Find the Closest Point Along a Line to Another Point

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2021-06-25

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Find Nearest 1

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Neart Point Along a Line Through Orgin to Another Point

We first have X_1 an Y_1 , given these, we are able to generate $R = \frac{X_2}{Y_2}$, a ratio. We want to iteratively update X_1 and X_2 , but we only know the ratio. Think of R as a line through the origin with R as the slope.

We generate X_2 and Y_2 by finding the point along the R as slope origin line that is the closest to the X_1 and Y_1 . At the resulting point, R will be respected, and it will differ least in distance to the earlier iteration's X_1 and Y_1 points.

- 1. The slope of the diagonal line is $-\frac{Y_2}{X_2} = -\frac{1}{R}$ 2. The diagonal line must cross X_1 and Y_1 , solve for this line's y-intercept
- 3. Solve for the intersection of the diagonal line and the origin line with R as slope

Implementing step (2):

$$Y_1 = I - \frac{Y_2}{X_2} \cdot X_1$$

$$I = Y_1 + \frac{X_1}{R}$$

$$I = \frac{Y_1 \cdot R + X_1}{R}$$

Implementing step (3):

$$Y = \frac{Y_1 \cdot R + X_1}{R} - \frac{1}{R} \cdot X$$

$$Y = R \cdot X$$

$$R \cdot X = \frac{Y_1 \cdot R + X_1}{R} - \frac{1}{R} \cdot X$$

$$\left(R + \frac{1}{R}\right) \cdot X = \frac{Y_1 \cdot R + X_1}{R}$$

$$\frac{R^2 + 1}{R} \cdot X = \frac{Y_1 \cdot R + X_1}{R}$$

$$X = \frac{Y_1 \cdot R + X_1}{R} \cdot \frac{R}{R^2 + 1}$$

And we have:

$$X = \frac{Y_1 \cdot R + X_1}{R^2 + 1}$$

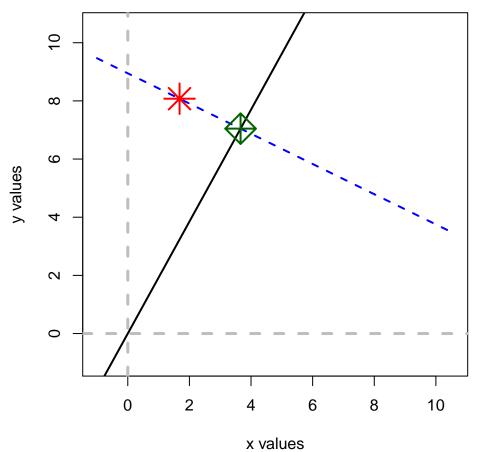
$$Y = \frac{Y_1 \cdot R^2 + X_1 \cdot R}{R^2 + 1}$$

Visualize the results:

```
# Set random parameter Values for X1, Y1, and X2/Y2 ratio
set.seed(3)
fl_x1 <- runif(1) * 10
fl_y1 <- runif(1) * 10
fl_r <- runif(1) * 5
# Diaganol
fl_diag_slope <- -1 / fl_r
fl_diag_yintercept <- (fl_y1 * fl_r + fl_x1) / fl_r</pre>
# Closest point
fl_x2 \leftarrow (fl_y1 * fl_r + fl_x1) / (fl_r^2 + 1)
fl_y2 \leftarrow (fl_y1 * fl_r^2 + fl_x1 * fl_r) / (fl_r^2 + 1)
# Print state
print(paste("x1=", fl_x1, "x2=", fl_x2, "R=", fl_r, sep = " "))
## [1] "x1= 1.68041526339948 x2= 3.6609038475849 R= 1.92471175687388"
print(paste("x2=", fl_x2, "y2=", fl_y2, sep = " "))
## [1] "x2= 3.6609038475849 y2= 7.04618467623146"
# X and y lims
ar_xylim \leftarrow c(-1, max(fl_x1, fl_y2) * 1.5)
# Visualize
par(mfrow = c(1, 1))
# Line through origin
curve(0 + fl_r * x, ar_xylim[1], ar_xylim[2],
 col = "black", lwd = 2, lty = 1,
 ylim = ar_xylim,
 ylab = "", xlab = ""
# Diaganol line
```

```
curve(fl_diag_yintercept + fl_diag_slope * x,
 add = TRUE,
 col = "blue", lwd = 2, lty = 2,
 ylim = ar_xylim,
 ylab = "", xlab = ""
# Point
points(fl_x1, fl_y1,
 add = TRUE,
pch = 8, col = "red", cex = 3, lwd = 2,
 ylab = "", xlab = ""
points(fl_x2, fl_y2,
add = TRUE,
pch = 9, col = "darkgreen", cex = 3, lwd = 2,
 ylab = "", xlab = ""
# Origin lines
abline(
v = 0, h = 0,
col = "gray", lwd = 3, lty = 2
# Titles
title(
 main = paste0(
   "Line through origin and orthogonal line\n",
   "Find closest point along black line to red star"
 ),
 sub = paste0(
   "Black line goes through origin,",
  " blue line goes through (x1,y1) and (x2, y2)"
 ),
 xlab = "x values", ylab = "y values"
)
```

Line through origin and orthogonal line Find closest point along black line to red star



Black line goes through origin, blue line goes through (x1,y1) and (x2,