CSIT6000F Artificial Intelligence Fall 2018 Final 12/12/2018

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Name:

Time Limit: 180 Minutes

Instructions:

- 1. This exam contains 17 pages (including this cover page) and 13 questions.
- 2. This is a closed book exam.
- 3. Please write only in the exam paper. You can use either pen or pencil.

Grade Table (for teacher use only)

Question	Points	Score
Production Systems	5	
Search Problem Formulation	8	
Probabilistic Transition Relation	2	
A* Search	12	
Alpha-Beta Pruning	6	
Game Theory	8	
Representation in PL	5	
Representation in FOL	10	
Uncertainty	10	
MDP	10	
Fitness Function	3	
Linear Features	3	
Perceptron Learning and GSCA Rule Learning	18	
Total:	100	

Question 1: Production Systems 5 points

Recall that our boundary-following robot has eight sensors s_1 - s_8 that detect if the eight surrounding cells are free for it to occupy: clockwisely, s_1 returns 1 iff the surrounding cell in the north-west direction is not free for it to occupy, s_2 returns 1 iff the surrounding cell in the north direction is not free for it to occupy, and so on. The robot has four actions: going north, east, south, and west. Now consider the following production system:

 $\overline{s_2} \rightarrow north,$

 $\overline{s_4} \rightarrow east,$

 $\overline{s_6} \rightarrow south,$

 $\overline{s_8} \rightarrow west,$

 $1 \rightarrow north.$

Give the sequence of moves by a robot controlled by this production system in a 5x5 grid without any obstacles, starting at cell (1,5) (the top left corner).

two neighbouring numbers. • Formulate this problem as a search problem by describing states, initial					
actions, and goals.					
	• Give a non-trivial admissible heuristic function for this search problem.				

Fore	Stion 3: Probabilistic Transition Relation
la	ast question. We will take any reasonable definition. (This question may be conceptual difficult to you. It's just 2 points, so don't spent too much time on it.)

Consider the following state space with the indicated initial state and the goal state. The number next to an arc is the cost of the corresponding operator, and the number next to a state is its heuristic value.

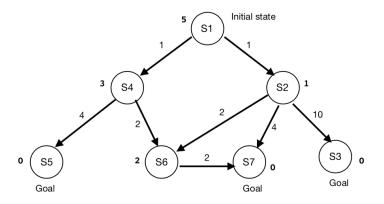


Figure 1: A search problem

- (8 pts) Give the sequence of the nodes expanded by A^* algorithm, starting from the root and terminating at a goal node. Notice that whenever there is a tie, we prefer newly generated nodes (i.e. those at deeper levels), and on the same level, left to right.
- (2 pts) Can you come up with an admissible heuristic function so that using it, your A* search will return the goal state S3? If yes, give such an admissible heuristic function. If no, please explain why not.
- (2 pts) Can you come up with an admissible heuristic function so that using it, your A* search will return the goal state S5 without using any tie-breaking rule? If yes, give such an admissible heuristic function. If no, please explain why not.

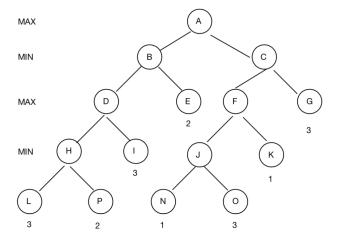


Figure 2: A minimax search tree

- (2 pts) What are the values of nodes A, B and C?
- (4 pts) Perform a left-to-right alpha-beta pruning. Which nodes are pruned? Notice that Left-to-right means that whenever a node is expanded, it's children are considered in the order from left to right. This means the leaf nodes are generated from left to right. So the first leaf node considered is L, followed by P, followed by I and so on.

Question 6: Game Theory. There are two bars. Each can choose to set its price for a beer, either \$2, \$4, cost of obtaining and serving the beer can be neglected. It is expected that per month are drunk in a bar by tourists, who choose one of the two bars rand 4000 beers per month are drunk by natives who go to the bar with the lowest split evenly in case both bars offer the same price. What prices would the bar	or \$5. The 6000 beers domly, and price, and				
Solve this problem by formalizing the strategic situation as a game in normal between these two bars and find a solution by computing the pure Nash equilibrium.					

Question 7: Representation	in PL	.5 poir	ıts
Suppose we use			

- \bullet p for "He has a high CGA",
- q for "He took Math3211",
- \bullet r for "He will graduate with first-class honor".

Represent the following sentences in propositional logic:

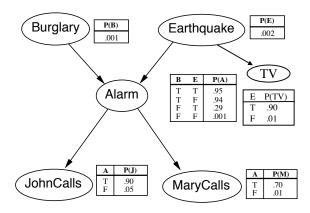
- 1. He has a high CGA and will graduate with first-class honor.
- 2. He does not have a high CGA but will still graduate with first-class honor.
- 3. He has a high CGA because he did not take Math3211.
- 4. If he has a high CGA, then he did not take Math3211.
- 5. He either has a high CGA or took Math3211, but not both.

- on(x, y): box x is on top of box y.
- ontable(x): box x is on the table.
- clear(x): box x is clear to move.
- CanMove(x, y, z): box x can be moved from y to z.

Represent the following statements in first-order logic:

- 1. (2 pts) A box can have at most one box on top of it.
- 2. (2 pts) A box is either on top of another box or on the table.
- 3. (2 pts) A box cannot be on top of two different boxes.
- 4. (2 pts) A box is clear to move if and only if there is no other box on top of it.
- 5. (2 pts) A box x can be moved from y to z if and only if x is clear to move, x is on y, and z is clear to move.

Consider the following Bayesian network which adds one more node, TV (whether there is a TV report on earthquake), to Pearl's example. There is also a new arc from Earthquake to TV and the associated conditional probability table:



- 1. (2 pts) Are Burglary and TV independent given JohnCalls? Explain your answer using D-separation.
- 2. (4 pts) Compute the probability of Earthquake given Alarm is true: P(E|A). There is no need to perform numerical calculations. Your answer can be an expression of numbers like $P(E)P(B)/P(TV|E) = .001 \times .002/.90$.
- 3. (4 pts) Compute the probability of Earthquake given Alarm is true and TV is not true: $P(E|A, \neg TV)$. Again, there is no need to perform numerical calculations.



Consider a 4×3 stochastic grid world laid out in the figure below (the crossed-out cell is an obstacle). The agent starts in state (1,1), and has four available actions: *North*, *South*, *West*, *East*. For each action, the agent goes forward with 0.8 probability, goes left and right with 0.1 probability respectively. If there is a wall, the agent stays at current location. For example, if the agent move *East* in cell (1,3), then she'll end up with 0.8 probability in cell (2,3), 0.1 probability in (1,2) (goes right instead), and 0.1 probability in the same cell (1,3) (goes left, which is a wall). At the terminating states (4,2) and (4,3), the only action is *Exit*. The reward function is defined as follows:

$$R(s, a, s') = R(s') = \begin{cases} -1, & s' = (4, 2) \\ +1, & s' = (4, 3) \\ 0, & \text{otherwise} \end{cases}$$

Assume that the discount factor $\gamma = 0.9$.

Now consider the initial policy π given in the left grid in the following figure:

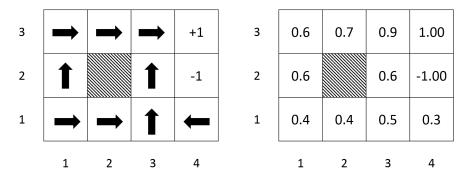


Figure 3: A 4x3 grid world and a policy: left is the policy, right its values

We have calculated its value $V_{\pi}(s)$ in every state s, as shown in the right grid of the above figure. Now for $s_0 = (1, 1)$, do the following:

- 1. Compute $T(s_0, North, s)$ for all s.
- 2. Compute $Q_{\pi}(s_0, North)$.

Give the result rounded up to one significant point. Recall the following formula for $Q_{\pi}(s, a)$:

$$Q_{\pi}(s, a) = \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma V_{\pi}(s')]$$

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or $x_1 \bigoplus x_2$ given by the following truth table is	_
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	, f_k so that each feature f_i can be defined linearly from the output $x_1 \bigoplus x_2$ can be defined linearly from

Question 13: Perceptron Learning and GSCA Rule Learning 18 points Consider the following data set:

ID	x_1	x_2	x_3	OK
1	0	0	0	Yes
2	0	0	1	No
3	1	0	0	Yes
4	1	1	0	No

where $x_1, x_2,$ and x_3 are some features that should not concern us here.

1. (8 pts) Use these four instances to train a single perceptron using the error-correction procedure. Use the learning rate = 1, and the initial weights all equal to 0. Recall that the threshold is considered to be a new input that always have value "1". Please give your answer by filling in the following table, where weight vector (w_1, w_2, w_3, t) means that w_i is the weight of input x_i , and t is the weight for the new input corresponding to the threshold. Stop when the weight vector converges. If it doesn't converge, explain why not.

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ID	Weight vector (w_1, w_2, w_3, t)
Initial	(0, 0, 0, 0)
1	
2	
3	
4	
1	
2	
3	
4	
1	
2	
3	
4	

2. (4 pts) What is the Boolean function corresponding to your perceptron?