

# Lecture 12: Visualizing and Understanding

# Administrative

Milestones due tonight on Canvas, 11:59pm

Midterm grades released on Gradescope this week

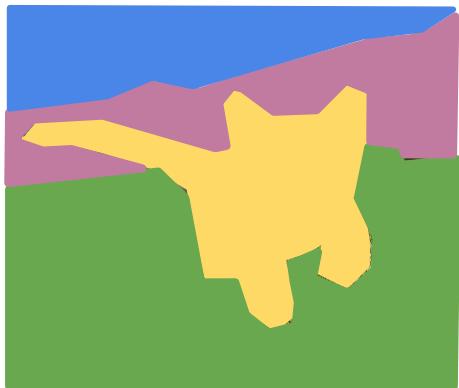
A3 due next Friday, 5/26

HyperQuest deadline extended to Sunday 5/21, 11:59pm

Poster session is June 6

# Last Time: Lots of Computer Vision Tasks

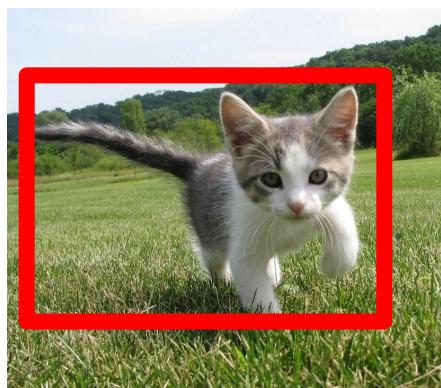
## Semantic Segmentation



GRASS, CAT,  
TREE, SKY

No objects, just pixels

## Classification + Localization



CAT

Single Object

## Object Detection



DOG, DOG, CAT

Multiple Object

## Instance Segmentation



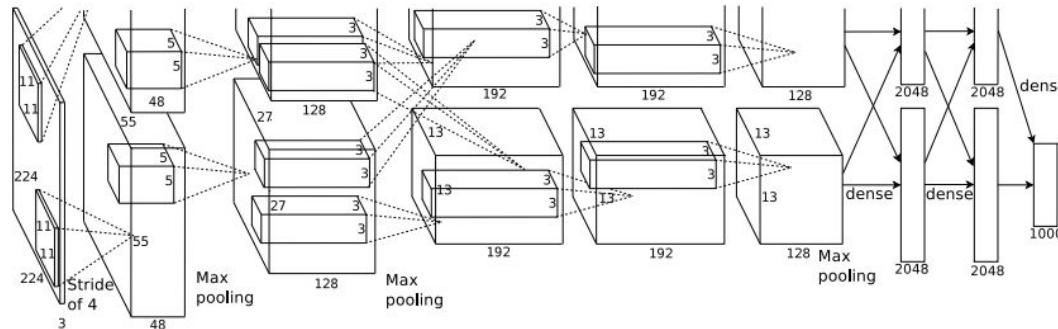
DOG, DOG, CAT

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# What's going on inside ConvNets?

This image is CC0 public domain



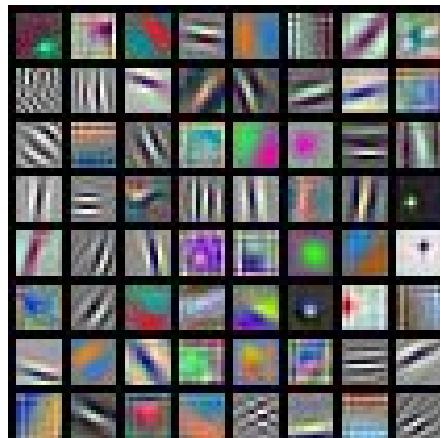
Input Image:  
3 x 224 x 224

What are the intermediate features looking for?

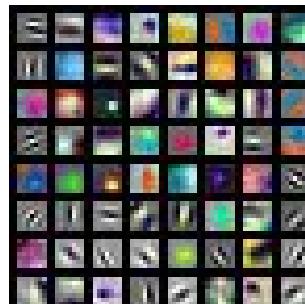
Class Scores:  
1000 numbers

Krizhevsky et al, "ImageNet Classification with Deep Convolutional Neural Networks", NIPS 2012.  
Figure reproduced with permission.

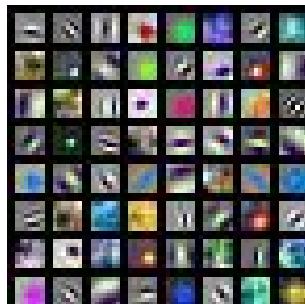
# First Layer: Visualize Filters



AlexNet:  
 $64 \times 3 \times 11 \times 11$



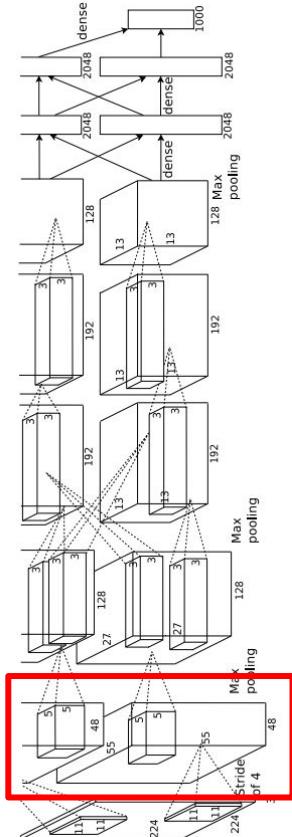
ResNet-18:  
 $64 \times 3 \times 7 \times 7$



ResNet-101:  
 $64 \times 3 \times 7 \times 7$



DenseNet-121:  
 $64 \times 3 \times 7 \times 7$



Krizhevsky, "One weird trick for parallelizing convolutional neural networks", arXiv 2014

He et al, "Deep Residual Learning for Image Recognition", CVPR 2016

Huang et al, "Densely Connected Convolutional Networks", CVPR 2017

# Visualize the filters/kernels (raw weights)

We can visualize filters at higher layers, but not that interesting

(these are taken from ConvNetJS  
CIFAR-10 demo)

Weights:  


layer 1 weights

$16 \times 3 \times 7 \times 7$

Weights:  


layer 2 weights

$20 \times 16 \times 7 \times 7$

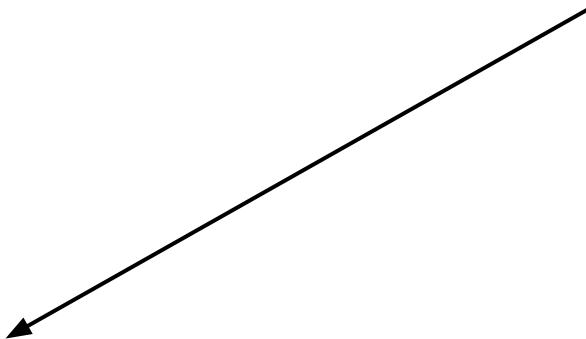
Weights:  


layer 3 weights

$20 \times 20 \times 7 \times 7$

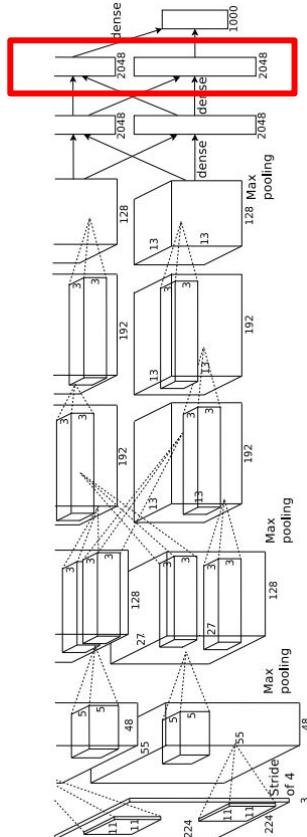
# Last Layer

FC7 layer



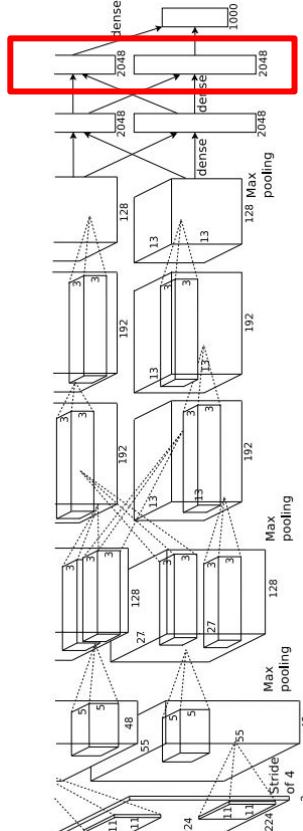
4096-dimensional feature vector for an image  
(layer immediately before the classifier)

Run the network on many images, collect the  
feature vectors



# Last Layer: Nearest Neighbors

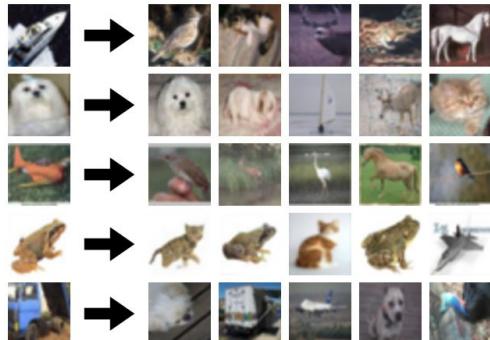
4096-dim vector



Test image L2 Nearest neighbors in feature space



**Recall:** Nearest neighbors  
in pixel space



Krizhevsky et al, "ImageNet Classification with Deep Convolutional Neural Networks", NIPS 2012.

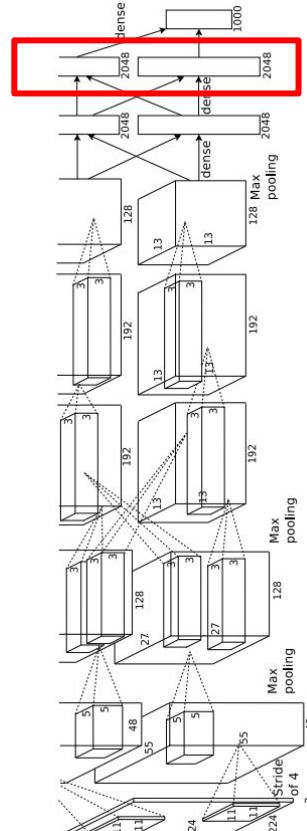
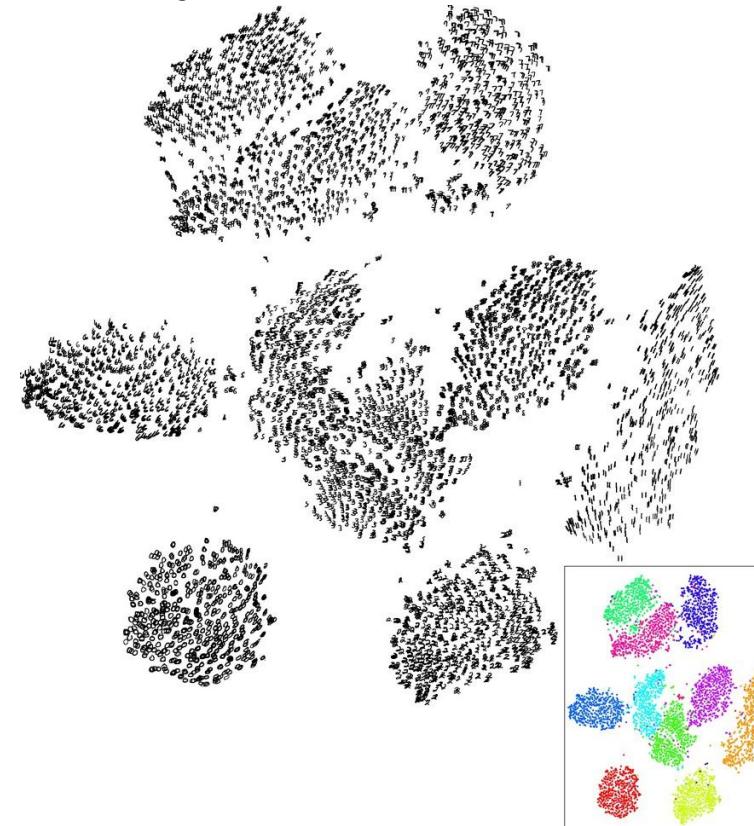
Figures reproduced with permission.

# Last Layer: Dimensionality Reduction

Visualize the “space” of FC7 feature vectors by reducing dimensionality of vectors from 4096 to 2 dimensions

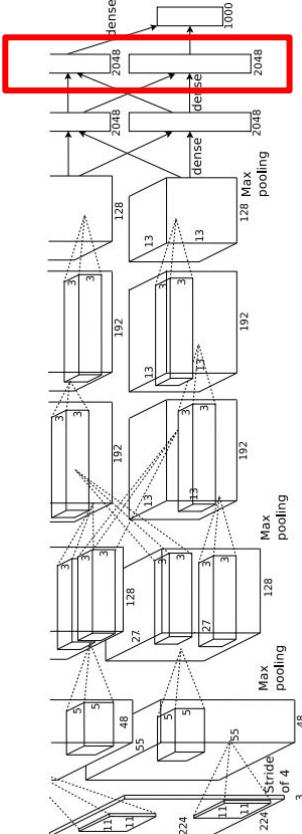
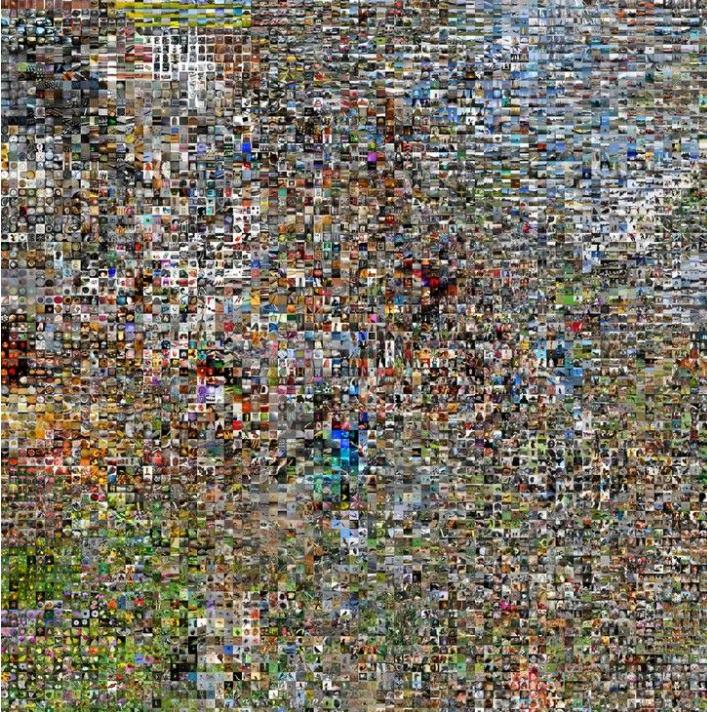
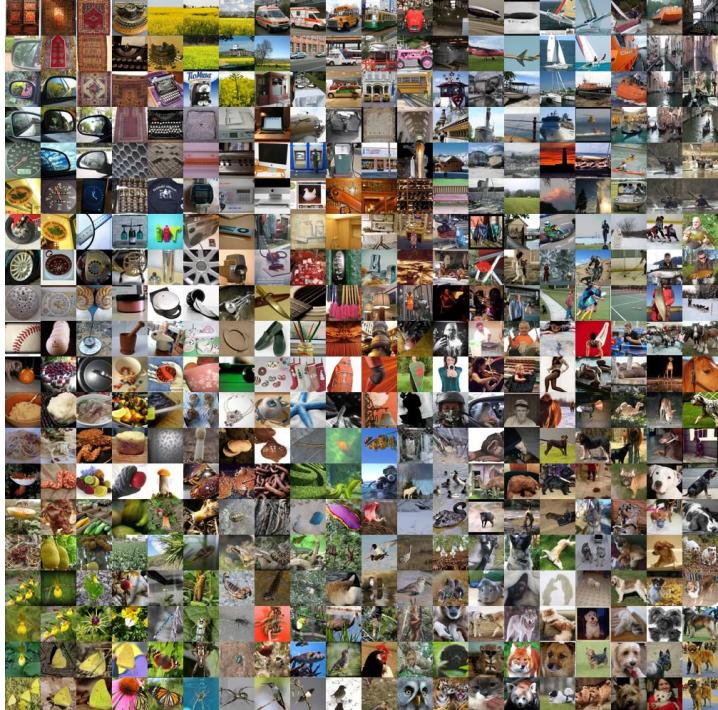
Simple algorithm: Principle Component Analysis (PCA)

More complex: t-SNE



Van der Maaten and Hinton, “Visualizing Data using t-SNE”, JMLR 2008  
Figure copyright Laurens van der Maaten and Geoff Hinton, 2008. Reproduced with permission.

# Last Layer: Dimensionality Reduction

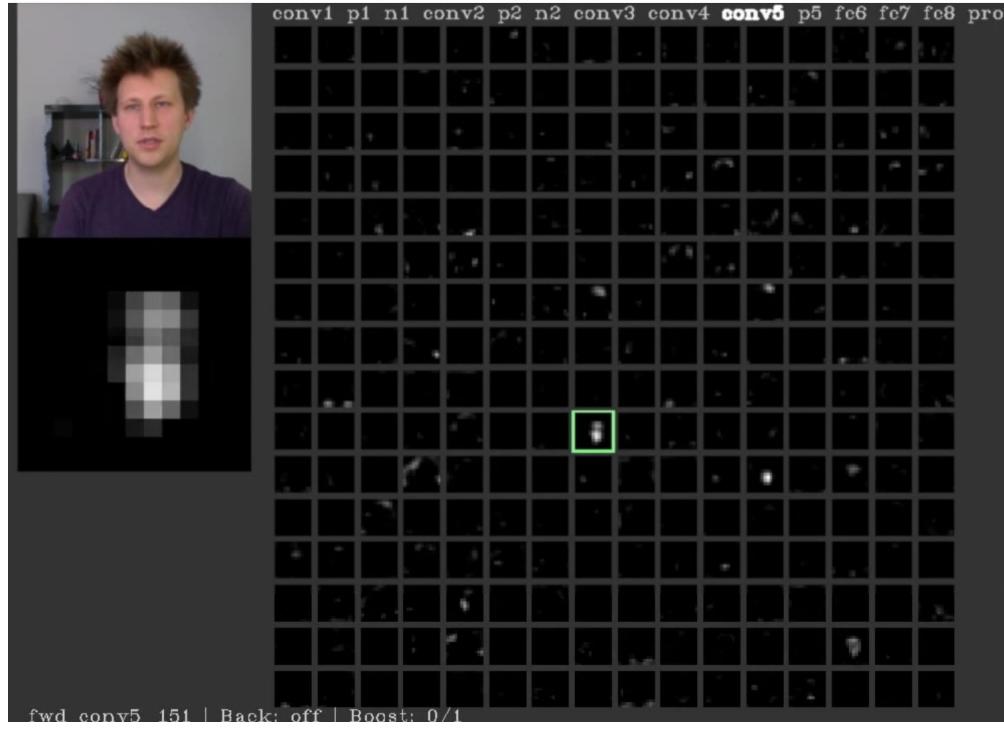


Van der Maaten and Hinton, "Visualizing Data using t-SNE", JMLR 2008  
Krizhevsky et al, "ImageNet Classification with Deep Convolutional Neural Networks", NIPS 2012.  
Figure reproduced with permission.

See high-resolution versions at  
<http://cs.stanford.edu/people/karpathy/cnnembed/>

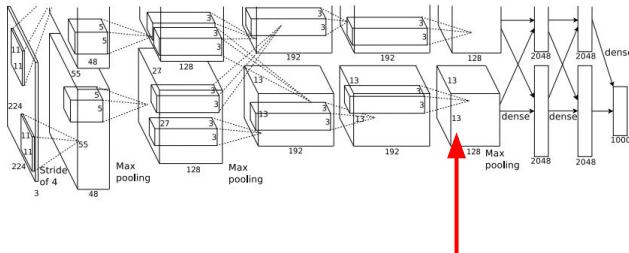
# Visualizing Activations

conv5 feature map is  
128x13x13; visualize  
as 128 13x13  
grayscale images



Yosinski et al, "Understanding Neural Networks Through Deep Visualization", ICML DL Workshop 2014.  
Figure copyright Jason Yosinski, 2014. Reproduced with permission.

# Maximally Activating Patches



Pick a layer and a channel; e.g. conv5 is 128 x 13 x 13, pick channel 17/128

Run many images through the network,  
record values of chosen channel

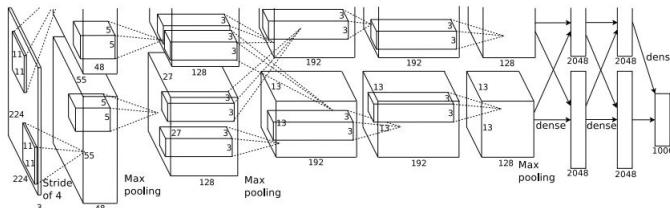
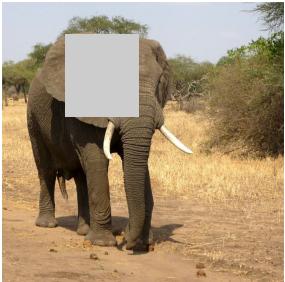
Visualize image patches that correspond  
to maximal activations



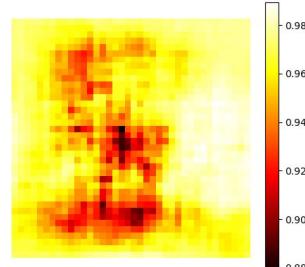
Springenberg et al, "Striving for Simplicity: The All Convolutional Net", ICLR Workshop 2015  
Figure copyright Jost Tobias Springenberg, Alexey Dosovitskiy, Thomas Brox, Martin Riedmiller, 2015;  
reproduced with permission.

# Occlusion Experiments

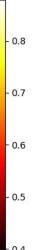
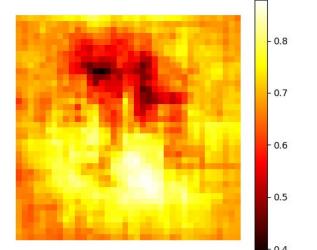
Mask part of the image before feeding to CNN, draw heatmap of probability at each mask location



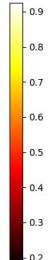
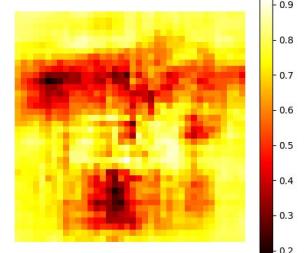
schooner



African elephant, Loxodonta africana



go-kart

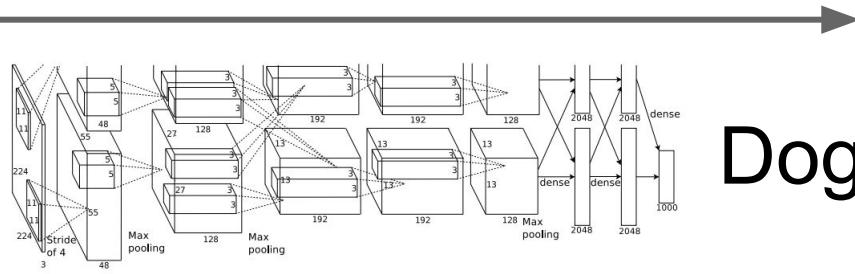


Zeiler and Fergus, "Visualizing and Understanding Convolutional Networks", ECCV 2014

Boat image is [CC0 public domain](#)  
Elephant image is [CC0 public domain](#)  
Go-Karts image is [CC0 public domain](#)

# Saliency Maps

How to tell which pixels matter for classification?



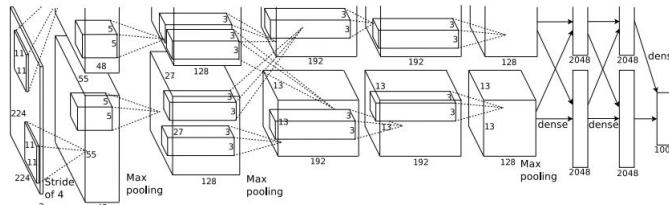
Dog

Simonyan, Vedaldi, and Zisserman, "Deep Inside Convolutional Networks: Visualising Image Classification Models and Saliency Maps", ICLR Workshop 2014.

Figures copyright Karen Simonyan, Andrea Vedaldi, and Andrew Zisserman, 2014; reproduced with permission.

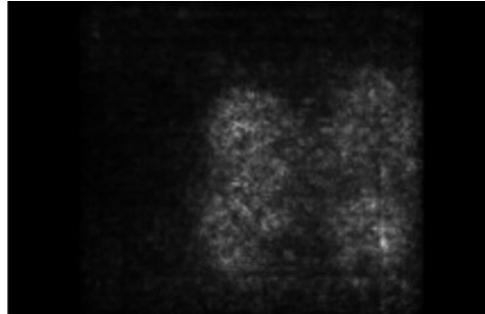
# Saliency Maps

How to tell which pixels matter for classification?



Dog

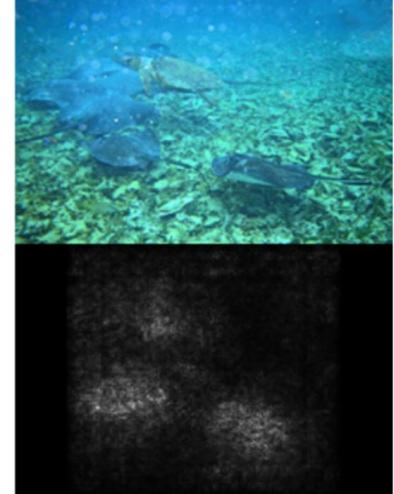
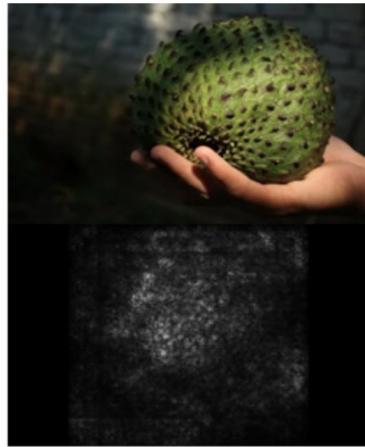
Compute gradient of (unnormalized) class score with respect to image pixels, take absolute value and max over RGB channels



Simonyan, Vedaldi, and Zisserman, "Deep Inside Convolutional Networks: Visualising Image Classification Models and Saliency Maps", ICLR Workshop 2014.

Figures copyright Karen Simonyan, Andrea Vedaldi, and Andrew Zisserman, 2014; reproduced with permission.

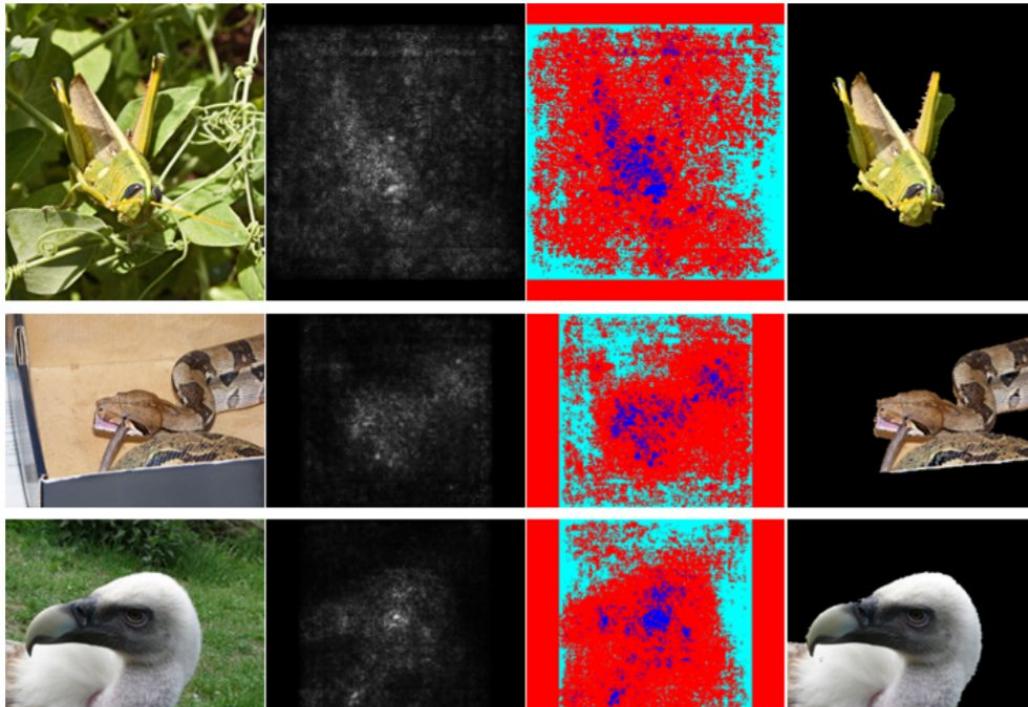
# Saliency Maps



Simonyan, Vedaldi, and Zisserman, "Deep Inside Convolutional Networks: Visualising Image Classification Models and Saliency Maps", ICLR Workshop 2014.

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# Saliency Maps: Segmentation without supervision



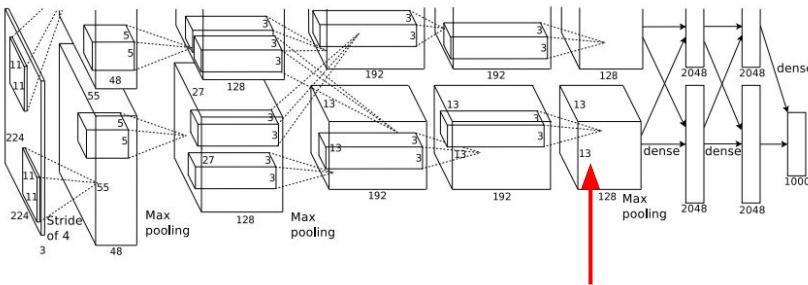
Use GrabCut on  
saliency map

Simonyan, Vedaldi, and Zisserman, "Deep Inside Convolutional Networks: Visualising Image Classification Models and Saliency Maps", ICLR Workshop 2014.

Figures copyright Karen Simonyan, Andrea Vedaldi, and Andrew Zisserman, 2014; reproduced with permission.

Rother et al, "Grabcut: Interactive foreground extraction using iterated graph cuts", ACM TOG 2004

# Intermediate Features via (guided) backprop

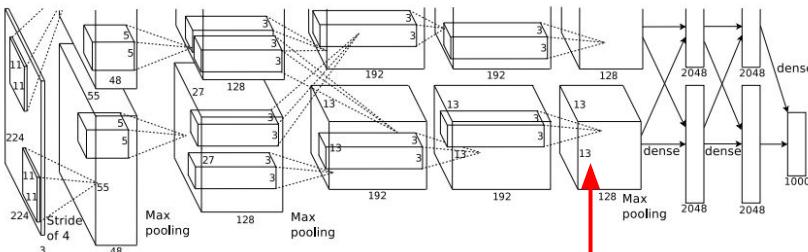


Pick a single intermediate neuron, e.g. one value in  $128 \times 13 \times 13$  conv5 feature map

Compute gradient of neuron value with respect to image pixels

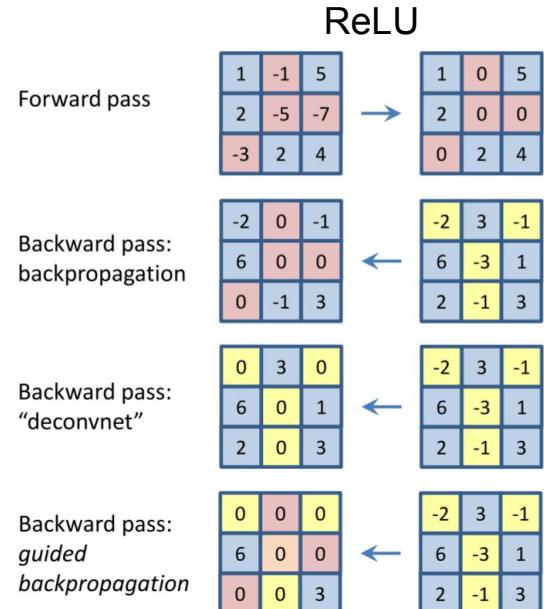
Zeiler and Fergus, "Visualizing and Understanding Convolutional Networks", ECCV 2014  
Springenberg et al, "Striving for Simplicity: The All Convolutional Net", ICLR Workshop 2015

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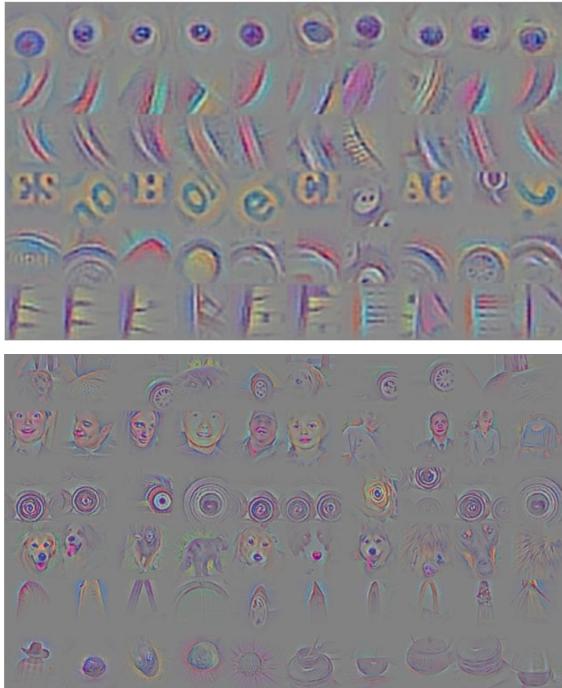


Images come out nicer if you only backprop positive gradients through each ReLU (guided backprop)

Zeiler and Fergus, "Visualizing and Understanding Convolutional Networks", ECCV 2014  
Springenberg et al, "Striving for Simplicity: The All Convolutional Net", ICLR Workshop 2015

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# Intermediate features via (guided) backprop



Zeiler and Fergus, "Visualizing and Understanding Convolutional Networks", ECCV 2014

Springenberg et al, "Striving for Simplicity: The All Convolutional Net", ICLR Workshop 2015

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# Visualizing CNN features: Gradient Ascent

**(Guided) backprop:**

Find the part of an image that a neuron responds to

**Gradient ascent:**

Generate a synthetic image that maximally activates a neuron

$$I^* = \arg \max_I f(I) + R(I)$$

Neuron value

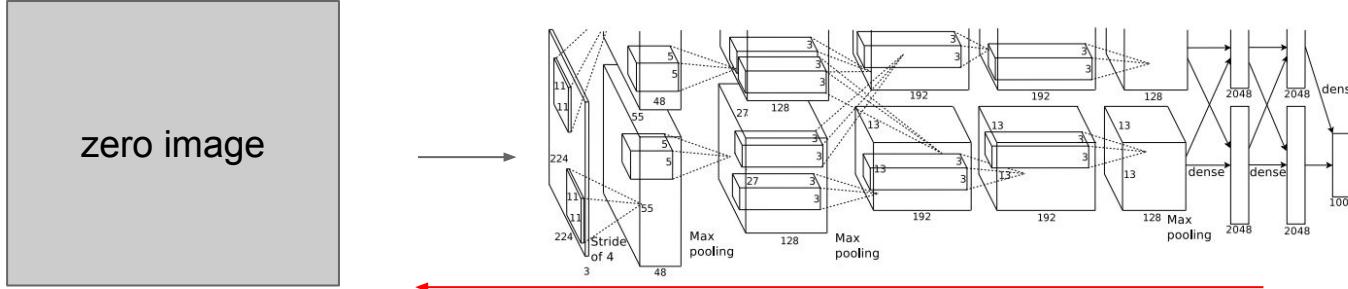
Natural image regularizer

# Visualizing CNN features: Gradient Ascent

1. Initialize image to zeros

$$\arg \max_I S_c(I) - \lambda \|I\|_2^2$$

score for class c (before Softmax)



Repeat:

2. Forward image to compute current scores
3. Backprop to get gradient of neuron value with respect to image pixels
4. Make a small update to the image

# Visualizing CNN features: Gradient Ascent

$$\arg \max_I S_c(I) - \boxed{\lambda \|I\|_2^2}$$

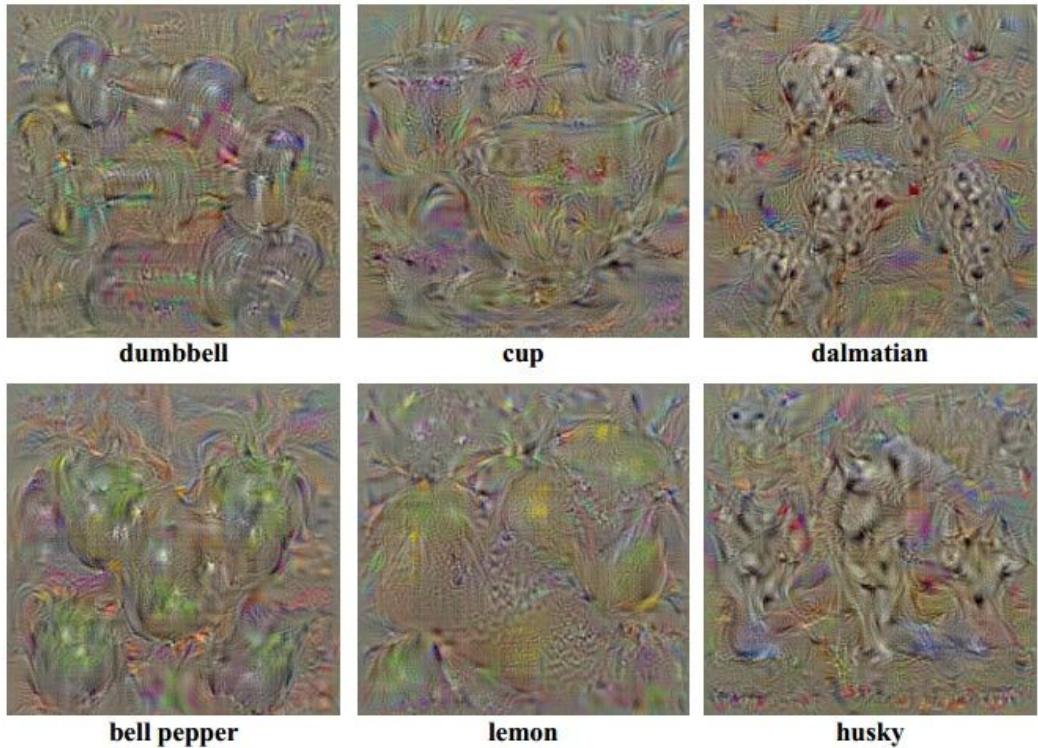
Simple regularizer: Penalize L2  
norm of generated image

Simonyan, Vedaldi, and Zisserman, "Deep Inside Convolutional Networks: Visualising Image Classification Models and Saliency Maps", ICLR Workshop 2014.  
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# Visualizing CNN features: Gradient Ascent

$$\arg \max_I S_c(I) - \boxed{\lambda \|I\|_2^2}$$

Simple regularizer: Penalize L2 norm of generated image



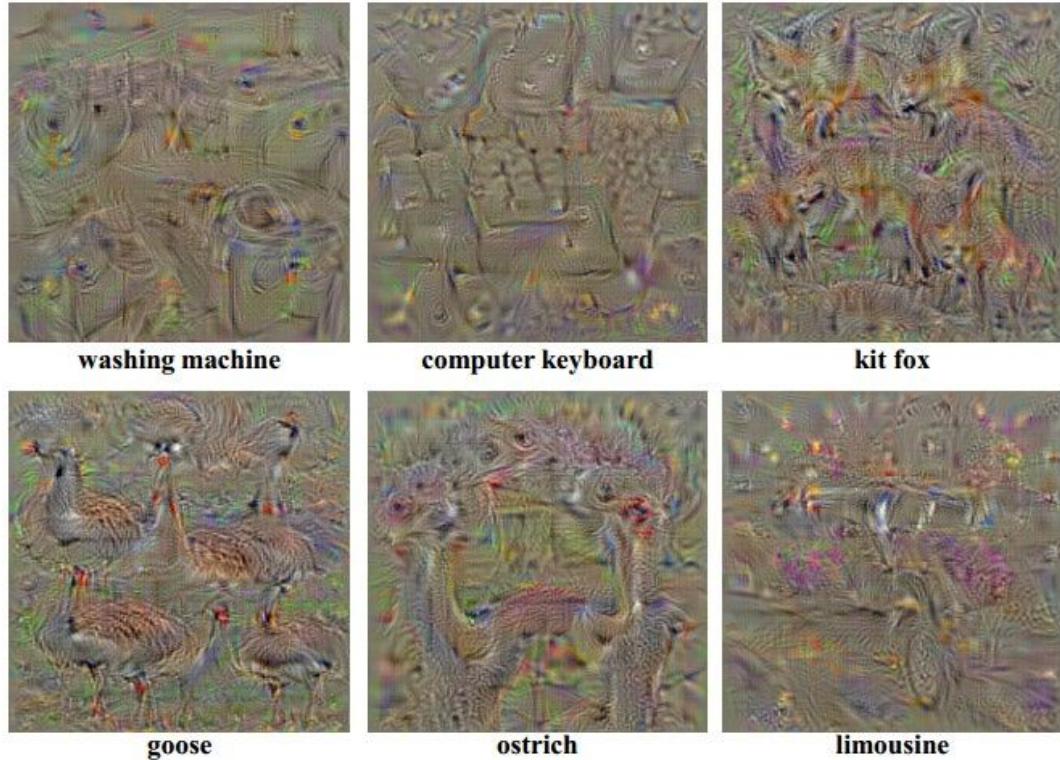
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# Visualizing CNN features: Gradient Ascent

$$\arg \max_I S_c(I) - \boxed{\lambda \|I\|_2^2}$$

Simple regularizer: Penalize L2  
norm of generated image



Yosinski et al, "Understanding Neural Networks Through Deep Visualization", ICML DL Workshop 2014.  
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# Visualizing CNN features: Gradient Ascent

$$\arg \max_I S_c(I) - \lambda \|I\|_2^2$$

Better regularizer: Penalize L2 norm of image; also during optimization periodically

- (1) Gaussian blur image
- (2) Clip pixels with small values to 0
- (3) Clip pixels with small gradients to 0

# Visualizing CNN features: Gradient Ascent

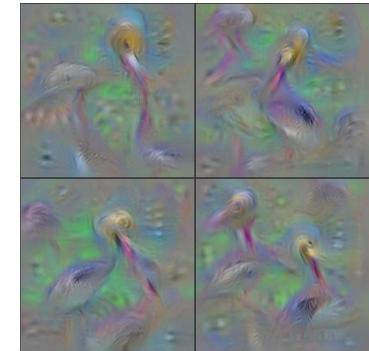
$$\arg \max_I S_c(I) - \lambda \|I\|_2^2$$

Better regularizer: Penalize L2 norm of image; also during optimization periodically

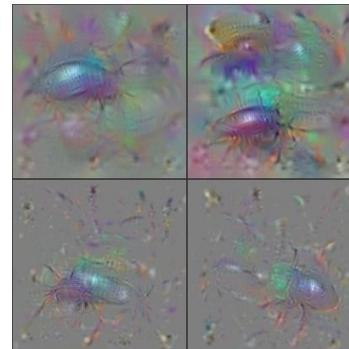
- (1) Gaussian blur image
- (2) Clip pixels with small values to 0
- (3) Clip pixels with small gradients to 0



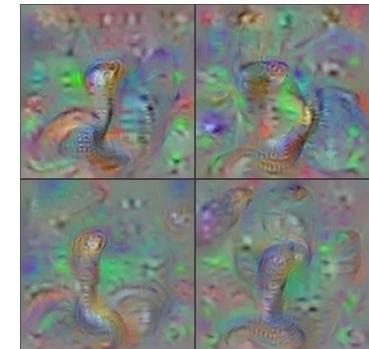
Flamingo



Pelican



Ground Beetle



Indian Cobra

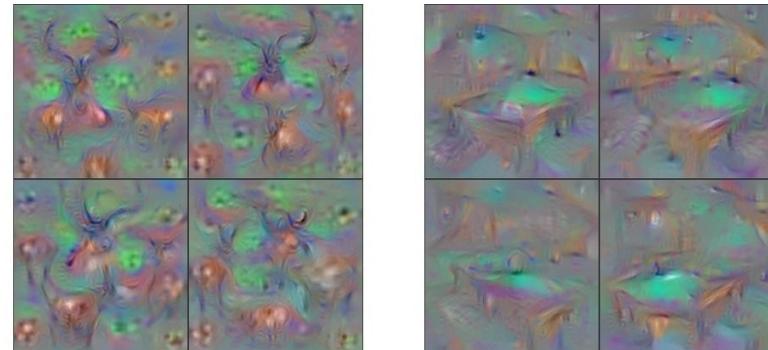
Yosinski et al, "Understanding Neural Networks Through Deep Visualization", ICML DL Workshop 2014.  
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# Visualizing CNN features: Gradient Ascent

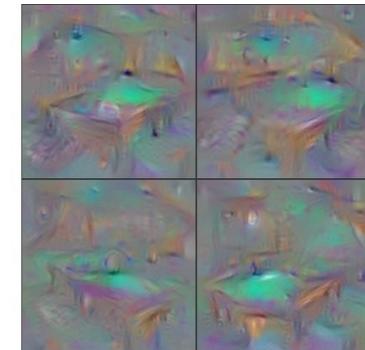
$$\arg \max_I S_c(I) - \lambda \|I\|_2^2$$

Better regularizer: Penalize L2 norm of image; also during optimization periodically

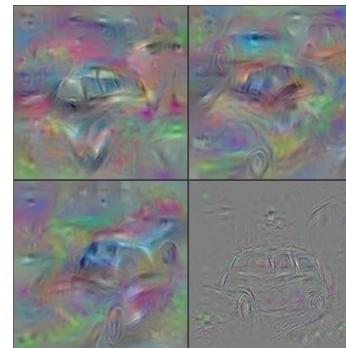
- (1) Gaussian blur image
- (2) Clip pixels with small values to 0
- (3) Clip pixels with small gradients to 0



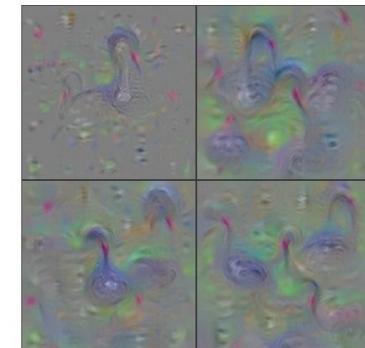
Hartebeest



Billiard Table



Station Wagon

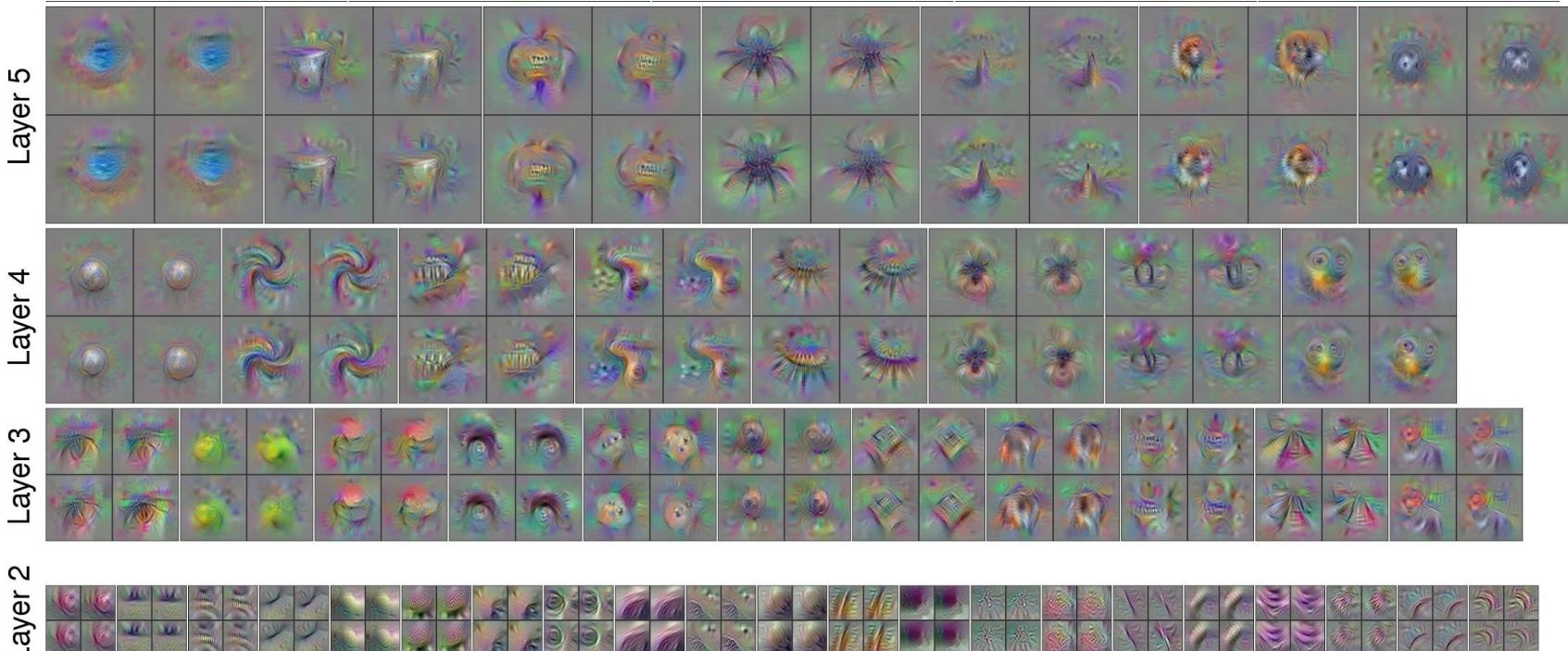


Black Swan

Yosinski et al, "Understanding Neural Networks Through Deep Visualization", ICML DL Workshop 2014.  
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# Visualizing CNN features: Gradient Ascent

Use the same approach to visualize intermediate features

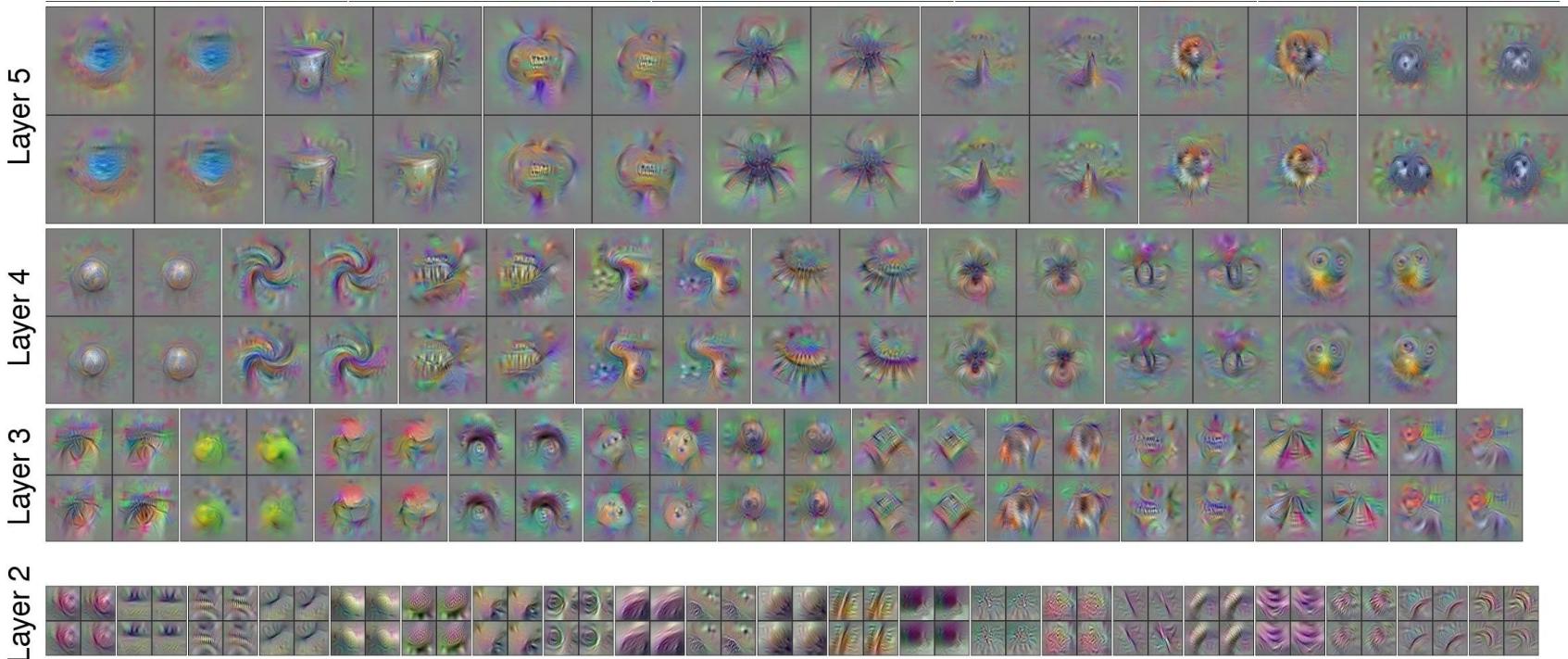


Yosinski et al, "Understanding Neural Networks Through Deep Visualization", ICML DL Workshop 2014.

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# Visualizing CNN features: Gradient Ascent

Use the same approach to visualize intermediate features



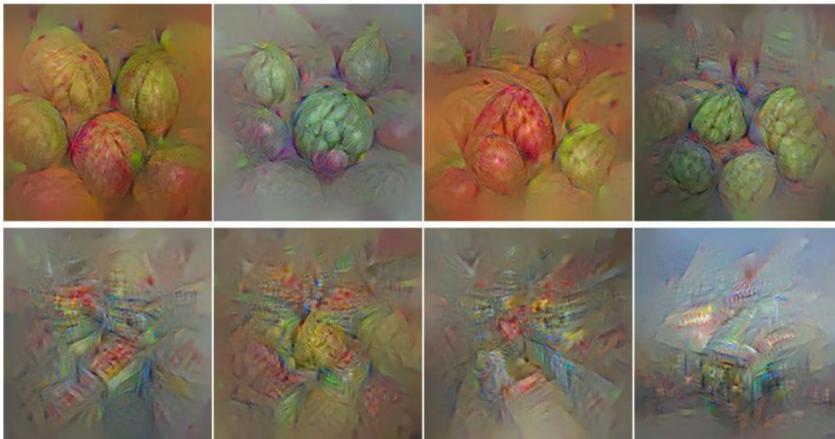
Yosinski et al, "Understanding Neural Networks Through Deep Visualization", ICML DL Workshop 2014.

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# Visualizing CNN features: Gradient Ascent

Adding “multi-faceted” visualization gives even nicer results:  
(Plus more careful regularization, center-bias)

Reconstructions of multiple feature types (facets) recognized by the same “grocery store” neuron



Corresponding example training set images recognized by the same neuron as in the “grocery store” class



Nguyen et al., “Multifaceted Feature Visualization: Uncovering the Different Types of Features Learned By Each Neuron in Deep Neural Networks”, ICML Visualization for Deep Learning Workshop 2016.  
Figures copyright Anh Nguyen, Jason Yosinski, and Jeff Clune, 2016; reproduced with permission.

# Visualizing CNN features: Gradient Ascent



Nguyen et al., "Multifaceted Feature Visualization: Uncovering the Different Types of Features Learned By Each Neuron in Deep Neural Networks", ICML Visualization for Deep Learning Workshop 2016.

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# Visualizing CNN features: Gradient Ascent

Optimize in FC6 latent space instead of pixel space:



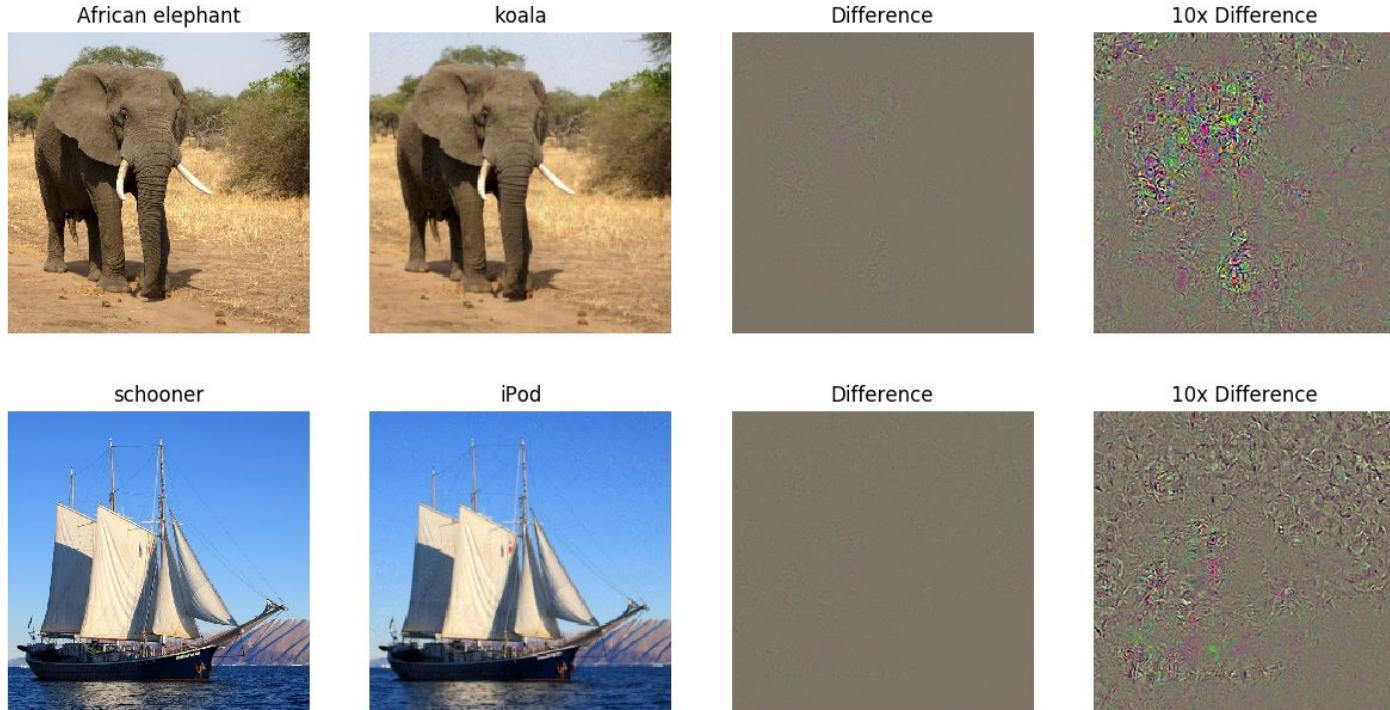
Nguyen et al., "Synthesizing the preferred inputs for neurons in neural networks via deep generator networks," NIPS 2016

Figure copyright Nguyen et al, 2016; reproduced with permission.

# Fooling Images / Adversarial Examples

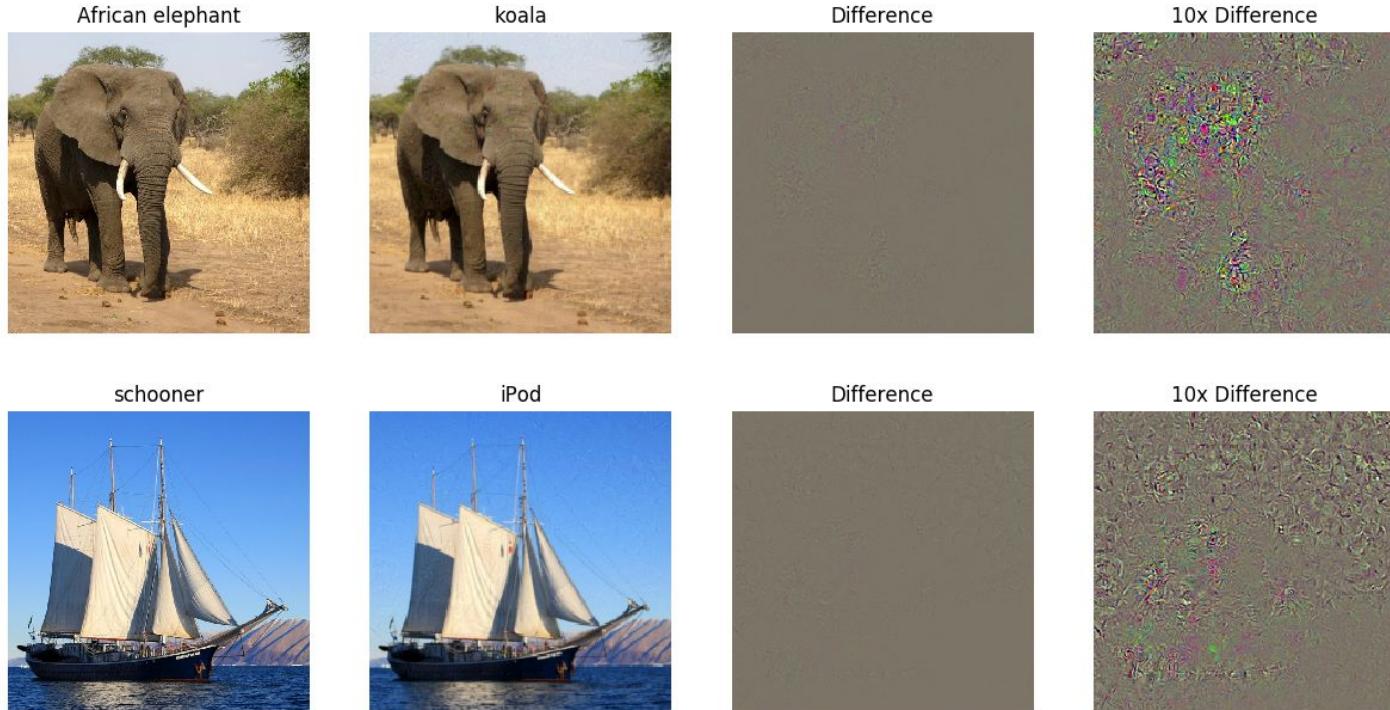
- (1) Start from an arbitrary image
- (2) Pick an arbitrary class
- (3) Modify the image to maximize the class
- (4) Repeat until network is fooled

# Fooling Images / Adversarial Examples



[Boat image is CC0 public domain](#)  
[Elephant image is CC0 public domain](#)

# Fooling Images / Adversarial Examples

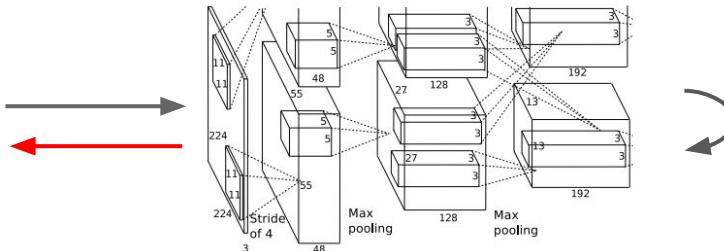


What is going on? Ian Goodfellow will explain

Boat image is CC0 public domain  
Elephant image is CC0 public domain

# DeepDream: Amplify existing features

Rather than synthesizing an image to maximize a specific neuron, instead try to **amplify** the neuron activations at some layer in the network



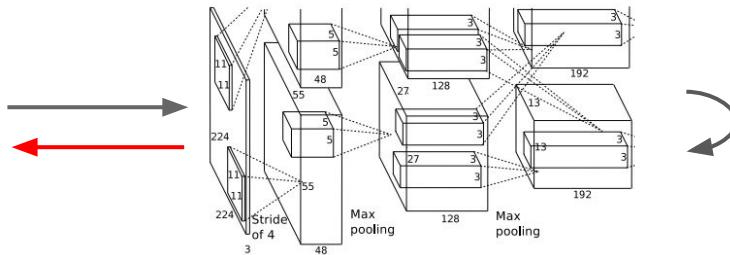
Choose an image and a layer in a CNN; repeat:

1. Forward: compute activations at chosen layer
2. Set gradient of chosen layer *equal to its activation*
3. Backward: Compute gradient on image
4. Update image

Mordvintsev, Olah, and Tyka, "Inceptionism: Going Deeper into Neural Networks", [Google Research Blog](#). Images are licensed under [CC-BY 4.0](#)

# DeepDream: Amplify existing features

Rather than synthesizing an image to maximize a specific neuron, instead try to **amplify** the neuron activations at some layer in the network



Choose an image and a layer in a CNN; repeat:

1. Forward: compute activations at chosen layer
2. Set gradient of chosen layer *equal to its activation*
3. Backward: Compute gradient on image
4. Update image

Equivalent to:

$$I^* = \arg \max_I \sum_i f_i(I)^2$$

Mordvintsev, Olah, and Tyka, "Inceptionism: Going Deeper into Neural Networks", [Google Research Blog](#). Images are licensed under [CC-BY 4.0](#).

# DeepDream: Amplify existing features

```
def objective_L2(dst):
    dst.diff[:] = dst.data

def make_step(net, step_size=1.5, end='inception_4c/output',
             jitter=32, clip=True, objective=objective_L2):
    '''Basic gradient ascent step.'''
    src = net.blobs['data'] # input image is stored in Net's 'data' blob
    dst = net.blobs[end]

    ox, oy = np.random.randint(-jitter, jitter+1, 2)
    src.data[0] = np.roll(np.roll(src.data[0], ox, -1), oy, -2) # apply jitter shift

    net.forward(end=end)
    objective(dst) # specify the optimization objective
    net.backward(start=end)
    g = src.diff[0]
    # apply normalized ascent step to the input image
    src.data[:] += step_size/np.abs(g).mean() * g

    src.data[0] = np.roll(np.roll(src.data[0], -ox, -1), -oy, -2) # unshift image

    if clip:
        bias = net.transformer.mean['data']
        src.data[:] = np.clip(src.data, -bias, 255-bias)
```

[Code](#) is very simple but it uses a couple tricks:

(Code is licensed under [Apache 2.0](#))

# DeepDream: Amplify existing features

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Jitter image

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[Code](#) is very simple but it uses a couple tricks:

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Jitter image

L1 Normalize gradients

# DeepDream: Amplify existing features

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def objective_L2(dst):
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        src.data[:] = np.clip(src.data, -bias, 255-bias)
```

[Code](#) is very simple but it uses a couple tricks:

(Code is licensed under Apache 2.0)

Jitter image

L1 Normalize gradients

Clip pixel values

Also uses multiscale processing for a fractal effect (not shown)



Sky image is licensed under CC-BY SA 3.0

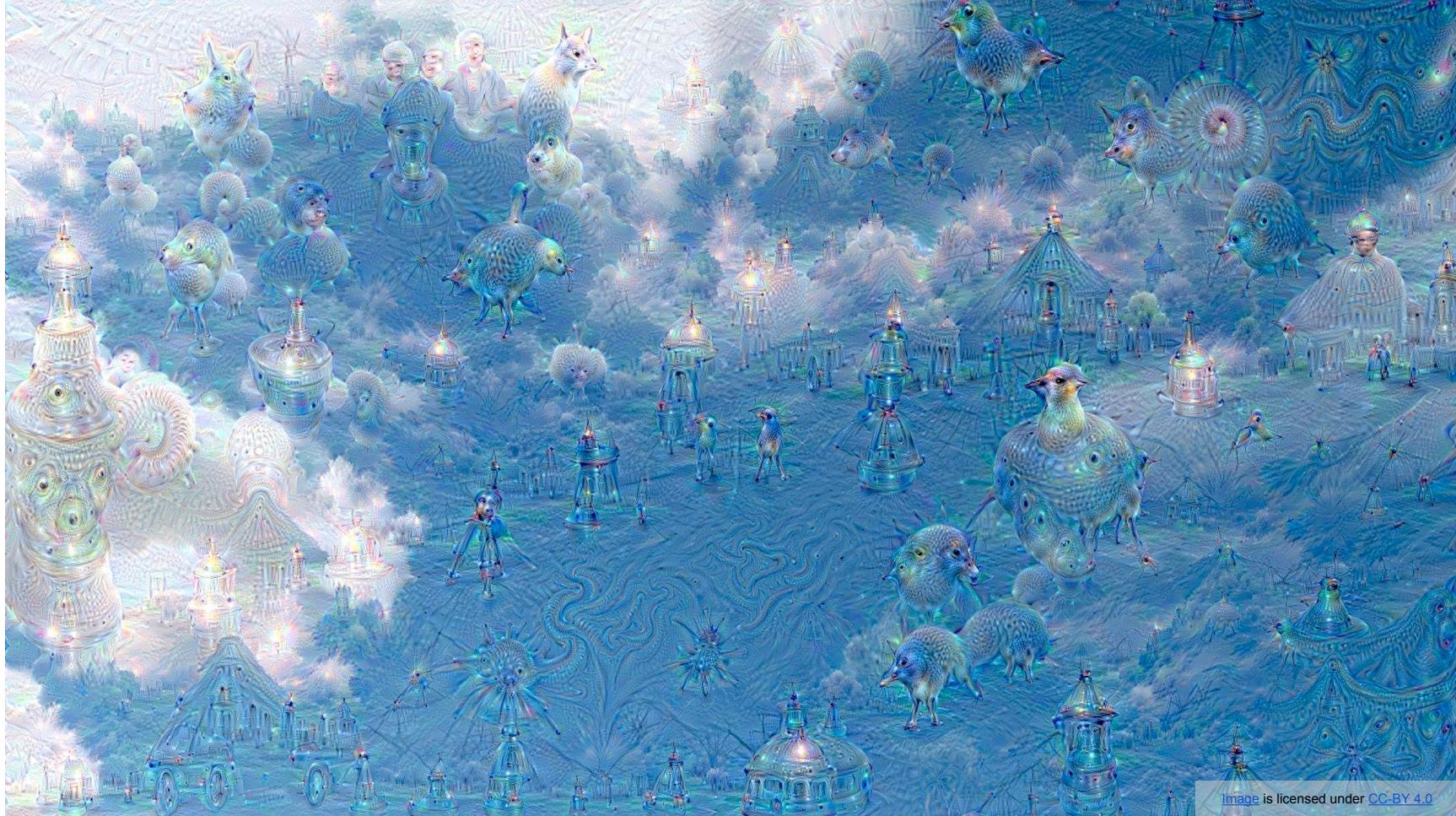
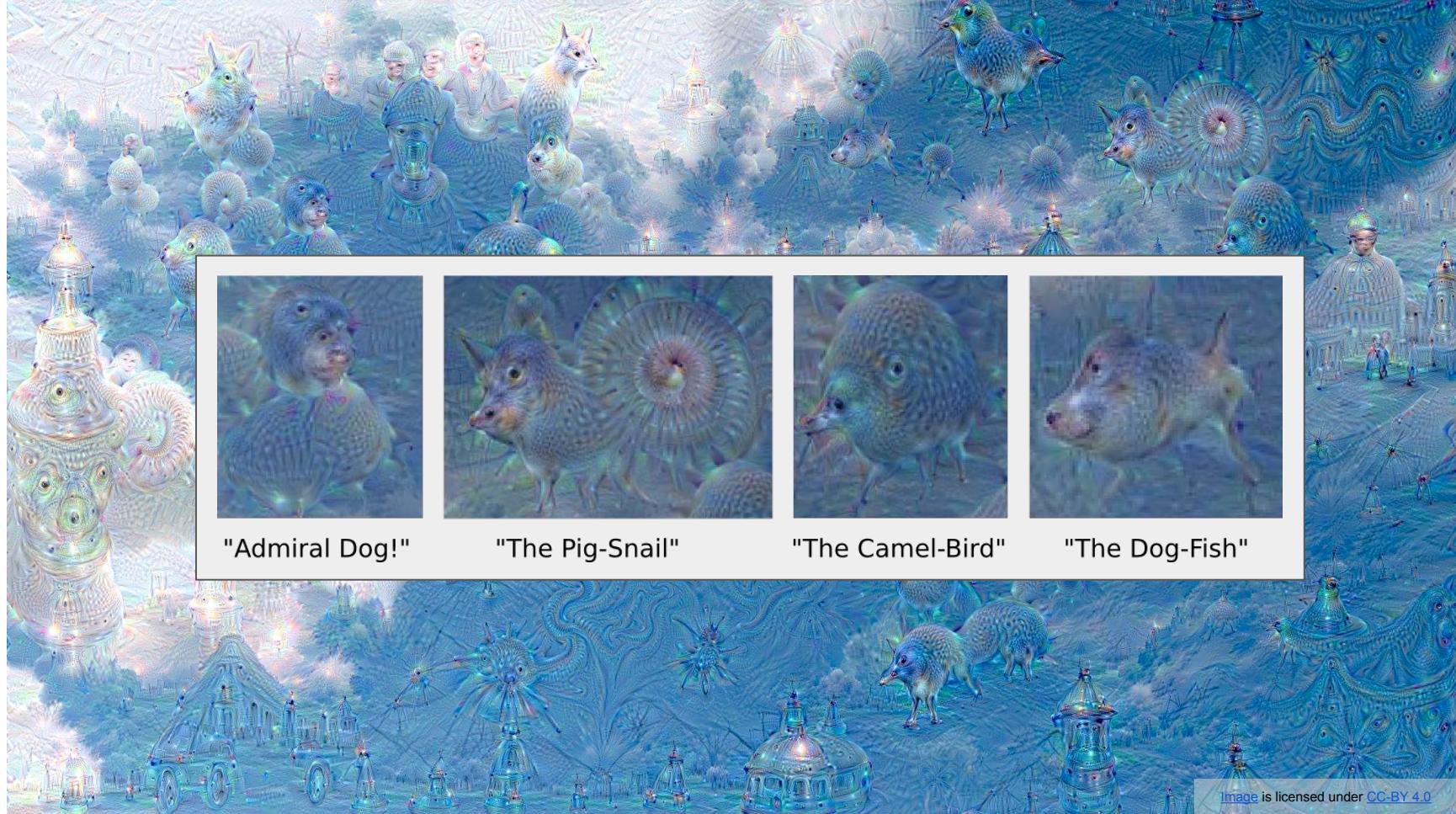


Image is licensed under CC-BY 4.0



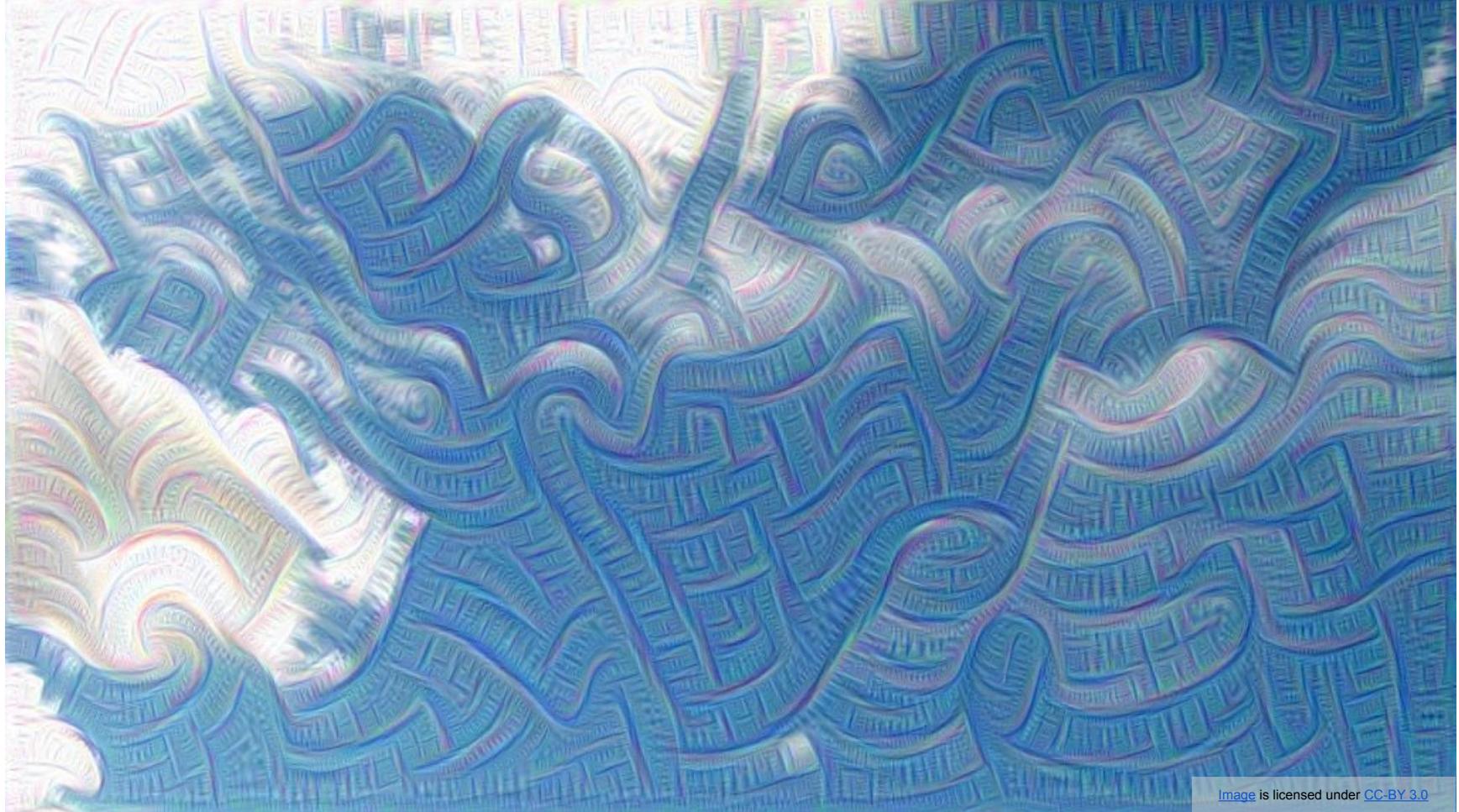
"Admiral Dog!"

"The Pig-Snail"

"The Camel-Bird"

"The Dog-Fish"

Image is licensed under CC-BY 4.0



[Image](#) is licensed under [CC-BY 3.0](#)



[Image](#) is licensed under [CC-BY 3.0](#)

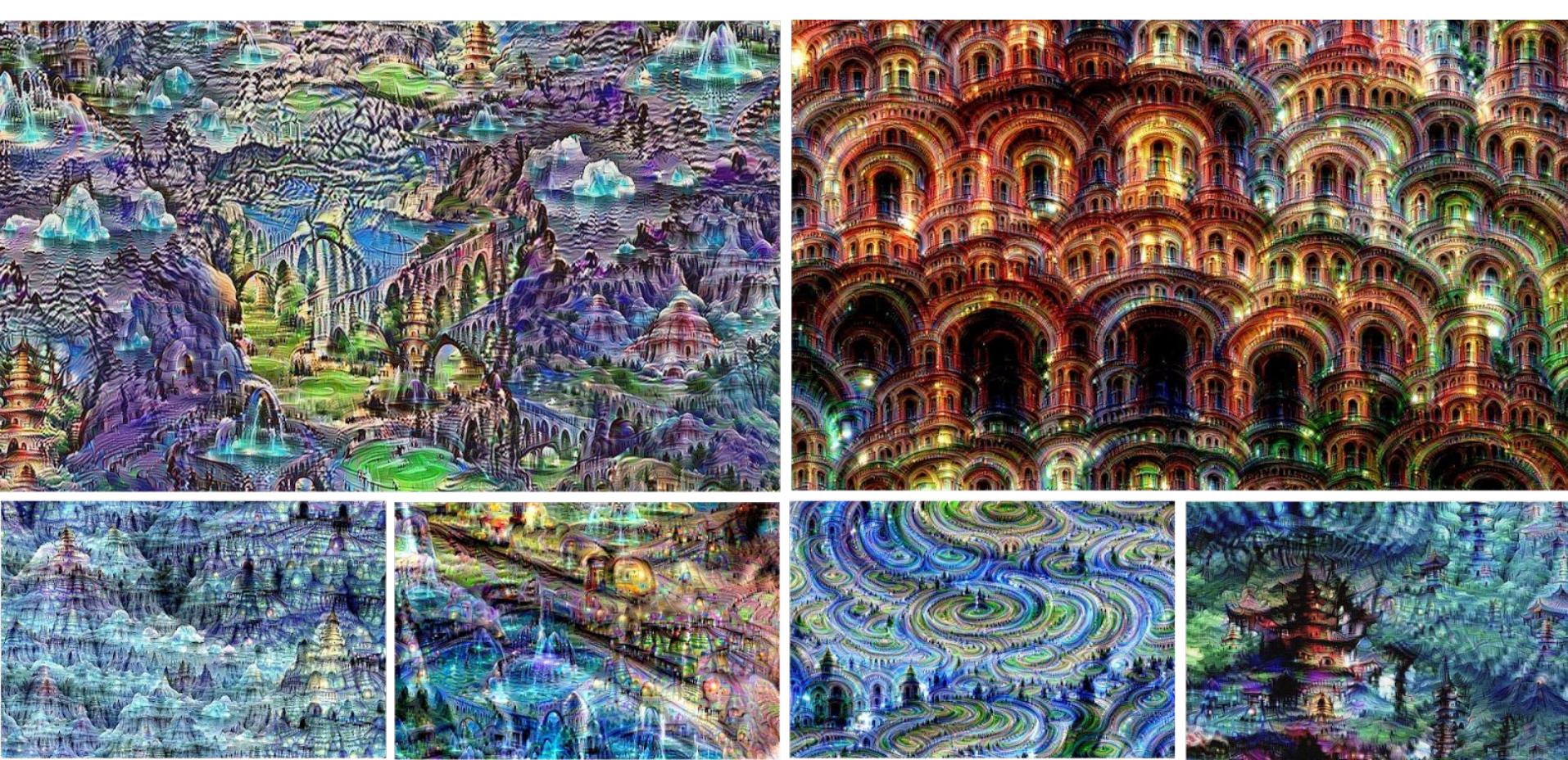


Image is licensed under CC-BY 4.0

# Feature Inversion

Given a CNN feature vector for an image, find a new image that:

- Matches the given feature vector
- “looks natural” (image prior regularization)

$$\mathbf{x}^* = \underset{\mathbf{x} \in \mathbb{R}^{H \times W \times C}}{\operatorname{argmin}} \ell(\Phi(\mathbf{x}), \Phi_0) + \lambda \mathcal{R}(\mathbf{x})$$

Given feature vector

Features of new image

$$\ell(\Phi(\mathbf{x}), \Phi_0) = \|\Phi(\mathbf{x}) - \Phi_0\|^2$$

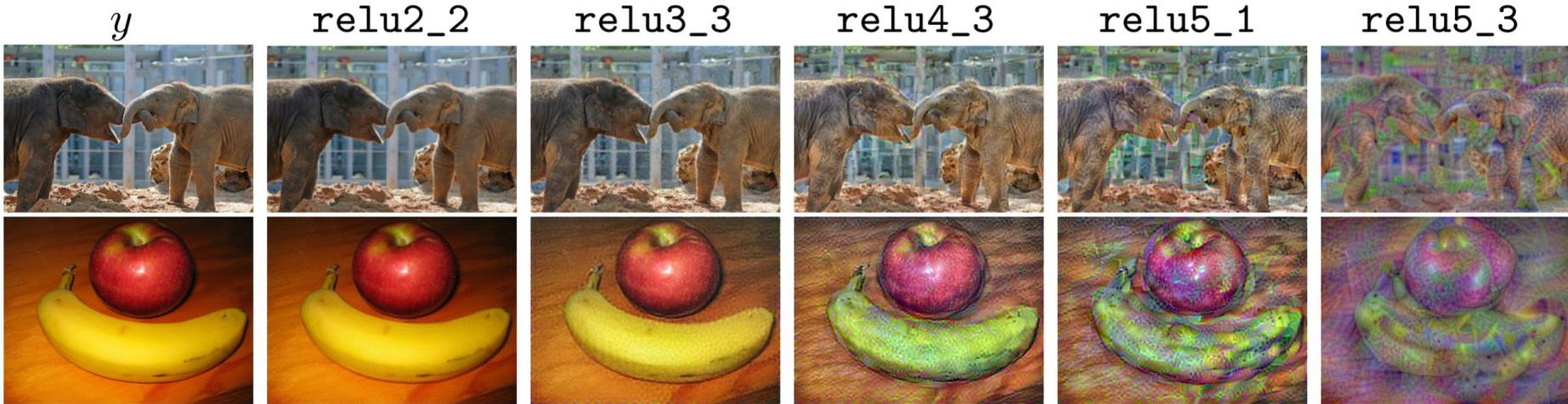
$$\mathcal{R}_{V^\beta}(\mathbf{x}) = \sum_{i,j} \left( (x_{i,j+1} - x_{ij})^2 + (x_{i+1,j} - x_{ij})^2 \right)^{\frac{\beta}{2}}$$

Total Variation regularizer  
(encourages spatial smoothness)

Mahendran and Vedaldi, “Understanding Deep Image Representations by Inverting Them”, CVPR 2015

# Feature Inversion

Reconstructing from different layers of VGG-16



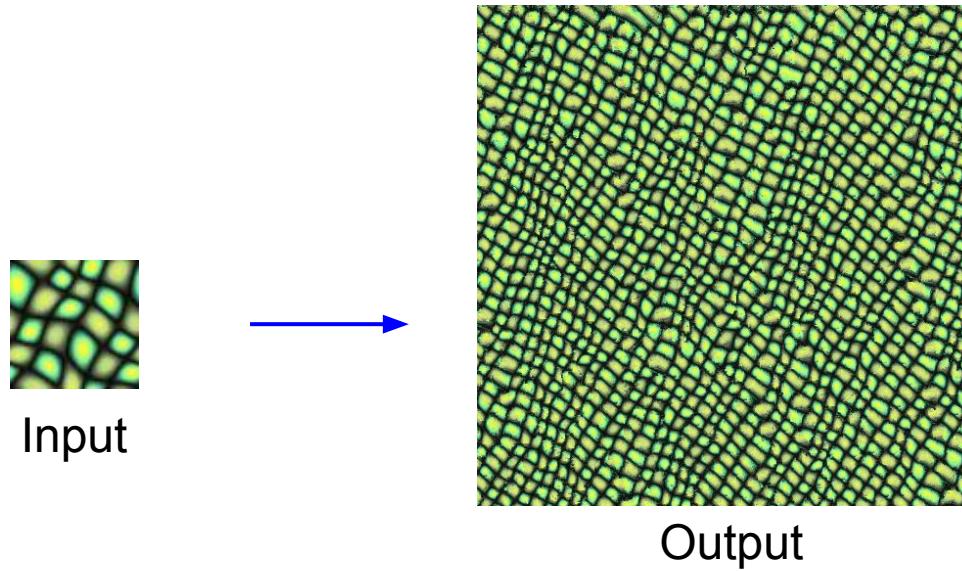
Mahendran and Vedaldi, "Understanding Deep Image Representations by Inverting Them", CVPR 2015

Figure from Johnson, Alahi, and Fei-Fei, "Perceptual Losses for Real-Time Style Transfer and Super-Resolution", ECCV 2016. Copyright Springer, 2016.

Reproduced for educational purposes.

# Texture Synthesis

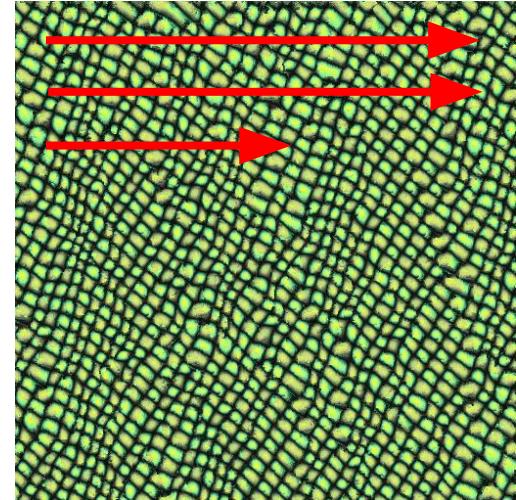
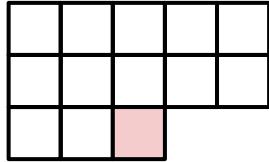
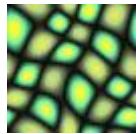
Given a sample patch of some texture, can we generate a bigger image of the same texture?



Output image is licensed under the [MIT license](#)

# Texture Synthesis: Nearest Neighbor

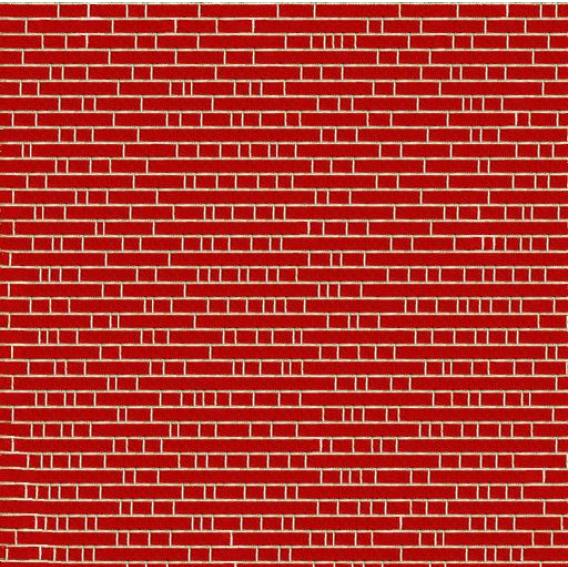
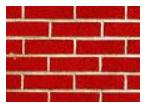
Generate pixels one at a time in scanline order; form neighborhood of already generated pixels and copy nearest neighbor from input



Wei and Levoy, "Fast Texture Synthesis using Tree-structured Vector Quantization", SIGGRAPH 2000

Efros and Leung, "Texture Synthesis by Non-parametric Sampling", ICCV 1999

# Texture Synthesis: Nearest Neighbor



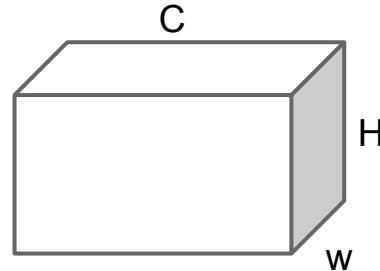
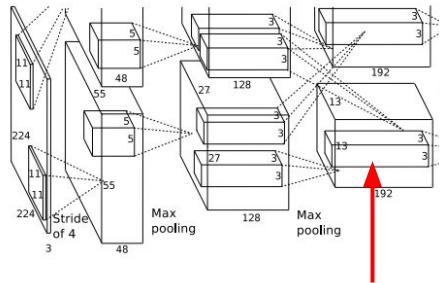
This diagram illustrates the process of texture synthesis using the Nearest Neighbor method. It shows a small input image of a brick wall on the left, which is transformed by two intermediate steps into a larger, synthesized brick wall texture on the right. The first intermediate step shows a distorted version of the input, and the second shows a more refined, larger version.

Images licensed under the [MIT license](#).

# Neural Texture Synthesis: Gram Matrix



This image is in the public domain.

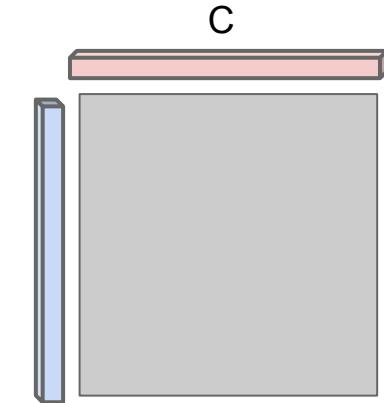
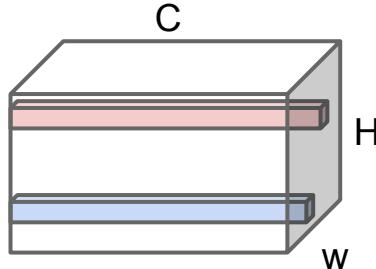
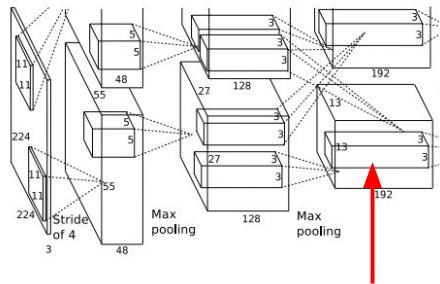


Each layer of CNN gives  $C \times H \times W$  tensor of features;  $H \times W$  grid of  $C$ -dimensional vectors

# Neural Texture Synthesis: Gram Matrix



This image is in the public domain.



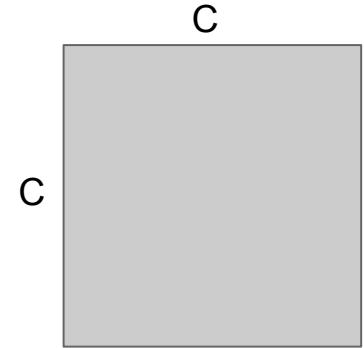
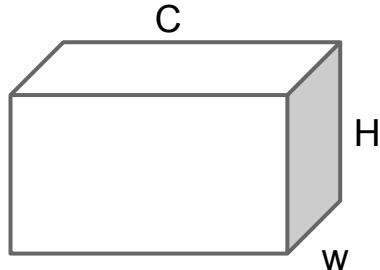
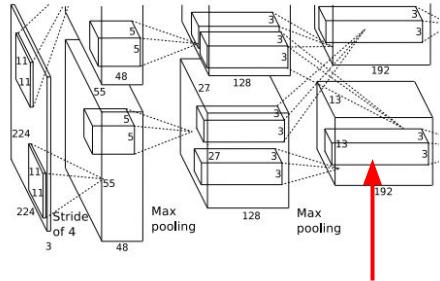
Each layer of CNN gives  $C \times H \times W$  tensor of features;  $H \times W$  grid of  $C$ -dimensional vectors

Outer product of two  $C$ -dimensional vectors gives  $C \times C$  matrix measuring co-occurrence

# Neural Texture Synthesis: Gram Matrix



This image is in the public domain.



Each layer of CNN gives  $C \times H \times W$  tensor of features;  $H \times W$  grid of  $C$ -dimensional vectors

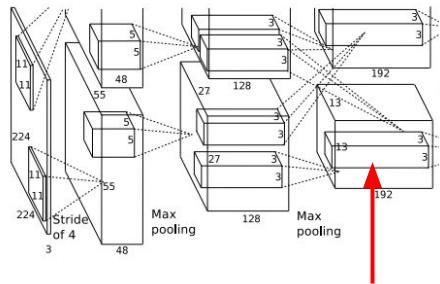
Outer product of two  $C$ -dimensional vectors gives  $C \times C$  matrix measuring co-occurrence

Average over all  $HW$  pairs of vectors, giving **Gram matrix** of shape  $C \times C$

# Neural Texture Synthesis: Gram Matrix



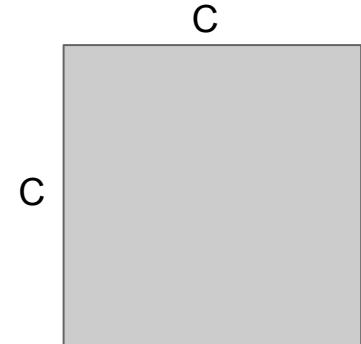
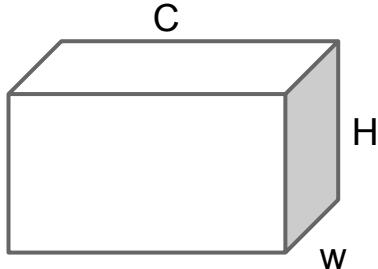
This image is in the public domain.



Each layer of CNN gives  $C \times H \times W$  tensor of features;  $H \times W$  grid of  $C$ -dimensional vectors

Outer product of two  $C$ -dimensional vectors gives  $C \times C$  matrix measuring co-occurrence

Average over all  $HW$  pairs of vectors, giving **Gram matrix** of shape  $C \times C$



Efficient to compute; reshape features from

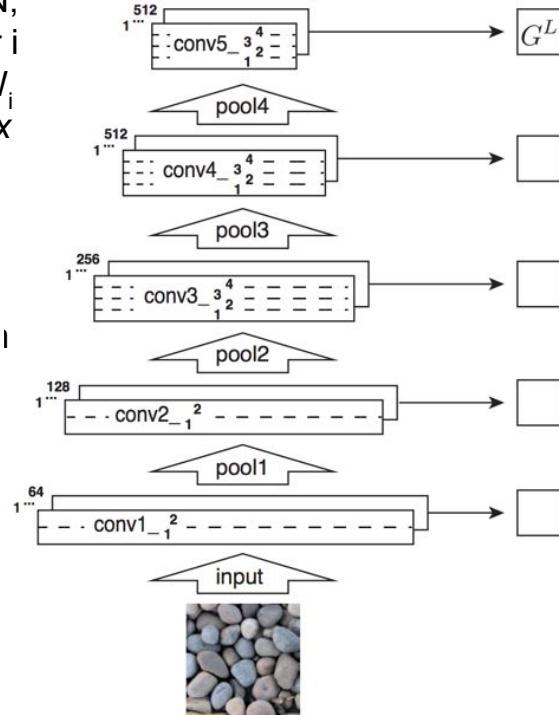
$C \times H \times W$  to  $=C \times HW$

then compute  $G = FF^T$

# Neural Texture Synthesis

1. Pretrain a CNN on ImageNet (VGG-19)
2. Run input texture forward through CNN, record activations on every layer; layer  $i$  gives feature map of shape  $C_i \times H_i \times W_i$
3. At each layer compute the *Gram matrix* giving outer product of features:

$$G_{ij}^l = \sum_k F_{ik}^l F_{jk}^l \text{ (shape } C_i \times C_i\text{)}$$



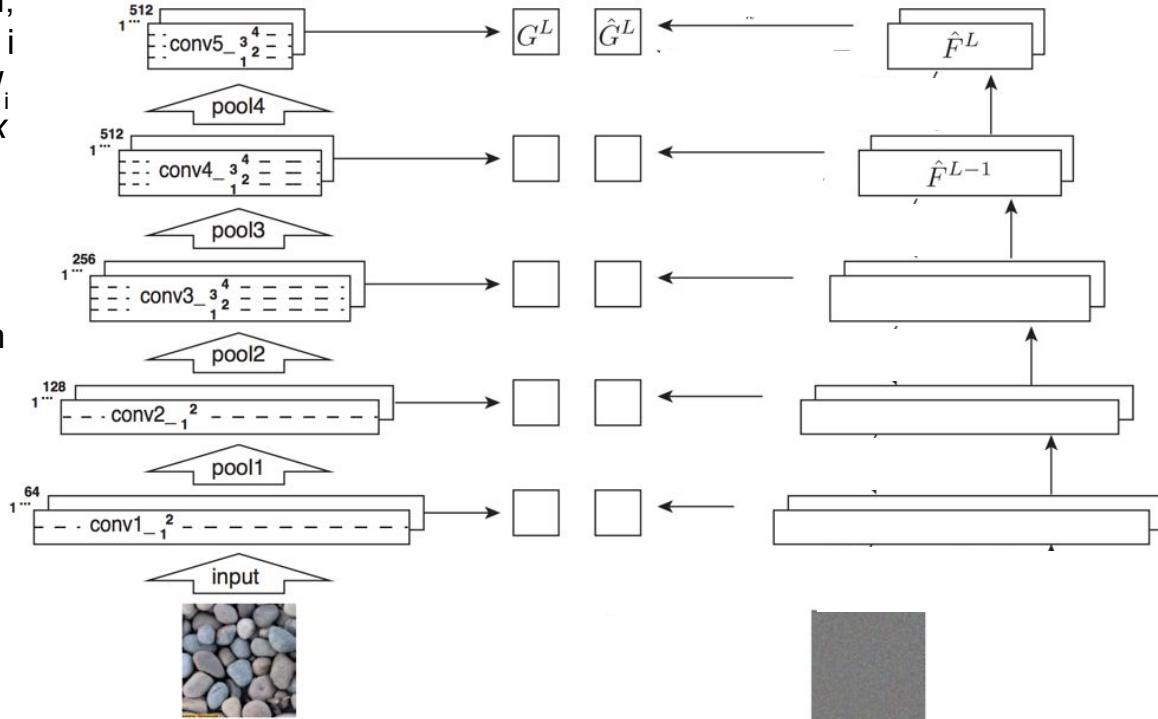
Gatys, Ecker, and Bethge, "Texture Synthesis Using Convolutional Neural Networks", NIPS 2015  
Figure copyright Leon Gatys, Alexander S. Ecker, and Matthias Bethge, 2015. Reproduced with permission.

# Neural Texture Synthesis

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4. Initialize generated image from random noise
5. Pass generated image through CNN, compute Gram matrix on each layer



Gatys, Ecker, and Bethge, "Texture Synthesis Using Convolutional Neural Networks", NIPS 2015  
Figure copyright Leon Gatys, Alexander S. Ecker, and Matthias Bethge, 2015. Reproduced with permission.

# Neural Texture Synthesis

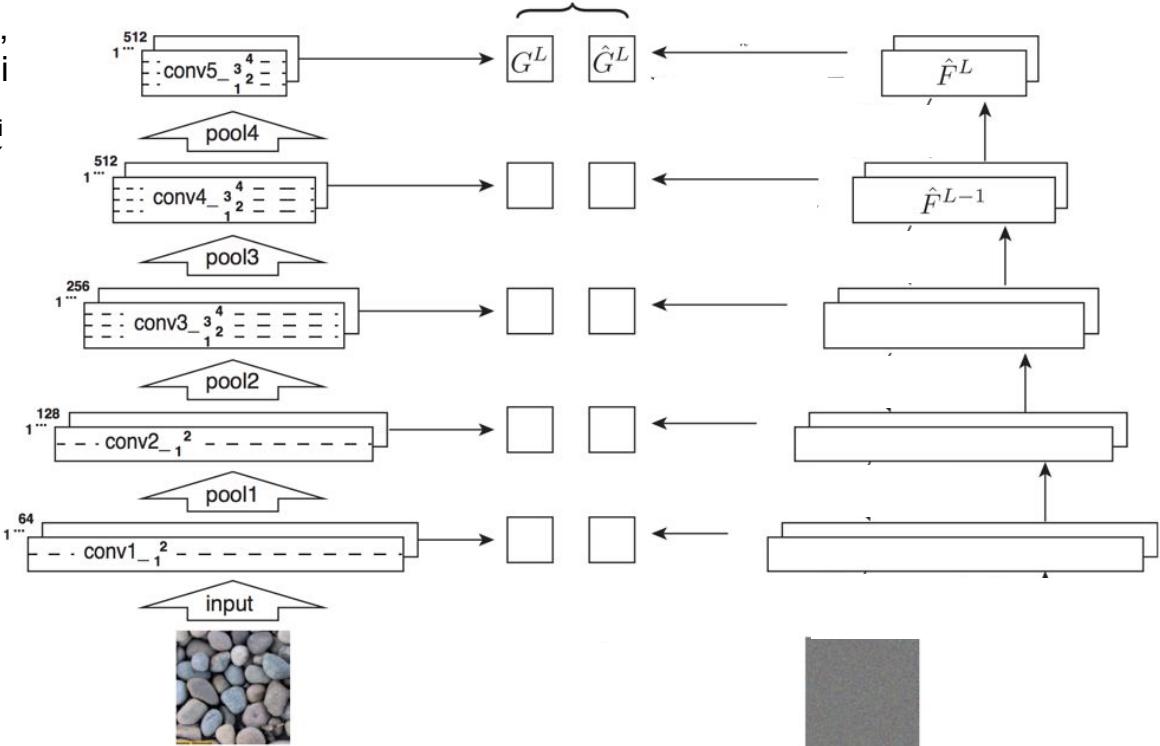
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4. Initialize generated image from random noise
5. Pass generated image through CNN, compute Gram matrix on each layer
6. Compute loss: weighted sum of L2 distance between Gram matrices

$$E_l = \frac{1}{4N_l^2 M_l^2} \sum_{i,j} \left( G_{ij}^l - \hat{G}_{ij}^l \right)^2$$

$$\mathcal{L}(\vec{x}, \hat{x}) = \sum_{l=0}^L w_l E_l$$



Gatys, Ecker, and Bethge, "Texture Synthesis Using Convolutional Neural Networks", NIPS 2015  
 Figure copyright Leon Gatys, Alexander S. Ecker, and Matthias Bethge, 2015. Reproduced with permission.

# Neural Texture Synthesis

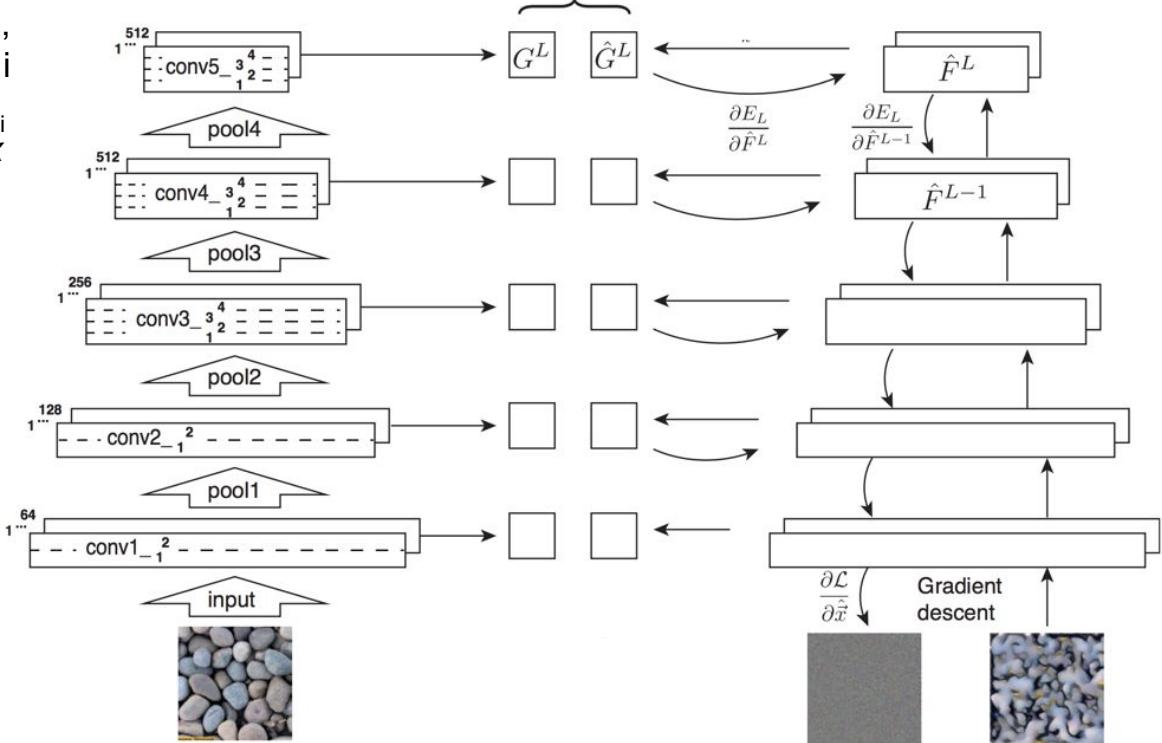
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$$G_{ij}^l = \sum_k F_{ik}^l F_{jk}^l \text{ (shape } C_i \times C_i\text{)}$$

4. Initialize generated image from random noise
5. Pass generated image through CNN, compute Gram matrix on each layer
6. Compute loss: weighted sum of L2 distance between Gram matrices
7. Backprop to get gradient on image
8. Make gradient step on image
9. GOTO 5

$$E_l = \frac{1}{4N_l^2 M_l^2} \sum_{i,j} \left( G_{ij}^l - \hat{G}_{ij}^l \right)^2$$

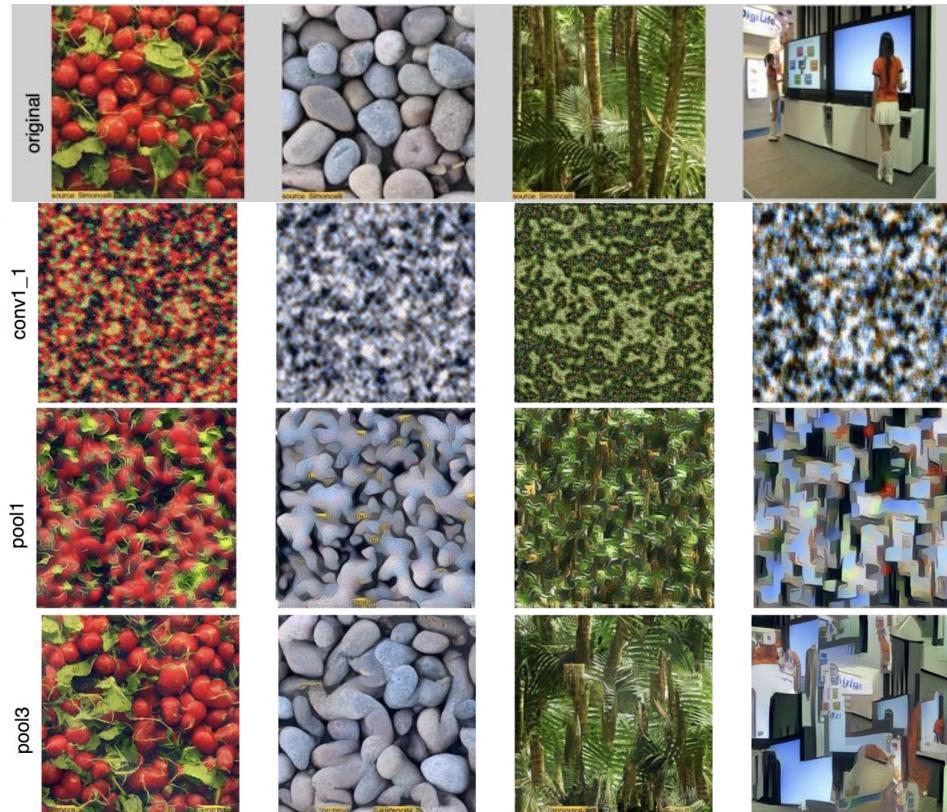
$$\mathcal{L}(\vec{x}, \hat{x}) = \sum_{l=0}^L w_l E_l$$



Gatys, Ecker, and Bethge, "Texture Synthesis Using Convolutional Neural Networks", NIPS 2015  
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# Neural Texture Synthesis

Reconstructing texture from higher layers recovers larger features from the input texture



Gatys, Ecker, and Bethge, "Texture Synthesis Using Convolutional Neural Networks", NIPS 2015  
Figure copyright Leon Gatys, Alexander S. Ecker, and Matthias Bethge, 2015. Reproduced with permission.

# Neural Texture Synthesis: Texture = Artwork

Texture synthesis  
(Gram  
reconstruction)

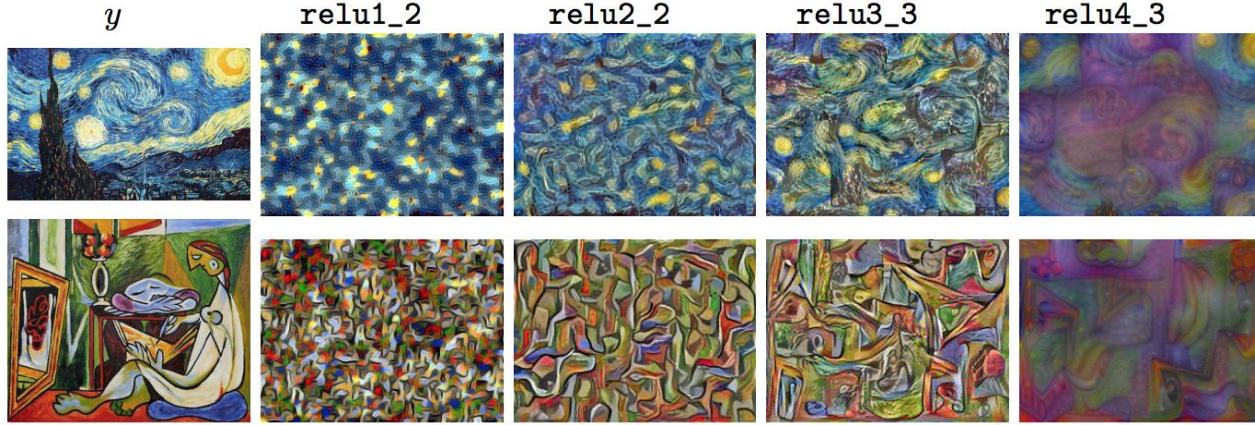
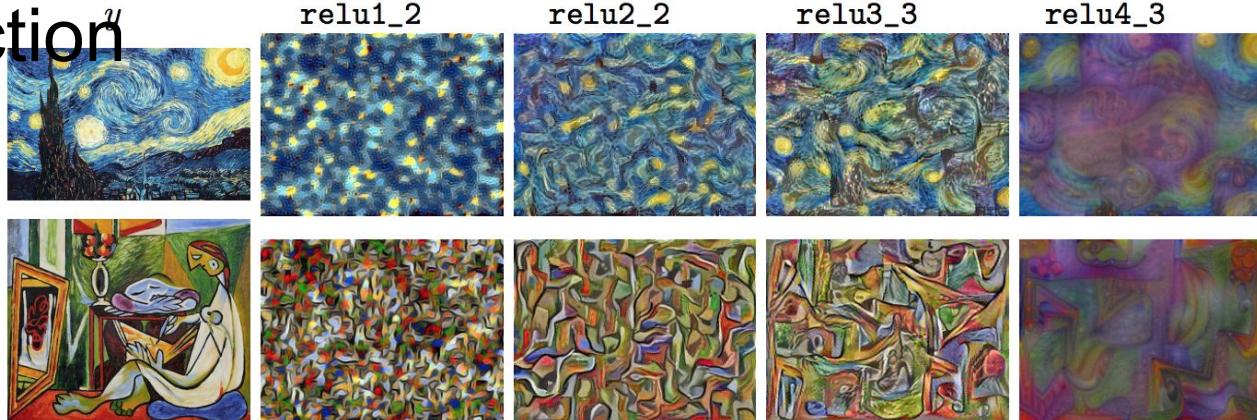


Figure from Johnson, Alahi, and Fei-Fei, "Perceptual Losses for Real-Time Style Transfer and Super-Resolution", ECCV 2016. Copyright Springer, 2016.  
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# Neural Style Transfer: Feature + Gram

## Reconstruction

Texture synthesis  
(Gram  
reconstruction)



Feature  
reconstruction

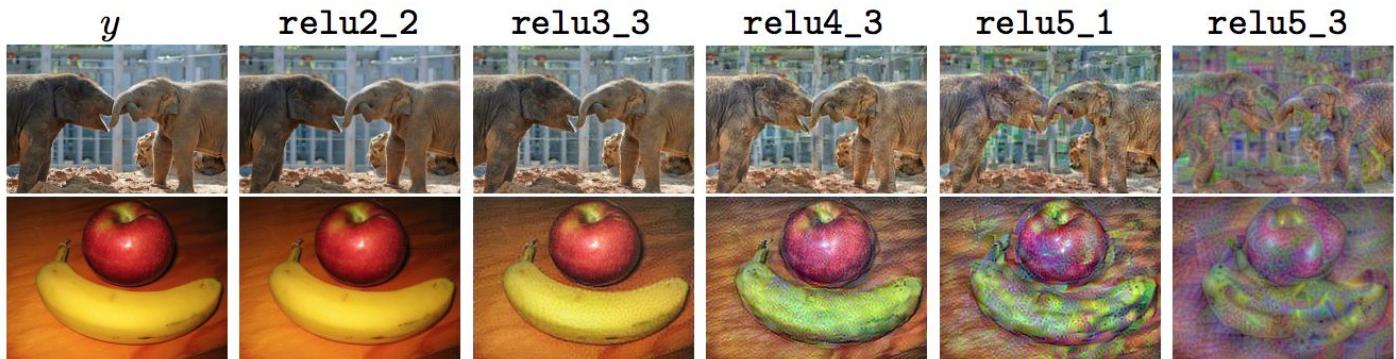


Figure from Johnson, Alahi, and Fei-Fei, "Perceptual Losses for Real-Time Style Transfer and Super-Resolution", ECCV 2016. Copyright Springer, 2016. Reproduced for educational purposes.

# Neural Style Transfer

Content Image



[This image is licensed under CC-BY 3.0](#)

+

Style Image



[Starry Night by Van Gogh is in the public domain](#)

Gatys, Ecker, and Bethge, "Texture Synthesis Using Convolutional Neural Networks", NIPS 2015

# Neural Style Transfer

Content Image



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Style Image



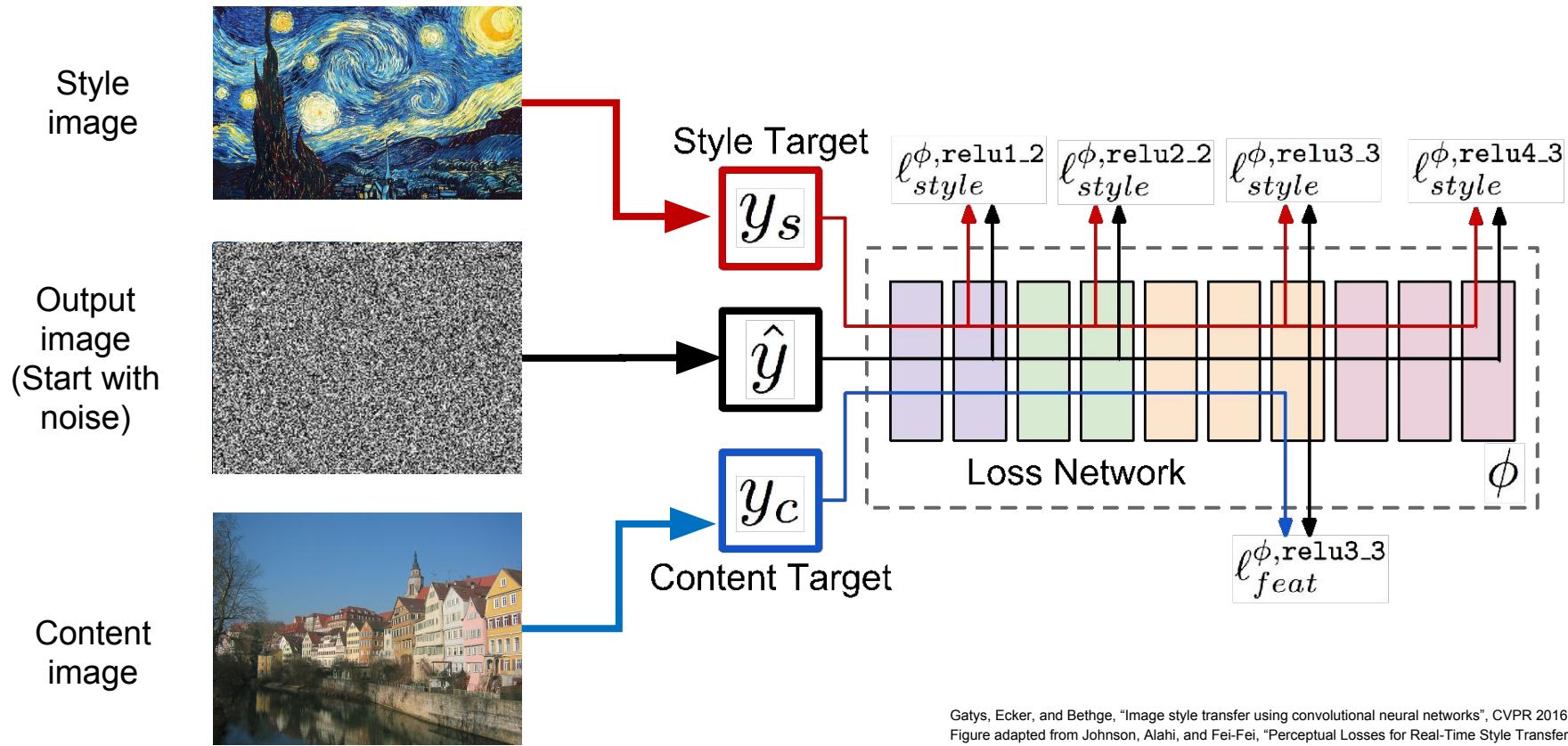
[Starry Night](#) by Van Gogh is in the public domain

=

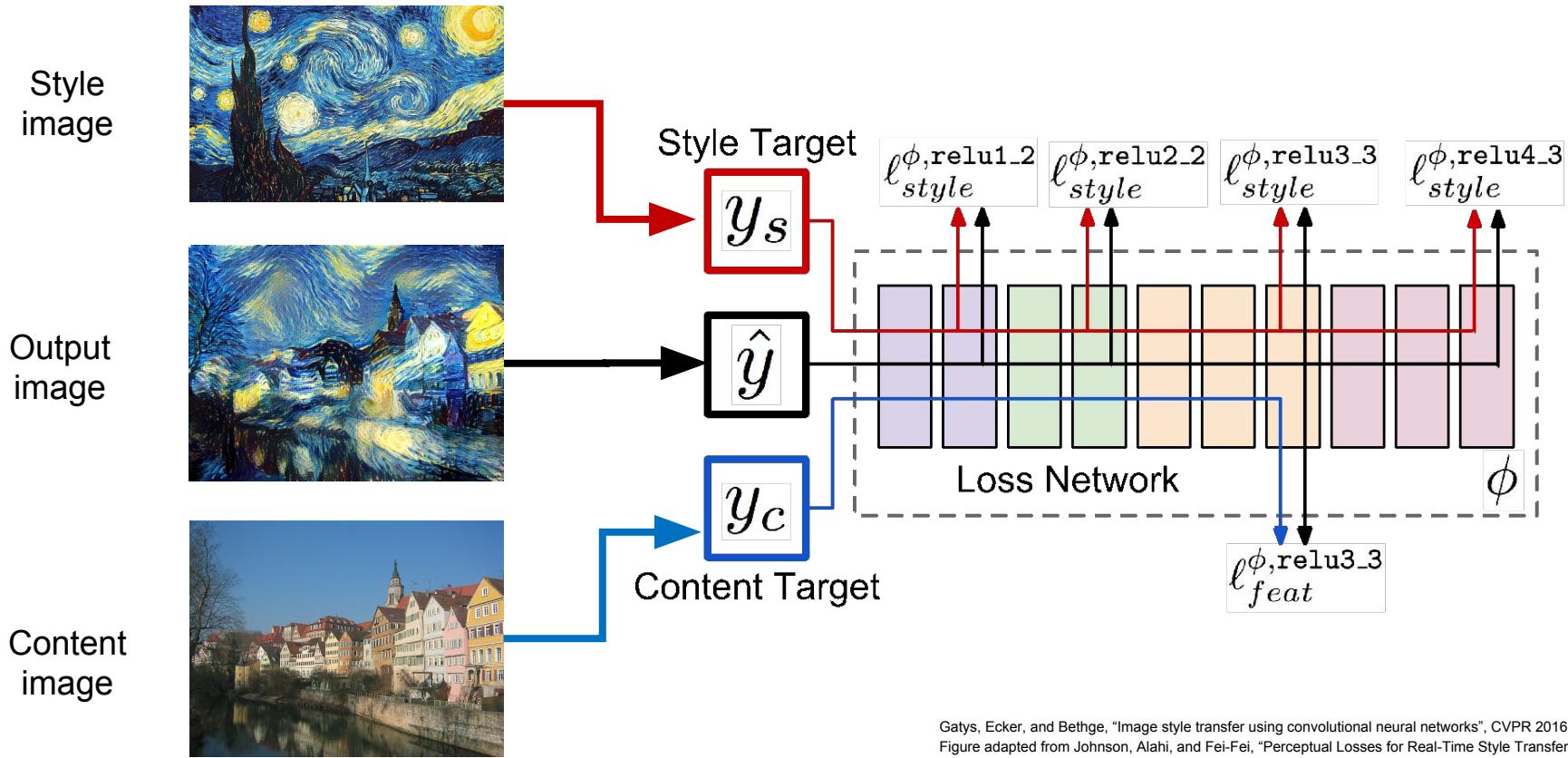


[This image](#) copyright Justin Johnson, 2015. Reproduced with permission.

Gatys, Ecker, and Bethge, "Image style transfer using convolutional neural networks", CVPR 2016



Gatys, Ecker, and Bethge, "Image style transfer using convolutional neural networks", CVPR 2016  
 Figure adapted from Johnson, Alahi, and Fei-Fei, "Perceptual Losses for Real-Time Style Transfer and Super-Resolution", ECCV 2016. Copyright Springer, 2016. Reproduced for educational purposes.



Gatys, Ecker, and Bethge, "Image style transfer using convolutional neural networks", CVPR 2016  
 Figure adapted from Johnson, Alahi, and Fei-Fei, "Perceptual Losses for Real-Time Style Transfer and Super-Resolution", ECCV 2016. Copyright Springer, 2016. Reproduced for educational purposes.

# Neural Style Transfer

Example outputs from  
[my implementation](#)  
(in Torch)



Gatys, Ecker, and Bethge, "Image style transfer using convolutional neural networks", CVPR 2016  
Figure copyright Justin Johnson, 2015.

# Neural Style Transfer



More weight to  
content loss

More weight to  
style loss

# Neural Style Transfer

Resizing style image before running style transfer algorithm can transfer different types of features



Larger style  
image

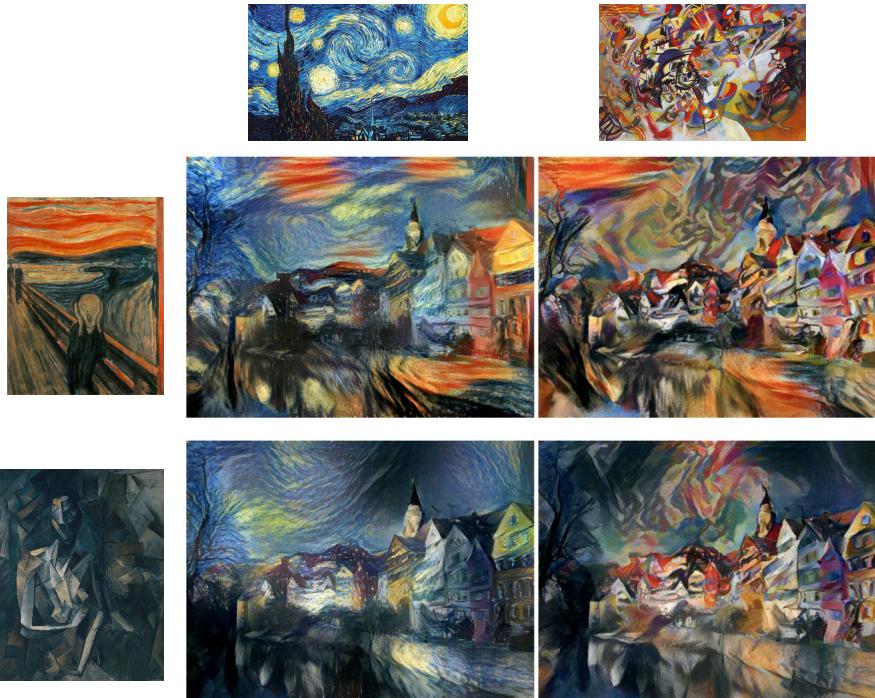


Smaller style  
image

Gatys, Ecker, and Bethge, "Image style transfer using convolutional neural networks", CVPR 2016  
Figure copyright Justin Johnson, 2015.

# Neural Style Transfer: Multiple Style Images

Mix style from multiple images by taking a weighted average of Gram matrices



Gatys, Ecker, and Bethge, "Image style transfer using convolutional neural networks", CVPR 2016  
Figure copyright Justin Johnson, 2015.







Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 11 - 75 May 10, 2017

# Neural Style Transfer

**Problem:** Style transfer  
requires many forward /  
backward passes through  
VGG; very slow!

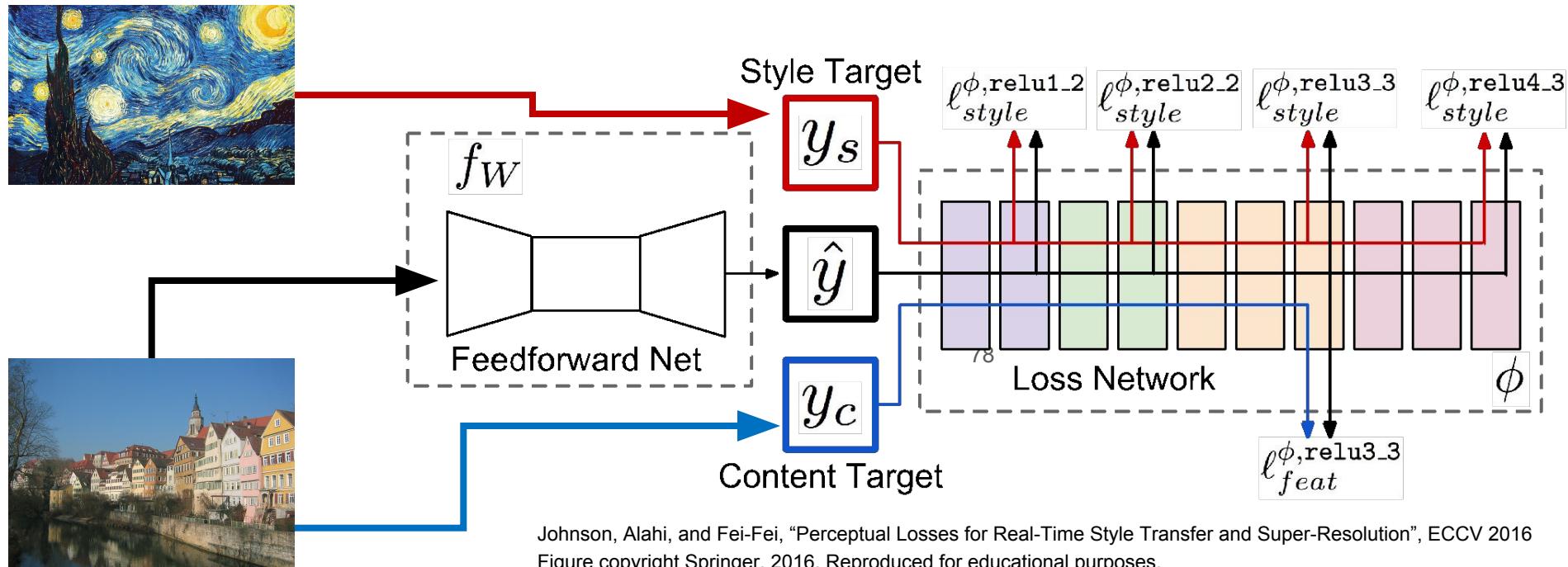
# Neural Style Transfer

**Problem:** Style transfer requires many forward / backward passes through VGG; very slow!

**Solution:** Train another neural network to perform style transfer for us!

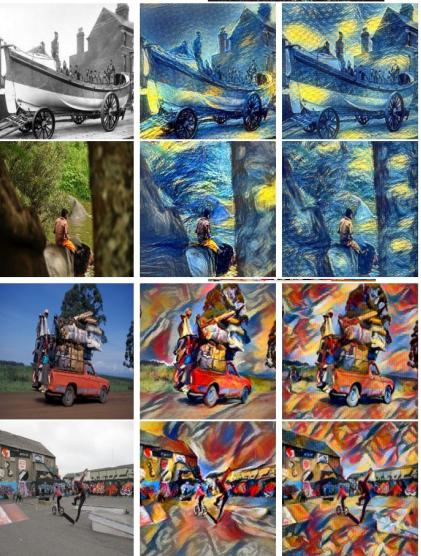
# Fast Style Transfer

- (1) Train a feedforward network for each style
- (2) Use pretrained CNN to compute same losses as before
- (3) After training, stylize images using a single forward pass



Johnson, Alahi, and Fei-Fei, "Perceptual Losses for Real-Time Style Transfer and Super-Resolution", ECCV 2016  
Figure copyright Springer, 2016. Reproduced for educational purposes.

# Fast Style Transfer



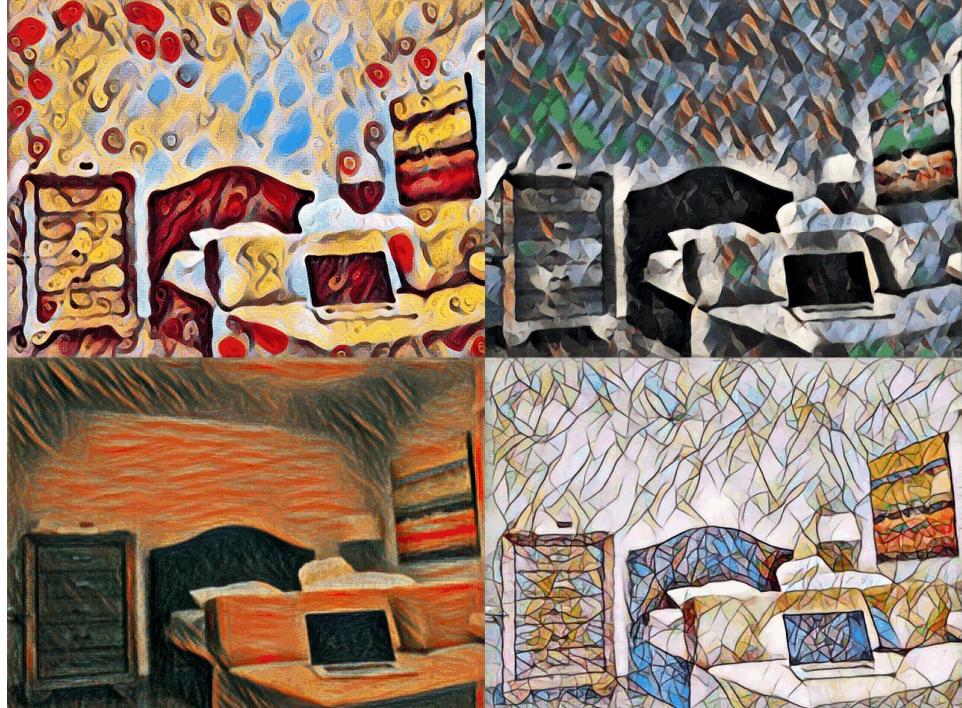
Slow

Fast



Slow

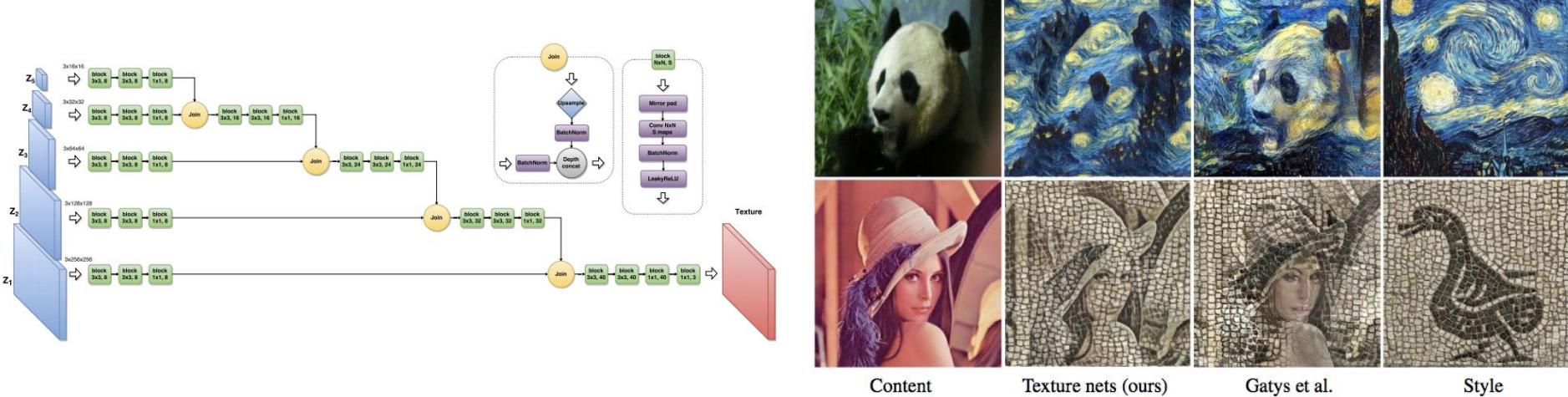
Fast



<https://github.com/jcjohnson/fast-neural-style>

Johnson, Alahi, and Fei-Fei, "Perceptual Losses for Real-Time Style Transfer and Super-Resolution", ECCV 2016  
Figure copyright Springer, 2016. Reproduced for educational purposes.

# Fast Style Transfer



Concurrent work from Ulyanov et al, comparable results

Ulyanov et al, "Texture Networks: Feed-forward Synthesis of Textures and Stylized Images", ICML 2016

Ulyanov et al, "Instance Normalization: The Missing Ingredient for Fast Stylization", arXiv 2016

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# Fast Style Transfer



Replacing batch normalization with Instance Normalization improves results

Ulyanov et al. "Texture Networks: Feed-forward Synthesis of Textures and Stylized Images", ICML 2016

Ulyanov et al. "Instance Normalization: The Missing Ingredient for Fast Stylization", arXiv 2016

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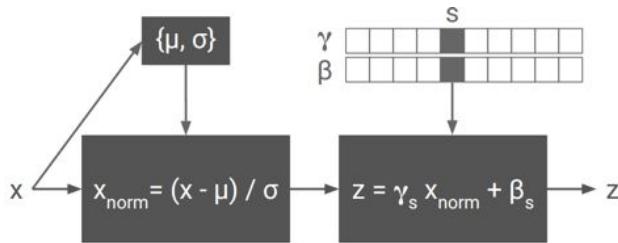
# One Network, Many Styles



Dumoulin, Shlens, and Kudlur, "A Learned Representation for Artistic Style", ICLR 2017.  
Figure copyright Vincent Dumoulin, Jonathon Shlens, and Manjunath Kudlur, 2016; reproduced with permission.

# One Network, Many Styles

Use the same network for multiple styles using conditional instance normalization: learn separate scale and shift parameters per style



Single network can blend styles after training

Dumoulin, Shlens, and Kudlur, "A Learned Representation for Artistic Style", ICLR 2017.  
Figure copyright Vincent Dumoulin, Jonathon Shlens, and Manjunath Kudlur, 2016; reproduced with permission.

# Summary

Many methods for understanding CNN representations

**Activations:** Nearest neighbors, Dimensionality reduction, maximal patches, occlusion

**Gradients:** Saliency maps, class visualization, fooling images, feature inversion

**Fun:** DeepDream, Style Transfer.

Next time: **Unsupervised Learning**  
Autoencoders  
Variational Autoencoders  
Generative Adversarial Networks