

# Superhard pseudocubic BC<sub>2</sub>N superlattices

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## Abstract:

It is currently under debate whether diamond-like BC<sub>2</sub>N may be harder than the second-hardest material, cubic BN (c-BN). Using the bond counting rule, which states that for a non-isovalent semiconductor alloy such as BC<sub>2</sub>N, the low energy configurations should have a minimum of "wrong bonds", we have performed an unconstrained search and identified a series of short period (111) superlattice structures that have much lower total energy than previously proposed structures. According to the larger ideal strength of this BC<sub>2</sub>N superlattice, it is harder than c-BN. Our results are consistent with recent experimental findings, but in contrast to a recent theoretical study, which claimed that the optimal BC<sub>2</sub>N structure is less hard than c-BN.

## I. Motivation

### Finding superhard material:

Diamond is the hardest.

c-BN is the second, but with better thermal and chemical stability.

### Synthesis of cubic BC<sub>2</sub>N and its structure:

Experiment: large bulk modulus and shear modulus, high Vickers hardness: 76 GPa (Diamond: 115 GPa, c-BN: 62 GPa.) still unknown atomic configuration.

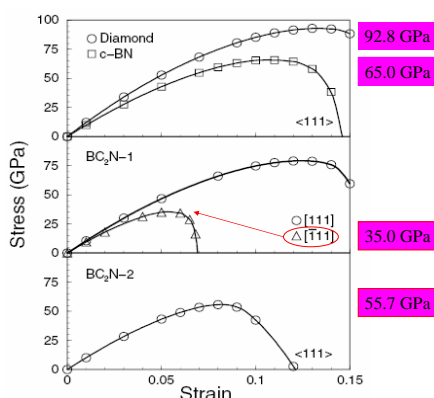
V. L. Solozhenko et al., Appl. Phys. Lett. 78, 1385 (2001)

Theory: a number of structures proposed with bulk and shear modulus larger than c-BN.

Which one is the most stable?

### Ideal strength of BC<sub>2</sub>N:

Ideal strength: the tensile or shear stress at which a perfect crystal becomes mechanically unstable, that sets an upper bound for material strength.

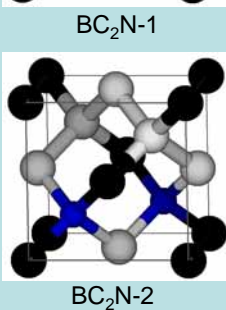
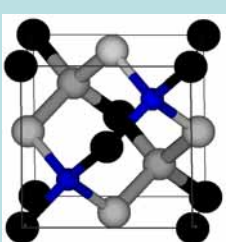
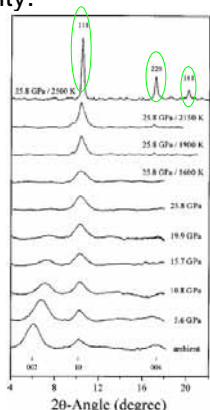


Y. Zhang, et al, Phys. Rev. Lett. 93, 195504 (2004).

Although previous BC<sub>2</sub>N structures have larger bulk modulus, but they have lower ideal strength than c-BN.

Is there a BC<sub>2</sub>N structure with bulk modulus and ideal strength both bigger than c-BN?

New material harder than c-BN, more stable than diamond



## II. Calculation details

- ◆ DFT, ABINIT code, plane wave basis, Energy cutoff 80 Ry;
- ◆ Troullier-Martins pseudopotential;
- ◆ LDA, Perdew-Wang exchange-correlation functional parameterized by Goedecker,
- ◆ k-points: 8x8x8 Monkhorst-Pack grid for an eight-atom cubic unit cell or equivalent.

Ideal stress: Hellymann-Feynman stress tensor orthogonal to the applied stress less than 0.1 GPa after relaxation. [D. Roundy, et al. Philos. Mag. A 81, 1725 (2001).

## III. <111> (C<sub>2</sub>)<sub>n</sub>(BN)<sub>n</sub> Superlattices

We propose <111> (C<sub>2</sub>)<sub>n</sub>(BN)<sub>n</sub> superlattices, BC<sub>2</sub>N<sub>n</sub>x<sub>n</sub> (n = 1, 2, 3), which are more stable than all previous structures due to less wrong bonds, and have larger bulk modulus.

### Ratio of the bond numbers

More stable bonds Less stable bonds Least stable bonds  
B-N : C-C : B-C : N-C : N-N : B-B

3 : 3 : 1 : 1 : 0 : 0

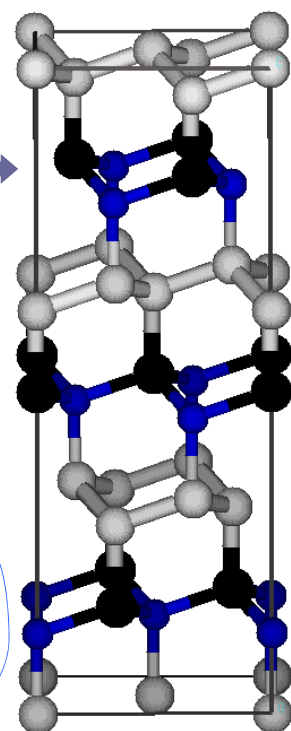
1 : 1 : 1 : 1 : 0 : 0

Calculated volume *V*, bulk modulus *B*, and formation energy *E* = *E*(BC<sub>2</sub>N) - *E*(C<sub>2</sub>) - *E*(BN).

Structure	<i>V</i> (Å <sup>3</sup> /4-atoms)	<i>B</i> (GPa)	<i>E</i> (eV/4-atoms)
Diamond	22.22	453.7	-
c-BN	23.19	392.0	-
BC <sub>2</sub> N <sub>1x1</sub>	22.92	419.5	0.76
BC <sub>2</sub> N <sub>2x2</sub>	22.84	419.5	0.52
BC <sub>2</sub> N <sub>3x3</sub>	22.80	421.9	0.39
BC <sub>2</sub> N-1	23.06	397.6	1.78
BC <sub>2</sub> N-2	23.06	400.2	1.80

### Phase segregation to diamond and c-BN

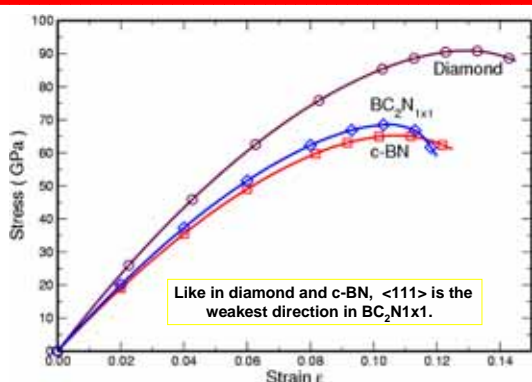
The calculated structure factors of BC<sub>2</sub>N<sub>n</sub>x<sub>n</sub> superlattices show weak 200 Bragg line and intensive 111, 221, 311 lines, indicating BC<sub>2</sub>N<sub>n</sub>x<sub>n</sub> are diamond-like pseudocubic structures.



BC<sub>2</sub>N<sub>1x1</sub>

## IV. Ideal strength of <111> BC<sub>2</sub>N superlattices

<111> BC<sub>2</sub>N superlattice have bigger ideal strength than c-BN, in contrast with previous study.



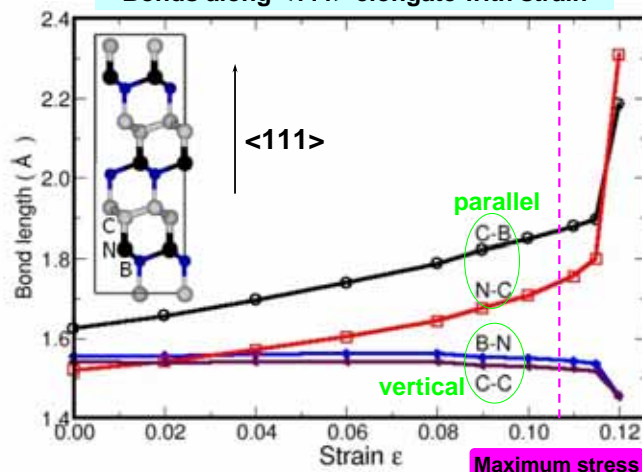
Like in diamond and c-BN, <111> is the weakest direction in BC<sub>2</sub>N<sub>1x1</sub>.

Calculated ideal tensile strength and the corresponding strain at which the maximum stress (in GPa) occurs.

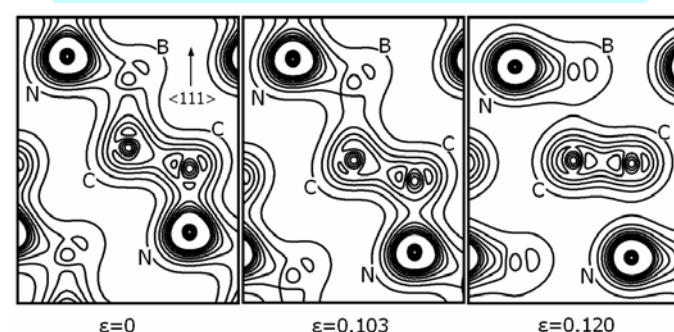
Structure	Direction	Strain	Stress	Stress*
Diamond	<111>	0.130	90.8	92.8
c-BN	<111>	0.108	65.2	65.0
BC <sub>2</sub> N <sub>1x1</sub>	<111>	0.103	68.4	
BC <sub>2</sub> N-1	<111>	0.053	33.0	35.0
BC <sub>2</sub> N-2	<111>	0.078	53.4	55.7

\*: From Y. Zhang, et al, Phys. Rev. Lett. 93, 195504 (2004).

### Bonds along <111> elongate with strain



### Charge distribution at different <111> strains



B-C and N-C along <111> elongate significantly after the stress reaches its top. N-C bond length increases faster than C-B and breaks first. After both bonds break, the system converts into alternating graphite and hexagonal BN layers.

## V. Summary:

We have identified the short period (C<sub>2</sub>)<sub>n</sub>(BN)<sub>n</sub> (111) superlattice structures with larger bulk modulus and ideal strength than c-BN, indicating that BC<sub>2</sub>N could be harder than c-BN. This is consistent with experimental findings.

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