- · Intelligence
 - · the ability to understand, learn and think
- Intelligence of humans is achieved—not by purely reflex mechanisms but by processes of reasoning that operate on internal representations of knowledge

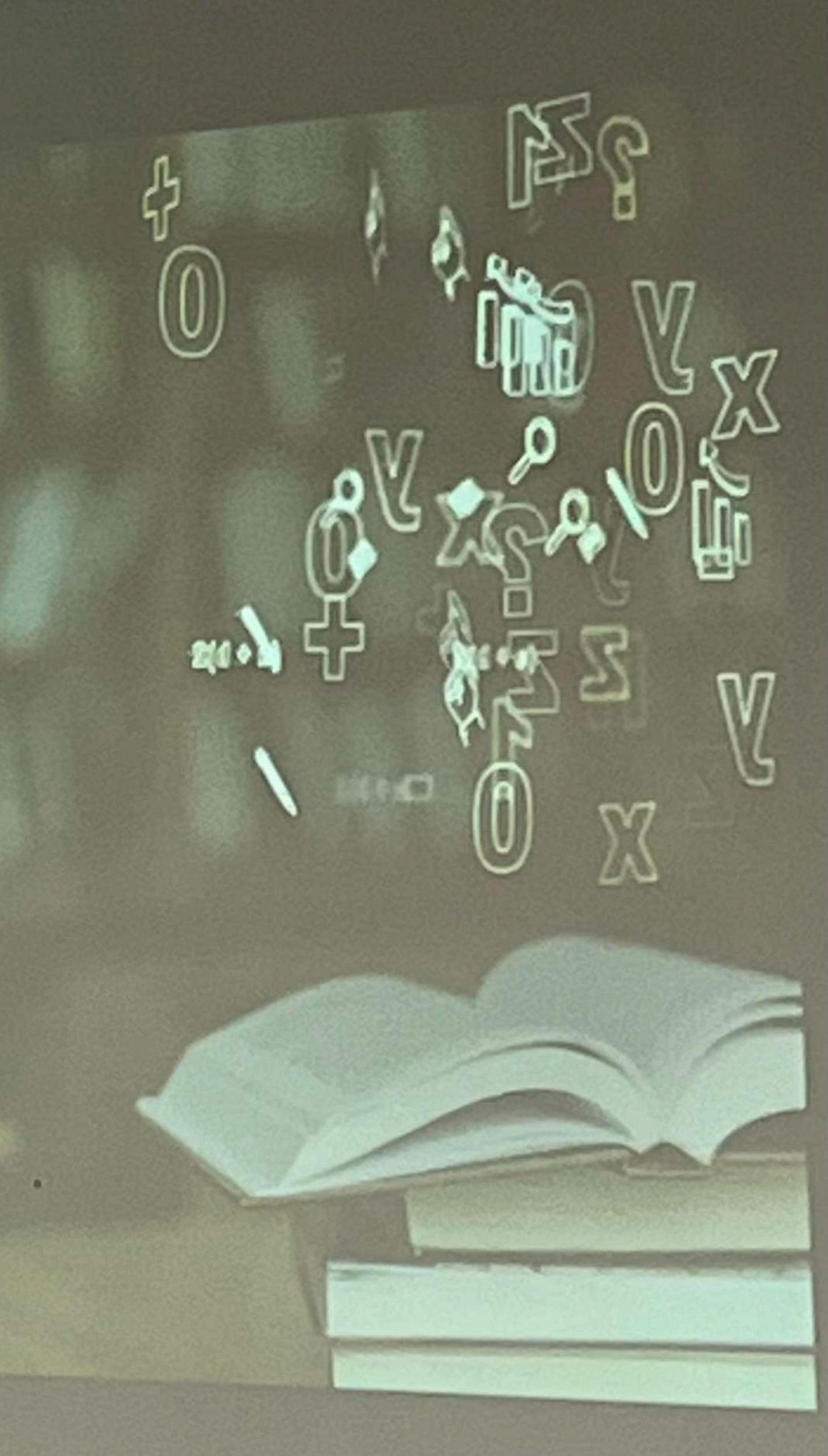


- Artificial Intelligence (AI) is about building machines and systems that
 can reason, learn, and solve problems, similar to how humans do. In many
 Al applications, logical reasoning plays a crucial role, allowing systems to
 make decisions based on given conditions and facts
- · Leads to knowledge-based agents approach for Al

Knowledge Base

 Knowledge Base – Set of sentences represented in knowledge representation language

- Knowledge representation language— Expressing knowledge explicitly in a computer-tractable way
 - · (logic)



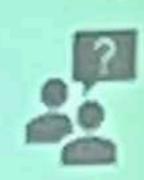
Logic

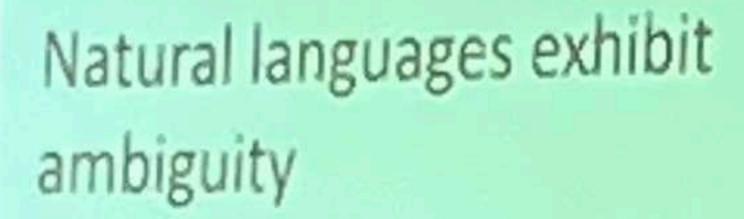
- Oxford dictionary
 - · a way of thinking or explaining something
 - · sensible reasons for doing something
 - the science of thinking about or explaining the reason for something using formal methods

 Logic is the basis of all mathematical reasoning and all automated reasoning

Formal vs Informal

Formal Uses formal language	Informal
	Natural language Studies informal fallacies, Critical Thinking,
Study of logical truths	
Symbolic logic, mathematical logic,	





The boy saw a girl with a telescope

Our shoes are guaranteed to give

you a fit

Ambiguity makes reasoning difficult / incomplete



Why formal languages

Formal languages

promote rigour and thereby reduce possibility of human error

help reduce implicit / unstated assumptions by removing familiarity with subject matter

help achieve generality due to possibility of finding alternative interpretations for sentences and arguments.

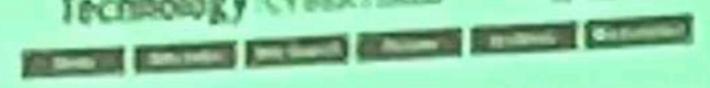
Formal logic

- Formal logic: Uses syllogisms to make inferences, and examines how conclusions follow from premises based on the structure of arguments
 - Symbolic logic: Uses symbols to accurately map out valid and invalid arguments.
 - Mathematical logic: Uses mathematical symbols to prove theoretical arguments
 - · Propositional Logic

Why is it important?

- · Core of Al
 - Possibility of automating reasoning
 Reasoning: draw inferences from knowledge
 - answer queries
 - * discover facts that follow from the knowledge base decide what to do etc.
- In AI, propositional logic is essential for knowledge representation, reasoning, and decision-making processes

Impact of Logic in Al



December 15, 1986

Computer Math Proof Shows Reasoning Power

BYCESI KELLER

Company or whiteen when I cames to the grant work of mathematics. But the complete and elegant architecture to head mathematical problems, replang has When still to heat the bosses mond. That is, pushaps, and area

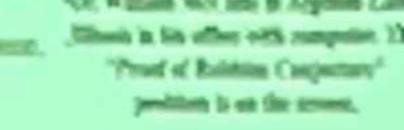
A company program written by communities at Augment Statemed Laboratory in Elements has cover up with a resign mathematical proof that would have been called creative if a horses had thought of it, in doing us, the computer has, for the few time, put a tookeld into pure mathematics, it field described by its parameters as more of an art form that a science. And the implementary, some way are produced, allowing you have presented computers can be at recoming itself, at monotony the Sades of repeal angle or even person that have characterized the best format minds.

 Company long hand people of mathematical conjugations below, of course, but those conjugations were easy to prove. The difference this tree is that the companie has unlessed a conjuntare that therepaid water of the heat mathematicisms for 40 poses. And it did so with a program that was serogrand to reason, and so, solve a specific problems, for that some. Our program is very Attenue has along playing company programs, for example, which are introded to online past one problems; the terries of \$ 1. Code Line before The No. Yes, Deep desc pane

"It's a sign of power, of manerical power," said the Lamy Wou, the supervisor of the computer recoming present at Adjusteet, And with this small, obtained by a colleague, Dr. William McCore, by cost, "We've taken a quantum loop forward,"

Was products that the result may mark the ingreening of the end for mathematics rewards to it is new practiced, eventually ferring indicenticate to from an discovering new connections, and having the proof to companies,

-Dr. William McCossi at Argonna Lable, Ellowic in his office with competite. The "Proof of Building Conjectury"



6 C Y

* https://archive.org/www.org/mes.com/abrany/sybes/week/1210math.html?pagewantedwall

But the result also ware (full-come for very maries of creasure flustrate, resolute the possibility that interestings could take a totalled early in reach the asset.

Logical Arguments

- · (A) All humans have 2 eyes.
- · (B) Sujit is a human.
 - Therefore (P) Sujit has 2 eyes.
- " (C) All humans have 4 eyes.
- (B) Sujit is a human.
 - Therefore (Q) Sujit has 4 eyes.
- * Which of P and Q are true / false ?
- * Is deducing P from A and B correct? Q from B and C?

- · All humans have 2 eyes.
- · Kishore has 2 eyes.
 - · Therefore (P) Kishore is a human.
- · No human has 4 eyes.
- · Kishore has 2 eyes.
 - · Therefore (Q) Kishore is not human.
- · Which of P and Q are true / false?
- · Is deducing P correct? Q?

· ...fallacy conclusion may be correct. The reasoning is incorrect

Propositional Logic

Deals with propositions which are true or false

Also known as propositional calculus

Zero-order logic

Foundations for first order and higher order logics

Order of 'Logic'

- The order of a logic refers to the degree of quantification that can be performed over sets:
 - First-order logic: Quantifies only over individuals. It is also known as predicate logic, predicate calculus, or quantificational logic.
 - Second-order logic: Quantifies over sets.
 - Third-order logic: Quantifies over sets of sets.
 - Higher-order logic: The union of first-, second-, third-, and higher-order logic. It allows quantification over sets that are nested arbitrarily deeply.

Propositional Logic

- Propositions are Declarative Statements
- Atomic Propositions:
 - · Simple, indivisible statements, cannot be broken down further
 - · Each atomic proposition represents a basic fact or condition
 - . Example: "The door is closed."
- Compound Propositions:
 - Multiple atomic propositions can be combined using logical connectives (like AND, OR, NOT) to create compound propositions.
 - * Example: "The door is closed AND the heater is on."

Exercise

Given: A and B are true; X and Y are false, determine truth values of:

¬(A v X)

AV(XAY)

AA(X V (BAY))

 $[(A \wedge X) \vee \neg B] \wedge \neg [(A \vee X) \vee \neg B]$

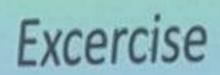
(PAQ) A (¬A v X)

 $[(X \land Y) \rightarrow A] \rightarrow [X \rightarrow (Y \rightarrow A)]$

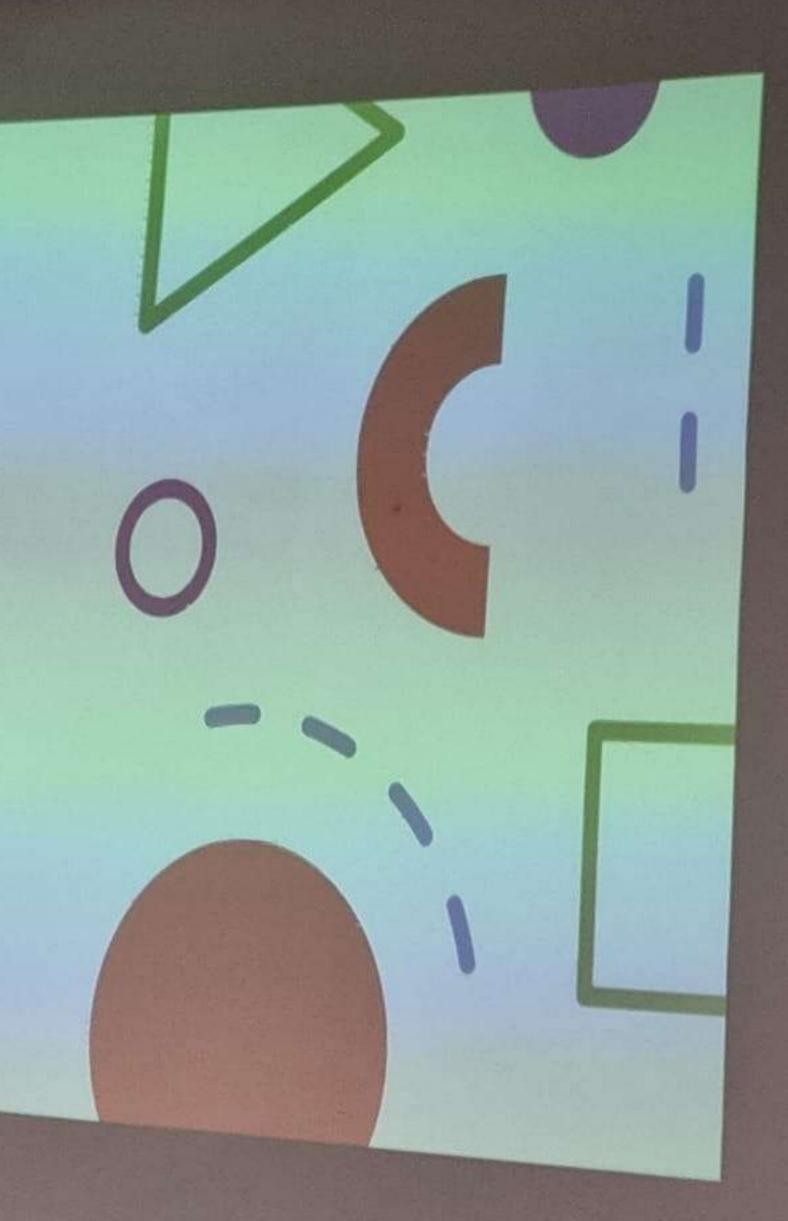
Truth Table

- A truth table is a breakdown of all the possible truth values returned by a logical expression
- Write down truth tables for, P, Q, $\neg P$, P \lor Q, P \rightarrow Q, P \leftrightarrow Q, $\neg P$ \lor Q, $\neg P$ \lor Q, $\neg P$ \lor Q,
 - One row for each possible assignment of True/False to propositional variables
 - · Important: Above P and Q can be any sentence, including complex sentences

PHQ $P \rightarrow Q$ $Q \rightarrow P$ If $P \leftrightarrow Q$ is true • P and Q are equivalent • P is necessary and Sufficient for Q • Q is necessary and Sufficient for P



- Which of the following are propositions
 - * (P) Today is Wednesday
 - (Q) It is raining today
- (R) It will be raining tomorrow.
- (S) Close the door
- · (S) 2+7=9
- (T) 3+9 = 10
- (U) X+2 = 1



Logical connections

AND (A) conjunction	S: P AND Q S: P ^ Q	S is true if both P and Q are true
OR (V) disjunction	S: P OR Q S: P V Q	S is true if any of P, Q is true
NOT (¬): Negation.	S: →P	S is true only if P is false
IMPLIES (→)	S: P → Q S: ¬P V Q	S is true if P implies Q
IFF (↔)	S: $P \leftrightarrow Q$ S: $\neg P \times Q$	S is true if P and Q are true or false together

P-)Q

The only time P+Q evaluates to False is when

• P is True and Q is False

If P→Q is True, then:

- P is a sufficient condition for Q
- · Q is a necessary condition for P