

## Programming Assignment #1

Programming assignments are to be done individually. Do not make your code publicly available (such as a Github repo) as this enables others to cheat and you will be held responsible. You may discuss the problem and general concepts with other students, but there should be no sharing of code. You may not submit code other than that which you write yourself or is provided with the assignment. This restriction specifically prohibits downloading code from the Internet, or from any internet tools such as ChatGPT. If any code you submit is in violation of this policy, you will receive no credit for the entire assignment.

This programming assignment is due **Monday, February 12th at 11:59 PM**. If you are unable to complete the assignment by this time, you may submit the assignment late until Wednesday, February 14th at 11:59 PM for a 20 point penalty.

The goals of this lab are:

- Familiarize you with programming in Java
- Show an application of the stable matching problem
- Understand the difference between the two optimal stable matchings
- Place the stable matching algorithm in the context of engineering solutions with high social impact

### Problem Description

In this project, you will implement a variation of the stable matching problem adapted from the textbook Chapter 1, Exercise 4, and write a small report. We have provided Java code skeletons that you will fill in with your own solution. Please read through this document and the documentation in the starter code thoroughly before beginning.

The International Study Abroad Department sends university students over the summer to international universities, which have openings for study abroad students. The students can rank the varying university abroad programs by which programs they prefer. However, universities also rank students based on a variety of factors, including spoken language, past coursework, and their main area of study. Your job is to devise and implement an algorithm to automate this process based off of the Gale-Shapley algorithm presented in class.

There are  $n$  students, each interested in attending one of  $m$  universities. Each university has a set number of students they seek to recruit for the summer, which can vary between universities. Every student submits their preference list of universities, and every university's admissions board creates a preference list of students based on their submitted profiles. We will assume that there are at least as many students as the total openings available across all  $m$  universities. This means that all openings will be filled, but some students may be left unmatched to a university. The

interest lies in finding a way of assigning each student to at most one university in such a way that all available openings are filled.

We say that an assignment of students to universities is *stable* if neither of the following situations arises:

- First type of instability: There are students  $i$  and  $i'$ , and a university  $c$ , such that
  - $i$  is assigned to  $c$ , and
  - $i'$  is assigned to no university, and
  - $c$  prefers  $i'$  to  $i$
- Second type of instability: There are students  $i$  and  $i'$ , and university  $c$  and  $c'$ , so that
  - $i$  is assigned to  $c$ , and
  - $i'$  is assigned to  $c'$ , and
  - $c$  prefers  $i'$  to  $i$ , and
  - $i'$  prefers  $c$  to  $c'$ .

So, we basically have the Stable Matching Problem as presented in class, except that (i) a university may want one or more students, and (ii) there is potentially a surplus of students. There are several parts to this problem.

### Part 1: Report: Algorithm Design [20 points]

Write a short report that includes the following information:

- (a) Give an algorithm in pseudocode (either an outline or paragraph works) to find a stable assignment that is **university** optimal.
- (b) Give the runtime complexity of your algorithm in (a) in Big O notation and explain why.  
**Note: Full credit will be given to solutions that have a complexity of  $O(mn)$ .**
- (c) Give an algorithm in pseudocode (either an outline or paragraph works) to find a stable assignment that is **student** optimal.
- (d) Give the runtime complexity of your algorithm in (c) in Big O notation and explain why.  
**Note: Try to make your algorithm as efficient as you can, but you will get full credit even if it does not match the runtime in (b) as long as you clearly explain your runtime and the difficulty of optimizing it further.**

For the programming assignment, you do not need to submit a proof that your algorithm returns a stable matching, or of student/university optimality.

### Part 2: Implement a Checker to check the stability of any given matching [15 points]

Given a Matching object `problem`, you should implement a boolean function to determine if the pairing of students to universities (stored in the variable returned by `problem.getstudentMatching()`)

is stable or not. Your code will go inside a function called `isStableMatching(Matching problem)` inside `Program1.java`. A file named `Matching.java` contains the data structure for a matching. Note that you do not need to optimize the runtime of this function, a brute force approach is sufficient. See the instructions section for more information on how to test this method.

### Part 3: Implement Gale Shapley Algorithm [45 points]

Implement both algorithms from parts (a) (university optimal) and (c) (student optimal) of your report. Again, you are provided several files to work with. Implement the function that yields a student optimal solution `stableMatchingGaleShapley_studentoptimal()` and university optimal solution

`stableMatchingGaleShapley_universityoptimal()` inside of `Program1.java`.

Of the files we have provided, please only modify `Problem1.java`, so that your solution remains compatible with ours. However, feel free to add any additional Java files (of your own authorship) as you see fit.

### Part 4: Report: Analyze the Impact [20 points]

#### ***Real Example: Stable Matching in Organ Transplant***

Now that you've designed and implemented Gale-Shapley, let's take a look at a real-world example. The United Network for Organ Sharing (UNOS) works to help provide organs to needy patients. Let's start by reading a little bit about this problem space, in general, and its relationship to algorithmic matching problems:

<https://mashable.com/archive/big-data-organ-transplants>

The final section of your report will expand your knowledge of Gale-Shapley and have you consider its impact.

- (a) Describe the organ donation problem *in your own words*. (Write this in a way a well-informed outsider can comprehend; you may want to run it by such a well-informed outsider and ask them for a critique.)
- (b) Discuss how one may want to apply Gale-Shapley to the organ matching problem. (Some questions to answer: what would the rankings be based on, which party would be proposing and which accepting.) Justify your choices and explain what the Gale-Shapley algorithm would accomplish in this context.
- (c) Discuss some reasons why you would *not* want to use Gale-Shapley in the context of the organ matching problem.

### Coding Instructions

- Download and import the code into your favorite development environment. We will be grading in Java 1.8. Therefore, we recommend you use Java 1.8 and NOT other versions of

Java, as we can not guarantee that other versions of Java will be compatible with our grading scripts. **It is YOUR responsibility to ensure that your solution compiles with Java 1.8.** If you have doubts, email a TA or post your question on Piazza.

- If you do not know how to download Java or are having trouble choosing and running an IDE, email a TA, post your question on Ed, or visit the TAs during Office Hours.
- **Do not add any package statements to your code.** Some IDEs will make a new package for you automatically. If your IDE does this, make sure that you remove the package statements from your source files before turning in the assignment.
- There are several `.java` files, but you only need to make modifications to `Program1.java`. **Do not modify the other files.** However, you may add additional source files in your solution if you so desire. **Do not add extra imports to `Program1.java`;** the included imports should be all you need for your solution. There is a lot of starter code; carefully study the code provided for you, and ensure that you understand it before starting to code your solution. The set of provided files should compile and run successfully before you modify them.
- The main data structure for a matching is defined and documented in `Matching.java`. A `Matching` object includes:
  - **m**: Number of universities
  - **n**: Number of students
  - **university\_preference**: An `ArrayList` of `ArrayList`s containing each of the university's preferences of students, in order from most preferred to least preferred. The universities are in order from 0 to  $m - 1$ . Each university has an `ArrayList` that ranks its preferences of students who are identified by numbers 0 through  $n - 1$ .
  - **student\_preference**: An `ArrayList` of `ArrayList`s containing each of the student's preferences for universities, in order from most preferred to least preferred. The students are in order from 0 to  $n - 1$ . Each student has an `ArrayList` that ranks its preferences of universities who are identified by numbers 0 to  $m - 1$ .
  - **university\_openings**: An `ArrayList` that specifies how many openings each university has. The index of the value corresponds to which university it represents.
  - **student\_matching**: An `ArrayList` to hold the final matching. This `ArrayList` (should) hold the number of the university each student is assigned to. This field will be empty in the `Matching` which is passed to your functions. The results of your algorithm should be stored in this field either by calling `setstudentMatching(<your_solution>)` or constructing a new `Matching(data, <your_solution>)`, where `data` is the `Matching` we pass into the function. The index of this `ArrayList` corresponds to each student. The value at that index indicates to which university they are matched. A value of -1 at that index indicates that the student is not matched up. For example, if student 0 is matched to university 55, student 1 is unmatched, and student 2 is matched to university 3, the `ArrayList` should contain `{55, -1, 3}`. If using the flag `[-bf]`, an input with an existing matching can be given to check correctness of the `isStableMatching()` function.

- You must implement the methods
  - `isStableMatching()`
  - `stableMatchingGaleShapley_studentoptimal()`
  - `stableMatchingGaleShapley_universityoptimal()`
- Test cases take the format of text files, which either have the file extension of `.in` or `.extended.in`. Here's how to interpret each test case, line by line:
  - Line 1: `m n`
  - Line 2: `m` space separated integers, denoting the number of openings available in each university. The first integer represents the number of open openings in university 0, the next integer represents the number for university 1, and so on.
  - The next `m` lines are the preference lists of the universities, where each space-separated integer represents a student. The list goes from left to right, from most to least desirable. The first of these `m` lines is the preference list for university 0, the next line is for university 1, and so on.
  - The next `n` lines are the preference lists of the students, where each space-separated integer represents a university. The list goes from left to right, from most to least desirable. The first of these `n` lines is the preference list for student 0, the next line is for student 1, and so on.
  - Last line (optional): `n` space separated integers representing a student-university matching. If the first integer is `x`, then the first student is assigned to university `x`, the second student to the second integer, and so on. This is a way of hard coding in a matching to test your implementation of `isStableMatching()` in Part 2 before you complete Part 3. To see examples, see the last lines of the test cases with the file extension `.extended.in`.
- `Driver.java` is the main driver program. Use command line arguments to choose between your checker and your university optimal or student optimal algorithms and to specify an input file. Use `-gc` for university optimal, `-gi` for student optimal, and `-bf` for importing an existing matching (to check correctness of `isStableMatching()`). (i.e. `java -classpath . Driver [-gc] [-gi] [-bf] <filename>` on a linux machine). As a test, the `3-10-3.in` input file should output the following for both a student and university optimal solution:
  - student 0 university -1
  - student 1 university 1
  - student 2 university -1
  - student 3 university -1
  - student 4 university -1
  - student 5 university -1
  - student 6 university -1
  - student 7 university 2
  - student 8 university 0

– student 9 university -1

- When you run `Driver.java`, it will tell you if the results of your algorithm(s) pass the `isStableMatching()` function that *you coded* for this particular set of data. When we grade your program, however, we will use *our* implementation of `isStableMatching()` to verify the correctness of your solutions.

## Getting Started:

- (a) Download the starter material from canvas.
- (b) Do an initial compile of the starter code in your favorite Java IDE or on the ECE LRC Linux machines(recommended), see note below on how to compile.
- (c) Test your code using the inputs given and the Driver class.
- (d) Submit your code to Gradescope to validate your code. You have unlimited submissions before the due date. Your latest submission will be the only submission we look at.

**NOTE:** To avoid receiving a 0 for the coded portion of this assignment, you **MUST** ensure that your code correctly compiles **with the original, unmodified starter files** on Java 1.8. Do not modify the signatures of or remove existing methods of `Program1.java`. Do not add package statements. Do not add extra imports. We recommend testing compilation of your code using the ECE LRC Linux machines (using “`javac *.java`” and “`java Driver inputfile.in`”) after redownloading the starter files from Canvas.

## What To Submit:

You should submit to Gradescope `Program1.java` (and, any extra `.java` files you added or modified). Please do not submit `Driver.java`. Failure to follow these instructions will result in a penalty of up to 10 points.

Your PDF report should be legibly scanned and submitted to Gradescope. Both your code and PDF report must be submitted by 11:59 PM on Monday, February 12th, 2024. If you are unable to complete the assignment by this time, you may submit the assignment late until Wednesday, February 14th, 2024 at 11:59 PM for a 20 point penalty.