R Example Binary Outcome Estimation with Binary Regressor

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Binary Logit

Go to the RMD, R, PDF, or HTML version of this file. Go back to fan's REconTools Package, R4Econ Repository (bookdown site), or Intro Stats with R Repository.

Data Preparation

```
df_mtcars <- mtcars</pre>
# X-variables to use on RHS
ls_st_xs <- c('mpg', 'qsec')</pre>
ls_st_xs <- c('mpg')</pre>
ls_st_xs <- c('qsec')</pre>
ls_st_xs <- c('wt')</pre>
ls_st_xs <- c('mpg', 'wt', 'vs')</pre>
svr_binary <- 'hpLowHigh'</pre>
svr_binary_lb0 <- 'LowHP'</pre>
svr binary lb1 <- 'HighHP'</pre>
svr_outcome <- 'am'</pre>
sdt_name <- 'mtcars'</pre>
# Discretize hp
df_mtcars <- df_mtcars %>%
    mutate(!!sym(svr_binary) := cut(hp,
                               breaks=c(-Inf, 210, Inf),
                               labels=c(svr_binary_lb0, svr_binary_lb1)))
```

Logit Regresion and Prediction logit regression with glm, and predict using estimation data. Prediction and estimation with one variable.

- LOGIT REGRESSION R DATA ANALYSIS EXAMPLES
- Generalized Linear Models

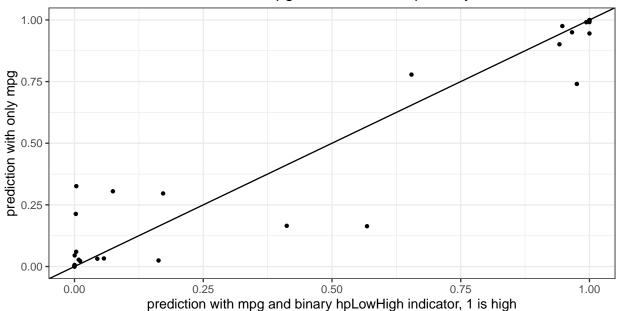
```
## glm(formula = as.formula(paste(svr_outcome, "~", paste(ls_st_xs,
##
       collapse = "+"))), family = "binomial", data = df_mtcars)
##
## Deviance Residuals:
                   1Q
                         Median
                                       3Q
                                                Max
## -1.73603 -0.25477 -0.04891
                                            1.90321
                                  0.13402
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 22.69008
                          13.95112
                                     1.626
                                             0.1039
              -0.01786
                           0.33957 -0.053
                                             0.9581
               -6.73804
                           3.01400 -2.236
                                             0.0254 *
## wt
## vs
              -4.44046
                           2.84247 -1.562
                                             0.1182
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 43.230 on 31 degrees of freedom
## Residual deviance: 13.092 on 28 degrees of freedom
## AIC: 21.092
##
## Number of Fisher Scoring iterations: 7
# Predcit Using Regression Data
df_mtcars$p_mpg <- predict(rs_logit, newdata = df_mtcars, type = "response")</pre>
```

Prediction with Observed Binary Input Logit regression with a continuous variable and a binary variable. Predict outcome with observed continuous variable as well as observed binary input variable.

```
# Regress
rs_logit_bi <- glm(as.formula(paste(svr_outcome,</pre>
                                     "~ factor(", svr_binary,") + ",
                                    paste(ls_st_xs, collapse="+")))
                   , data = df mtcars, family = "binomial")
summary(rs_logit_bi)
##
## Call:
  glm(formula = as.formula(paste(svr_outcome, "~ factor(", svr_binary,
       ") + ", paste(ls_st_xs, collapse = "+"))), family = "binomial",
##
##
       data = df_mtcars)
##
## Deviance Residuals:
                   1Q
                         Median
                                        3Q
                                                 Max
## -1.45771 -0.09563 -0.00875
                                 0.00555
                                             1.87612
##
## Coefficients:
##
                           Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                             3.8285
                                       18.0390
                                                 0.212
                                                          0.8319
## factor(hpLowHigh)HighHP
                             6.9907
                                        5.5176
                                                 1.267
                                                          0.2052
                                        0.8906
                                                 1.009
## mpg
                             0.8985
                                                          0.3131
## wt
                            -6.7291
                                        3.3166 -2.029
                                                          0.0425 *
                            -5.9206
                                        4.1908 -1.413
## vs
                                                          0.1577
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 43.2297
                              on 31 degrees of freedom
## Residual deviance: 8.9777
                              on 27 degrees of freedom
## AIC: 18.978
##
## Number of Fisher Scoring iterations: 9
# Predcit Using Regresion Data
df_mtcars$p_mpg_hp <- predict(rs_logit_bi, newdata = df_mtcars, type = "response")</pre>
# Predicted Probabilities am on mgp with or without hp binary
scatter <- ggplot(df_mtcars, aes(x=p_mpg_hp, y=p_mpg)) +</pre>
      geom_point(size=1) +
      # geom_smooth(method=lm) + # Trend line
      geom_abline(intercept = 0, slope = 1) + # 45 degree line
      labs(title = paste0('Predicted Probabilities ', svr_outcome, ' on ', ls_st_xs, ' with or without ')
           x = paste0('prediction with ', ls_st_xs, ' and binary ', svr_binary, ' indicator, 1 is high'
           y = paste0('prediction with only ', ls_st_xs),
           caption = 'mtcars; prediction based on observed data') +
      theme bw()
print(scatter)
```

Predicted Probabilities am on mpg with or without hp binary

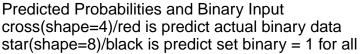


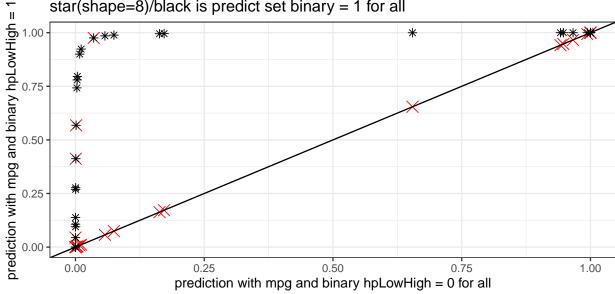
Prediction with Binary set to 0 and 1 Now generate two predictions. One set where binary input is equal to 0, and another where the binary inputs are equal to 1. Ignore whether in data binary input is equal to 0 or 1. Use the same regression results as what was just derived.

mtcars; prediction based on observed data

Note that given the example here, the probability changes a lot when we

```
# Previous regression results
summary(rs_logit_bi)
##
## Call:
## glm(formula = as.formula(paste(svr_outcome, "~ factor(", svr_binary,
       ") + ", paste(ls st xs, collapse = "+"))), family = "binomial",
##
       data = df_mtcars)
##
## Deviance Residuals:
                         Median
                 10
                                       3Q
                                                Max
## -1.45771 -0.09563 -0.00875
                                            1.87612
                                0.00555
## Coefficients:
                           Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                             3.8285
                                       18.0390
                                                0.212
                                                         0.8319
## factor(hpLowHigh)HighHP
                             6.9907
                                        5.5176
                                                 1.267
                                                         0.2052
                                                 1.009
                             0.8985
                                        0.8906
                                                         0.3131
## wt
                            -6.7291
                                        3.3166 -2.029
                                                         0.0425 *
                            -5.9206
                                        4.1908 -1.413
## vs
                                                         0.1577
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 43.2297 on 31 degrees of freedom
## Residual deviance: 8.9777 on 27 degrees of freedom
## AIC: 18.978
##
## Number of Fisher Scoring iterations: 9
# Two different dataframes, mutate the binary regressor
df_mtcars_bi0 <- df_mtcars %>% mutate(!!sym(svr_binary) := svr_binary_lb0)
df_mtcars_bi1 <- df_mtcars %>% mutate(!!sym(svr_binary) := svr_binary_lb1)
# Predcit Using Regresion Data
df_mtcars$p_mpg_hp_bi0 <- predict(rs_logit_bi, newdata = df_mtcars_bi0, type = "response")</pre>
df_mtcars$p_mpg_hp_bi1 <- predict(rs_logit_bi, newdata = df_mtcars_bi1, type = "response")</pre>
# Predicted Probabilities and Binary Input
scatter <- ggplot(df_mtcars, aes(x=p_mpg_hp_bi0)) +</pre>
      geom point(aes(y=p mpg hp), size=4, shape=4, color="red") +
      geom_point(aes(y=p_mpg_hp_bi1), size=2, shape=8) +
      # geom_smooth(method=lm) + # Trend line
      geom_abline(intercept = 0, slope = 1) + # 45 degree line
      labs(title = paste0('Predicted Probabilities and Binary Input',
                          '\ncross(shape=4)/red is predict actual binary data',
                          '\nstar(shape=8)/black is predict set binary = 1 for all'),
            x = paste0('prediction with ', ls_st_xs, ' and binary ', svr_binary, ' = 0 for all'),
            y = paste0('prediction with ', ls_st_xs, ' and binary ', svr_binary, ' = 1'),
           caption = paste0(sdt_name)) +
      theme bw()
print(scatter)
```



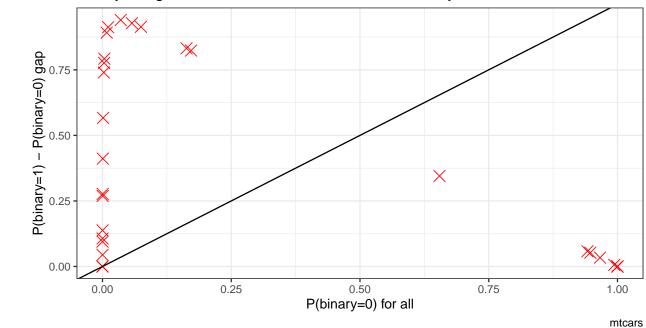


Prediction with Binary set to 0 and 1 Difference What is the difference in probability between binary = 0 vs binary = 1. How does that relate to the probability of outcome of interest when binary = 0 for all.

mtcars

In the binary logit case, the relationship will be hump-shaped by construction between A_i and α_i . In the exponential wage cases, the relationship is convex upwards.

Binary Marginal Effects and Prediction without Binary

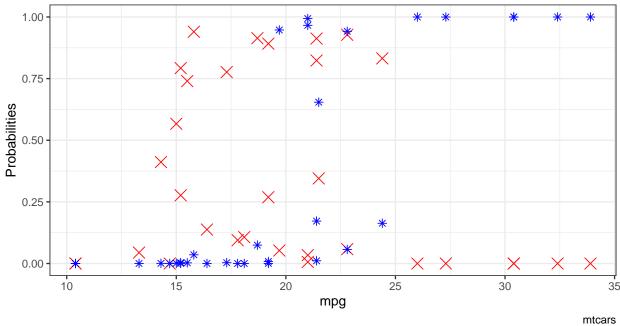


X variables and A and alpha Given the x-variables included in the logit regression, how do they relate to A_i and alpha_i

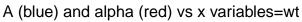
```
# Generate Gap Variable
df_mtcars <- df_mtcars %>% mutate(alpha_i = p_mpg_hp_bi1 - p_mpg_hp_bi0) %>%
                mutate(A_i = p_mpg_hp_bi0)
# Binary Marginal Effects and Prediction without Binary
ggplot.A.alpha.x <- function(svr_x, df,</pre>
                              svr_alpha = 'alpha_i', svr_A = "A_i"){
  scatter <- ggplot(df, aes(x=!!sym(svr_x))) +</pre>
        geom_point(aes(y=alpha_i), size=4, shape=4, color="red") +
        geom_point(aes(y=A_i), size=2, shape=8, color="blue") +
        geom_abline(intercept = 0, slope = 1) + # 45 degree line
        labs(title = paste0('A (blue) and alpha (red) vs x variables=', svr_x),
             x = svr_x,
             y = 'Probabilities',
             caption = paste0(sdt_name)) +
        theme bw()
return(scatter)
}
# Plot over multiple
lapply(ls_st_xs,
       ggplot.A.alpha.x,
       df = df_mtcars)
```

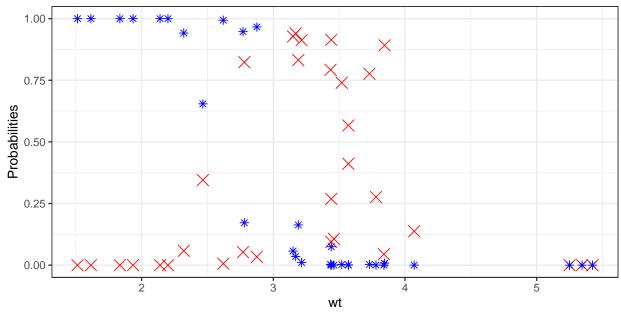
[[1]]





[[2]]





##

[[3]]

mtcars

