

Assignment 3

2023-April

Session-04-10-2023-shift:2-1-15

EE24BTECH11049
Patnam Shariq Faraz Muhammed

MCQ

1) If the coefficients of x and x^2 in $(1+x)^p (1-x)^q$ are 4 and -5 respectively, then $2p+3q$ is equal to

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- a) 60 b) 63 c) 66 d) 69

2) let $A = \{2, 3, 4\}$ and $B = \{8, 9, 12\}$. . Then the number of elements in the relation $R = \{((a_1, b_1), (a_2, b_2)) \in (A \times B, A \times B) : a_1 \text{ divides } b_2 \text{ and } a_2 \text{ divides } b_1\}$ is

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- a) 18 b) 24 c) 12 d) 36

3) Let time image of the point $\mathbf{P}(1, 2, 6)$ n the plane passing through the points $\mathbf{A}(1, 2, 0)$, $\mathbf{B}(1, 4, 1)$ and $\mathbf{C}(0, 5, 1)$ be $\mathbf{Q}(\alpha, \beta, \gamma)$. Then $(\alpha^2 + \beta^2 + \gamma^2)$ is equal to

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- a) 70 b) 76 c) 62 d) 65

4) The statement $\sim [p \vee (\sim (p \wedge q))]$ is equivalent to

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- a) $(\sim (p \wedge q)) \wedge q$ b) $\sim (p \vee q)$ c) $\sim (p \wedge q)$ d) $(p \wedge q) \wedge (\sim)$

5) let

$$S = \left\{ x \in \left(-\frac{\pi}{2}, \frac{\pi}{2} \right) : 9^{1-\tan^2 x} + 9^{\tan^2 x} = 10 \right\} \text{ and } b = \sum_{x \in S} \tan^2 \left(\frac{x}{3} \right), \text{ then } \frac{1}{6} (\beta - 14)^2$$

is equal to

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a) 16

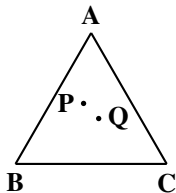
b) 32

c) 8

d) 64

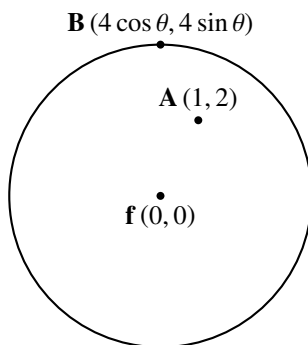
- 6) If the points **P** and **Q** are respectively the circumcenter and the orthocentre of a $\triangle ABC$, the $\overline{PA} + \overline{PB} + \overline{PC}$ is equal to

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a) $2\overline{QP}$ b) \overline{QP} c) $2\overline{PQ}$ d) \overline{PQ} 

- 7) Let **A** be the point $(1, 2)$ and **B** be any point on the curve $x^2 + y^2 = 16$. **f** the centre of the locus of the point **P**, which divides the line segment **AB** in the ratio $3 : 2$ is the point **C** (α, β) then the length of the line segment **AC** is

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a) $\frac{6\sqrt{5}}{5}$ b) $\frac{2\sqrt{5}}{5}$ c) $\frac{3\sqrt{5}}{5}$ d) $\frac{4\sqrt{5}}{5}$ 

- 8) Let m be the mean and σ be the standard deviation of the distribution

x_i	0	1	2	3	4	5
f_i	$k + 2$	$2k$	$k^2 - 1$	$k^2 - 1$	$k^2 + 1$	$k - 3$

where $\sum f_i = 62$. If $[x]$ denotes the greatest integer $\leq x$, then $[\mu^2 + \sigma^2]$ is equal to

(2023-Apr)

- a) 8 b) 7 c) 6 d) 9

9) If $S_n = 4 + 11 + 21 + 34 + 50 + \dots$ to n terms, then $\frac{1}{60} (S_{29} - S_9)$ (2023-Apr)

- a) 220 b) 227 c) 226 d) 223

10) Eight persons are to be transported from city A to city B in three cars different makes. If each car can accommodate at most three persons, then the number of ways, in which they can be transported, is (2023-Apr)

- a) 1120 b) 560 c) 3360 d) 1680

11) If

$$A = \frac{1}{5!6!7!} \begin{pmatrix} 5! & 6! & 7! \\ 6! & 7! & 8! \\ 7! & 8! & 9! \end{pmatrix}, \text{ then } |\text{adj}(\text{adj}(2A))|$$

is equal to

(2023-Apr)

- a) 2^{16} b) 2^8 c) 2^{12} d) 2^{20}

12) Let the number $(22)^2 022 + (2022)^2 2$ leave the remainder α when divided by 3 and β when divided by 7. Then $(\alpha^2 + \beta^2)$ is equal to (2023-Apr)

- a) 13 b) 20 c) 10 d) 5

13) let

$$g(x) = f(x) + f(1-x) \text{ and } f^n(x) > 0, x \in (0, 1).$$

If g is decreasing in the interval $(0, \alpha)$ and increasing in the interval $(\alpha, 1)$, then

$$\tan^{-1}(2\alpha) + \tan^{-1}\left(\frac{\alpha+1}{\alpha}\right)$$

is equal to

(2023-Apr)

- a) $\frac{5\pi}{4}$ b) π c) $\frac{3\pi}{4}$ d) $\frac{3\pi}{2}$

14) For $\alpha, \beta, \gamma, \delta \in \mathbf{N}$, if

$$\int \left(\left(\frac{x}{e} \right)^{2x} + \left(\frac{e}{x} \right)^{2x} \right) \log_e x \, dx = \frac{1}{\alpha} \left(\frac{x}{e} \right)^{\beta x} - \frac{1}{\gamma} \left(\frac{e}{x} \right)^{\delta x} + C, \text{ where } e = \sum_{n=0}^{\infty} \frac{1}{n!}$$

and C is constant of integration, then $\alpha + 2\beta + 3\gamma - 4\delta$ is equal to

(2023-Apr)

a) 4

b) -4

c) -8

d) 1

15) Let f be a continuous function satisfying

$$\int_0^{t^2} (f(x) + x^2) dx = \frac{4}{3}t^3, \forall t > 0. \text{ Then } f\left(\frac{\pi^2}{4}\right)$$

is equal to

(2023-Apr)

a) $-\pi^2 \left(1 + \frac{\pi^2}{16}\right)$

b) $\pi \left(1 - \frac{\pi^3}{16}\right)$

c) $-\pi \left(1 + \frac{\pi^3}{16}\right)$

d) $\pi^2 \left(1 - \frac{\pi^3}{16}\right)$