Inequality in Environmental Exposure Across Population Groups

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1 Location, Population, and Pollution

Go to the RMD, R, PDF, or HTML version of this file. Go back to fan's REconTools Package, R Code Examples Repository (bookdown site), or Intro Stats with R Repository (bookdown site).

1.1 Simulate Population Distribution over Location and Demographics

Use the binomial distribution to generate heterogenous demographic break-down by location. There are N demographic cells, and the binomial distribution provides the probability mass in each of the N cell. Different bernoulli "win" chance for each location. There is also probability distribution over population in each location.

First, construct empty population share dataframe:

```
# 7 different age groups and 12 different locationso
it_N_pop_groups <- 7
it_M_location <- 12
# Matrix of demographics by location
mt_pop_data_frac <- matrix(data=NA, nrow=it_M_location, ncol=it_N_pop_groups)
colnames(mt_pop_data_frac) <- pasteO('popgrp', seq(1,it_N_pop_groups))
rownames(mt_pop_data_frac) <- pasteO('location', seq(1,it_M_location))
# Display
mt_pop_data_frac %>% kable() %>% kable_styling_fc()
```

Second, generate conditional population distribution for each location, and then multiply by the share of population in each locality:

```
# Share of population per location
set.seed(123)
ar_p_loc <- dbinom(0:(3*it_M_location-1), 3*it_M_location-1, 0.5)
it_start <- length(ar_p_loc)/2-it_M_location/2
ar_p_loc <- ar_p_loc[it_start:(it_start+it_M_location+1)]
ar_p_loc <- ar_p_loc/sum(ar_p_loc)</pre>
```

	popgrp1	popgrp2	popgrp3	popgrp4	popgrp5	popgrp6	popgrp7
location1	NA						
location2	NA						
location3	NA						
location4	NA						
location5	NA						
location6	NA						
location7	NA						
location8	NA						
location9	NA						
location10	NA						
location11	NA						
location12	NA						

```
# Different bernoulli "win" probability for each location
set.seed(234)
# ar_fl_unif_prob <- sort(runif(it_M_location)*(0.25)+0.4)
ar_fl_unif_prob <- sort(runif(it_M_location))
# Generate population proportion by locality
for (it_loc in 1:it_M_location) {
    ar_p_pop_condi_loc <- dbinom(0:(it_N_pop_groups-1), it_N_pop_groups-1, ar_fl_unif_prob[it_loc])
    mt_pop_data_frac[it_loc,] <- ar_p_pop_condi_loc*ar_p_loc[it_loc]
}
# Sum of cells, should equal to 1
print(paste0('pop frac sum = ', sum(mt_pop_data_frac)))
## [1] "pop frac sum = 0.962953679726938"
# Display
round(mt_pop_data_frac*100, 2) %>%
    kable(caption='Share of population in each location and demographic cell') %>%
    kable_styling_fc()
```

Share of population in each location and demographic cell

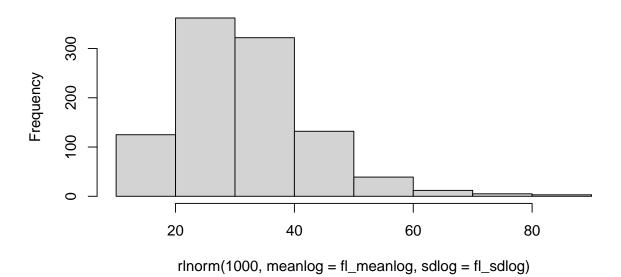
	popgrp1	popgrp2	popgrp3	popgrp4	popgrp5	popgrp6	popgrp7
location1	1.09	0.13	0.01	0.00	0.00	0.00	0.00
location2	1.63	0.70	0.13	0.01	0.00	0.00	0.00
location3	0.59	1.40	1.39	0.74	0.22	0.03	0.00
location4	0.06	0.43	1.29	2.09	1.90	0.92	0.19
location5	0.07	0.55	1.73	2.89	2.71	1.36	0.28
location6	0.02	0.26	1.19	2.89	3.93	2.85	0.86
location7	0.01	0.10	0.66	2.23	4.26	4.33	1.83
location8	0.00	0.06	0.47	1.83	4.03	4.72	2.31
location9	0.00	0.03	0.27	1.26	3.28	4.55	2.63
location10	0.00	0.02	0.20	0.96	2.57	3.68	2.19
location11	0.00	0.00	0.00	0.04	0.40	2.05	4.38
location12	0.00	0.00	0.00	0.02	0.24	1.28	2.82

1.2 Simulate Environmental Exposure

Use log-normal distribution to describe average daily PM10 exposures distribution by locality:

```
fl_meanlog <- 3.4
fl_sdlog <- 0.35
hist(rlnorm(1000, meanlog = fl_meanlog, sdlog = fl_sdlog))</pre>
```

Histogram of rlnorm(1000, meanlog = fl_meanlog, sdlog = fl_sdlog)



First, draw pollution measure for each locality:

```
# draw
set.seed(123)
ar_pollution_loc <- rlnorm(it_M_location, meanlog = fl_meanlog, sdlog = fl_sdlog)
# pollution dataframe
# 5 by 3 matrix

# Column Names
ar_st_varnames <- c('location','avgdailypm10')

# Combine to tibble, add name col1, col2, etc.
tb_loc_pollution <- as_tibble(ar_pollution_loc) %>%
    rowid_to_column(var = "id") %>%
    rename_all(~c(ar_st_varnames)) %>%
    mutate(location = pasteO('location', location))

# Display
kable(tb_loc_pollution) %>% kable_styling_fc()
```

Second, reshape population data:

```
# Reshape population data, so each observation is location/demo
df_pop_data_frac_long <- as_tibble(mt_pop_data_frac, rownames='location') %>%
```

location	avgdailypm10
location1	24.62676
location2	27.64481
location3	51.70466
location4	30.71275
location5	31.35114
location6	54.61304
location7	35.20967
location8	19.24456
location9	23.56121
location10	25.63653
location11	45.99021
location12	33.98553

Third, join with pollution data:

```
# Reshape population data, so each observation is location/demo
df_pop_pollution_long <- df_pop_data_frac_long %>%
    left_join(tb_loc_pollution, by='location')

# display
df_pop_pollution_long[1:round(it_N_pop_groups*2.5),] %>% kable() %>% kable_styling_fc()
```

location	popgrp	pop_frac	avgdailypm10
location1	1	0.0109366	24.62676
location1	2	0.0013417	24.62676
location1	3	0.0000686	24.62676
location1	4	0.0000019	24.62676
location1	5	0.0000000	24.62676
location1	6	0.0000000	24.62676
location1	7	0.0000000	24.62676
location2	1	0.0163003	27.64481
location2	2	0.0070132	27.64481
location2	3	0.0012573	27.64481
location2	4	0.0001202	27.64481
location2	5	0.0000065	27.64481
location2	6	0.0000002	27.64481
location2	7	0.0000000	27.64481
location3	1	0.0058760	51.70466
location3	2	0.0140000	51.70466
location3	3	0.0138984	51.70466
location3	4	0.0073587	51.70466

1.3 Compute Demographic Group Specific Exposure Distributions

What is the p10, median, p90 and mean pollution exposure for each demographic group?

1. group by population group

- 2. sort by pollution exposure within group
- 3. generate population group specific conditional population weights
- 4. generate population CDF for each population group (sorted by pollution)

location	popgrp	pop_frac	avgdailypm10	cdf_pop_condi_popgrp_sortpm10	pmf_pop_condi_popgrp_sortp
location8	1	0.0000364	19.24456	0.0010453	0.0010
location9	1	0.0000151	23.56121	0.0014804	0.0004
location1	1	0.0109366	24.62676	0.3156484	0.3141
location10	1	0.0000104	25.63653	0.3159471	0.0002
location2	1	0.0163003	27.64481	0.7841942	0.4682
location4	1	0.0005879	30.71275	0.8010816	0.0168
location5	1	0.0007392	31.35114	0.8223166	0.0212
location12	1	0.0000000	33.98553	0.8223168	0.0000
location7	1	0.0000681	35.20967	0.8242718	0.0019
location11	1	0.0000000	45.99021	0.8242721	0.0000
location3	1	0.0058760	51.70466	0.9930669	0.1687
location6	1	0.0002413	54.61304	1.0000000	0.0069
location8	2	0.0006400	19.24456	0.0172871	0.0172
location9	2	0.0003150	23.56121	0.0257947	0.0085
location1	2	0.0013417	24.62676	0.0620374	0.0362
location10	2	0.0002235	25.63653	0.0680736	0.0060
location2	2	0.0070132	27.64481	0.2575157	0.1894
location4	2	0.0042712	30.71275	0.3728918	0.1153
location5	2	0.0055479	31.35114	0.5227547	0.1498
location12	2	0.0000004	33.98553	0.5227662	0.0000
location7	2	0.0010378	35.20967	0.5508009	0.0280
location11	2	0.0000008	45.99021	0.5508213	0.0000
location3	2	0.0140000	51.70466	0.9289930	0.3781
location6	2	0.0026287	54.61304	1.0000000	0.0710
location8	3	0.0046896	19.24456	0.0638166	0.0638
location9	3	0.0027290	23.56121	0.1009539	0.0371
location1	3	0.0000686	24.62676	0.1018872	0.0009
location10	3	0.0020006	25.63653	0.1291118	0.0272
location2	3	0.0012573	27.64481	0.1462207	0.0171
location4	3	0.0129304	30.71275	0.3221799	0.1759
location5	3	0.0173492	31.35114	0.5582709	0.2360
location12	3	0.0000141	33.98553	0.5584625	0.0001
location7	3	0.0065945	35.20967	0.6482016	0.0897
location11	3	0.0000242	45.99021	0.6485305	0.0003
location3	3	0.0138984	51.70466	0.8376617	0.1891
location6	3	0.0119295	54.61304	1.0000000	0.1623
location8	4	0.0183277	19.24456	0.1224562	0.1224
location9	4	0.0126118	23.56121	0.2067219	0.0842

1.4 Compute the Gini Index by Population Subgroup

The Gini index from fs gini disc.

```
ffi_dist_gini_random_var_pos_test <- function(ar_x_sorted, ar_prob_of_x) {
  fl_mean <- sum(ar_x_sorted*ar_prob_of_x);
  ar_mean_cumsum <- cumsum(ar_x_sorted*ar_prob_of_x);
  ar_height <- ar_mean_cumsum/fl_mean;
  fl_area_drm <- sum(ar_prob_of_x*ar_height);
  fl_area_below45 <- sum(ar_prob_of_x*(cumsum(ar_prob_of_x)/sum(ar_prob_of_x)))
  fl_gini_index <- (fl_area_below45-fl_area_drm)/fl_area_below45
  return(fl_gini_index)
}</pre>
```

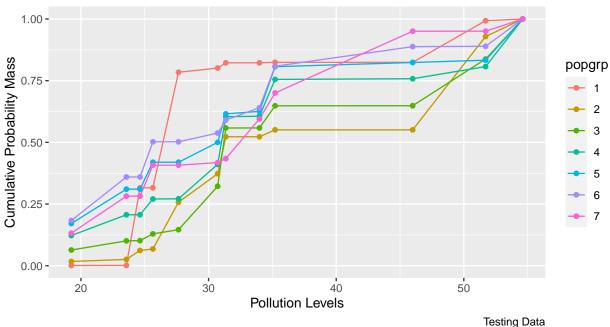
Compute Gini index for sub-group:

popgrp	popgrp_gini
1	0.1206861
2	0.1075096
3	0.1380319
4	0.1543002
5	0.1680265
6	0.1754309
7	0.1453136
7	0.1453136

1.5 Visualize the Distributions

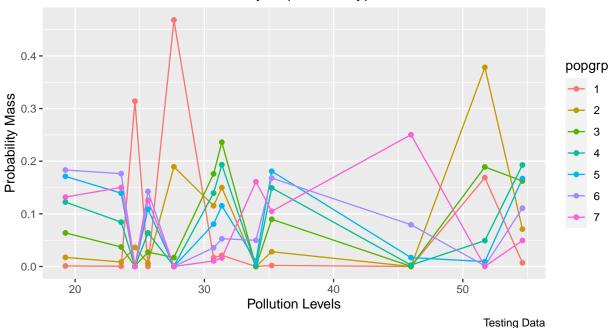
Visualizing distributions. Visualize the CDF:





Visualize the Probability Mass (real data should look much less chaotic than this):

Prob Mass Func of Pollution by Population Types



1.6 Various Quantiles

Measure quantiles of pollution exposures for different population groups:

- 1. Consider CDF larger than current quantile of interest.
- 2. Slice group-specific CDF that is higher and closest to quantile of interest.
- 3. Merge results for different quantiles together.

```
# Generate pollution quantiles by population groups
df_pop_pollution_distribution <- df_pop_pollution_by_popgrp_cdf %>%
  mutate(pm10_mean = weighted.mean(avgdailypm10, pop_frac)) %>%
  filter(cdf pop condi popgrp sortpm10 >= 0.10) %>%
  slice(1) %>%
  mutate(pm10 p10 = avgdailypm10) %>%
  select(popgrp, pm10_mean, pm10_p10) %>%
  left_join(df_pop_pollu_gini, by='popgrp') %>%
  left_join(df_pop_pollution_by_popgrp_cdf %>%
              filter(cdf_pop_condi_popgrp_sortpm10 >= 0.20) %>%
              slice(1) %>%
              mutate(pm10_p20 = avgdailypm10) %>%
              select(popgrp, pm10_p20),
            by='popgrp') %>%
  left_join(df_pop_pollution_by_popgrp_cdf %>%
              filter(cdf_pop_condi_popgrp_sortpm10 >= 0.50) %>%
              slice(1) %>%
              mutate(pm10_p50 = avgdailypm10) %>%
              select(popgrp, pm10_p50),
            by='popgrp') %>%
  left_join(df_pop_pollution_by_popgrp_cdf %>%
              filter(cdf_pop_condi_popgrp_sortpm10 >= 0.80) %>%
              slice(1) %>%
              mutate(pm10_p80 = avgdailypm10) %>%
```

```
select(popgrp, pm10_p80),
    by='popgrp') %>%
left_join(df_pop_pollution_by_popgrp_cdf %>%
    filter(cdf_pop_condi_popgrp_sortpm10 >= 0.90) %>%
    slice(1) %>%
    mutate(pm10_p90 = avgdailypm10) %>%
    select(popgrp, pm10_p90),
    by='popgrp') %>%
select(popgrp, pm10_mean, popgrp_gini, everything())
# display
df_pop_pollution_distribution %>%
    kable(caption = 'PM10 Exposure Distribution by Population Groups') %>%
kable_styling_fc()
```

PM10 Exposure Distribution by Population Groups

popgrp	pm10_mean	popgrp_gini	pm10_p10	pm10_p20	pm10_p50	pm10_p80	pm10_p90
1	31.07894	0.1206861	24.62676	24.62676	27.64481	30.71275	51.70466
2	39.47897	0.1075096	27.64481	27.64481	31.35114	51.70466	51.70466
3	37.92901	0.1380319	23.56121	30.71275	31.35114	51.70466	54.61304
4	34.86470	0.1543002	19.24456	23.56121	31.35114	51.70466	54.61304
5	32.56731	0.1680265	19.24456	23.56121	30.71275	35.20967	54.61304
6	31.46626	0.1754309	19.24456	23.56121	25.63653	35.20967	54.61304
7	33.50541	0.1453136	19.24456	23.56121	33.98553	45.99021	45.99021