## 1 Quantitative model of sovereign debt

Use the model presented in section 6 of Aguiar and Amador (2014) to solve the following:

1. Compute the Bond-price schedule  $q(b_{t+1}, y_t)$  using the following parametrization:

$$\bullet \ \beta \ = \ 0.95, \ y \ \in \ \{0.9,1,1.05\}, \ \pi_{yy'} \ = \ \left[ \begin{array}{ccc} 0.5 & 0.3 & 0.2 \\ 0.1 & 0.6 & 0.3 \\ 0.2 & 0.4 & 0.4 \end{array} \right], \ u(c) \ = \ \frac{c^{1-\sigma}}{1-\sigma}; \sigma = 2, \ R = 1, \ \lambda = 0.3 \ \text{and} \ \tau = 0.2.$$

- Discretize the space for b.
- 2. Is there default along the equilibrium path?
  - (a) Adjust the parameters to have that the country is 3% of the time in default (excluded from financial markets).
  - (b) Plot the probability of default at t+1 conditional on the debt-to-GDP ratio  $b_{t+1}/y_t$ .
- 3. Using the data in default IDEA.dta (Stata file),
  - (a) Estimate a logit for the probability of default using debt/GDP as the only regressor and fixed effects.
  - (b) Simulate your model.
    - i. Estimate the logit of (a) with the simulated data.
    - ii. Select  $\tau$  and  $\beta$  such that the parameter estimates of the simulated and actual data are as close as possible.