

The Complete Smith Chart

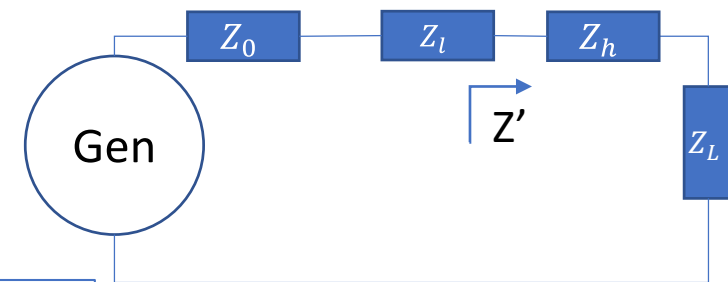
Black Magic Design

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$$\text{High impedance } Z_h = 100\Omega, m = \frac{Z_h}{Z_0} = \frac{100}{50} = 2$$

$$\text{Low impedance } Z_l = 25\Omega, n = \frac{Z_0}{Z_l} = \frac{50}{25} = 2$$

$$P = \frac{1}{m^2 n^2} = 0.0625, Q = \frac{1}{n^2} = 0.25, R = n^2 = 4, R = n^2 m^2 = 16$$



Load $Z_L = 20 - j15$, normalize to generator

$$z_L = \frac{Z_L}{Z_0} = \frac{20 - j15}{50} = 0.8 - j0.6, \text{ which falls in } Z_h \text{ region, so } Z_h \text{ is closer to load}$$

Load $Z_L = 20 - j15$, normalize to $Z_h = 100\Omega$

$$z_{L100} = \frac{Z_L}{Z_h} = \frac{20 - j15}{100} = 0.2 - j0.15$$

So point $A = 0.2, B = 5$

Renormalize A & B to Load $Z_l = 25\Omega$

$$A' = A \times \frac{100}{25} = 0.8, B' = B \times \frac{100}{25} = 20$$

Generator normalize to $Z_l = 25\Omega$

$$z_{025} = \frac{50}{25} = 2$$

By smith chart, $z'_{25} = 0.84\Omega + j0.77\Omega$

Z' is seen at $Z_l = 25\Omega$ from $Z_h = 100\Omega$

$$\text{De-normalize } Z' = z'_{25} \times 25 = (0.81 + j0.6) \times 25 = 20.25\Omega + j15\Omega$$

$$\text{Renormalize } Z' \text{ to } Z_h, z'_{100} = \frac{z'_{100}}{100} = \frac{20.25 + j15}{100} = 0.2 + j0.15$$

Given $f=4\text{GHz}$, From smith chart,

$$\lambda_h = (0.5 - 0.476) + 0.026 = 0.05\lambda \rightarrow \text{Degree}_h = 18^\circ$$

$$W_h = 0.74913\text{mm}, L_h = 2.19827\text{mm}$$

$$\lambda_l = 0.25 - 0.126 = 0.124\lambda \rightarrow \text{Degree}_l = 44.64^\circ$$

$$W_l = 8.61031\text{mm}, L_l = 4.97798\text{mm}$$

