_skill_ro | | | | | 28 | 0.30 | |
| | _ | agg_y1989 | | | | 10 | 29 | 1.4 | 1905 |
| | | agg_y1992 | | | | 11 | 30 | 1.4 | 1602 |
| | | agg_y1994 | | | | | 31 | | 3493 |
| | | agg_y1996 | | | | | 32 | | 7686 |
| | | agg_y1998 agg_y2000 | | | | | 33 34 | | 3018 0599 |
| | 11_yZ | 288_y2000 | | | | 10 | J- 1 | 2.0 | ,U33 |

| fl_yzagg_y2002 | 16 | 35 | 2.0597 |
|----------------|----|----|---------|
| fl_yzagg_y2004 | 17 | 36 | 2.2803 |
| fl_yzagg_y2005 | 18 | 37 | 2.3392 |
| fl_yzagg_y2008 | 19 | 38 | 2.4908 |
| fl_yzagg_y2010 | 20 | 39 | 2.7153 |
| fl_yzagg_y2012 | 21 | 40 | 2.822 |
| fl_yzagg_y2014 | 22 | 41 | 2.8707 |
| psi1 | 23 | 44 | 0.96625 |

Data

4.1 bfw_mp_data

This is the example vignette for function: bfw_mp_data from the PrjLabEquiBFW Package.

4.1.1 Get All Data

```
bl_verbose = false;
mp_data = bfw_mp_data(bl_verbose);
```

4.1.2 Dataset 1

disp(mp_data('tb_data_pq'));

| year | category | numberWorkers | ${\tt meanWage}$ |
|------|----------|---------------|------------------|
| | | | |
| 1989 | {'C001'} | 1.4486e+06 | 1.942 |
| 1989 | {'C002'} | 1.1256e+06 | 3.2247 |
| 1989 | {'C003'} | 1.5156e+06 | 3.3738 |
| 1989 | {'C004'} | 8.4266e+06 | NaN |
| 1989 | {'C011'} | 9199 | 2.1604 |
| 1989 | {'C012'} | 1.1011e+05 | 5.6589 |
| 1989 | {'C013'} | 4.816e+05 | 5.8023 |
| 1989 | {'C014'} | 2.533e+05 | NaN |
| 1989 | {'C101'} | 4.4275e+06 | 2.3157 |
| 1989 | {'C102'} | 3.1277e+06 | 3.2178 |
| 1989 | {'C103'} | 1.9279e+06 | 4.329 |
| 1989 | {'C104'} | 4.8562e+05 | NaN |
| 1989 | {'C111'} | 96487 | 4.5245 |
| 1989 | {'C112'} | 2.7718e+05 | 5.4146 |
| 1989 | {'C113'} | 1.3868e+06 | 8.0437 |
| 1989 | {'C114'} | 1.187e+05 | NaN |
| 1992 | {'C001'} | 1.7431e+06 | 1.8431 |
| 1992 | {'C002'} | 1.3773e+06 | 3.4764 |
| 1992 | {'C003'} | 1.428e+06 | 4.079 |
| 1992 | {'C004'} | 8.7758e+06 | NaN |
| 1992 | {'C011'} | 18205 | 4.5495 |
| 1992 | {'C012'} | 1.6703e+05 | 5.752 |
| 1992 | {'C013'} | 6.2931e+05 | 7.0257 |
| 1992 | {'C014'} | 3.657e+05 | NaN |
| 1992 | {'C101'} | 4.7927e+06 | 2.052 |
| 1992 | {'C102'} | 4.0642e+06 | 2.9976 |
| | | | |

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| 1992 | {'C103'} | 1.6709e+06 | 4.7971 |
|------|----------------------|------------|---------------|
| 1992 | {'C104'} | 5.5e+05 | NaN |
| 1992 | {'C111'} | 74782 | 4.0857 |
| 1992 | {'C112'} | 3.3189e+05 | 7.9404 |
| 1992 | {'C113'} | 1.4371e+06 | 10.001 |
| 1992 | {'C114'} | 1.3064e+05 | NaN |
| 1994 | {'C001'} | 2.5091e+06 | 1.9678 |
| 1994 | {'C002'} | 1.5404e+06 | 3.5099 |
| 1994 | {'C003'} | 1.5569e+06 | 4.3758 |
| 1994 | {'C004'} | 8.8237e+06 | NaN |
| 1994 | {'C011'} | 10653 | 2.8112 |
| 1994 | {'C012'} | 2.4128e+05 | 6.9136 |
| 1994 | {'C013'} | 7.5302e+05 | 8.6943 |
| 1994 | {'C014'} | 4.1888e+05 | NaN |
| 1994 | {'C101'} | 5.3134e+06 | 2.1107 |
| 1994 | {'C102'} | 4.0308e+06 | 3.1178 |
| 1994 | {'C103'} | 1.6829e+06 | 4.8591 |
| 1994 | {'C104'} | 7.1707e+05 | NaN |
| 1994 | {'C111'} | 1.5239e+05 | 7.0725 |
| 1994 | {'C112'} | 4.3682e+05 | 11.505 |
| 1994 | {'C113'} | 1.557e+06 | 12.719 |
| 1994 | {'C114'} | 1.2058e+05 | NaN |
| 1996 | {'C001'} | 2.8324e+06 | 1.459 |
| 1996 | {'C002'} | 2.1046e+06 | 2.4083 |
| 1996 | {'C003'} | 1.753e+06 | 2.7709 |
| 1996 | {'C004'} | 8.7805e+06 | NaN |
| 1996 | {'C011'} | 57074 | 2.3762 |
| 1996 | {'C012'} | 2.5339e+05 | 4.8631 |
| 1996 | {'C012'} | 9.465e+05 | 5.8817 |
| 1996 | {'C014'} | 5.1589e+05 | 0.0017 NaN |
| 1996 | {'C101'} | 5.4919e+06 | 1.7407 |
| 1996 | {'C101'} | 4.4873e+06 | 2.385 |
| 1996 | {'C102'} | 1.9182e+06 | 3.3137 |
| 1996 | {'C104'} | 6.9559e+05 | 3.3137 NaN |
| 1996 | {'C104'} {'C111'} | 2.0215e+05 | 5.7586 |
| 1996 | {'C111'} | 4.858e+05 | 6.221 |
| | {'C112'} {'C113'} | | |
| 1996 | | 1.6429e+06 | 7.9771 |
| 1996 | {'C114'} {'C001'} | 1.7307e+05 | NaN |
| 1998 | | 3.1189e+06 | 1.3076 |
| 1998 | {'C002'} | 2.0101e+06 | 2.5758 |
| 1998 | {'C003'} | 2.0265e+06 | 2.9886 |
| 1998 | {'C004'} | 8.8847e+06 | NaN |
| 1998 | {'C011'} | 36132 | 3.694 |
| 1998 | {'C012'} | 3.2575e+05 | 5.0667 |
| 1998 | {'C013'} | 9.3514e+05 | 5.6322 |
| 1998 | {'C014'} | 5.4905e+05 | NaN |
| 1998 | {'C101'} | 5.5182e+06 | 1.7357 |
| 1998 | {'C102'} | 4.8667e+06 | 2.4162 |
| 1998 | {'C103'} | 2.1473e+06 | 3.3496 |
| 1998 | {'C104'} | 6.7234e+05 | NaN |
| 1998 | {'C111'} | 1.6247e+05 | 4.0171 |
| 1998 | {'C112'} | 5.3722e+05 | 7.4345 |
| 1998 | {'C113'} | 1.6662e+06 | 8.7309 |
| 1998 | {'C114'} | 1.9321e+05 | NaN |
| 2000 | {'C001'} | 2.7625e+06 | 1.659 |
| 2000 | {'C002'} | 2.7297e+06 | 2.5901 |
| 2000 | {'C003'} | 2.2657e+06 | 3.2971 |
| 2000 | {'C004'} | 9.3772e+06 | NaN |
| | | | |

| 2000 | {'C011'} | 77107 | 2.8732 |
|------|----------|------------|--------|
| 2000 | {'C012'} | 4.0734e+05 | 5.2881 |
| 2000 | {'C013'} | 1.1005e+06 | 6.5806 |
| 2000 | {'C014'} | 7.5089e+05 | NaN |
| | | | |
| 2000 | {'C101'} | 5.6807e+06 | 1.8978 |
| 2000 | {'C102'} | 5.3498e+06 | 2.4629 |
| 2000 | {'C103'} | 2.2554e+06 | 3.968 |
| 2000 | {'C104'} | 6.7471e+05 | NaN |
| 2000 | {'C111'} | 2.1108e+05 | 3.8076 |
| 2000 | {'C112'} | 6.6682e+05 | 7.0165 |
| 2000 | {'C113'} | 2.2414e+06 | 10.509 |
| 2000 | {'C114'} | 1.9925e+05 | NaN |
| | | | |
| 2002 | {'C001'} | 3.6671e+06 | 1.6863 |
| 2002 | {'C002'} | 2.5202e+06 | 2.826 |
| 2002 | {'C003'} | 2.4393e+06 | 3.292 |
| 2002 | {'C004'} | 9.291e+06 | NaN |
| 2002 | {'C011'} | 1.0685e+05 | 3.7516 |
| 2002 | {'C012'} | 4.5408e+05 | 5.83 |
| 2002 | {'C013'} | 1.3436e+06 | 7.9012 |
| 2002 | {'C014'} | 5.9194e+05 | NaN |
| | - | | |
| 2002 | {'C101'} | 5.9945e+06 | 2.0088 |
| 2002 | {'C102'} | 5.2352e+06 | 2.7613 |
| 2002 | {'C103'} | 2.2663e+06 | 4.1455 |
| 2002 | {'C104'} | 6.7629e+05 | NaN |
| 2002 | {'C111'} | 2.4805e+05 | 4.0453 |
| 2002 | {'C112'} | 5.9178e+05 | 7.1763 |
| 2002 | {'C113'} | 2.0465e+06 | 8.9213 |
| 2002 | {'C114'} | 3.2278e+05 | NaN |
| 2002 | {'C001'} | 3.5389e+06 | 1.755 |
| | | | |
| 2004 | {'C002'} | 2.5059e+06 | 2.6069 |
| 2004 | {'C003'} | 2.5599e+06 | 3.1199 |
| 2004 | {'C004'} | 9.5136e+06 | NaN |
| 2004 | {'C011'} | 1.4496e+05 | 3.4155 |
| 2004 | {'C012'} | 4.5696e+05 | 5.4516 |
| 2004 | {'C013'} | 1.8123e+06 | 6.7 |
| 2004 | {'C014'} | 7.7668e+05 | NaN |
| 2004 | {'C101'} | 5.9652e+06 | 2.215 |
| 2004 | {'C102'} | 5.7124e+06 | 2.8839 |
| 2004 | {'C103'} | 2.3318e+06 | 3.8541 |
| | | | |
| 2004 | {'C104'} | 9.677e+05 | NaN |
| 2004 | {'C111'} | 2.8065e+05 | 5.1077 |
| 2004 | {'C112'} | 5.9455e+05 | 6.7843 |
| 2004 | {'C113'} | 2.2218e+06 | 8.6393 |
| 2004 | {'C114'} | 2.6115e+05 | NaN |
| 2005 | {'C001'} | 3.604e+06 | 1.8015 |
| 2005 | {'C002'} | 2.9152e+06 | 2.6792 |
| 2005 | {'C003'} | 2.4463e+06 | 3.3468 |
| 2005 | {'C004'} | 9.2417e+06 | NaN |
| 2005 | {'C011'} | 1.2085e+05 | 2.4982 |
| | | | |
| 2005 | {'C012'} | 5.9567e+05 | 4.9431 |
| 2005 | {'C013'} | 1.6771e+06 | 6.3435 |
| 2005 | {'C014'} | 8.2842e+05 | NaN |
| 2005 | {'C101'} | 5.9621e+06 | 2.2032 |
| 2005 | {'C102'} | 5.4187e+06 | 2.7741 |
| 2005 | {'C103'} | 2.5829e+06 | 3.7258 |
| 2005 | {'C104'} | 9.6341e+05 | NaN |
| 2005 | {'C111'} | 3.5414e+05 | 3.7752 |
| 2005 | {'C111'} | 6.5345e+05 | 6.9592 |
| 2000 | (0112 } | 0.00406705 | 0.3032 |

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| 2005 | {'C113'} | 2.3148e+06 | 8.3387 |
|------|----------|------------|--------|
| 2005 | {'C114'} | 2.8472e+05 | NaN |
| 2008 | {'C001'} | 3.9395e+06 | 1.8657 |
| 2008 | {'C002'} | 2.8968e+06 | 2.6475 |
| 2008 | {'C003'} | 2.361e+06 | 3.1947 |
| 2008 | {'C004'} | 9.2787e+06 | NaN |
| | | | |
| 2008 | {'C011'} | 1.5621e+05 | 3.0013 |
| 2008 | {'C012'} | 6.771e+05 | 5.3544 |
| 2008 | {'C013'} | 1.9227e+06 | 6.8198 |
| 2008 | {'C014'} | 9.0351e+05 | NaN |
| 2008 | {'C101'} | 6.0495e+06 | 2.3736 |
| 2008 | {'C102'} | 5.8662e+06 | 2.9056 |
| 2008 | {'C103'} | 2.4905e+06 | 3.7731 |
| 2008 | {'C104'} | 1.2219e+06 | NaN |
| 2008 | {'C111'} | 2.8368e+05 | 3.9143 |
| 2008 | {'C112'} | 7.9417e+05 | 6.3566 |
| 2008 | {'C112'} | 2.4155e+06 | |
| | | | 8.3053 |
| 2008 | {'C114'} | 2.6468e+05 | NaN |
| 2010 | {'C001'} | 3.9036e+06 | 1.7636 |
| 2010 | {'C002'} | 2.8717e+06 | 2.4062 |
| 2010 | {'C003'} | 2.7349e+06 | 2.8429 |
| 2010 | {'C004'} | 9.9169e+06 | NaN |
| 2010 | {'C011'} | 1.2713e+05 | 3.1825 |
| 2010 | {'C012'} | 6.661e+05 | 4.7299 |
| 2010 | {'C013'} | 2.2114e+06 | 6.1872 |
| 2010 | {'C014'} | 1.2068e+06 | NaN |
| 2010 | {'C101'} | 6.6858e+06 | 2.263 |
| 2010 | {'C101'} | 5.9638e+06 | 2.5991 |
| | | | |
| 2010 | {'C103'} | 2.4368e+06 | 3.6533 |
| 2010 | {'C104'} | 1.4088e+06 | NaN |
| 2010 | {'C111'} | 3.6653e+05 | 3.5758 |
| 2010 | {'C112'} | 7.4601e+05 | 6.2607 |
| 2010 | {'C113'} | 2.7576e+06 | 8.101 |
| 2010 | {'C114'} | 3.7913e+05 | NaN |
| 2012 | {'C001'} | 5.1813e+06 | 1.7308 |
| 2012 | {'C002'} | 3.049e+06 | 2.4089 |
| 2012 | {'C003'} | 3.0537e+06 | 2.7185 |
| 2012 | {'C004'} | 8.7224e+06 | NaN |
| 2012 | {'C011'} | 1.9743e+05 | 3.3489 |
| 2012 | {'C012'} | 7.3753e+05 | 4.1924 |
| 2012 | {'C013'} | 2.3311e+06 | 6.4194 |
| 2012 | | | |
| | {'C014'} | 1.0551e+06 | NaN |
| 2012 | {'C101'} | 7.139e+06 | 2.1453 |
| 2012 | {'C102'} | 6.2508e+06 | 2.5302 |
| 2012 | {'C103'} | 2.5895e+06 | 3.1115 |
| 2012 | {'C104'} | 1.512e+06 | NaN |
| 2012 | {'C111'} | 4.3101e+05 | 3.2287 |
| 2012 | {'C112'} | 9.0347e+05 | 5.0768 |
| 2012 | {'C113'} | 2.7373e+06 | 7.5722 |
| 2012 | {'C114'} | 3.9649e+05 | NaN |
| 2014 | {'C001'} | 4.5694e+06 | 1.7262 |
| 2014 | {'C002'} | 3.2584e+06 | 2.4145 |
| 2014 | {'C002'} | 2.8512e+06 | 2.6173 |
| | | | |
| 2014 | {'C004'} | 9.733e+06 | NaN |
| 2014 | {'C011'} | 2.5971e+05 | 2.9667 |
| 2014 | {'C012'} | 8.2213e+05 | 5.6007 |
| 2014 | {'C013'} | 2.5873e+06 | 6.1866 |
| 2014 | {'C014'} | 1.3462e+06 | NaN |
| | | | |

| 2014 | {'C101'} | 7.0339e+06 | 2.212 |
|------|----------|------------|--------|
| 2014 | {'C102'} | 6.3219e+06 | 2.5069 |
| 2014 | {'C103'} | 2.7689e+06 | 3.1292 |
| 2014 | {'C104'} | 1.5334e+06 | NaN |
| 2014 | {'C111'} | 4.3522e+05 | 3.3786 |
| 2014 | {'C112'} | 8.8807e+05 | 5.4313 |
| 2014 | {'C113'} | 3.0431e+06 | 8.6421 |
| 2014 | {'C114'} | 4.8022e+05 | NaN |

4.1.3 Dataset 1 Aux

disp(mp_data('tb_category2sexskillocc_key'));

| category | sex | skill | occupation | categoryhigher | nesttier |
|----------|------------|---------------|---------------------|----------------|----------|
| | | | | | |
| {'C001'} | {'Female'} | {'unskilled'} | {'Manual' } | {'B001' } | 3 |
| {'C002'} | {'Female'} | {'unskilled'} | {'Routine' } | {'B002' } | 3 |
| {'C003'} | {'Female'} | {'unskilled'} | {'Analytical' } | {'B003' } | 3 |
| {'C004'} | {'Female'} | {'unskilled'} | {'Home Production'} | {0x0 char} | 3 |
| {'C011'} | {'Female'} | {'skilled' } | {'Manual' } | {'B101' } | 3 |
| {'C012'} | {'Female'} | {'skilled' } | {'Routine' } | {'B102' } | 3 |
| {'C013'} | {'Female'} | {'skilled' } | {'Analytical' } | {'B103' } | 3 |
| {'C014'} | {'Female'} | {'skilled' } | {'Home Production'} | {0x0 char} | 3 |
| {'C101'} | {'Male' } | {'unskilled'} | {'Manual' } | {'B001' } | 3 |
| {'C102'} | {'Male' } | {'unskilled'} | {'Routine' } | {'B002' } | 3 |
| {'C103'} | {'Male' } | {'unskilled'} | {'Analytical' } | {'B003' } | 3 |
| {'C104'} | {'Male' } | {'unskilled'} | {'Home Production'} | {0x0 char} | 3 |
| {'C111'} | {'Male' } | {'skilled' } | {'Manual' } | {'B101' } | 3 |
| {'C112'} | {'Male' } | {'skilled' } | {'Routine' } | {'B102' } | 3 |
| {'C113'} | {'Male' } | {'skilled' } | {'Analytical' } | {'B103' } | 3 |
| {'C114'} | {'Male' } | {'skilled' } | {'Home Production'} | {0x0 char} | 3 |
| {'B001'} | {'All' } | {'unskilled'} | {'Manual' } | {'A001' } | 2 |
| {'B002'} | {'All' } | {'unskilled'} | {'Routine' } | {'A002' } | 2 |
| {'B003'} | {'All' } | {'unskilled'} | {'Analytical' } | {'A003'} | 2 |
| {'B101'} | {'All' } | {'skilled' } | {'Manual' } | {'A001' } | 2 |
| {'B102'} | {'All' } | {'skilled' } | {'Routine' } | {'A002' } | 2 |
| {'B103'} | {'All' } | {'skilled' } | {'Analytical' } | {'A003'} | 2 |
| {'A001'} | {'All' } | {'All' } | {'Manual' } | {'AAO1' } | 1 |
| {'A002'} | {'All' } | {'All' } | {'Routine' } | {'AAO1' } | 1 |
| {'AAO1'} | {'All' } | {'All' } | {'ManualRoutine' } | {'AAO2' } | 0 |
| {'8003'} | {'All' } | {'All' } | {'Analytical' } | {'AA02' } | 0 |
| {'AA02'} | {'All' } | {'All' } | {'All' } | {0x0 char} | NaN |

4.1.4 Dataset 2

disp(mp_data('tb_supply_potwrklei'));

| 1989 {'G00'} "Female" "unskilled" 1.2516e+07 0.88971 1992 {'G00'} "Female" "unskilled" 1.3324e+07 0.90306 1994 {'G00'} "Female" "unskilled" 1.443e+07 0.89015 | reChi |
|---|-------|
| 1992 {'G00'} "Female" "unskilled" 1.3324e+07 0.90306 | |
| • | 0. |
| 1004 | 0. |
| 1334 \ GOO \ | 0. |
| 1996 {'G00'} "Female" "unskilled" 1.547e+07 0.88061 | 0. |
| 1998 {'G00'} "Female" "unskilled" 1.604e+07 0.86928 | 0. |
| 2000 {'G00'} "Female" "unskilled" 1.7135e+07 0.85884 | 0. |
| 2002 {'G00'} "Female" "unskilled" 1.7918e+07 0.85017 | 0. |

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0 0. 0.

0. 0. 0. 0. 0. Ο. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. Ο.

0. 0.

| 2004 | {'G00'} | "Female" | "unskilled" | 1.8118e+07 | 0.82951 |
|------|---------|----------|-------------|------------|---------|
| 2005 | {'G00'} | "Female" | "unskilled" | 1.8207e+07 | 0.82472 |
| 2008 | {'G00'} | "Female" | "unskilled" | 1.8476e+07 | 0.82096 |
| 2010 | {'G00'} | "Female" | "unskilled" | 1.9427e+07 | 0.81832 |
| 2012 | {'G00'} | "Female" | "unskilled" | 2.0006e+07 | 0.81686 |
| 2014 | {'G00'} | "Female" | "unskilled" | 2.0412e+07 | 0.82762 |
| 1989 | {'G01'} | "Female" | "skilled" | 8.5421e+05 | 0.87768 |
| 1992 | {'G01'} | "Female" | "skilled" | 1.1802e+06 | 0.82152 |
| 1994 | {'G01'} | "Female" | "skilled" | 1.4238e+06 | 0.81836 |
| 1996 | {'G01'} | "Female" | "skilled" | 1.7729e+06 | 0.8449 |
| 1998 | {'G01'} | "Female" | "skilled" | 1.8461e+06 | 0.82028 |
| 2000 | {'G01'} | "Female" | "skilled" | 2.3358e+06 | 0.83775 |
| 2002 | {'G01'} | "Female" | "skilled" | 2.4965e+06 | 0.81416 |
| 2004 | {'G01'} | "Female" | "skilled" | 3.1909e+06 | 0.81625 |
| 2005 | {'G01'} | "Female" | "skilled" | 3.2221e+06 | 0.79637 |
| 2008 | {'G01'} | "Female" | "skilled" | 3.6595e+06 | 0.77916 |
| 2010 | {'G01'} | "Female" | "skilled" | 4.2115e+06 | 0.76377 |
| 2012 | {'G01'} | "Female" | "skilled" | 4.3212e+06 | 0.77164 |
| 2014 | {'G01'} | "Female" | "skilled" | 5.0153e+06 | 0.78454 |
| 1989 | {'G10'} | "Male" | "unskilled" | 9.9687e+06 | 0.94927 |
| 1992 | {'G10'} | "Male" | "unskilled" | 1.1078e+07 | 0.95081 |
| 1994 | {'G10'} | "Male" | "unskilled" | 1.1744e+07 | 0.93806 |
| 1996 | {'G10'} | "Male" | "unskilled" | 1.2593e+07 | 0.94471 |
| 1998 | {'G10'} | "Male" | "unskilled" | 1.3205e+07 | 0.94507 |
| 2000 | {'G10'} | "Male" | "unskilled" | 1.3961e+07 | 0.93873 |
| 2002 | {'G10'} | "Male" | "unskilled" | 1.4172e+07 | 0.9392 |
| 2004 | {'G10'} | "Male" | "unskilled" | 1.4977e+07 | 0.93382 |
| 2005 | {'G10'} | "Male" | "unskilled" | 1.4927e+07 | 0.93314 |
| 2008 | {'G10'} | "Male" | "unskilled" | 1.5628e+07 | 0.91783 |
| 2010 | {'G10'} | "Male" | "unskilled" | 1.6495e+07 | 0.92582 |
| 2012 | {'G10'} | "Male" | "unskilled" | 1.7491e+07 | 0.91384 |
| 2014 | {'G10'} | "Male" | "unskilled" | 1.7658e+07 | 0.91783 |
| 1989 | {'G11'} | "Male" | "skilled" | 1.8792e+06 | 0.9391 |
| 1992 | {'G11'} | "Male" | "skilled" | 1.9744e+06 | 0.94708 |
| 1994 | {'G11'} | "Male" | "skilled" | 2.2668e+06 | 0.92429 |
| 1996 | {'G11'} | "Male" | "skilled" | 2.5039e+06 | 0.92112 |
| 1998 | {'G11'} | "Male" | "skilled" | 2.5591e+06 | 0.90398 |
| 2000 | {'G11'} | "Male" | "skilled" | 3.3185e+06 | 0.90086 |
| 2002 | {'G11'} | "Male" | "skilled" | 3.2091e+06 | 0.90837 |
| 2004 | {'G11'} | "Male" | "skilled" | 3.3582e+06 | 0.89767 |
| 2005 | {'G11'} | "Male" | "skilled" | 3.6072e+06 | 0.89235 |
| 2008 | {'G11'} | "Male" | "skilled" | 3.758e+06 | 0.86831 |
| 2010 | {'G11'} | "Male" | "skilled" | 4.2492e+06 | 0.87325 |
| 2012 | {'G11'} | "Male" | "skilled" | 4.4683e+06 | 0.83196 |
| 2014 | {'G11'} | "Male" | "skilled" | 4.8466e+06 | 0.86615 |

4.1.5 Dataset 2 Aux

disp(mp_data('tb_group2category_key'));

| group | groupName | category | sex | skill |
|---------|----------------------|----------|------------|---------------|
| | | | | |
| {'G00'} | {'female-unskilled'} | {'C001'} | {'female'} | {'unskilled'} |
| {'G00'} | {'female-unskilled'} | {'C002'} | {'female'} | {'unskilled'} |
| {'G00'} | {'female-unskilled'} | {'C003'} | {'female'} | {'unskilled'} |
| {'G00'} | {'female-unskilled'} | {'C004'} | {'female'} | {'unskilled'} |
| {'CO1'} | {'female-skilled' } | {'C011'} | {'female'} | {'skilled' } |

| {'G01'} | {'female-skilled' | } | {'C012'} | {'female'} | {'skilled' } |
|---------|-------------------|---|----------|------------|---------------|
| {'G01'} | {'female-skilled' | } | {'C013'} | {'female'} | {'skilled' } |
| {'G01'} | {'female-skilled' | } | {'C014'} | {'female'} | {'skilled' } |
| {'G10'} | {'male-unskilled' | } | {'C101'} | {'male' } | {'unskilled'} |
| {'G10'} | {'male-unskilled' | } | {'C102'} | {'male' } | {'unskilled'} |
| {'G10'} | {'male-unskilled' | } | {'C103'} | {'male' } | {'unskilled'} |
| {'G10'} | {'male-unskilled' | } | {'C104'} | {'male' } | {'unskilled'} |
| {'G11'} | {'male-skilled' | } | {'C111'} | {'male' } | {'skilled' } |
| {'G11'} | {'male-skilled' | } | {'C112'} | {'male' } | {'skilled' } |
| {'G11'} | {'male-skilled' | } | {'C113'} | {'male' } | {'skilled' } |
| {'G11'} | {'male-skilled' | } | {'C114'} | {'male' } | {'skilled' } |

30 CHAPTER 4. DATA

Demand

5.1 Solve Nested CES Optimal Demand (CRS)

Testing the bfw_crs_nested_ces function from the PrjLabEquiBFW Package. This function solves optimal choices given CES production function under cost minimization. Works with Constant Elasticity of Substitution problems with constant returns, up to four nest layers, and two inputs in each sub-nest. Takes as inputs share and elasticity parameters across layers of sub-nests, as well as input unit costs at the bottom-most layer. Works with Constant Elasticity of Substitution problems with constant returns, up to four nest layers, and two inputs in each sub-nest. Allows for uneven branches, so that some branches go up to four layers, but others have less layers, works with BFW (2022) nested labor input problem.

5.1.1 Key Inputs and Outputs for bfw_mp_func_demand

Here are the key inputs for the CES demand solver function:

- \mathbf{FL} _ \mathbf{YZ} float output divided by productivity, aggregate single term
- CL_MN_PRHO cell array of rho (elasticity) parameter between negative infinity and 1. For example, suppose there are four nest layers, and there are two branches at each layer, then we have 1, 2, 4, and 8 ρ parameter values at the 1st, 2nd, 3rd, and 4th nest layers: size(CL_MN_PRHO{1})= [1,1], size(CL_MN_PRHO{2}) = [1,2], size(CL_MN_PRHO{3}) = [2,2], size(CL_MN_PRHO{4}) = [2,2,2]. Note that if the model has 4 nest layers, not all cells need to be specified, some branches could be deeper than others.
- CL_MN_PSHARE cell array of share (between 0 and 1) for the first input of the two inputs for each nest. The structure for this is similar to CL_MN_PRHO.
- CL_MN_PRICE cell array of wages for both wages for the first and second nest, the last index in each element of the cell array indicates first (1) or second (2) wage. For example, suppose we have four layers, with 2 branches at each layer, as in the example for CL_MN_PRHO, then we have 2, 4, 8, and 16 wage values at the 1st, 2nd, 3rd, and 4th nest layers: size(CL_MN_PRICE{1}) = [1,2], size(CL_MN_PRICE{2}) = [2,2], size(CL_MN_PRICE{3}) = [2,2,2], size(CL_MN_PRICE{4}) = [2,2,2,2]. Note that only the last layer of wage needs to be specified, in this case, the 16 wages at the 4th layer. Given optimal solutions, we solve for the 2, 4, and 8 aggregate wages at the higher nest layers. If some branches are deeper than other branches, then can specific NA for non-reached layers along some branches.
- BL_BFW_MODEL boolean true by default if true then will output outcomes specific to the BFW 2022 problem.

Here are the key outputs for the CES demand solver function:

• CL_MN_YZ_CHOICES has the same dimension as CL_MN_PRICE, suppose there are four layers, the CL_MN_PRICE{4} results at the lowest layer includes quantity choices that might be

std

coefvari

0.4714

0.51918

observed in the data. CL_MN_PRICE cell values at non-bottom layers include aggregate quantity outcomes.

• CL_MN_PRICE includes at the lowest layer observed wages, however, also includes higher layer aggregate solved waves. CL_MN_PRHO and CL_MN_PSHARE are identical to inputs.

Single Nest Layer Two Inputs CES Problem (Demand) 5.1.2

In this first example, we solve a constant returns to scale problem with a single nest, meaning just two inputs and a single output.

```
clc;
close all;
clear all;
% Output requirement
fl_yz = 1;
% rho = 0.5, 1/(1-0.5)=2, elasticity of substitution of 2
cl_mn_prho = {[0.1]};
% equal share, similar "productivity"
cl_mn_pshare = {[0.5]};
% wages for the two inputs, identical wage
cl_mn_price = \{[1.5, 0.75]\};
% print option
bl_verbose = true;
mp_func = bfw_mp_func_demand();
bl_bfw_model = false;
[cl_mn_yz_choices, cl_mn_price] = ...
   bfw_crs_nested_ces(fl_yz, cl_mn_prho, cl_mn_pshare, cl_mn_price, ...
   mp_func, bl_verbose, bl_bfw_model);
CONTAINER NAME: mp_container_map ND Array (Matrix etc)
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
              i
                   idx
                         ndim
                                 numel
                                         rowN
                                                 colN
                                                         SIIM
                                                                  mean
                                                 ----
                                                                  _____
                                                                           -----
   price_c1
              1
                    2
                          2
                                   2
                                          1
                                                  2
                                                          2.25
                                                                  1.125
                                                                           0.53033
   yz_c1
              2
                    4
                          2
                                   2
                                          1
                                                  2
                                                        2.1343
                                                                  1.0671
                                                                           0.55403
xxx TABLE:price_c1 xxxxxxxxxxxxxxxxxx
         c1
                c2
               0.75
   r1
         1.5
xxx TABLE:yz_c1 xxxxxxxxxxxxxxxxxx
           с1
                     c2
         0.67537
                   1.4589
   r1
_____
```

CONTAINER NAME: mp_container_map Scalars xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx i

idx

value

```
prho_c1 1 1 0.1
pshare_c1 2 3 0.5
```

5.1.3 Single Nest Layer Two Inputs CES Problem, Vary Share and Elasticity (Demand)

In this second example, we test over different rho values, explore optimal relative choices, as share and elasticity change. In this exercise, we also check, at every combination of rho and share parameter, whether the FOC condition is satisfied by the optimal choices. Also check if at the optimal choices, the minimization output requirement is met.

```
% Approximately close function
rel_tol=1e-09;
abs_tol=0.0;
if_{is_{close}} = @(a,b) (abs(a-b) \le max(rel_tol * max(abs(a), abs(b)), abs_tol));
% Define share and rho arrays
fl_yz = 1;
ar_pshare = linspace(0.1, 0.9, 9);
ar_prho = 1 - 10.^(linspace(-2, 2, 30));
% Loop over share and rho values
mt_rela_opti = NaN([length(ar_pshare), length(ar_prho)]);
mt_x1_opti = NaN([length(ar_pshare), length(ar_prho)]);
for it_pshare_ctr = 1:length(ar_pshare)
    for it_prho_ctr = 1:length(ar_prho)
        % A. Parameters
        % rho
        fl_prho = ar_prho(it_prho_ctr);
        cl_mn_prho = {[fl_prho]};
        % share
        fl_pshare = ar_pshare(it_pshare_ctr);
        cl_mn_pshare = {[fl_pshare]};
        % wages for the two inputs, identical wage
        cl_mn_price = {[1, 1]};
        % print option
        bl_verbose = false;
        % B. Call function
        [cl_mn_yz_choices, cl_mn_price, cl_mn_prho, cl_mn_pshare] = ...
            bfw_crs_nested_ces(fl_yz, cl_mn_prho, cl_mn_pshare, cl_mn_price, ...
            mp_func, bl_verbose, bl_bfw_model);
        % Store results for optimal choice
        fl_opti_x1 = cl_mn_yz_choices{1}(1);
        fl_opti_x2 = cl_mn_yz_choices{1}(2);
        mt_x1_opti(it_pshare_ctr, it_prho_ctr) = fl_opti_x1;
        % C. Check if relative optimality FOC condition is met
        fl_rela_opti = fl_opti_x1/fl_opti_x2;
        % From FOC give wages = 1 both
        % Using What is above Equation A.20 in draft.
        fl_rela_opti_foc = (((fl_pshare/(1-fl_pshare)))*(1))^(1/(1-ar_prho(it_prho_ctr)));
        if (~if_is_close(fl_rela_opti_foc, fl_rela_opti))
            error('There is an error, optimal relative not equal to expected foc ratio')
        end
        % D. Check if output quantity requirement is met
        fl_output = ((fl_pshare)*fl_opti_x1^(fl_prho) + (1-fl_pshare)*fl_opti_x2^(fl_prho))^(1/fl_pr
```

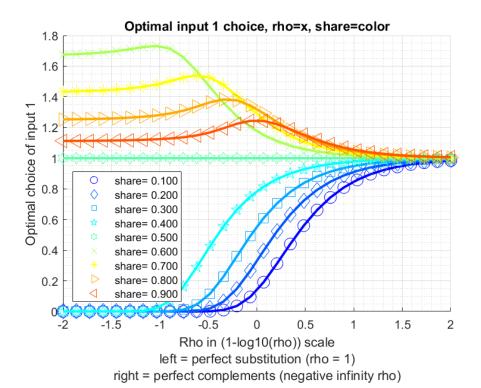
```
if (~if_is_close(fl_output, fl_yz))
    error('There is an error, output is not equal to required expenditure minimizing output'
end
```

end end

Key results: (1) As share parameter of input 1 goes to zero, optimal choice goes to zero when inputs are elastic; (2) When inputs are inelasticty, even very low share input 1 asymptote to equal input 2; (3) When input 1 is more productive (higher share), actually hire less as productivity (share) increases, becasue less of it is needed to achieve production for high rho, elastictic production function; (4) For

inelastic production, monotonic relationship between input and shares.

```
% Visualize
% Generate some Data
rng(456);
ar_row_grid = ar_pshare;
ar_col_grid = log(1-ar_prho)/log(10);
rng(123);
mt_value = mt_x1_opti;
% container map settings
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_graph_title') = {'Optimal input 1 choice, rho=x, share=color'};
mp_support_graph('cl_st_ytitle') = {'Optimal choice of input 1'};
mp_support_graph('cl_st_xtitle') = {'Rho in (1-log10(rho)) scale', ...
    'left = perfect substitution (rho = 1)', ...
    'right = perfect complements (negative infinity rho)'};
mp_support_graph('st_legend_loc') = 'southwest';
mp_support_graph('bl_graph_logy') = false; % do not log
mp_support_graph('st_rowvar_name') = 'share=';
mp_support_graph('it_legend_select') = 5; % how many shock legends to show
mp_support_graph('st_rounding') = '6.3f'; % format shock legend
mp_support_graph('cl_colors') = 'jet'; % any predefined matlab colormap
% Call function
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```



mean

-0.325

3.8894

2.2626

18

4.5

0.59

2.2431 0.68863

std

0.95459

2.0959

0.41012

2.7086

3.873

coefvar

-2.9372

0.53886

0.86066

0.69512

0.307

1.1971

5.1.4 Doubly Nest Layer Two Inputs Each Sub-nest CES Problem (Demand)

In this third example, solve for optimal choices for a doubly nested problem. Below, we first solve for the optimal choices, then we do a number of checks, to make sure that the solutions are correct, as expected.

```
% output requirement
fl_yz = 2.1;
\% upper nest 0.1, lower nests 0.35 and -1 separately for rho values
cl_mn_prho = \{[0.1], [0.35, -1]\};
\% unequal shares of share values
cl_mn_pshare = \{[0.4], [0.3, 0.88]\};
% differential wages
% in lower-left nest, not productive and very expensive, not very elastic
% last index for left or right,
cl_mn_price = {[nan, nan], [10, 1;3, 4]};
% print option
bl_verbose = true;
[cl_mn_yz_choices, cl_mn_price, cl_mn_prho, cl_mn_pshare] = ...
   bfw_crs_nested_ces(fl_yz, cl_mn_prho, cl_mn_pshare, cl_mn_price, ...
   mp_func, bl_verbose, bl_bfw_model);
_____
CONTAINER NAME: mp_container_map ND Array (Matrix etc)
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
              i
                 idx ndim numel
                                        rowN
                                               colN
                                                       sum
                         ----
                   ---
                                ----
                                        ----
              1 2
2 3
   prho_c2
                                         1
                                                2
                                                       -0.65
                         2
                                 2
                                                2
   price_c1
                                         1
                                                      7.7788
              3
4
                         2
                                 4
                                        2
                                                2
   price_c2
                   4
                                 2 2
                   6
                                        1
1
                                              2
                        2
                                                        1.18
   pshare_c2
              5
                    7
                         2
                                              2
   yz_c1
                                                      4.4862
                          2
              6
                                        2
                                              2
                                                      9.0506
   yz_c2
xxx TABLE:prho_c2 xxxxxxxxxxxxxxxxx
         с1
               c2
   r1
        0.35
               -1
xxx TABLE:price_c1 xxxxxxxxxxxxxxxxxx
          c1
                  c2
   r1
        2.4074
                 5.3714
xxx TABLE:price_c2 xxxxxxxxxxxxxxxxx
        c1
            c2
```

10

3

c1

0.3

1

4

c2

0.88

r1

r2

r1

```
xxx TABLE:yz_c1 xxxxxxxxxxxxxxxxxx
         c1 c2
   r1
         2.73 1.7561
xxx TABLE:yz_c2 xxxxxxxxxxxxxxxxx
           c1 c2
                    -----
      0.047893 6.0934
   r1
          2.2044 0.70496
   r2
_____
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
CONTAINER NAME: mp_container_map Scalars
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
               i idx value
               - ---
                          ----
            1 1
                         0.1
   prho_c1
               2
   pshare_c1
                    5
                           0.4
\% there are four optimal choices, they are
fl_opti_x11 = cl_mn_yz_choices{2}(1,1);
fl_opti_x12 = cl_mn_yz_choices{2}(1,2);
fl_opti_x21 = cl_mn_yz_choices{2}(2,1);
fl_opti_x22 = cl_mn_yz_choices{2}(2,2);
% display
st_print = strjoin(...
   ["completed double nest test:", ...
   ['nest 1 input 1, fl_opti_x11=' num2str(fl_opti_x11)], ...
   ['nest 1 input 2, fl_opti_x12=' num2str(fl_opti_x12)], ...
   ['nest 2 input 1, fl_opti_x21=' num2str(fl_opti_x21)], ...
   ['nest 2 input 2, fl_opti_x22=' num2str(fl_opti_x22)], ...
   ], ";");
st_out = st_print;
ar_ch_out = char(strsplit(st_print,";")');
disp(ar_ch_out);
completed double nest test:
nest 1 input 1, fl_opti_x11=0.047893
nest 1 input 2, fl_opti_x12=6.0934
nest 2 input 1, fl_opti_x21=2.2044
nest 2 input 2, fl_opti_x22=0.70496
```

5.1.5 Doubly Nest Layer Two Inputs Each Sub-nest CES Problem-Solution Check (Demand)

Checking output equality, if there are problems, would output an error.

```
% A. Check output Equality
fl_pshare_0 = cl_mn_pshare{1}(1);
fl_pshare_1 = cl_mn_pshare{2}(1);
fl_pshare_2 = cl_mn_pshare{2}(2);
fl_prho_0 = cl_mn_prho{1}(1);
fl_prho_1 = cl_mn_prho{2}(1);
fl_prho_2 = cl_mn_prho{2}(2);
```

```
fl_output_0 = ((fl_pshare_0)*fl_output_1^(fl_prho_0) + (1-fl_pshare_0)*fl_output_2^(fl_prho_0))^(1/f
if (~if_is_close(fl_output_0, fl_yz))
   error('There is an error, output is not equal to required expenditure minimizing output')
end
Checking FOC within-nest optimality, if there are problems, would output an error.
% B. Check FOC Optimality inner nest
fl_wage_x11 = cl_mn_price{2}(1,1);
fl_wage_x12 = cl_mn_price{2}(1,2);
fl_wage_x21 = cl_mn_price{2}(2,1);
fl_wage_x22 = cl_mn_price{2}(2,2);
% B1. Checking via Method 1
fl_rela_opti_foc_1 = (((fl_pshare_1/(1-fl_pshare_1)))*(fl_wage_x12/fl_wage_x11))^(1/(1-fl_prho_1));
fl_rela_opti_foc_2 = (((fl_pshare_2/(1-fl_pshare_2)))*(fl_wage_x22/fl_wage_x21))^(1/(1-fl_prho_2));
if (~if_is_close(fl_rela_opti_foc_1, fl_opti_x11/fl_opti_x12))
   error('B1. There is an error, optimal relative not equal to expected foc ratio, nest 1')
if (~if_is_close(fl_rela_opti_foc_2, fl_opti_x21/fl_opti_x22))
   error('B1. There is an error, optimal relative not equal to expected foc ratio, nest 2')
end
% B2. Equation left to right, right to left, checking via method 2
% Check FOC Optimality cross nests (actually within) T1
fl_dy_dx11 = fl_pshare_1*(fl_opti_x11^(fl_prho_1-1));
fl_dy_dx12 = (1-fl_pshare_1)*(fl_opti_x12^(fl_prho_1-1));
fl_rwage_x11dx12 = fl_dy_dx11/fl_dy_dx12;
if (~if_is_close(fl_rwage_x11dx12, fl_wage_x11/fl_wage_x12))
   error('B2. There is an error, relative price x11 and x12 does not satisfy within optimality acro
end
Generate aggregate prices, if there are problems, would output an error.
\% C. Aggregate prices and optimality within higher tier
% Is optimality satisfied given aggregate prices?
fl_rela_wage_share_11 = ...
   ((fl_wage_x11/fl_wage_x12)*((1-fl_pshare_1)/(fl_pshare_1)))^(fl_prho_1/(1-fl_prho_1));
fl_rela_wage_share_12 = ...
   ((fl_wage_x12/fl_wage_x11)*((fl_pshare_1)/(1-fl_pshare_1)))^(fl_prho_1/(1-fl_prho_1));
fl_agg_prc_1 = ...
   fl_wage_x11*(fl_pshare_1 + (1-fl_pshare_1)*(fl_rela_wage_share_11))^(-1/fl_prho_1) + ...
   fl_rela_wage_share_21 = ...
   ((fl_wage_x21/fl_wage_x22)*((1-fl_pshare_2)/(fl_pshare_2)))^(fl_prho_2/(1-fl_prho_2));
fl_rela_wage_share_22 = ...
   ((fl_wage_x22/fl_wage_x21)*((fl_pshare_2)/(1-fl_pshare_2)))^(fl_prho_2/(1-fl_prho_2));
fl_agg_prc_2 = ...
   fl_wage_x22*(fl_pshare_2*(fl_rela_wage_share_22) + (1-fl_pshare_2))^(-1/fl_prho_2);
% What is returned by the omega function that is suppose to have aggregate prices?
mp_func = bfw_mp_func_demand();
params_group = values(mp_func, {'fc_OMEGA', 'fc_d1', 'fc_d2'});
[fc_OMEGA, fc_d1, fc_d2] = params_group{:};
% Aggregate price
```

end

```
fl_aggregate_price_1 = fc_OMEGA(...
    fl_wage_x11, fl_wage_x12, ...
    fl_prho_1, ...
   fl_pshare_1, 1 - fl_pshare_1);
fl_aggregate_price_2 = fc_OMEGA(...
   fl_wage_x21, fl_wage_x22, ...
    fl_prho_2, ...
    fl_pshare_2, 1 - fl_pshare_2);
```

Check relative price within nest and across nests, if there are problems, would output an error.

```
% D. Check FOC Optimality cross nests
\% D1a. Two within-nest relative wages and four cross-nest relative wages
fl_rwage_x11dx12 = fl_wage_x11/fl_wage_x12;
fl_rwage_x21dx22 = fl_wage_x21/fl_wage_x22;
% across
fl_rwage_x11dx21 = fl_wage_x11/fl_wage_x21;
fl_rwage_x11dx22 = fl_wage_x11/fl_wage_x22;
fl_rwage_x12dx21 = fl_wage_x12/fl_wage_x21;
fl_rwage_x12dx22 = fl_wage_x12/fl_wage_x22;
% D1b. Generate relative wages within nest and across nests own equations
fl_dy_dx1_shared = (fl_pshare_0*(fl_output_1)^(fl_prho_0-1))*((fl_output_1)^(1-fl_prho_1));
fl_dy_dx11 = fl_dy_dx1_shared*(fl_pshare_1*fl_opti_x11^(fl_prho_1-1));
fl_dy_dx12 = fl_dy_dx1_shared*((1-fl_pshare_1)*fl_opti_x12^(fl_prho_1-1));
fl_dy_dx2_shared = ((1-fl_pshare_0)*(fl_output_2)^(fl_prho_0-1))*((fl_output_2)^(1-fl_prho_2));
fl_dy_dx21 = fl_dy_dx2_shared*(fl_pshare_2*fl_opti_x21^(fl_prho_2-1));
fl_dy_dx22 = fl_dy_dx2_shared*((1-fl_pshare_2)*fl_opti_x22^(fl_prho_2-1));
% within
fl_rwage_x11dx12_foc = fl_dy_dx11/fl_dy_dx12;
fl_rwage_x21dx22_foc = fl_dy_dx21/fl_dy_dx22;
% across
fl_rwage_x11dx21_foc = fl_dy_dx11/fl_dy_dx21;
fl_rwage_x11dx22_foc = fl_dy_dx11/fl_dy_dx22;
fl_rwage_x12dx21_foc = fl_dy_dx12/fl_dy_dx21;
fl_rwage_x12dx22_foc = fl_dy_dx12/fl_dy_dx22;
if (~if_is_close(fl_rwage_x11dx21_foc, fl_wage_x11/fl_wage_x21))
    error('There is an error, relative price x11 and x21 does not satisfy cross optimality across ne
end
if (~if_is_close(fl_rwage_x12dx22_foc, fl_wage_x12/fl_wage_x22))
    error('There is an error, relative price x12 and x22 does not satisfy cross optimality across ne
end
% D2. Check FOC Optimality cross nests, simplified equation
fl_rela_wage_x11_x21 = log((fl_pshare_0/(1-fl_pshare_0))* ...
    ((fl_pshare_1*fl_opti_x11^(fl_prho_1-1)*fl_output_2^(fl_prho_2))/(fl_pshare_2*fl_opti_x21^(fl_prho_2))
    fl_prho_0*log(fl_output_1/fl_output_2);
if (~if_is_close(fl_rela_wage_x11_x21, log(fl_wage_x11/fl_wage_x21)))
```

error('There is an error, relative price x11 and x21 does not satisfy cross optimality across ne

5.1.6 BFW (2022) Nested Three Branch (Four Layer) Problem (Demand)

The model BFW 2022 has three branches and four layers. one of the branches go down only three layers, the other two branches go down four layers.

First, we prepare the various inputs: % Controls bl_verbose = true; bl_bfw_model = true; % Given rho and beta, solve for equilibrium quantities bl_log_wage = false; mp_func = bfw_mp_func_demand(bl_log_wage); % Following instructions in: PrjFLFPMexicoBFW\solvedemand\README.md % Nests/layers $it_nests = 4;$ % Input cell of mn matrixes it_prho_cl = 1; it_pshare_cl = 2; it_price_cl = 3; for it_cl_ctr = [1,2,3]cl_mn_cur = cell(it_nests,1); % Fill each cell element with NaN mn array for it_cl_mn = 1:it_nests bl_price = (it_cl_ctr == it_price_cl); if (~bl_price && it_cl_mn == 1) mn_nan = NaN; elseif (~bl_price && it_cl_mn == 2) || (bl_price && it_cl_mn == 1) mn_nan = [NaN, NaN]; elseif (~bl_price && it_cl_mn == 3) || (bl_price && it_cl_mn == 2) $mn_nan = NaN(2,2);$ elseif (~bl_price && it_cl_mn == 4) || (bl_price && it_cl_mn == 3) $mn_nan = NaN(2,2,2);$ elseif (~bl_price && it_cl_mn == 5) || (bl_price && it_cl_mn == 4) $mn_nan = NaN(2,2,2,2);$ elseif (~bl_price && it_cl_mn == 6) || (bl_price && it_cl_mn == 5) $mn_nan = NaN(2,2,2,2,2);$ cl_mn_cur{it_cl_mn} = mn_nan; end % Name cell arrays if (it_cl_ctr == it_prho_cl) cl_mn_prho = cl_mn_cur; elseif (it_cl_ctr == it_pshare_cl) cl_mn_pshare = cl_mn_cur; elseif (it_cl_ctr == it_price_cl) cl_mn_price = cl_mn_cur; end

% Initialize share matrix

end

```
rng(123);
for it_cl_mn = 1:it_nests
    mn_pshare = cl_mn_pshare{it_cl_mn};
    if it_cl_mn == 4
        mn_pshare(2,:,:) = rand(2,2);
    else
        mn_pshare = rand(size(mn_pshare));
    cl_mn_pshare{it_cl_mn} = mn_pshare;
end
% Initialize rho matrix
rng(456);
for it_cl_mn = 1:it_nests
    mn_prho = cl_mn_prho{it_cl_mn};
    if it_cl_mn == 4
        mn_prho(2,:,:) = rand(2,2);
    else
        mn_prho = rand(size(mn_prho));
    end
    \% Scalling rho between 0.7500 and -3.0000
    % 1 - 2.^{(linspace(-2,2,5))}
    mn_prho = 1 - 2.^(mn_prho*(4) - 2);
    cl_mn_prho{it_cl_mn} = mn_prho;
end
% Initialize wage matrix
rng(789);
for it_cl_mn = 1:it_nests
    mn_price = cl_mn_price{it_cl_mn};
    if it_cl_mn == 3
        mn_price(1,:,:) = rand(2,2);
    elseif it_cl_mn == 4
        mn_price(2,:,:,:) = rand(2,2,2);
    % Scalling rho between 3 amd 5
    mn_price = mn_price*(2) + 3;
    cl_mn_price{it_cl_mn} = mn_price;
% Initialize yz matrix
rng(101112);
fl_yz = rand();
Second, display created inputs:
disp(['fl_yz=' num2str(fl_yz)]);
fl_yz=0.89726
celldisp(cl_mn_prho);
cl_mn_prho{1} =
    0.5017
```

```
{\tt cl\_mn\_prho\{2\}} \; = \;
    0.6071 -1.1955
cl_mn_prho{3} =
   -1.3523 -0.3346
   -0.4167 -1.9136
cl_mn_prho{4} =
(:,:,1) =
       {\tt NaN}
                 NaN
   -1.0512
           0.5869
(:,:,2) =
       NaN
                 NaN
    0.6209
              0.1633
celldisp(cl_mn_pshare);
cl_mn_pshare{1} =
    0.6965
cl_mn_pshare{2} =
    0.2861
            0.2269
cl_mn_pshare{3} =
    0.5513
            0.4231
    0.7195
              0.9808
```

cl_mn_pshare{4} =

 ${\tt NaN}$

0.6848

 ${\tt NaN}$

0.4809

(:,:,1) =

(:,:,2) =

NaN NaN 0.3921 0.3432

celldisp(cl_mn_price);

 ${\tt cl_mn_price\{1\}} \; = \;$

NaN NaN

 $cl_mn_price{2} =$

NaN NaN NaN NaN

 $cl_mn_price{3} =$

(:,:,1) =

3.6467 3.4605 NaN NaN

(:,:,2) =

4.5876 4.2488 NaN NaN

 $cl_mn_price{4} =$

(:,:,1,1) =

NaN NaN 4.9508 4.5178

(:,:,2,1) =

NaN NaN 3.0212 3.0495

(:,:,1,2) =

0.

NaN NaN 3.2221 4.0763

(:,:,2,2) =

NaN NaN 3.0909 4.1031

Third, call function and solve for optimal demand:

% Call function

[cl_mn_yz_choices, cl_mn_price, cl_mn_prho, cl_mn_pshare] = ...
 bfw_crs_nested_ces(fl_yz, cl_mn_prho, cl_mn_pshare, cl_mn_price, ...
 mp_func, bl_verbose, bl_bfw_model);

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean |
|----------------------|----|-----|------|-------|------|------|----------|----------|
| | | | | | | | | |
| mt_fl_labor_demanded | 1 | 1 | 2 | 12 | 4 | 3 | 5.4455 | 0.45379 |
| prho_c2 | 2 | 3 | 2 | 2 | 1 | 2 | -0.58844 | -0.29422 |
| prho_c3 | 3 | 4 | 2 | 4 | 2 | 2 | -4.0173 | -1.0043 |
| prho_c4 | 4 | 5 | 3 | 8 | 2 | 4 | NaN | NaN |
| price_c1 | 5 | 6 | 2 | 2 | 1 | 2 | 35.345 | 17.673 |
| price_c2 | 6 | 7 | 2 | 4 | 2 | 2 | 40.906 | 10.226 |
| price_c3 | 7 | 8 | 3 | 8 | 2 | 4 | 45.403 | 5.6754 |
| price_c4 | 8 | 9 | 4 | 16 | 2 | 8 | NaN | NaN |
| pshare_c2 | 9 | 11 | 2 | 2 | 1 | 2 | 0.51299 | 0.2565 |
| pshare_c3 | 10 | 12 | 2 | 4 | 2 | 2 | 2.6747 | 0.66866 |
| pshare_c4 | 11 | 13 | 3 | 8 | 2 | 4 | NaN | NaN |
| yz_c1 | 12 | 14 | 2 | 2 | 1 | 2 | 1.6003 | 0.80016 |
| yz_c2 | 13 | 15 | 2 | 4 | 2 | 2 | 2.645 | 0.66124 |
| yz_c3 | 14 | 16 | 3 | 8 | 2 | 4 | 5.1962 | 0.64953 |
| yz_c4 | 15 | 17 | 4 | 16 | 2 | 8 | NaN | NaN |

| | C1 | c2 | СЗ | |
|----|----------|----------|---------|--|
| | | | | |
| r1 | 0.020122 | 0.024929 | 2.1857 | |
| r2 | 0.060227 | 0.037985 | 2.3642 | |
| r3 | 0.069088 | 0.093774 | 0.21107 | |
| r4 | 0.058349 | 0.14469 | 0.17539 | |

xxx TABLE:prho_c2 xxxxxxxxxxxxxxxxx

c1 c2

r1 0.60709 -1.1955

xxx TABLE:prho_c3 xxxxxxxxxxxxxxxx

c1 c2 -----r1 -1.3523 -0.33464

| | r2 | -0.41668 | -1.913 | 6 | | | | | |
|-----|-----------|--------------------------|--------------------------|--------------------------|---------|---------------|---------------|---------------|---------------|
| xxx | TABLE | | xxxxxxxxx | | | | | | |
| | | c1 | c2 | c3 | c4 | | | | |
| | | | | | | - | | | |
| | r1 r2 | NaN -1 0512 | NaN 0.58694 | NaN 0.62089 | | | | | |
| | 12 | -1.0512 | 0.56094 | 0.62089 | 0.1033 | ± | | | |
| xxx | TABLE | | xxxxxxxx | xxxxxxx | | | | | |
| | | c1 | c2 | | | | | | |
| | | | | | | | | | |
| | r1 | 12.695 | 22.65 | | | | | | |
| xxx | TABI.F. | :price c2 | xxxxxxxx | xxxxxxx | | | | | |
| | | c1 | | | | | | | |
| | | | | | | | | | |
| | r1 | 8.1518 | 7.7015 | | | | | | |
| | | 13.522 | | | | | | | |
| | T 1 D 1 D | | | | | | | | |
| XXX | IABLE | | xxxxxxxxx c2 | | c4 | | | | |
| | | | | | | | | | |
| | 4 | 2 6467 | 2 4605 | 4 5076 | 4 0400 | | | | |
| | | | 3.4605 8.5114 | | 7.0309 | | | | |
| | | | | | | | | | |
| XXX | TABLE | | xxxxxxxxx c2 | c3 | c4 | c 5 | c6 | с7 | c8 |
| | | C1 | | | | | | | |
| | | | | | | | | | |
| | r1 r2 | NaN 4 9508 | NaN 4.5178 | NaN 3 0212 | | NaN 3 2221 | NaN 4 0763 | NaN 3.0909 | NaN 4.1031 |
| | 12 | 1.0000 | 1.0170 | 0.0212 | 0.0100 | 0.2221 | 1.0700 | 0.0000 | 1.1001 |
| xxx | TABLE | | xxxxxxxx | xxxxxxxx | | | | | |
| | | c1 | c2 | | | | | | |
| | | | | | | | | | |
| | r1 | 0.28614 | 0.22685 | | | | | | |
| xxx | TABLE | :pshare c3 | xxxxxxxx | xxxxxxxx | | | | | |
| | | c1 | c2 | | | | | | |
| | | | | | | | | | |
| | r1 | 0.55131 | 0.42311 | | | | | | |
| | r2 | 0.71947 | 0.98076 | | | | | | |
| vvv | TARIF | ·nghare c4 | · xxxxxxxx | **** | | | | | |
| VVV | | · honare_ca | | | 2.1 | | | | |
| | 111222 | c1 | c2 | c3 | c4 | | | | |
| | 111000 | c1 | c2 | c3 | | _ | | | |
| | | | | | | - - | | | |
| | r1 r2 | c1 NaN 0.68483 | c2 NaN 0.48093 | c3 NaN 0.39212 | Nal | | | | |
| | r1 r2 | NaN 0.68483 | NaN | NaN 0.39212 | Nal | | | | |

c1 c2

с8

0.03798

Na

| 1 | r1 | 1.511 | 0.089284 | | | | | |
|-------|-------|--------------|-------------------|---------------------|----------|----------|---------|----------|
| xxx 7 | TABLE | :yz c2 xxx | xxxxxxxxxx | xxx | | | | |
| | | - | c2 | | | | | |
| | | | | | | | | |
| 1 | r1 | 0.19312 | 2.2864 | | | | | |
| | | 0.057461 | | | | | | |
| 7 | TADIE | ··· •2 ····· | | | | | | |
| XXX . | IADLE | | xxxxxxxxxxx c2 | c3 | c4 | | | |
| | | | | | | | | |
| _ | 1 | 0 01107 | 0 1057 | 0 17520 | 0.3640 | | | |
| | | | | 0.17539 0.042587 | | | | |
| - | | 0.00020 | 011100. | 0101200. | 0.00200 | | | |
| xxx 7 | TABLE | :yz_c4 xxx | xxxxxxxxxx | xxx | | | | |
| | | c1 | c2 | сЗ | c4 | с5 | с6 | с7 |
| | | | | | | | | |
| 1 | r1 | NaN | NaN | NaN | NaN | NaN | NaN | NaN |
| 1 | r2 | 0.069088 | 0.093774 | 0.020122 | 0.024929 | 0.058349 | 0.14469 | 0.060227 |
| | | | | | | | | |
| xxxx | xxxx | xxxxxxxx | xxxxxxxxxxx | xxxxxxxx | | | | |
| CONTA | AINER | NAME: mp_ | container_ma | p Scalars | | | | |
| xxxxx | xxxxx | xxxxxxxxx | xxxxxxxxxx | xxxxxxxx | | | | |
| | | i | idx v | ralue | | | | |
| | | - | | | | | | |

5.2 Compute Nested CES MPL Given Demand (CRS)

0.50172

0.69647

Testing the bfw_crs_nested_ces_mpl function from the PrjLabEquiBFW Package. Given labor quantity demanded, using first-order relative optimality conditions, find the marginal product of labor given CES production function. Results match up with correct relative wages, but not wage levels. Takes as inputs share and elasticity parameters across layers of sub-nests, as well as quantity demanded at each bottom-most CES nest layer. Works with Constant Elasticity of Substitution problems with constant returns, up to four nest layers, and two inputs in each sub-nest. Allows for uneven branches, so that some branches go up to four layers, but others have less layers, works with BFW (2022) nested labor input problem.

Key Inputs and Outputs for bfw crs nested ces mpl

Here are the key inputs for the CES demand solver function:

2

10

1 2

prho_c1

pshare_c1

- CL_MN_PRHO cell array of rho (elasticity) parameter between negative infinity and 1. For example, suppose there are four nest layers, and there are two branches at each layer, then we have 1, 2, 4, and 8 ρ parameter values at the 1st, 2nd, 3rd, and 4th nest layers: $\operatorname{size}(\operatorname{CL_MN_PRHO}\{1\}) = [1,1], \operatorname{size}(\operatorname{CL_MN_PRHO}\{2\}) = [1,2], \operatorname{size}(\operatorname{CL_MN_PRHO}\{3\}) = [1,2], \operatorname{size}(\operatorname{CL_M$ [2,2], size(CL_MN_PRHO $\{4\}$) = [2,2,2]. Note that if the model has 4 nest layers, not all cells need to be specified, some branches could be deeper than others.
- CL MN PSHARE cell array of share (between 0 and 1) for the first input of the two inputs for each nest. The structure for this is similar to CL_MN_PRHO.

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• CL_MN_YZ_CHOICES cell array of quantity demanded for the first and second inputs of the bottom-most layer of sub-nests. The last index in each element of the cell array indicates first (1) or second (2) quantities. For example, suppose we have four layers, with 2 branches at each layer, as in the example for CL_MN_PRHO, then we have 2, 4, 8, and 16 quantity values at the 1st, 2nd, 3rd, and 4th nest layers: size(CL_MN_YZ_CHOICES{1})= [1,2], size(CL_MN_YZ_CHOICES $\{2\}$)= [2,2], size(CL_MN_YZ_CHOICES $\{3\}$)= [2,2,2], $size(CL_MN_YZ_CHOICES\{4\}) = [2, 2, 2, 2]$. Note that only the last layer of quantities needs to be specified, in this case, the 16 quantities at the 4th layer. Given first order conditions, we solve for the 2, 4, and 8 aggregate quantities at the higher nest layers. If some branches are deeper than other branches, then can specific NA for non-reached layers along some branches.

• BL BFW MODEL boolean true by default if true then will output outcomes specific to the BFW 2022 problem.

Here are the key outputs for the CES demand solver function:

- CL_MN_MPL_PRICE has the same dimension as CL_MN_YZ_CHOICES, suppose there are four layers, the CL_MN_MPL_PRICE{4} results at the lowest layer includes wages that might be observed in the data. CL_MN_MPL_PRICE cell values at non-bottom layers include aggregate wages.
- CL_MN_YZ_CHOICES includes at the lowest layer observed wages, however, also includes higher layer aggregate solved quantities. CL_MN_PRHO and CL_MN_PSHARE are identical to inputs.

5.2.2Single Nest Layer Two Inputs CES Problem (MPL)

In this first example, we solve a constant returns to scale problem with a single nest, meaning just two inputs and a single output.

```
clc;
close all;
clear all;
% rho = 0.5, 1/(1-0.5)=2, elasticity of substitution of 2
cl_mn_prho = {[0.1]};
% equal share, similar "productivity"
cl_mn_pshare = {[0.5]};
% levels of the two inputs, Values picked from demand problem parallel
% example.
cl_mn_yz_choices = \{[0.67537, 1.4589]\};
% print option
bl_verbose = true;
mp_func = bfw_mp_func_demand();
bl bfw model = false;
[cl_mn_yz_choices, cl_mn_mpl_price] = ...
    bfw_crs_nested_ces_mpl(cl_mn_prho, cl_mn_pshare, cl_mn_yz_choices, ...
   mp_func, bl_verbose, bl_bfw_model);
```

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| ^^^^^ | | | | -^^ | | | | | | , |
|--------------|---|-----|------|-------|------|------|--------|---------|---------|-----|
| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coe |
| | - | | | | | | | | | |
| mpl_price_c1 | 1 | 1 | 2 | 2 | 1 | 2 | 1.0678 | 0.53388 | 0.25168 | 0.4 |
| yz_c1 | 2 | 4 | 2 | 2 | 1 | 2 | 2.1343 | 1.0671 | 0.55404 | 0.5 |

xxx TABLE:mpl_price_c1 xxxxxxxxxxxxxxxxx

```
-----
              -----
      0.71184 0.35592
  r1
xxx TABLE:yz_c1 xxxxxxxxxxxxxxxxx
        c1
               c2
      0.67537
              1.4589
  r1
_____
CONTAINER NAME: mp_container_map Scalars
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
           i
             idx
                    value
               2
                     0.1
  prho_c1
           1
  pshare_c1
           2
                3
                     0.5
```

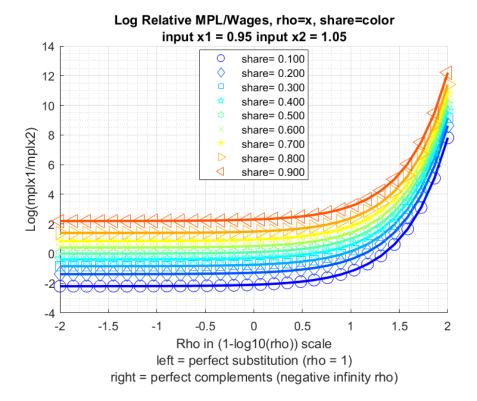
5.2.3 Single Nest Layer Two Inputs CES Problem, Vary Share and Elasticity (MPL)

In this second example, we test over different rho values, explore optimal relative choices, as share and elasticity change. In this exercise, we also check, at every combination of rho and share parameter, whether the FOC condition is satisfied by the optimal choices. Also check if at the optimal choices, the minimization output requirement is met.

```
% Approximately close function
rel_tol=1e-09;
abs_tol=0.0;
if_{is_close} = @(a,b) (abs(a-b) \le max(rel_tol * max(abs(a), abs(b)), abs_tol));
% Input 1 and 2 fixed
fl x 1 = 0.95;
fl_x_2 = 1.05;
% Define share and rho arrays
ar_pshare = linspace(0.1, 0.9, 9);
ar_prho = 1 - 10.^(linspace(-2, 2, 30));
% Loop over share and rho values
mt_rela_opti = NaN([length(ar_pshare), length(ar_prho)]);
mt_rela_wage = NaN([length(ar_pshare), length(ar_prho)]);
for it_pshare_ctr = 1:length(ar_pshare)
    for it_prho_ctr = 1:length(ar_prho)
        % A. Parameters
        % rho
        fl_prho = ar_prho(it_prho_ctr);
        cl_mn_prho = {[fl_prho]};
        % share
        fl_pshare = ar_pshare(it_pshare_ctr);
        cl_mn_pshare = {[fl_pshare]};
        % wages for the two inputs, identical wage
        % Note that if chosee \{[1,1]\} below, \log(1/1) = \log(1) = 0,
        % elasticity does not matter.
        cl_mn_yz_choices = \{[fl_x_1, fl_x_2]\};
        % print option
        bl_verbose = false;
```

Key results: (1) As share parameter of input 1 goes to zero, input 1 is less productive, and the log(mplx1/mplx2) ratio is lower. (2) Becaus x2 input in this example is larger than x1 input, so as two inputs become more inelastic (more leontief), relative MPL for the lower level input is now larger. At the Leontief extreme, the MPL of the input provided at lower level is infinity.

```
% Visualize
% Generate some Data
rng(456);
ar_row_grid = ar_pshare;
ar_col_grid = log(1-ar_prho)/log(10);
rng(123);
mt_value = mt_rela_wage;
% container map settings
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_graph_title') = {...
    ['Log Relative MPL/Wages, rho=x, share=color'] ...
    ['input x1 = ' num2str(fl_x_1) ' input x2 = ' num2str(fl_x_2)]
mp_support_graph('cl_st_ytitle') = {'Log(mplx1/mplx2)'};
mp_support_graph('cl_st_xtitle') = {'Rho in (1-log10(rho)) scale', ...
    'left = perfect substitution (rho = 1)', ...
    'right = perfect complements (negative infinity rho)'};
mp_support_graph('st_legend_loc') = 'best';
mp_support_graph('bl_graph_logy') = false; % do not log
mp_support_graph('st_rowvar_name') = 'share=';
mp_support_graph('it_legend_select') = 5; % how many shock legends to show
mp_support_graph('st_rounding') = '6.3f'; % format shock legend
mp_support_graph('cl_colors') = 'jet'; % any predefined matlab colormap
% Call function
ff_graph_grid(mt_value, ar_row_grid, ar_col_grid, mp_support_graph);
```



5.2.4 Doubly Nest Layer Two Inputs Each Sub-nest CES Problem

In this third example, solve for optimal choices for a doubly nested problem. Below, we first solve for the optimal choices, then we do a number of checks, to make sure that the solutions are correct, as expected.

```
% output requirement
fl_yz = 2.1;
\% upper nest 0.1, lower nests 0.35 and -1 separately for rho values
cl_mn_prho = \{[0.1], [0.35, -1]\};
% unequal shares of share values
cl_mn_pshare = \{[0.4], [0.3, 0.88]\};
% differential wages
% in lower-left nest, not productive and very expensive, not very elastic
% last index for left or right. Values picked from demand problem parallel
% example.
cl_mn_yz_choices = {[nan, nan], [0.04789, 6.0934; 2.2044, 0.70496]};
% print option
bl verbose = true;
[cl_mn_yz_choices, cl_mn_mpl_price] = ...
    bfw_crs_nested_ces_mpl(cl_mn_prho, cl_mn_pshare, cl_mn_yz_choices, ...
    mp_func, bl_verbose, bl_bfw_model);
```

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| | i | idx | ndim | numel | rowN | colN | sum | mean | std | coe |
|--------------|---|-----|------|-------|------|------|--------|---------|---------|-----|
| | - | | | | | | | | | |
| mpl_price_c1 | 1 | 1 | 2 | 2 | 1 | 2 | 1.0206 | 0.51032 | 0.27499 | 0.5 |
| mpl_price_c2 | 2 | 2 | 2 | 4 | 2 | 2 | 2.3618 | 0.59045 | 0.5082 | 0.8 |
| prho_c2 | 3 | 4 | 2 | 2 | 1 | 2 | -0.65 | -0.325 | 0.95459 | -2. |
| pshare_c2 | 4 | 6 | 2 | 2 | 1 | 2 | 1.18 | 0.59 | 0.41012 | 0.6 |
| yz_c1 | 5 | 7 | 2 | 2 | 1 | 2 | 4.4862 | 2.2431 | 0.68863 | 0 |

2.2627

2.7086

1.

9.0507

2 2

```
6 8 2 4
   yz_c2
xxx TABLE:mpl_price_c1 xxxxxxxxxxxxxxxxx
          c1
                  c2
        -----
        0.31587 0.70476
   r1
xxx TABLE:mpl_price_c2 xxxxxxxxxxxxxxxxx
          c1
                 c2
         1.3121
                 0.13121
   r1
   r2
        0.39362
                 0.52484
xxx TABLE:prho_c2 xxxxxxxxxxxxxxxxx
         c1
               c2
        ----
        0.35
               -1
   r1
c1
               c2
        ---
              ----
        0.3 0.88
   r1
xxx TABLE:yz_c1 xxxxxxxxxxxxxxxxx
         c1
               c2
               -----
   r1
        2.73
             1.7562
xxx TABLE:yz_c2 xxxxxxxxxxxxxxxxx
         c1
                  c2
        ----
                 -----
        0.04789
                 6.0934
   r1
         2.2044
                 0.70496
   r2
CONTAINER NAME: mp_container_map Scalars
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
              i idx value
   prho_c1
              1
                   3
                         0.1
                         0.4
   pshare_c1
                   5
              2
% there are four optimal choices, they are
fl_mpl_x11 = cl_mn_mpl_price{2}(1,1);
fl_mpl_x12 = cl_mn_mpl_price{2}(1,2);
fl_mpl_x21 = cl_mn_mpl_price{2}(2,1);
fl_mpl_x22 = cl_mn_mpl_price{2}(2,2);
% display
st_print = strjoin(...
   ["completed double nest test:", ...
```

```
['nest 1 input 1, fl_mpl_x11=' num2str(fl_mpl_x11)], ...
    ['nest 1 input 2, fl_mpl_x12=' num2str(fl_mpl_x12)], ...
    ['nest 2 input 1, fl_mpl_x21=' num2str(fl_mpl_x21)], ...
    ['nest 2 input 2, fl_mpl_x22=' num2str(fl_mpl_x22)], ...
    ['nest 1 input 1, fl_mpl_x11/fl_mpl_x11=' num2str(fl_mpl_x11/fl_mpl_x11)], ...
    ['nest 1 input 2, fl_mpl_x12/fl_mpl_x11=' num2str(fl_mpl_x12/fl_mpl_x11)], ...
    ['nest 2 input 1, fl_mpl_x21/fl_mpl_x11=' num2str(fl_mpl_x21/fl_mpl_x11)], ...
    ['nest 2 input 2, fl_mpl_x22/fl_mpl_x11=' num2str(fl_mpl_x22/fl_mpl_x11)], ...
   ], ";");
st_out = st_print;
ar_ch_out = char(strsplit(st_print,";")');
disp(ar_ch_out);
completed double nest test:
nest 1 input 1, fl_mpl_x11=1.3121
nest 1 input 2, fl_mpl_x12=0.13121
nest 2 input 1, fl_mpl_x21=0.39362
nest 2 input 2, fl_mpl_x22=0.52484
nest 1 input 1, fl_mpl_x11/fl_mpl_x11=1
nest 1 input 2, fl_mpl_x12/fl_mpl_x11=0.099995
nest 2 input 1, fl_mpl_x21/fl_mpl_x11=0.29998
nest 2 input 2, fl_mpl_x22/fl_mpl_x11=0.39999
```

5.2.5 BFW (2022) Nested Three Branch (Four Layer) Problem (MPL)

The model BFW 2022 has three branches and four layers. one of the branches go down only three layers, the other two branches go down four layers.

First, we prepare the various inputs:

```
% Controls
bl_verbose = true;
bl_bfw_model = true;
% Given rho and beta, solve for equilibrium quantities
mp_func = bfw_mp_func_demand();
% Following instructions in: PrjFLFPMexicoBFW\solvedemand\README.md
% Nests/layers
it_nests = 4;
% Input cell of mn matrixes
it_prho_cl = 1;
it_pshare_cl = 2;
it_yz_share_cl = 3;
for it_cl_ctr = [1,2,3]
    cl_mn_cur = cell(it_nests,1);
   % Fill each cell element with NaN mn array
    for it_cl_mn = 1:it_nests
        bl_yz_share = (it_cl_ctr == it_yz_share_cl);
        if (~bl_yz_share && it_cl_mn == 1)
            mn nan = NaN;
        elseif (~bl_yz_share && it_cl_mn == 2) || (bl_yz_share && it_cl_mn == 1)
            mn_nan = [NaN, NaN];
```

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```
elseif (~bl_yz_share && it_cl_mn == 3) || (bl_yz_share && it_cl_mn == 2)
            mn_nan = NaN(2,2);
        elseif (~bl_yz_share && it_cl_mn == 4) || (bl_yz_share && it_cl_mn == 3)
            mn_nan = NaN(2,2,2);
        elseif (~bl_yz_share && it_cl_mn == 5) || (bl_yz_share && it_cl_mn == 4)
            mn_nan = NaN(2,2,2,2);
        elseif (~bl_yz_share && it_cl_mn == 6) || (bl_yz_share && it_cl_mn == 5)
            mn_nan = NaN(2,2,2,2,2);
        cl_mn_cur{it_cl_mn} = mn_nan;
    end
    % Name cell arrays
    if (it_cl_ctr == it_prho_cl)
        cl_mn_prho = cl_mn_cur;
    elseif (it_cl_ctr == it_pshare_cl)
        cl_mn_pshare = cl_mn_cur;
    elseif (it_cl_ctr == it_yz_share_cl)
        cl_mn_yz_choices = cl_mn_cur;
    end
end
% Initialize share matrix
rng(123);
for it_cl_mn = 1:it_nests
    mn_pshare = cl_mn_pshare{it_cl_mn};
    if it cl mn == 4
        mn_pshare(2,:,:) = rand(2,2);
    else
        mn_pshare = rand(size(mn_pshare));
    cl_mn_pshare{it_cl_mn} = mn_pshare;
end
% Initialize rho matrix
rng(456);
for it_cl_mn = 1:it_nests
    mn_prho = cl_mn_prho{it_cl_mn};
    if it_cl_mn == 4
        mn_prho(2,:,:) = rand(2,2);
    else
        mn_prho = rand(size(mn_prho));
    end
    % Scalling rho between 0.7500 and -3.0000
    % 1 - 2.^{(linspace(-2,2,5))}
    mn_prho = 1 - 2.^(mn_prho*(4) - 2);
    cl_mn_prho{it_cl_mn} = mn_prho;
end
% Initialize quantities matrix
rng(789);
for it_cl_mn = 1:it_nests
    mn_yz_choices = cl_mn_yz_choices{it_cl_mn};
    if it_cl_mn == 3
        mn_yz_choices(1,:,:) = rand(2,2);
    elseif it_cl_mn == 4
        mn_yz_choices(2,:,:,:) = rand(2,2,2);
    end
```

```
\% Scalling quantities between 3 amd 5
    mn_yz_choices = mn_yz_choices*(2) + 3;
    cl_mn_yz_choices{it_cl_mn} = mn_yz_choices;
end
% Initialize yz matrix
rng(101112);
Second, display created inputs:
celldisp(cl_mn_prho);
cl_mn_prho\{1\} =
    0.5017
cl_mn_prho{2} =
    0.6071 -1.1955
cl_mn_prho{3} =
   -1.3523
             -0.3346
   -0.4167 -1.9136
cl_mn_prho{4} =
(:,:,1) =
       {\tt NaN}
                  {\tt NaN}
   -1.0512
              0.5869
(:,:,2) =
       NaN
                  \mathtt{NaN}
    0.6209
               0.1633
celldisp(cl_mn_pshare);
cl_mn_pshare{1} =
    0.6965
cl_mn_pshare{2} =
```

0.2861 0.2269

 $cl_mn_pshare{3} =$

 $cl_mn_pshare{4} =$

(:,:,1) =

NaN NaN 0.6848 0.4809

(:,:,2) =

NaN NaN 0.3921 0.3432

celldisp(cl_mn_yz_choices);

cl_mn_yz_choices{1} =

NaN NaN

cl_mn_yz_choices{2} =

NaN NaN NaN NaN

 $cl_mn_yz_choices{3} =$

(:,:,1) =

3.6467 3.4605 NaN NaN

(:,:,2) =

4.5876 4.2488 NaN NaN

```
cl_mn_yz_choices{4} =
```

(:,:,1,1) =

NaN NaN 4.9508 4.5178

(:,:,2,1) =

NaN NaN 3.0212 3.0495

(:,:,1,2) =

NaN NaN 3.2221 4.0763

(:,:,2,2) =

NaN NaN 3.0909 4.1031

Third, call function and solve for optimal demand:

% Call function

[cl_mn_yz_choices, cl_mn_mpl_price] = ...
 bfw_crs_nested_ces_mpl(cl_mn_prho, cl_mn_pshare, cl_mn_yz_choices, ...
 mp_func, bl_verbose, bl_bfw_model);

CONTAINER NAME: mp_container_map ND Array (Matrix etc)

| *********** | i | idx | ndim | numel | rowN | colN | sum | mean | std |
|--------------|----|-----|------|-------|------|------|----------|----------|----------|
| | - | Idh | nan | Humor | TOWN | COIN | bam | moun | boa |
| | | | | | | | | | |
| mpl_price_c1 | 1 | 1 | 2 | 2 | 1 | 2 | 1.0002 | 0.5001 | 0.28686 |
| mpl_price_c2 | 2 | 2 | 2 | 4 | 2 | 2 | 1.0009 | 0.25022 | 0.17949 |
| mpl_price_c3 | 3 | 3 | 3 | 8 | 2 | 4 | 1.0088 | 0.1261 | 0.10191 |
| mpl_price_c4 | 4 | 4 | 4 | 16 | 2 | 8 | NaN | NaN | NaN |
| prho_c2 | 5 | 6 | 2 | 2 | 1 | 2 | -0.58844 | -0.29422 | 1.2746 |
| prho_c3 | 6 | 7 | 2 | 4 | 2 | 2 | -4.0173 | -1.0043 | 0.76195 |
| prho_c4 | 7 | 8 | 3 | 8 | 2 | 4 | NaN | NaN | NaN |
| pshare_c2 | 8 | 10 | 2 | 2 | 1 | 2 | 0.51299 | 0.2565 | 0.041923 |
| pshare_c3 | 9 | 11 | 2 | 4 | 2 | 2 | 2.6747 | 0.66866 | 0.24087 |
| pshare_c4 | 10 | 12 | 3 | 8 | 2 | 4 | NaN | NaN | NaN |
| yz_c1 | 11 | 13 | 2 | 2 | 1 | 2 | 8.0897 | 4.0448 | 0.173 |
| yz_c2 | 12 | 14 | 2 | 4 | 2 | 2 | 16.015 | 4.0039 | 0.19166 |
| yz_c3 | 13 | 15 | 3 | 8 | 2 | 4 | 31.235 | 3.9044 | 0.51337 |
| yz_c4 | 14 | 16 | 4 | 16 | 2 | 8 | NaN | NaN | NaN |
| | | | | | | | | | |

xxx TABLE:mpl_price_c1 xxxxxxxxxxxxxxxxx

c1 c2

c5 c6 c7

 ${\tt NaN}$

0.11203

 ${\tt NaN}$

0.027845

с8

N 0.00380

0.018861

 ${\tt NaN}$

| | r1 | 0.70294 | 0.29725 | | |
|-----|---------|------------|-------------|-----------|-----------|
| xxx | TABLE | | c2 xxxxxxxx | xxxxxxxx | |
| | | c1 | c2 | | |
| | | | | | |
| | r1 | 0.19946 | 0.50351 | | |
| | | 0.080381 | | | |
| | | | | | |
| xxx | TABLE | mpl_price_ | | xxxxxxxxx | |
| | | c1 | c2 | c3 | c4 |
| | | | | | |
| | r1 | 0.13727 | 0.24893 | 0.065108 | 0.25809 |
| | r2 | 0.050551 | 0.21139 | 0.031132 | 0.0063057 |
| | | | | | |
| xxx | TABLE | mpl_price_ | | xxxxxxxxx | |
| | | c1 | c2 | сЗ | c4 |
| | | | | | |
| | r1 | NaN | NaN | NaN | NaN |
| | | | | | 0.0025507 |
| | 12 | 0.02001 | 0.000101 | 0.012272 | 0.0020001 |
| xxx | TABLE | prho_c2 xx | xxxxxxxxx | xxxx | |
| | | c1 | c2 | | |
| | | | | | |
| | r1 | 0.60709 | -1.1955 | | |
| | | 1 0 | | | |
| XXX | I ABLE: | c1 | c2 | XXXXX | |
| | | | | | |
| | | | | | |
| | r1 | -1.3523 | -0.33464 | | |
| | r2 | -0.41668 | -1.9136 | | |
| | | | | | |
| xxx | TABLE | = | xxxxxxxxxx | _ | |
| | | c1 | c2 | c3 | c4 |
| | | | | | |
| | r1 | NaN | NaN | NaN | NaN |
| | r2 | -1.0512 | 0.58694 | 0.62089 | 0.16334 |
| | | | | | |
| xxx | TABLE | | xxxxxxxxx | xxxxxx | |
| | | c1 | c2 | | |
| | | | | | |
| | r1 | 0.28614 | 0.22685 | | |
| | | _ | | | |
| XXX | TABLE | _ | xxxxxxxxxx | XXXXXX | |
| | | c1 | c2 | | |
| | | | | | |
| | r1 | 0.55131 | 0.42311 | | |
| | r2 | 0.71947 | 0.98076 | | |
| | | | | | |

| | c1 | c2 | c3 | c4 | _ | | | |
|----------|----------------|----------------|----------------|------------------|-----|-----|-----|--------|
| r1 r2 | NaN 0.68483 | NaN 0.48093 | NaN 0.39212 | N Na 2 0.3431 | | | | |
| xxx TAE | LE:yz_c1 xx | | XXXXX | | | | | |
| | c1 | c2 | | | | | | |
| | | | | | | | | |
| r1 | 3.9225 | 4.1672 | | | | | | |
| xxx TAE | LE:yz_c2 xx | xxxxxxxxx | xxxxx | | | | | |
| | c1 | c2 | | | | | | |
| | | | | | | | | |
| r1 | 4.0073 | 3.8887 | | | | | | |
| | 3.8468 | | | | | | | |
| xxx TAE | LE:yz_c3 xx | xxxxxxxxxx | xxxxx | | | | | |
| | c1 | c2 | | c4 | | | | |
| | | | | | | | | |
| r1 | 3.6467 | 3.4605 | 4.5876 | 4.2488 | | | | |
| r2 | 4.23 | | | 3.7118 | | | | |
| xxx TAE | SLE:yz_c4 xx | xxxxxxxxx | xxxxx | | | | | |
| | c1 | c2 | c 3 | c4 | с5 | c6 | с7 | c8 |
| | | | | | | | | |
| r1 | NaN | NaN | NaN | NaN | NaN | NaN | NaN | NaN |
| r2 | | | | 3.0495 | | | | 4.1031 |

| | i | idx | value |
|-----------|---|-----|---------|
| | - | | |
| prho_c1 | 1 | 5 | 0.50172 |
| pshare_c1 | 2 | 9 | 0.69647 |

Chapter 6

Supply

6.1 bfw mlogit

This is the example vignette for function: bfw mlogit from the PrjLabEquiBFW Package.

6.1.1 Default

[mp_fl_labor_occprbty,mp_fl_labor_supplied] = bfw_mlogit();

CONTAINER NAME: mp_wages Scalars

| | i | idx | value |
|------|---|-----|--------|
| | - | | |
| C011 | 1 | 1 | 2.1604 |
| C012 | 2 | 2 | 5.6589 |
| C013 | 3 | 3 | 5.8023 |
| C111 | 4 | 4 | 4.5245 |
| C112 | 5 | 5 | 5.4146 |
| C113 | 6 | 6 | 8.0437 |

BFW_SUPPLY_LEVELS_BF18; it_supplier_group=1; SNW_MP_CONTROL=; C011; time=; G01; f1_wage=2.1604 Supply data; potwrker=0.85421; shrmarid=0.87768; shrufive=0.54077; applianc=0.95588; jobscrys=0.613 BFW_SUPPLY_LEVELS_BF18; it_supplier_group=1; SNW_MP_CONTROL=; C012; time=; G01; f1_wage=5.6589 Supply data; potwrker=0.85421; shrmarid=0.87768; shrufive=0.54077; applianc=0.95588; jobscrys=0.613 BFW_SUPPLY_LEVELS_BF18; it_supplier_group=1; SNW_MP_CONTROL=; C013; time=; G01; f1_wage=5.8023 Supply data; potwrker=0.85421; shrmarid=0.87768; shrufive=0.54077; applianc=0.95588; jobscrys=0.613 BFW_SUPPLY_LEVELS_BF18; it_supplier_group=2; SNW_MP_CONTROL=; C111; time=; G11; f1_wage=4.5245 Supply data; potwrker=1.8792; shrmarid=0.9391; shrufive=0.54027; applianc=0.93209; jobscrys=0.613 BFW_SUPPLY_LEVELS_BF18; it_supplier_group=2; SNW_MP_CONTROL=; C112; time=; G11; f1_wage=5.4146 Supply data; potwrker=1.8792; shrmarid=0.9391; shrufive=0.54027; applianc=0.93209; jobscrys=0.613 BFW_SUPPLY_LEVELS_BF18; it_supplier_group=2; SNW_MP_CONTROL=; C113; time=; G11; f1_wage=8.0437 Supply data; potwrker=1.8792; shrmarid=0.9391; shrufive=0.54027; applianc=0.93209; jobscrys=0.613

i idx value
- --- -----C011 1 1 0.015821

```
60

      C012
      2
      2
      0.12787

      C013
      3
      3
      0.36854

      C111
      4
      4
      0.097357

      C112
      5
      5
      0.17795

      C113
      6
      6
      0.65443

_____
xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
CONTAINER NAME: mp_fl_labor_supplied Scalars
idx
                                                             value
                                           ---

      C011
      1
      1
      0.013514

      C012
      2
      2
      0.10923

      C013
      3
      3
      0.31481

      C111
      4
      4
      0.18296

      C112
      5
      5
      0.33441

      C113
      6
      6
      1.2298
```

CONTAINER NAME: mp_fl_labor_supplied_3v0f Scalars

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | i | idx | value |
|------|-----|-----|----------|
| | - | | |
| C011 | 1 1 | 1 | 0.013514 |
| C012 | 2 2 | 2 | 0.10923 |
| C013 | 3 3 | 3 | 0.31481 |
| C111 | 1 4 | 4 | 0.18296 |
| C112 | 2 5 | 5 | 0.33441 |
| C113 | 3 6 | 6 | 1.2298 |

CONTAINER NAME: mp_fc_labor_occprbty_3v0f Functions

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | i | idx | functionString |
|------|-----|-----|---|
| | | | |
| C011 | "1" | "1" | "@(w1,w2,w3)fc_ar_prob_wrk(fl_psi0_manual,psi1,w1,fc_prob_denom_wage(w1,w2 |
| C012 | "2" | "2" | "@(w1,w2,w3)fc_ar_prob_wrk(fl_psi0_routine,psi1,w2,fc_prob_denom_wage(w1,w |
| C013 | "3" | "3" | <pre>"@(w1,w2,w3)fc_ar_prob_wrk(fl_psi0_analytical,psi1,w3,fc_prob_denom_wage(w</pre> |
| C111 | "4" | "4" | "@(w1,w2,w3)fc_ar_prob_wrk(fl_psi0_manual,psi1,w1,fc_prob_denom_wage(w1,w2 |
| C112 | "5" | "5" | "@(w1,w2,w3)fc_ar_prob_wrk(fl_psi0_routine,psi1,w2,fc_prob_denom_wage(w1,w |
| C113 | "6" | "6" | "@(w1,w2,w3)fc_ar_prob_wrk(fl_psi0_analytical,psi1,w3,fc_prob_denom_wage(w |

CONTAINER NAME: mp_fc_labor_supplied_3v0f Functions

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | i | idx | functionString |
|------|-----|-----|--|
| | | | |
| C011 | "1" | "1" | "@(w1,w2,w3)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_3v0f(w1,w2,w |
| C012 | "2" | "2" | "@(w1,w2,w3)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_3v0f(w1,w2,w |
| C013 | "3" | "3" | "@(w1,w2,w3)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_3v0f(w1,w2,w |

| C111 | "4" | "4" | "@(w1,w2,w3)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_3v0f(w1,w2,w |
|------|-----|-----|--|
| C112 | "5" | "5" | "@(w1,w2,w3)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_3v0f(w1,w2,w |
| C113 | "6" | "6" | "@(w1,w2,w3)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_3v0f(w1,w2,w |

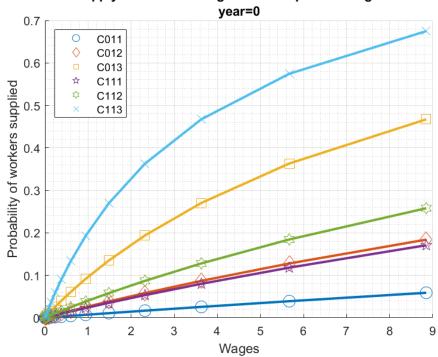
CONTAINER NAME: mp_fc_labor_occprbty_1v2f Functions

| | i | idx | functionString |
|------|-----|-----|--|
| | | | |
| C011 | "1" | "1" | "@(wage)fc_ar_prob_wrk(fl_psi0_manual,psi1,wage,fc_prob_denom_wage(wage,fl |
| C012 | "2" | "2" | "@(wage)fc_ar_prob_wrk(fl_psi0_routine,psi1,wage,fc_prob_denom_wage(fl_w1, |
| C013 | "3" | "3" | "@(wage)fc_ar_prob_wrk(fl_psi0_analytical,psi1,wage,fc_prob_denom_wage(fl_ |
| C111 | "4" | "4" | "@(wage)fc_ar_prob_wrk(fl_psi0_manual,psi1,wage,fc_prob_denom_wage(wage,fl |
| C112 | "5" | "5" | "@(wage)fc_ar_prob_wrk(fl_psi0_routine,psi1,wage,fc_prob_denom_wage(fl_w1, |
| C113 | "6" | "6" | "@(wage)fc_ar_prob_wrk(fl_psi0_analytical,psi1,wage,fc_prob_denom_wage(fl_ |

CONTAINER NAME: mp_fc_labor_supplied_1v2f Functions

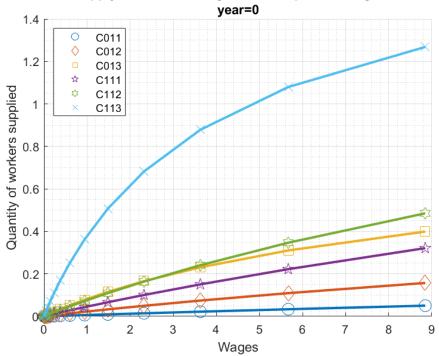
| | i | idx | functionString |
|------|-----|-----|---|
| | | | |
| C011 | "1" | "1" | "@(wage)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_1v2f(wage))" |
| C012 | "2" | "2" | "@(wage)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_1v2f(wage))" |
| C013 | "3" | "3" | "@(wage)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_1v2f(wage))" |
| C111 | "4" | "4" | "@(wage)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_1v2f(wage))" |
| C112 | "5" | "5" | "@(wage)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_1v2f(wage))" |
| C113 | "6" | "6" | <pre>"@(wage)fc_supply(fl_potwrklei_potwrker,fc_labor_occprbty_1v2f(wage))"</pre> |

Supply curves for edu-gender-occupation categories



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Supply curves for edu-gender-occupation categories

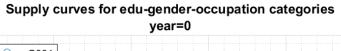


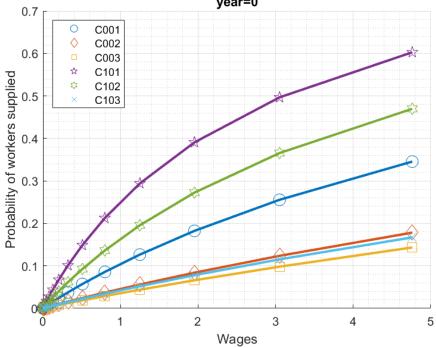
6.1.2 Visualize Supply Curves Different Years

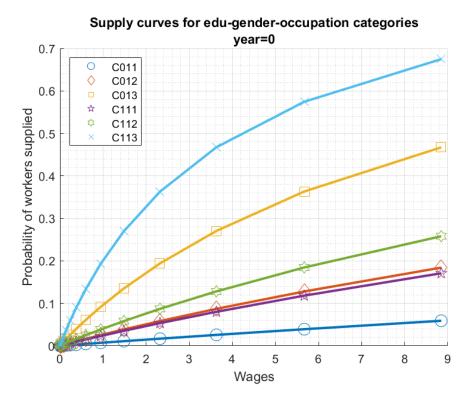
```
% 1. Print and Graph options
bl_verbose = false;
bl_graph = true;
ar_it_prob_or_quant = [1];
% 2. Get Parameters and data
bl_log_wage = true;
bl_verbose_nest = false;
% Get Parameters
mp_params = bfw_mp_param_esti(bl_log_wage);
mp_param_aux = bfw_mp_param_aux(bl_verbose_nest);
mp_params = [mp_params ; mp_param_aux];
% Get Data
mp_data = bfw_mp_data(bl_verbose_nest);
% Get Functions
mp_func = bfw_mp_func_supply(bl_log_wage, bl_verbose_nest);
% Get Controls
mp_controls = bfw_mp_control();
\ensuremath{\text{\%}} 3. Data from which year, only integer year value allowed
% ar_it_data_year = [1989 1994 2000 2008 2014];
ar_it_data_year = [1989 2000 2014];
for it_data_year=ar_it_data_year
    \% 4. Which categories to obtain data from, there are 12 possible
    % For non-college equilibrium, six wages, three female, three males
    % gen_occ = gender occupation
    for bl_skilled = [false true]
        if (bl_skilled)
            mt_st_gen_occ_categories = [...
                "C011", "C012", "C013"; ...
                 "C111", "C112", "C113"];
```

```
else
            mt_st_gen_occ_categories = [...
                "C001", "C002", "C003"; ...
                "C101", "C102", "C103"];
        end
        % 5. Array of wages, at most, since there are six nests, there are 12
        % prices possible. And there are 12 quantity supplies possible, coming
        % from four tyeps of workers, each supply 3 + home categories.
        mp_wages = containers.Map('KeyType', 'char', 'ValueType', 'any');
        % Obtain some equilibrium wage data as testing inputs
        mp_path = bfw_mp_path();
        spt_codem_data = mp_path('spt_codem_data');
        tb_data_pq = mp_data('tb_data_pq');
        tb_data_pq = tb_data_pq(:, ["year", "category", "numberWorkers", "meanWage"]);
        ar_st_gen_occ_categories = mt_st_gen_occ_categories(:)';
        for st_gen_occ=ar_st_gen_occ_categories
            tb_gen_occ_over_years = tb_data_pq(strcmp(tb_data_pq.category, st_gen_occ),:);
            fl_wage_one_year = tb_gen_occ_over_years(tb_gen_occ_over_years.year == (it_data_year), :
            mp_wages(st_gen_occ) = fl_wage_one_year{1, "meanWage"};
        end
        % Print Wages
        % ff_container_map_display(mp_wages);
        % Get date offset
        params_group = values(mp_data, {'date_esti_offset'});
        [date_esti_offset] = params_group{:};
        % Run function
        [mp_fl_labor_occprbty,mp_fl_labor_supplied] = bfw_mlogit(...
            mp_params, mp_data, mp_func, mp_controls, ...
            mt_st_gen_occ_categories, it_data_year - date_esti_offset, mp_wages, ...
            bl_verbose, bl_graph, ...
            ar_it_prob_or_quant);
    end
end
```

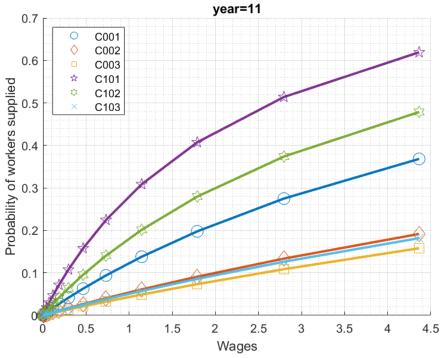
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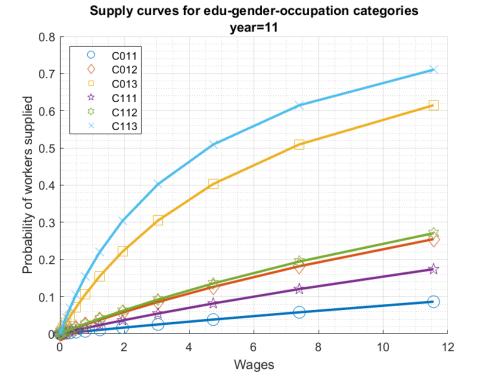






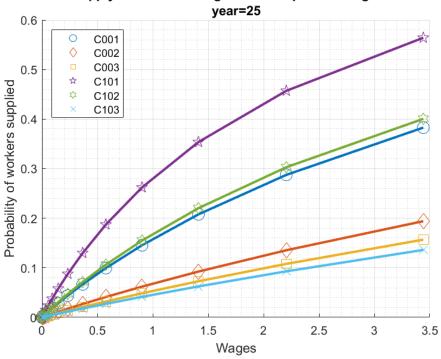




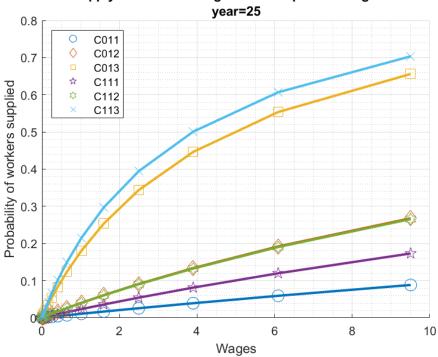


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Supply curves for edu-gender-occupation categories



Chapter 7

Equilibrium by Skill Nest Group

7.1 Root Search Equilibrium Wage Equations By Skill Group

This is the example vignette for function: bfw solveequi kwfw from the PrjLabEquiBFW Package.

7.1.1 Default

```
[mp_fl_labor_occprbty,mp_fl_labor_supplied] = bfw_solveequi_kwfw();
```

Completed BFW_SOLVEEQUI_KWFW;fl_potwrker_1=9.9687;fl_potwrker_2=12.5164;ar_fl_max_ratio_1=0.36095 BFW_SOLVEEQUI_KWFW-initial-Q;category_key=;C001;sexrhs=;Female;occ=;Manual;wxox=3.5484;laborsupplied BFW_SOLVEEQUI_KWFW-initial-Q;category_key=;C002;sexrhs=;Female;occ=;Routine;wxox=4.9268;laborsupplied BFW_SOLVEEQUI_KWFW-initial-Q;category_key=;C003;sexrhs=;Female;occ=;Analytical;wxox=3.523;laborsuppl BFW_SOLVEEQUI_KWFW-initial-Q;category_key=;C101;sexrhs=;Male;occ=;Manual;wxox=1.7656;laborsupplied=4 BFW_SOLVEEQUI_KWFW-initial-Q;category_key=;C102;sexrhs=;Male;occ=;Routine;wxox=5.9065;laborsupplied=BFW_SOLVEEQUI_KWFW-initial-Q;category_key=;C103;sexrhs=;Male;occ=;Analytical;wxox=2.222;laborsupplied=Completed BFW_SOLVEEQUI_KWFW;fl_mse_excess=4.4821e-13;ar_w1_iter_endo=1.5779 1.819 3.7951

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CONTAINER NAME: mp_wages Scalars

| | _ | | |
|------|---|---|--------|
| C001 | 1 | 1 | 1.2165 |
| C002 | 2 | 2 | 1.8629 |
| C003 | 3 | 3 | 3.227 |
| C101 | 4 | 4 | 1.5779 |
| C102 | 5 | 5 | 1.819 |
| C103 | 6 | 6 | 3.7951 |

i idx value
- --- ---
C001 1 1 1.6514

C002 2 2 1.0896

C003 3 3 1.4662

C101 4 4 4.3057

C102 5 5 3.1524

```
C103 6 6 1.9726
```

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| · AAAAAAA | ************************************ | | | | | | |
|-----------|--------------------------------------|-----|--------|--|--|--|--|
| | i | idx | value | | | | |
| | - | | | | | | |
| C001 | 1 | 1 | 1.6514 | | | | |
| C002 | 2 | 2 | 1.0896 | | | | |
| C003 | 3 | 3 | 1.4662 | | | | |
| C101 | 4 | 4 | 4.3057 | | | | |
| C102 | 5 | 5 | 3.1524 | | | | |
| C103 | 6 | 6 | 1.9726 | | | | |
| | | | | | | | |

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CONTAINER NAME: mp_fl_labor_occprbty Scalars

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| | 1 | ıax | value |
|------|---|-----|----------|
| | - | | |
| C001 | 1 | 1 | 0.13194 |
| C002 | 2 | 2 | 0.087055 |
| C003 | 3 | 3 | 0.11714 |
| C101 | 4 | 4 | 0.43193 |
| C102 | 5 | 5 | 0.31623 |
| C103 | 6 | 6 | 0.19788 |
| | | | |

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CONTAINER NAME: mp_fl_labor_excess_demand Scalars

| | i | idx | value |
|------|---|-----|-------------|
| | - | | |
| C001 | 1 | 1 | -3.4607e-08 |
| C002 | 2 | 2 | -2.3265e-07 |
| C003 | 3 | 3 | 6.268e-07 |
| C101 | 4 | 4 | -2.6645e-15 |
| C102 | 5 | 5 | -2.2204e-15 |
| C103 | 6 | 6 | -2.2204e-16 |

7.1.2 Vary Parameters, Solve Equilibrium Quantities/Wages, Root Search

```
% 2. Get Parameters and data
bl_log_wage = true;
bl_verbose_nest = false;

% Get Parameters
mp_params = bfw_mp_param_esti(bl_log_wage);
mp_param_aux = bfw_mp_param_aux(bl_verbose_nest);
mp_params = [mp_params ; mp_param_aux];

% Get Data
mp_data = bfw_mp_data(bl_verbose_nest);
```

```
% Get Functions
mp_func_demand = bfw_mp_func_demand(bl_verbose_nest);
mp_func_supply = bfw_mp_func_supply(bl_log_wage, bl_verbose_nest);
mp_func_equi = bfw_mp_func_equi(bl_verbose_nest);
mp_func = [mp_func_equi; mp_func_supply; mp_func_demand];
% Get Controls
mp_controls = bfw_mp_control();
mp_controls('bl_bfw_solveequi_kwfw_display') = false;
mp_controls('bl_bfw_solveequi_kwfw_display_verbose') = false;
st_exa_common_str = 'bfw_solveequi_kwfw()';
for it_example_inputs = [1,2,3,4]
    % Different testing scenariors
    if (it_example_inputs == 1)
        fl_rho_manual = 0.18;
        fl_rho_routine = 0.18;
        fl_rho_analytical = 0.18;
        fl_beta_1_manual = 1 - 0.26;
        fl_beta_1_routine = 1 - 0.30;
        fl_beta_1_analytical = 1 - 0.40;
        fl_Y_manual = 3.4084;
        fl_Y_routine = 2.3402;
        fl_Y_analytical = 1.7552;
        fl_w1o1_init = 2.315707;
        fl_w1o2_init = 3.217799;
        fl_w1o3_init = 4.329016;
        fl_w2o1_init = 1.942;
        fl_w2o2_init = 3.2247;
        fl_w2o3_init = 3.3738;
        it_data_year = 1989;
        fl_potwrker_1 = 9.9687;
        fl_potwrker_2 = 12.5164;
        bl_skilled = false;
        st_exa_string = "homogeneous rho at 0.18, unskilled";
    elseif (it_example_inputs == 2)
        fl_rho_manual = 0.64678;
        fl_rho_routine = 0.64678;
        fl_rho_analytical = 0.64678;
        fl_beta_1_manual = 0.63427;
        fl_beta_1_routine = 0.58738;
        fl_beta_1_analytical = 0.5784;
        fl_Y_manual = 3.2291;
        fl_Y_routine = 2.2223;
        fl_Y_analytical = 1.7487;
        fl_w1o1_init = 2.3157;
        fl_w1o2_init = 3.2178;
```

```
fl_w1o3_init = 4.329;
   fl_w2o1_init = 1.942;
   fl_w2o2_init = 3.2247;
   fl_w2o3_init = 3.3738;
    it_data_year = 1989;
    fl_potwrker_1 = 9.9687;
    fl_potwrker_2 = 12.5164;
   bl_skilled = false;
    st_exa_string = "homogeneous rho at 0.64, unskilled";
elseif (it_example_inputs == 3)
   fl_rho_manual = 0.34186;
    fl_rho_routine = 0.34186;
    fl_rho_analytical = 0.34186;
    fl_beta_1_manual = 0.63075;
    fl_beta_1_routine = 0.6326;
    fl_beta_1_analytical = 0.53894;
   fl_Y_manual = 5.5703;
   fl_Y_routine = 4.6673;
   fl_Y_analytical = 2.5644;
   fl_w1o1_init = 2.263;
   fl_w1o2_init = 2.5991;
   fl_w1o3_init = 3.6533;
   fl_w2o1_init = 1.7636;
    fl_w2o2_init = 2.4062;
    fl_w2o3_init = 2.8429;
    it_data_year = 2010;
    fl_potwrker_1 = 16.4952;
    fl_potwrker_2 = 19.4271;
   bl_skilled = false;
    st_exa_string = "homogeneous rho at 0.34, unskilled";
elseif (it_example_inputs == 4)
   fl_rho_manual = 0.75002424;
   fl_rho_routine = 0.244249613;
   fl_rho_analytical = 0.244249613;
   fl_beta_1_manual = 0.703785173;
    fl_beta_1_routine = 0.687107264;
    fl_beta_1_analytical = 0.706254232;
    fl_Y_manual = 0.124479951;
    fl_Y_routine = 0.39857586;
    fl_Y_analytical = 1.388880655;
    fl_w1o1_init = 5.758649;
    fl_w1o2_init = 6.221019;
```

```
fl_w1o3_init = 7.977073;
    fl_w2o1_init = 2.376239;
    fl_w2o2_init = 4.863073;
    fl_w2o3_init = 5.881686;
    it_data_year = 1996;
    fl_potwrker_1 = 16.4952;
    fl_potwrker_2 = 19.4271;
    bl_skilled = true;
    st_exa_string = "heter rho (0.75, 0.24, 0.24), skilled";
end
mp_params('fl_rho_manual') = fl_rho_manual;
mp_params('fl_rho_routine') = fl_rho_routine;
mp_params('fl_rho_analytical') = fl_rho_analytical;
mp_params('fl_beta_1_manual') = fl_beta_1_manual;
mp_params('fl_beta_1_routine') = fl_beta_1_routine;
mp_params('fl_beta_1_analytical') = fl_beta_1_analytical;
mp_params('fl_Y_manual') = fl_Y_manual;
mp_params('fl_Y_routine') = fl_Y_routine;
mp_params('fl_Y_analytical') = fl_Y_analytical;
mp_data('fl_w1o1_init') = fl_w1o1_init;
mp_data('fl_w1o2_init') = fl_w1o2_init;
mp_data('fl_w1o3_init') = fl_w1o3_init;
mp_data('fl_w2o1_init') = fl_w2o1_init;
mp_data('fl_w2o2_init') = fl_w2o2_init;
mp_data('fl_w2o3_init') = fl_w2o3_init;
mp_data('fl_potwrker_1') = fl_potwrker_1;
mp_data('fl_potwrker_2') = fl_potwrker_2;
it_data_year = it_data_year - 1989;
bl_checkminmax = true;
it_solve_n1n2n3 = 3;
[ar_w1_iter_endo, ar_w2_iter_hat, ar_w2_iter_gap, ...
   mp_wages, mp_fl_labor_demanded, mp_fl_labor_supplied, ...
    mp_fl_labor_occprbty, fl_mse_excess_demand, mp_fl_labor_excess_demand] = ...
    bfw_solveequi_kwfw(mp_params, mp_data, mp_func, mp_controls, ...
    it_solve_n1n2n3, it_data_year, bl_skilled, bl_checkminmax);
disp('');
disp('');
disp(['EXAMPLE ' num2str(it_example_inputs) ', ' st_exa_common_str ', ' char(st_exa_string)]);
ff_container_map_display(mp_wages);
ff_container_map_display(mp_fl_labor_demanded);
ff_container_map_display(mp_fl_labor_supplied);
ff_container_map_display(mp_fl_labor_occprbty);
ff_container_map_display(mp_fl_labor_excess_demand);
```

end

CONTAINER NAME: mp_wages Scalars

| | i | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| 0004 | | | 4 0405 | |
| C001 | 1 | 1 | 1.2165 | |
| C002 | 2 | 2 | 1.8629 | |
| C003 | 3 | 3 | 3.227 | |
| C101 | 4 | 4 | 1.5779 | |
| C102 | 5 | 5 | 1.819 | |
| C103 | 6 | 6 | 3.7951 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_demanded Scalars

| | 1 | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| C001 | 1 | 1 | 1.6514 | |
| C002 | 2 | 2 | 1.0896 | |
| C003 | 3 | 3 | 1.4662 | |
| C101 | 4 | 4 | 4.3057 | |
| C102 | 5 | 5 | 3.1524 | |
| C103 | 6 | 6 | 1.9726 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_supplied Scalars

| | i | idx | value |
|------|---|-----|--------|
| | - | | |
| C001 | 1 | 1 | 1.6514 |
| C002 | 2 | 2 | 1.0896 |
| C003 | 3 | 3 | 1.4662 |
| C101 | 4 | 4 | 4.3057 |
| C102 | 5 | 5 | 3.1524 |
| C103 | 6 | 6 | 1.9726 |
| | | | |

 ${\tt CONTAINER}\ {\tt NAME:}\ {\tt mp_fl_labor_occprbty}\ {\tt Scalars}$

| xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx | | | |
|--------------------------------------|---|-----|----------|
| | i | idx | value |
| | | | |
| | - | | |
| C001 | 1 | 1 | 0.13194 |
| C002 | 2 | 2 | 0.087055 |
| C003 | 3 | 3 | 0.11714 |
| C101 | 4 | 4 | 0.43193 |
| C102 | 5 | 5 | 0.31623 |
| C103 | 6 | 6 | 0.19788 |

CONTAINER NAME: mp_fl_labor_excess_demand Scalars

| | i | idx | value |
|------|---|-----|-------------|
| | - | | |
| C001 | 1 | 1 | -3.4607e-08 |
| C002 | 2 | 2 | -2.3265e-07 |
| C003 | 3 | 3 | 6.268e-07 |
| C101 | 4 | 4 | -2.6645e-15 |
| C102 | 5 | 5 | -2.2204e-15 |
| C103 | 6 | 6 | -2.2204e-16 |

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CONTAINER NAME: mp_wages Scalars

| | i | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| C001 | 1 | 1 | 1.2481 | |
| C002 | 2 | 2 | 1.8712 | |
| C003 | 3 | 3 | 3.1468 | |
| C101 | 4 | 4 | 1.5614 | |
| C102 | 5 | 5 | 1.8288 | |
| C103 | 6 | 6 | 3.8377 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_demanded Scalars

| | i | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| C001 | 1 | 1 | 1.6914 | |
| C002 | 2 | 2 | 1.0934 | |
| C003 | 3 | 3 | 1.4297 | |
| C101 | 4 | 4 | 4.2646 | |
| C102 | 5 | 5 | 3.1707 | |
| C103 | 6 | 6 | 1.9952 | |
| | | | | |

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CONTAINER NAME: mp_fl_labor_supplied Scalars

| | i | idx | value |
|------|---|-----|--------|
| | - | | |
| C001 | 1 | 1 | 1.6914 |
| C002 | 2 | 2 | 1.0934 |
| C003 | 3 | 3 | 1.4297 |
| C101 | 4 | 4 | 4.2646 |
| C102 | 5 | 5 | 3.1707 |
| C103 | 6 | 6 | 1.9952 |

CONTAINER NAME: mp_fl_labor_occprbty Scalars

| ************ | YYYYY |
|--------------|--------------|
| | |

| | i | idx | value | |
|------|---|-----|----------|--|
| | - | | | |
| C001 | 1 | 1 | 0.13513 | |
| C002 | 2 | 2 | 0.087358 | |
| C003 | 3 | 3 | 0.11423 | |
| C101 | 4 | 4 | 0.42779 | |
| C102 | 5 | 5 | 0.31807 | |
| C103 | 6 | 6 | 0.20015 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_excess_demand Scalars

| | i | idx | value |
|------|---|-----|-------------|
| | - | | |
| C001 | 1 | 1 | -9.373e-09 |
| C002 | 2 | 2 | -1.9675e-07 |
| C003 | 3 | 3 | 3.6084e-07 |
| C101 | 4 | 4 | -8.8818e-16 |
| C102 | 5 | 5 | 1.3323e-15 |
| C103 | 6 | 6 | -2.2204e-16 |
| | | | |

CONTAINER NAME: mp_wages Scalars

| | i | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| C001 | 1 | 1 | 1.5675 | |
| C002 | 2 | 2 | 2.5998 | |
| C003 | 3 | 3 | 3.0763 | |
| C101 | 4 | 4 | 1.9027 | |
| C102 | 5 | 5 | 2.7234 | |
| C103 | 6 | 6 | 3.72 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_demanded Scalars

| | i | idx | value |
|------|---|-----|--------|
| | - | | |
| C001 | 1 | 1 | 3.9729 |
| C002 | 2 | 2 | 2.8316 |
| C003 | 3 | 3 | 2.6363 |
| C101 | 4 | 4 | 6.6763 |
| C102 | 5 | 5 | 6.0249 |
| C103 | 6 | 6 | 2.5039 |

CONTAINER NAME: mp_fl_labor_supplied Scalars

i idx value

- ---

| C001 | 1 | 1 | 3.9729 | |
|------|---|---|--------|--|
| C002 | 2 | 2 | 2.8316 | |
| C003 | 3 | 3 | 2.6363 | |
| C101 | 4 | 4 | 6.6763 | |
| C102 | 5 | 5 | 6.0249 | |
| C103 | 6 | 6 | 2.5039 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_occprbty Scalars

| | | i | idx | value |
|---|------|---|-----|---------|
| | | - | | |
| (| C001 | 1 | 1 | 0.2045 |
| (| 0002 | 2 | 2 | 0.14575 |
| (| 0003 | 3 | 3 | 0.1357 |
| (| C101 | 4 | 4 | 0.40474 |
| (| C102 | 5 | 5 | 0.36525 |
| (| C103 | 6 | 6 | 0.1518 |
| | | | | |

CONTAINER NAME: mp_fl_labor_excess_demand Scalars

| | 1 | ıdx | value |
|------|---|-----|-------------|
| | - | | |
| C001 | 1 | 1 | 8.8193e-08 |
| C002 | 2 | 2 | 6.1579e-07 |
| C003 | 3 | 3 | -1.2231e-06 |
| C101 | 4 | 4 | -3.5527e-15 |
| C102 | 5 | 5 | 1.7764e-15 |
| C103 | 6 | 6 | 0 |

CONTAINER NAME: mp_wages Scalars

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| | i | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| C011 | 1 | 1 | 2.2661 | |
| | - | - | | |
| C012 | 2 | 2 | 5.3853 | |
| C013 | 3 | 3 | 6.7077 | |
| C111 | 4 | 4 | 3.5562 | |
| C112 | 5 | 5 | 6.838 | |
| C113 | 6 | 6 | 9.4355 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_demanded Scalars

| | i | idx | value |
|------|---|-----|----------|
| | - | | |
| C011 | 1 | 1 | 0.032483 |
| C012 | 2 | 2 | 0.23898 |

| C013 | 3 | 3 | 0.83121 |
|------|---|---|---------|
| C111 | 4 | 4 | 0.1707 |
| C112 | 5 | 5 | 0.49335 |
| C113 | 6 | 6 | 1.6895 |
| | | | |

CONTAINER NAME: mp_fl_labor_supplied Scalars

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| | i | idx | value | |
|------|---|-----|----------|--|
| | - | | | |
| C011 | 1 | 1 | 0.032483 | |
| C012 | 2 | 2 | 0.23898 | |
| C013 | 3 | 3 | 0.83121 | |
| C111 | 4 | 4 | 0.1707 | |
| C112 | 5 | 5 | 0.49335 | |
| C113 | 6 | 6 | 1.6895 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_occprbty Scalars

| | i | idx | value | |
|------|---|-----|----------|--|
| | - | | | |
| C011 | 1 | 1 | 0.018322 | |
| C012 | 2 | 2 | 0.1348 | |
| C013 | 3 | 3 | 0.46886 | |
| C111 | 4 | 4 | 0.068174 | |
| C112 | 5 | 5 | 0.19703 | |
| C113 | 6 | 6 | 0.67473 | |
| | | | | |

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CONTAINER NAME: mp_fl_labor_excess_demand Scalars

| | i | idx | value |
|------|---|-----|-------------|
| | - | | |
| C011 | 1 | 1 | -1.8041e-09 |
| C012 | 2 | 2 | 5.6774e-08 |
| C013 | 3 | 3 | 8.1332e-08 |
| C111 | 4 | 4 | -2.7756e-17 |
| C112 | 5 | 5 | 5.5511e-17 |
| C113 | 6 | 6 | 2.2204e-16 |

7.2 Equilibrium W to Q to W Contraction By Skill Group

This is the example vignette for function: bfw_solveequi_w2q2w from the PrjLabEquiBFW Package.

7.2.1 Default

```
[mp_fl_labor_occprbty,mp_fl_labor_supplied] = bfw_solveequi_w2q2w();
```

```
ITER:;it_speed_shifter_ctr=1;it_equi_wage_ctr=1;bl_continue=1;fl_ds_gap_mse=1.0294;fl_total_wage_cha
    2.9507    2.8632    5.2962
    1.7458    2.4472    3.9586

4.2925    3.7644    1.5416
    2.2735    1.6222    1.3410
```

```
3.9933
                                  2.9733
                                                            1.8551
         2.1150
                                  1.2813
                                                            1.6136
ITER:;it_speed_shifter_ctr=1;it_equi_wage_ctr=2;bl_continue=1;fl_ds_gap_mse=0.62115;fl_total_wage_ch
         2.0535
                                  2.6792
                                                          5.8550
                                   2.3313
                                                            4.0597
         1.4375
         4.9024
                                  3.0389
                                                        1.6928
         2.1150 1.2813 1.6136
         4.1907
                                   2.9908 1.7891
          1.8080
                                 1.2610
                                                        1.7054
ITER:;it_speed_shifter_ctr=1;it_equi_wage_ctr=10;bl_continue=1;fl_ds_gap_mse=0.0075186;fl_total_wage
         1.5739
                                  1.8511
                                                          3.9011
         1.2165
                                  1.8810
                                                           3.2705
         4.3801
                                  3.1280
                                                        1.9299
         1.6748
                                  1.0915
                                                        1.4595
         4.3088
                                   3.1446
                                                            1.9595
          1.6475
                                   1.0973
                                                            1.4818
ITER:;it_speed_shifter_ctr=1;it_equi_wage_ctr=20;bl_continue=1;fl_ds_gap_mse=6.4007e-05;fl_total_wage_shifter_ctr=1;it_equi_wage_ctr=20;bl_continue=1;fl_ds_gap_mse=6.4007e-05;fl_total_wage_shifter_ctr=1;it_equi_wage_ctr=20;bl_continue=1;fl_ds_gap_mse=6.4007e-05;fl_total_wage_shifter_ctr=1;it_equi_wage_shifter_ctr=1;it_equi_wage_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shifter_shif
          1.5762
                                 1.8205 3.8023
          1.2159
                                  1.8637
                                                           3.2298
         4.3126
                                   3.1498 1.9685
         1.6528
                                  1.0893
                                                           1.4649
         4.3065
                                   3.1520
                                                           1.9717
          1.6505
                                   1.0900
                                                            1.4673
ITER:;it_speed_shifter_ctr=1;it_equi_wage_ctr=30;bl_continue=1;fl_ds_gap_mse=6.0214e-07;fl_total_wag
         1.5778
                                 1.8191
                                                          3.7958
                                   1.8629
         1.2164
                                                            3.2273
         4.3064
                                   3.1522
                                                           1.9722
                                                        1.4660
         1.6515
                                 1.0896
         4.3058
                                   3.1524 1.9726
         1.6513
                                 1.0897
                                                          1.4663
ITER:;it_speed_shifter_ctr=1;it_equi_wage_ctr=39;bl_continue=0;fl_ds_gap_mse=9.1058e-09;fl_total_wag
         1.5780
                                 1.8190
                                                          3.7950
         1.2165
                                 1.8628 3.2270
         4.3057
                                  3.1524
                                                         1.9727
         1.6514
                                  1.0896
                                                        1.4662
                                                            1.9727
         4.3057
                                   3.1524
          1.6514
                                   1.0896
                                                            1.4662
```

CONTAINER NAME: mp_wages Scalars

| | i | idx | value |
|------|---|-----|--------|
| | - | | |
| C001 | 1 | 1 | 1.2165 |
| C002 | 2 | 2 | 1.8628 |
| C003 | 3 | 3 | 3.227 |
| C101 | 4 | 4 | 1.578 |
| C102 | 5 | 5 | 1.819 |
| C103 | 6 | 6 | 3.795 |
| | | | |

xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx

| | 1 | ıdx | value |
|------|---|-----|--------|
| | - | | |
| C001 | 1 | 1 | 1.6514 |
| C002 | 2 | 2 | 1.0896 |
| C003 | 3 | 3 | 1.4662 |
| C101 | 4 | 4 | 4.3057 |
| C102 | 5 | 5 | 3.1524 |
| C103 | 6 | 6 | 1.9727 |

CONTAINER NAME: mp_fl_labor_demanded Scalars

| | 1 | idx | value |
|------|---|-----|--------|
| | - | | |
| C001 | 1 | 1 | 1.6514 |
| C002 | 2 | 2 | 1.0896 |
| C003 | 3 | 3 | 1.4662 |
| C101 | 4 | 4 | 4.3057 |
| C102 | 5 | 5 | 3.1524 |
| C103 | 6 | 6 | 1.9727 |
| | | | |

7.2.2 Vary Parameters, Solve Equilibrium Quantities Wages, W to Q to W Contraction

```
% 2. Get Parameters and data
bl_log_wage = true;
bl_verbose_nest = false;

% Get Parameters
mp_params = bfw_mp_param_esti(bl_log_wage);
mp_param_aux = bfw_mp_param_aux(bl_verbose_nest);
mp_params = [mp_params ; mp_param_aux];

% Get Data
mp_data = bfw_mp_data(bl_verbose_nest);

% Get Functions
mp_func_demand = bfw_mp_func_demand(bl_verbose_nest);
mp_func_supply = bfw_mp_func_supply(bl_log_wage, bl_verbose_nest);
mp_func_equi = bfw_mp_func_equi(bl_verbose_nest);
mp_func = [mp_func_equi; mp_func_supply; mp_func_demand];
```

```
% Get Controls
mp_controls = bfw_mp_control();
mp_controls('bl_bfw_solveequi_w2q2w_display') = false;
mp_controls('bl_bfw_solveequi_w2q2w_display_verbose') = false;
st_exa_common_str = 'bfw_solveequi_w2q2w()';
for it_example_inputs = [1,2,3,4]
    % Different testing scenariors
    if (it_example_inputs == 1)
        fl_rho_manual = 0.18;
        fl_rho_routine = 0.18;
        fl_rho_analytical = 0.18;
        fl_beta_1_manual = 1 - 0.26;
        fl_beta_1_routine = 1 - 0.30;
        fl_beta_1_analytical = 1 - 0.40;
        fl_Y_manual = 3.4084;
        fl_Y_routine = 2.3402;
        fl_Y_analytical = 1.7552;
        fl_w1o1_init = 2.315707;
        fl_w1o2_init = 3.217799;
        fl_w1o3_init = 4.329016;
        fl_w2o1_init = 1.942;
        fl_w2o2_init = 3.2247;
        fl_w2o3_init = 3.3738;
        it_data_year = 1989;
        fl_potwrker_1 = 9.9687;
        fl_potwrker_2 = 12.5164;
        bl_skilled = false;
        st_exa_string = "homogeneous rho at 0.18, unskilled";
    elseif (it_example_inputs == 2)
        fl_rho_manual = 0.64678;
        fl_rho_routine = 0.64678;
        fl_rho_analytical = 0.64678;
        fl_beta_1_manual = 0.63427;
        fl_beta_1_routine = 0.58738;
        fl_beta_1_analytical = 0.5784;
        fl_Y_manual = 3.2291;
        fl_Y_routine = 2.2223;
        fl_Y_analytical = 1.7487;
        fl_w1o1_init = 2.3157;
        fl_w1o2_init = 3.2178;
        fl_w1o3_init = 4.329;
        fl_w2o1_init = 1.942;
        fl_w2o2_init = 3.2247;
        fl_w2o3_init = 3.3738;
```

```
it_data_year = 1989;
   fl_potwrker_1 = 9.9687;
   fl_potwrker_2 = 12.5164;
   bl_skilled = false;
   st_exa_string = "homogeneous rho at 0.64, unskilled";
elseif (it_example_inputs == 3)
   fl_rho_manual = 0.34186;
   fl_rho_routine = 0.34186;
   fl_rho_analytical = 0.34186;
   fl_beta_1_manual = 0.63075;
   fl_beta_1_routine = 0.6326;
   fl_beta_1_analytical = 0.53894;
   fl_Y_manual = 5.5703;
   fl_Y_routine = 4.6673;
   fl_Y_analytical = 2.5644;
   fl_w1o1_init = 2.263;
   fl_w1o2_init = 2.5991;
   fl_w1o3_init = 3.6533;
   fl w2o1 init = 1.7636;
   fl_w2o2_init = 2.4062;
   fl_w2o3_init = 2.8429;
   it_data_year = 2010;
   fl_potwrker_1 = 16.4952;
   fl_potwrker_2 = 19.4271;
   bl_skilled = false;
   st_exa_string = "homogeneous rho at 0.34, unskilled";
elseif (it_example_inputs == 4)
   fl_rho_manual = 0.75002424;
   fl_rho_routine = 0.244249613;
   fl_rho_analytical = 0.244249613;
   fl_beta_1_manual = 0.703785173;
   fl_beta_1_routine = 0.687107264;
   fl_beta_1_analytical = 0.706254232;
   fl_Y_manual = 0.124479951;
   fl_Y_routine = 0.39857586;
   fl_Y_analytical = 1.388880655;
   fl_w1o1_init = 5.758649;
   fl_w1o2_init = 6.221019;
   fl_w1o3_init = 7.977073;
   fl_w2o1_init = 2.376239;
   fl_w2o2_init = 4.863073;
   fl_w2o3_init = 5.881686;
```

```
it_data_year = 1996;
       fl_potwrker_1 = 16.4952;
       fl_potwrker_2 = 19.4271;
       bl_skilled = true;
       st_exa_string = "heter rho (0.75, 0.24, 0.24), skilled";
   end
   mp_params('fl_rho_manual') = fl_rho_manual;
   mp_params('fl_rho_routine') = fl_rho_routine;
   mp_params('fl_rho_analytical') = fl_rho_analytical;
   mp_params('fl_beta_1_manual') = fl_beta_1_manual;
   mp_params('fl_beta_1_routine') = fl_beta_1_routine;
   mp_params('fl_beta_1_analytical') = fl_beta_1_analytical;
   mp_params('fl_Y_manual') = fl_Y_manual;
   mp_params('fl_Y_routine') = fl_Y_routine;
   mp_params('fl_Y_analytical') = fl_Y_analytical;
   mp_data('fl_w1o1_init') = fl_w1o1_init;
   mp_data('fl_w1o2_init') = fl_w1o2_init;
   mp_data('fl_w1o3_init') = fl_w1o3_init;
   mp_data('fl_w2o1_init') = fl_w2o1_init;
   mp_data('fl_w2o2_init') = fl_w2o2_init;
   mp_data('fl_w2o3_init') = fl_w2o3_init;
   mp_data('fl_potwrker_1') = fl_potwrker_1;
   mp_data('fl_potwrker_2') = fl_potwrker_2;
   it_data_year = it_data_year - 1989;
   bl_checkminmax = true;
   it_solve_n1n2n3 = 3;
   [~, ~, ~, ~, ~, ~, ~, ~, ~, ...
       mp_wages, mp_fl_labor_demanded, mp_fl_labor_supplied, ...
       mp_fl_labor_occprbty] = ...
       bfw_solveequi_w2q2w(mp_params, mp_data, mp_func, mp_controls, ...
       it_solve_n1n2n3, it_data_year, bl_skilled, bl_checkminmax);
   disp('');
   disp('');
   disp(['EXAMPLE ' num2str(it_example_inputs) ', ' st_exa_common_str ', ' char(st_exa_string)]);
   ff_container_map_display(mp_wages);
   ff_container_map_display(mp_fl_labor_demanded);
   ff_container_map_display(mp_fl_labor_supplied);
   ff_container_map_display(mp_fl_labor_occprbty);
end
```

CONTAINER NAME: mp_wages Scalars

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| | | | |
|------|---|-----|--------|
| | i | idx | value |
| | - | | |
| | | | |
| C001 | 1 | 1 | 1.2165 |
| C002 | 2 | 2 | 1.8628 |
| C003 | 3 | 3 | 3.227 |
| C101 | 4 | 4 | 1.578 |
| C102 | 5 | 5 | 1.819 |
| C103 | 6 | 6 | 3.795 |
| | | | |

CONTAINER NAME: mp_fl_labor_demanded Scalars

| | i | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| C001 | 1 | 1 | 1.6514 | |
| C002 | 2 | 2 | 1.0896 | |
| C003 | 3 | 3 | 1.4662 | |
| C101 | 4 | 4 | 4.3057 | |
| C102 | 5 | 5 | 3.1524 | |
| C103 | 6 | 6 | 1.9727 | |
| | | | | |

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 ${\tt CONTAINER} \ {\tt NAME:} \ {\tt mp_fl_labor_supplied} \ {\tt Scalars}$

CONTAINER NAME: mp_fl_labor_occprbty Scalars

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| | i | idx | value |
|------|---|-----|----------|
| | - | | |
| C001 | 1 | 1 | 0.13194 |
| C002 | 2 | 2 | 0.087055 |
| C003 | 3 | 3 | 0.11714 |
| C101 | 4 | 4 | 0.43193 |
| C102 | 5 | 5 | 0.31623 |
| C103 | 6 | 6 | 0.19788 |

CONTAINER NAME: mp_wages Scalars

| *************************************** |
|---|
| |

| | i | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| C001 | 1 | 1 | 1.2482 | |
| C002 | 2 | 2 | 1.8713 | |
| C003 | 3 | 3 | 3.1469 | |
| C101 | 4 | 4 | 1.5614 | |
| C102 | 5 | 5 | 1.8289 | |
| C103 | 6 | 6 | 3.8378 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_demanded Scalars

| | i | idx | value |
|------|---|-----|--------|
| | - | | |
| C001 | 1 | 1 | 1.6914 |
| C002 | 2 | 2 | 1.0934 |
| C003 | 3 | 3 | 1.4297 |
| C101 | 4 | 4 | 4.2646 |
| C102 | 5 | 5 | 3.1708 |
| C103 | 6 | 6 | 1.9952 |
| | | | |

CONTAINER NAME: mp_fl_labor_supplied Scalars

| | i | idx | value |
|------|---|-----|--------|
| | - | | |
| C001 | 1 | 1 | 1.6914 |
| C002 | 2 | 2 | 1.0934 |
| C003 | 3 | 3 | 1.4297 |
| C101 | 4 | 4 | 4.2645 |
| C102 | 5 | 5 | 3.1707 |
| C103 | 6 | 6 | 1.9952 |

CONTAINER NAME: mp_fl_labor_occprbty Scalars

| | i | idx | value |
|------|---|-----|----------|
| | - | | |
| C001 | 1 | 1 | 0.13514 |
| C002 | 2 | 2 | 0.087359 |
| C003 | 3 | 3 | 0.11423 |
| C101 | 4 | 4 | 0.42779 |
| C102 | 5 | 5 | 0.31807 |
| C103 | 6 | 6 | 0.20014 |

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CONTAINER NAME: mp_wages Scalars

i idx value

- --- -----

| C001 | 1 | 1 | 1.5675 | |
|------|---|---|--------|--|
| C002 | 2 | 2 | 2.5998 | |
| C003 | 3 | 3 | 3.0763 | |
| C101 | 4 | 4 | 1.9027 | |
| C102 | 5 | 5 | 2.7234 | |
| C103 | 6 | 6 | 3.72 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_demanded Scalars

| | i | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| C001 | 1 | 1 | 3.9729 | |
| C002 | 2 | 2 | 2.8316 | |
| C003 | 3 | 3 | 2.6364 | |
| C101 | 4 | 4 | 6.6763 | |
| C102 | 5 | 5 | 6.0249 | |
| C103 | 6 | 6 | 2.5039 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_supplied Scalars

| | i | idx | value | |
|------|---|-----|--------|--|
| | - | | | |
| C001 | 1 | 1 | 3.9729 | |
| C002 | 2 | 2 | 2.8316 | |
| C003 | 3 | 3 | 2.6363 | |
| C101 | 4 | 4 | 6.6763 | |
| C102 | 5 | 5 | 6.0249 | |
| C103 | 6 | 6 | 2.5039 | |
| | | | | |

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CONTAINER NAME: mp_fl_labor_occprbty Scalars

| | i | idx | value |
|------|---|-----|---------|
| | - | | |
| C001 | 1 | 1 | 0.2045 |
| C002 | 2 | 2 | 0.14576 |
| C003 | 3 | 3 | 0.1357 |
| C101 | 4 | 4 | 0.40474 |
| C102 | 5 | 5 | 0.36525 |
| C103 | 6 | 6 | 0.1518 |

 ${\tt EXAMPLE~4,~bfw_solveequi_w2q2w(),~heter~rho~(0.75,~0.24,~0.24),~skilled}$

CONTAINER NAME: mp_wages Scalars

| | i | idx | value |
|------|---|-----|--------|
| | - | | |
| C011 | 1 | 1 | 2.2661 |
| C012 | 2 | 2 | 5.3851 |

| C013 | 3 | 3 | 6.7078 | |
|------|---|---|--------|--|
| C111 | 4 | 4 | 3.5562 | |
| C112 | 5 | 5 | 6.8374 | |
| C113 | 6 | 6 | 9.4358 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_demanded Scalars

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| | i | idx | : value | |
|------|-----|-----|----------|--|
| | - | | | |
| C01: | 1 1 | 1 | 0.032483 | |
| C012 | 2 2 | 2 | 0.23899 | |
| C013 | 3 3 | 3 | 0.8312 | |
| C11: | 1 4 | 4 | 0.1707 | |
| C112 | 2 5 | 5 | 0.49341 | |
| C113 | 3 6 | 6 | 1.6894 | |
| | | | | |

CONTAINER NAME: mp_fl_labor_supplied Scalars

idx i value - ---

 C011
 1
 1
 0.032483

 C012
 2
 2
 0.23897

 C013
 3
 3
 0.83122

 C111
 4
 4
 0.1707

 C112
 5
 5
 0.49336

 C113
 6
 6
 1.6895

 ${\tt CONTAINER} \ {\tt NAME:} \ {\tt mp_fl_labor_occprbty} \ {\tt Scalars}$

| | 1 | ıdx | value |
|------|---|-----|----------|
| | - | | |
| C011 | 1 | 1 | 0.018322 |
| C012 | 2 | 2 | 0.13479 |
| C013 | 3 | 3 | 0.46886 |
| C111 | 4 | 4 | 0.068174 |
| C112 | 5 | 5 | 0.19704 |
| C113 | 6 | 6 | 0.67473 |
| | | | |

Appendix A

Index and Code Links

A.1 Introduction links

- 1. The Labor Demand and Supply Problem: mlx | m | pdf | html
 - The Labor Demand and Supply Problem

A.2 Core Functions links

- 1. CES Demand Core Functions: $mlx \mid m \mid pdf \mid html$
 - This function generates a container map with key CES demand-side equation for a particular sub-nest.
 - PrjLabEquiBFW: bfw_mp_func_demand()
- 2. Multinomial Logit Core Functions: mlx | m | pdf | html
 - This function generates a container map with key multinomial logit supply-side equations.
 - PrjLabEquiBFW: bfw_mp_func_supply()
- 3. Equilibrium Core Functions: mlx | m | pdf | html
 - This function generates a container map with key equilibrium equations.
 - PrjLabEquiBFW: bfw mp func equi()

A.3 Parameters links

- 1. bfwx_mp_path: $\mathbf{mlx} \mid \mathbf{m} \mid \mathbf{pdf} \mid \mathbf{html}$
 - bfw mp path
 - PrjLabEquiBFW: bfw_mp_path()
- 2. bfwx_mp_control: mlx | m | pdf | html
 - bfw_mp_control
 - PrjLabEquiBFW: bfw_mp_control()
- 3. bfw_mp_param_esti: $mlx \mid m \mid pdf \mid html$
 - $\bullet \quad bfw_mp_param_esti$
 - PrjLabEquiBFW: bfw_mp_param_esti()

A.4 Data links

- 1. $bfwx_mp_data: mlx \mid m \mid pdf \mid html$
 - bfw mp data
 - PrjLabEquiBFW: bfw mp data()

A.5 Demand links

1. Solve Nested CES Optimal Demand (CRS): mlx | m | pdf | html

- This function solves optimal choices given CES production function under cost minimization.
- Works with Constant Elasticity of Substitution problems with constant returns, up to four nest layers, and two inputs in each sub-nest.
- Takes as inputs share and elasticity parameters across layers of sub-nests, as well as input unit costs at the bottom-most layer.
- Works with Constant Elasticity of Substitution problems with constant returns, up to four nest layers, and two inputs in each sub-nest.
- PrjLabEquiBFW: bfw crs nested ces()
- 2. Compute Nested CES MPL Given Demand (CRS): mlx | m | pdf | html
 - Given labor quantity demanded, using first-order relative optimality conditions, find the marginal product of labor given CES production function.
 - Takes as inputs share and elasticity parameters across layers of sub-nests, as well as quantity demanded at each bottom-most CES nest layer.
 - Works with Constant Elasticity of Substitution problems with constant returns, up to four nest layers, and two inputs in each sub-nest.
 - Allows for uneven branches, so that some branches go up to four layers, but others have less layers, works with BFW (2022) nested labor input problem.
 - PrjLabEquiBFW: bfw crs nested ces mpl()

A.6 Supply links

- 1. bfwx_mlogit: mlx | m | pdf | html
 - bfwx mlogit
 - PrjLabEquiBFW: bfwx_mlogit()

A.7 Equilibrium by Skill Nest Group links

- 1. bfw_solveequi_kwfw: mlx | m | pdf | html
 - $\bullet \quad bfw_solveequi_kwfw$
 - PrjLabEquiBFW: bfw_solveequi_kwfw()
- 2. $bfw_solvequi_w2q2w: mlx \mid m \mid pdf \mid html$
 - bfw_solveequi_w2q2w
 - PrjLabEquiBFW: bfw_solveequi_w2q2w()

Bibliography

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