

Performance Modeling of Computer Systems and Networks

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Abstract Priority

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Analytical models
abstract priority

QoS management

- Service provider
- Traffic flows with different QoS
- QoS: mean response time

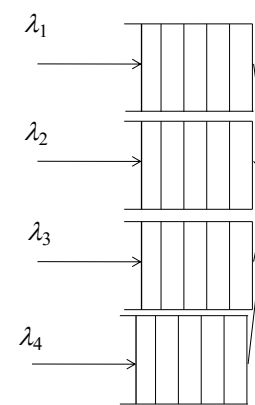
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Analytical models
abstract priority

M/M/1 – NP_priority



$$\lambda = \sum_{i=1}^r \lambda_i \quad \text{uniform partition: } \lambda_i = \frac{\lambda}{4}, p_i = \frac{1}{4}$$

$$\rho = 0.1, 0.2, 0.4, 0.6$$

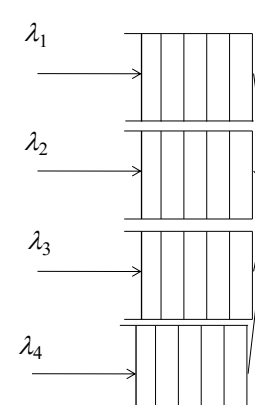
$$E(T_{Q_i})^{NP_priority} = \frac{\frac{\lambda}{2} E(S^2)}{\left(1 - \sum_{i=1}^k \rho_i\right) \left(1 - \sum_{i=1}^{k-1} \rho_i\right)}$$

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Analytical models
abstract priority

NP priority



$$E(T_{Q_1}) = \frac{\rho E(S)}{(1 - \rho_1)}$$

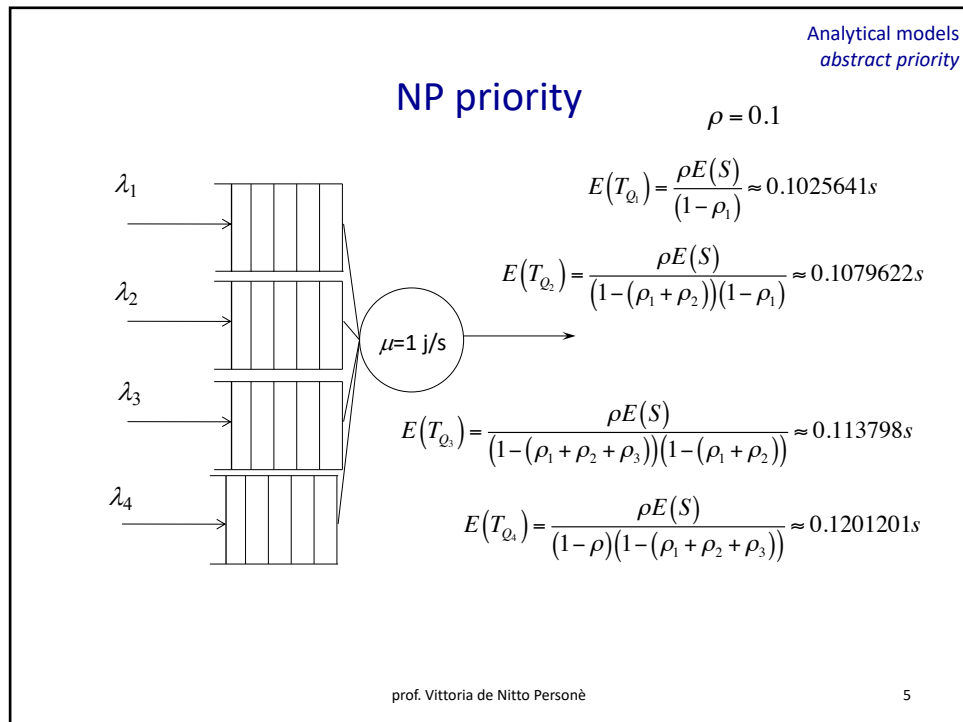
$$E(T_{Q_2}) = \frac{\rho E(S)}{(1 - (\rho_1 + \rho_2))(1 - \rho_1)}$$

$$E(T_{Q_3}) = \frac{\rho E(S)}{(1 - (\rho_1 + \rho_2 + \rho_3))(1 - (\rho_1 + \rho_2))}$$

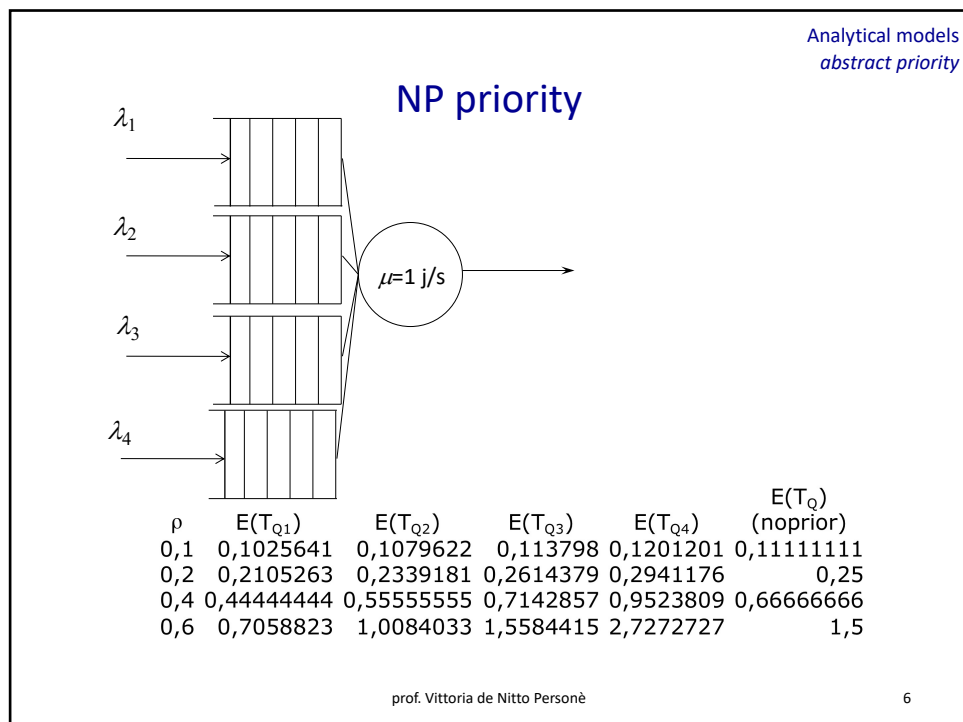
$$E(T_{Q_4}) = \frac{\rho E(S)}{(1 - \rho)(1 - (\rho_1 + \rho_2 + \rho_3))}$$

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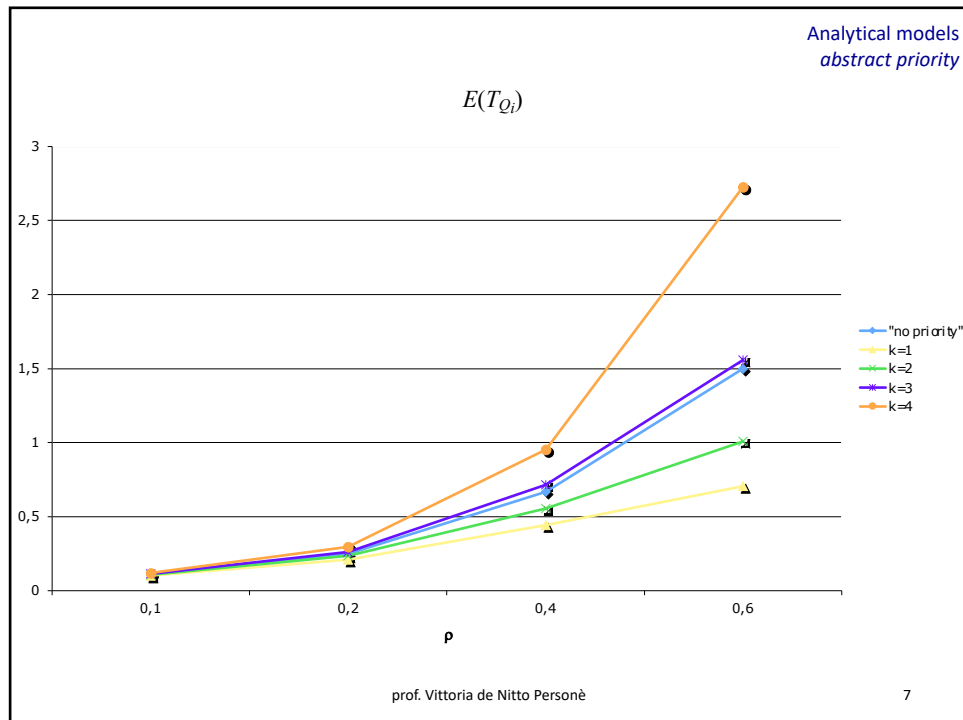
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Analytical models
priority scheduling

Goals:

- given a QoS requirement, decide if adopt priority classes
- note that if the policy is non-size-based, we can reason just in terms of waiting time

Mean service demand: 0.4 s

QoS requirement
the waiting time should not exceed the service demand, in particular:
the service provider will not incur in penalties if $T_Q \leq 0.45$ s;
the service provider will gain revenue if $T_Q < 0.4$ s

By simple "costless" analysis we can offer good insights

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Analytical models
priority scheduling

$E(S) = 0.4 \text{ s}$			
	Low load	medium load	high load
$\rho =$	0.4	0.6	0.8
$\lambda =$	1	1.5	2 job/s
$E(T_Q) =$	0.26	0.6	1.6 job/s
			without priority classes

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high load $\rho = 0.8$

not penalties if $T_Q \leq 0.45 \text{ s}$

gain revenue if $T_Q < 0.4 \text{ s}$

$$p_1 = 0.36, p_2 = 0.64$$

$$p_1 = 0.22, p_2 = 0.78$$

$$E(T_{Q1}) = 0.4494 \text{ s}$$

$$E(T_{Q1}) = 0.3883 \text{ s}$$

$$E(T_{Q2}) = 2.2472 \text{ s}$$

$$E(T_{Q2}) = 1.9417 \text{ s}$$

$$E(T_Q)_{glob} = E(T_Q)_{KP} = 1.6 \text{ s}$$

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Euristica per la ripartizione in classi di priorità astratta

$$\rho = 0.92, E(S) = 1 \text{ j/s} \quad E(T_Q) = 11.5 \text{ s}, E(T_S) = 12.5 \text{ s}$$

60%, 25 %, 15 %,

$$\begin{aligned} E(T_{Q1}) &= 2.05357 \text{ s} \\ E(T_{Q2}) &= 9.42005 \text{ s} \\ E(T_{Q3}) &= 52.75229 \text{ s} \end{aligned}$$

$$\begin{aligned} E(T_{S1}) &= 3.05357 \text{ s} \\ E(T_{S2}) &= 10.42005 \text{ s} \\ E(T_{S3}) &= 53.75229 \text{ s} \end{aligned}$$

15 %, 25 %, 60%,

$$\begin{aligned} E(T_{Q1}) &= 1.067285 \text{ s} \\ E(T_{Q2}) &= 1.688743 \text{ s} \\ E(T_{Q3}) &= 18.196203 \text{ s} \end{aligned}$$

$$\begin{aligned} E(T_{S1}) &= 2.067285 \text{ s} \\ E(T_{S2}) &= 2.688743 \text{ s} \\ E(T_{S3}) &= 19.196203 \text{ s} \end{aligned}$$

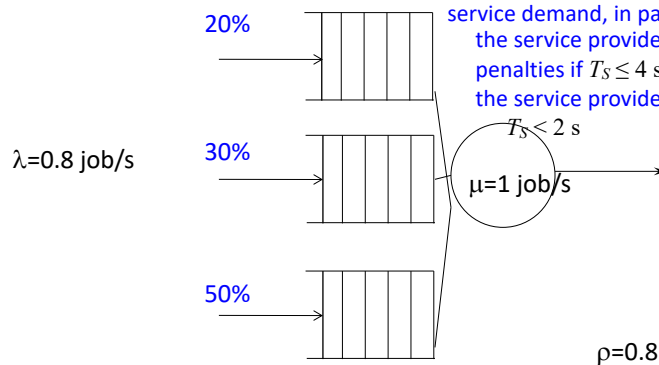
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Analytical models
abstract priority

M/M/1 Arrival flow: random, rate 0.8 job/s
Service process: quite variable rate 1 job/s
QoS requirements
the response time should not exceed twice the
service demand, in particular:
the service provider will not incur in
penalties if $T_S \leq 4 \text{ s}$;
the service provider will gain revenue if



$$E(T_Q) = \frac{\rho E(S)}{1 - \rho} = \frac{0.8}{0.2} = 4 \quad E(T_S) = 5$$

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Analytical models
abstract priority

M/M/1

Not penalties if $T_S \leq 4$ s;
gain revenue if $T_S < 2$ s

	NP	P	NP	P
class	$E(T_Q)$		$E(T_S)$	
1 - 20%	0.9523809523809524	0.19047619047619052	1.9523809523809526	1.1904761904761905
2 - 30%	1.5873015873015874	0.7936507936507937	2.5873015873015874	1.9841269841269842
3 - 50%	6.666666666666669	6.666666666666669	7.666666666666669	8.333333333333336
global	4.000000000000001	3.6095238095238105	5.000000000000001	5.000000000000001

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Analytical models
abstract priority

M/M/1

Not penalties if $T_S \leq 4$ s;
gain revenue if $T_S < 2$ s

	NP	P	NP	P
class	$E(T_Q)$		$E(T_S)$	
1 - 20%	0.9523809523809524	0.19047619047619052	1.9523809523809526	1.1904761904761905
2 - 30%	1.5873015873015874	0.7936507936507937	2.5873015873015874	1.9841269841269842
3 - 50%	6.666666666666669	6.666666666666669	7.666666666666669	8.333333333333336
global	4.000000000000001	3.6095238095238105	5.000000000000001	5.000000000000001

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Analytical models
abstract priority

M/M/1

Not penalties if $T_S \leq 4$ s;
gain revenue if $T_S < 2$ s

	NP	P	NP	P
class	$E(T_Q)$		$E(T_S)$	
1 - 20%	0.9523809523809524	0.19047619047619052	1.9523809523809526	1.1904761904761905
2 - 30%	1.5873015873015874	0.7936507936507937	2.5873015873015874	1.9841269841269842
3 - 50%	6.666666666666669	6.666666666666669	7.666666666666669	8.333333333333336
global	4.000000000000001	3.6095238095238105	5.000000000000001	5.000000000000001

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Analytical models
abstract priority

M/H₂/1

Not penalties if $T_S \leq 4$ s;
gain revenue if $T_S < 2$ s

No priority classes
 $g(0.1)=4.5556$,
 $E(T_Q)=11.1111$ s, $E(T_S)=12.1111$ s

	NP	P	NP	P
class	$E(T_Q)$		$E(T_S)$	
1 - 20%	2.645502645502645	0.5291005291005291	3.645502645502645	1.529100529100529
2 - 30%	4.409171075837742	2.204585537918871	5.409171075837742	3.3950617283950617
3 - 50%	18.51851851851852	18.51851851851852	19.51851851851852	20.185185185185187
global	11.111111111111111	10.026455026455027	12.111111111111111	11.416931216931218

p=0.1

10% $E(S)=5$ s

90% $E(S)=0.55555$ s

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Mean service demand (expo): 0.4 s

QoS requirement

the waiting time (average) should not exceed 0.1 s, in particular:

the service provider will gain c_1 for each service within QoS

the service provider will pay c_2 for each service violates QoS

$$R = p_1 c_1 - p_2 c_2$$

Abstract-P $\rightarrow \max R$

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$$E(S) = 0.4 \text{ s}, \lambda = 0.8 \text{ j/s}, \rho = 0.32$$

$$p_1 = 0.6, p_2 = 0.4, c_1 = 5, c_2 = 3 \rightarrow R = 2.2$$

$$E(T_{Q1}) = 0.095 \text{ s}, E(T_{S1}) = 0.495 \text{ s}$$

$$E(T_{Q2}) = 0.233 \text{ s}, E(T_{S2}) = 0.728 \text{ s}$$

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