

# Advancing Spatial Reasoning in Large Language Models: An In-Depth Evaluation and Enhancement Using the StepGame Benchmark

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## Introduction

AI has made remarkable progress across various domains, with large language models (LLMs) like ChatGPT gaining substantial attention for their human-like text-generation capabilities. However, spatial reasoning remains a significant challenge, with ChatGPT's performance on spatial benchmarks like StepGame being unsatisfactory. Our analysis of GPT's spatial reasoning on a rectified StepGame benchmark identifies its proficiency in mapping text to spatial relations, yet it struggles with complex reasoning. We provide a flawless solution to the benchmark by combining template-to-relation mapping with logic-based reasoning. To address the limitations of GPT models in spatial reasoning, we deploy Chain-of-Thought (CoT) and Tree-of-Thoughts (ToT) prompting strategies, offering insights into GPT's "cognitive process", and achieving notable improvements in accuracy.

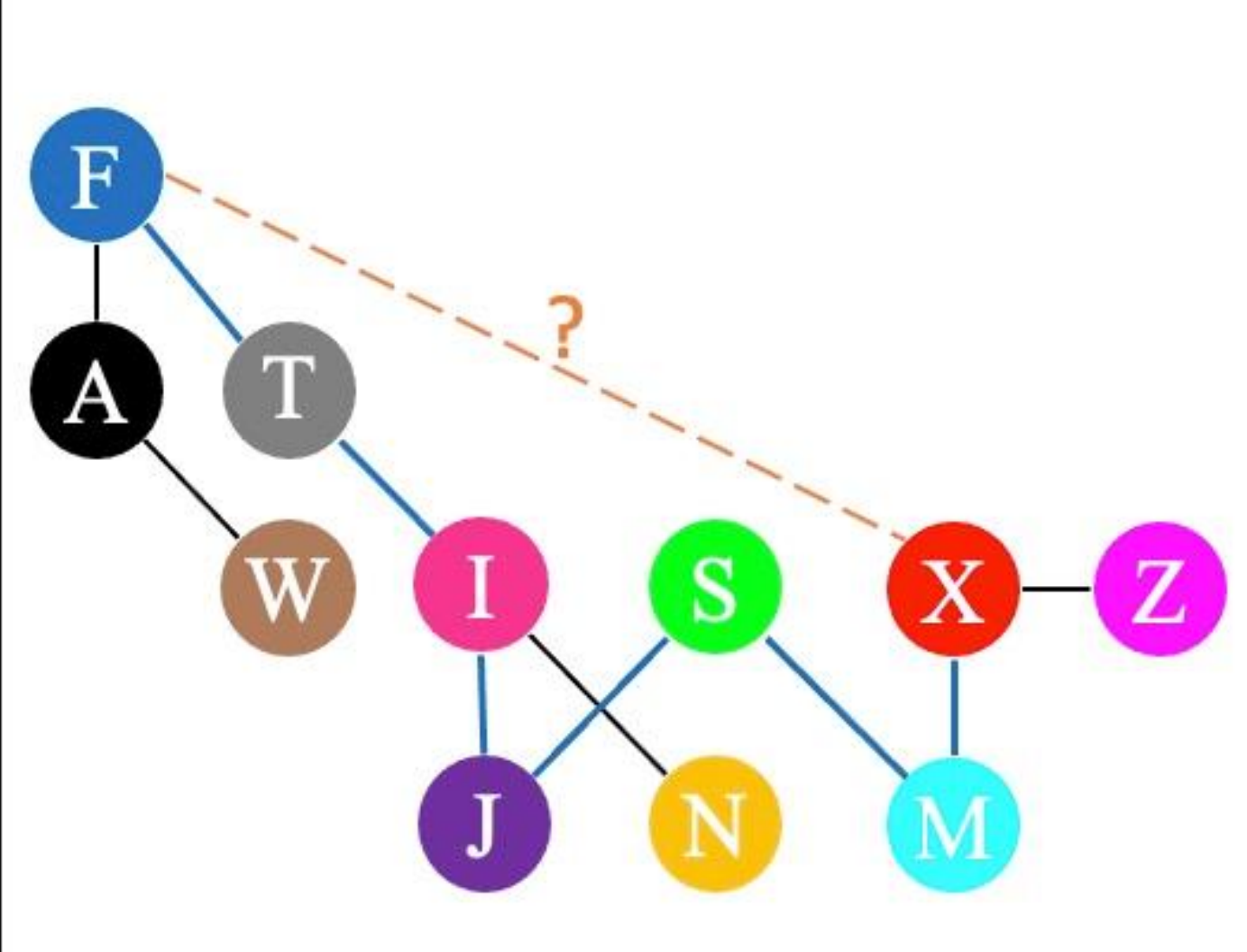
## The StepGame Benchmark

Task: multi-hop spatial reasoning in texts

### 10-hop story:

1. **F** is slightly off center to the top left and **I** is slightly off center to the bottom right.
2. **M** is at the bottom of **X**.
3. **Z** presents right to **X**.
4. **N** is lower right of **I**.
5. **S** is positioned above **J** and to the right.
6. **F** is above **I** at 10 o'clock.
7. **A** is to the upper left of **W**.
8. **A** is at the bottom of **F**.
9. **N** is sitting in the right direction of **J**.
10. **M** is placed at the lower right of **S**.

What is the relation of the agent **X** to the agent **F**?

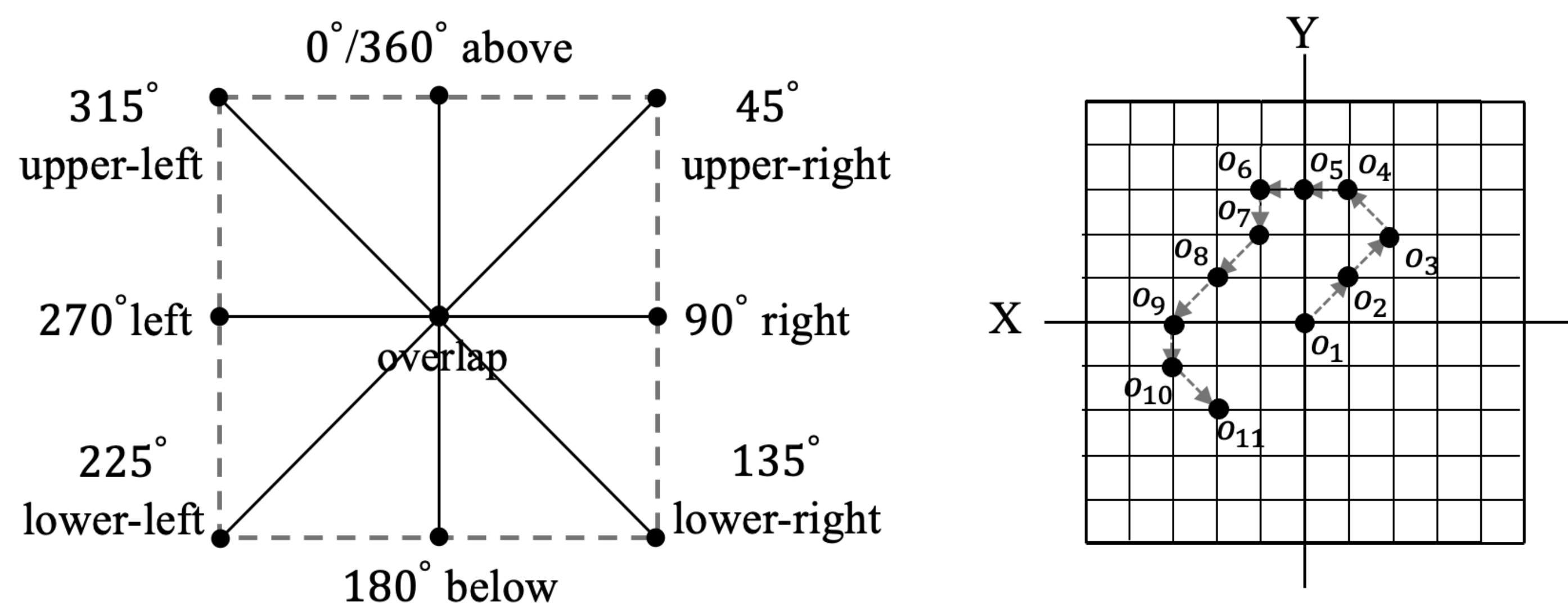


## Solution to StepGame

Sentence-to-Relation Mapping + ASP Reasoner

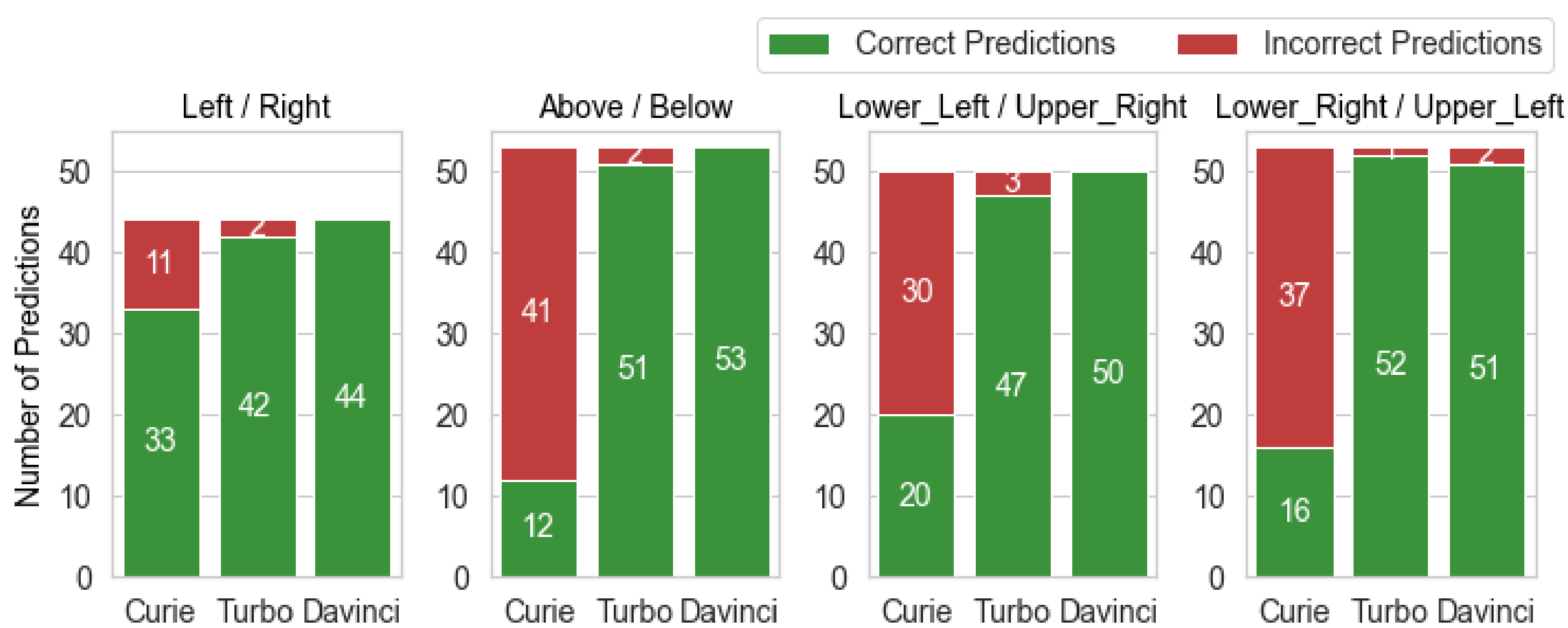
Sentences	Template	ASP Facts
Y and I are parallel, and Y is on top of I.	Y_above_I	above("Y", "I").
F is on the left side of and below Q.	F_lowerleft_Q	down_left("F", "Q").
J is at O's 6 o'clock.	J_below_O	below("J", "O").
A is directly north east of B.	A_upperright_B	up_right("A", "B").
What is the relation of the agent B to the agent J?	query_B_J	query("B", "J").

The ASP module calculates the location of  $o_i$  to  $o_j$  by adding the offsets  $v(o_i, o_j)$ .



## LLM + ASP

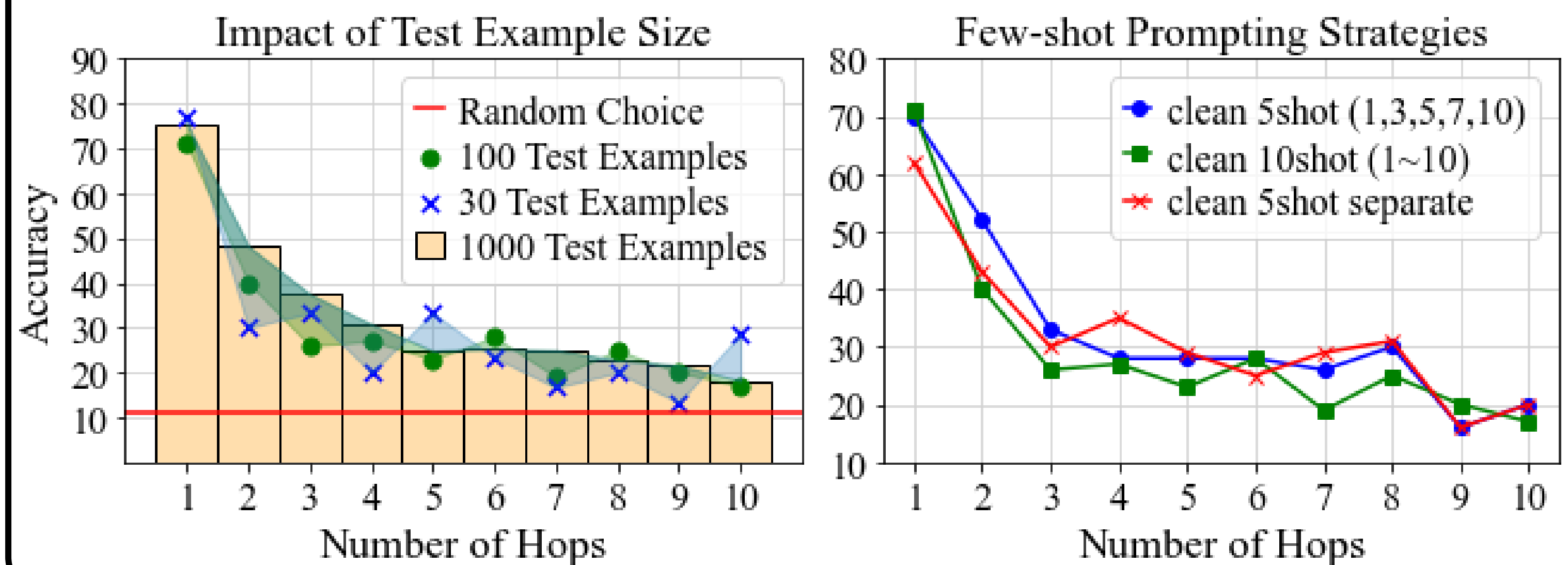
The relation extraction performance of GPT models.



Results of LLMs for relation extraction + ASP Reasoner

	k=1	k=2	k=3	k=4	k=5	k=6	k=7	k=8	k=9	k=10
Map+ASP	100	100	100	100	100	100	100	100	100	100
Curie+ASP	46	43	42	59	67	67	57	56	58	61
Davinci+ASP	100	100	99	100	100	99	100	100	100	100
SOTA	92.6	89.9	89.1	93.8	92.9	91.6	91.2	90.4	89.0	88.3

## Evaluation of GPT-3.5 Turbo on StepGame

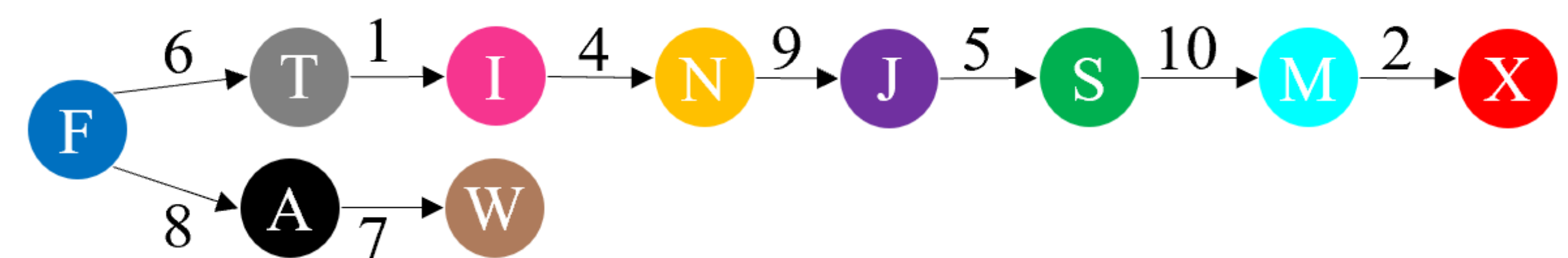


## Methods

**Our CoT approach** decomposes each step of thought  $c_i$  to incorporate a coherent and detailed reasoning process.

At reasoning step  $i$ ,  $c_i = [c_i^{link}, c_i^{map}, c_i^{calcu}]$

- $c_i^{link}$ : guide LLMs to examine all relations in story ( $R = [r^1, \dots, r^j, \dots, r^k]$ ) and select candidate  $r^j$  for each  $i$
- $c_i^{map}$ : map  $r^j$  to simple relation description  $o_i$  is to the  $v$  of  $o_{i+1}$
- $c_i^{calcu}$ : calculate the coordinate of  $o_{i+1}$  with  $r^j$ ,  $o_{i+1} = o_i + v(r^j) = (x_{o_i}, y_{o_i}) + (x_v, y_v) = (x_{o_{i+1}}, y_{o_{i+1}})$



**Our ToT approach** is designed to enhance the chain building process, allowing LLMs to consider different pathways.

Require: LLM, input  $x$

- 1:  $S_0 \leftarrow \text{Init}(x)$
- 2:  $i \leftarrow 1$
- 3: **while** no  $s_f \in S_{i-1}$  has arrived at  $o_t$  **do**
- 4:  $S'_i \leftarrow \{s \cdot c | c \in G(s, j) \wedge \text{ChainExtn}(c) \wedge s \in S_{i-1}\}$
- 5: **if**  $S'_i = \emptyset$  **then return failure**
- 6:  $S_i \leftarrow \text{select}(b, \{\langle s, y \rangle | s \in S'_i \wedge y = \sum_1^n \sigma(V(s))\})$
- 7:  $i = i + 1$
- 8: **end while**
- 9: **return**  $\text{Link}(S_f)$

## Results - Accuracy

		k=1	k=2	k=3	k=4	k=5	k=6	k=7	k=8	k=9	k=10
Turbo	base	62	43	30	35	29	25	29	31	16	20
	CoT	/	34	40	36	28	28	26	31	25	24
	ToT	/	/	35	35	25	45	15	40	40	35
Davinci	base	77	42	21	26	25	30	23	23	22	22
	CoT	/	48	53	46	46	48	40	45	41	32
	ToT	/	/	65	50	45	60	50	50	55	50
GPT-4	base	100	70	55	45	40	25	40	35	35	25
	CoT	/	80	75	95	85	85	90	80	60	65
	ToT	/	/	85	85	90	90	85	90	100	95