1

EE24BTECH11049 Patnam Shariq Faraz Muhammed

QUESTION

If the points A = (k + 1, 2k), B = (3k, 2k + 3), and C = (5k - 1, 5k) are collinear, then find the value of k.

SOLUTION:

Variables	Description	Formula
A	A point in the 2-D plane whose coordinates are $(k + 1, 2k)$	$\binom{k+1}{2k}$
В	A point in the 2-D plane whose coordinates are $(3k, 2k + 3)$	$\binom{3k}{2k+3}$
С	A point in the 2-D plane whose coordinates are $(5k - 1, 5k)$	$\binom{5k-1}{5k}$

TABLE 0: Variables Used

Points A, B, C are defined to be collinear if

$$Rank (B-A \quad C-A)^T$$

is equal to 1.

$$(B - A \quad C - A)^{T} = \begin{pmatrix} 2k - 1 & 3\\ 4k - 2 & 3k \end{pmatrix}$$
 (0.1)

$$\stackrel{R_2=R_2-2R_1}{\longrightarrow} \begin{pmatrix} k-1 & 3\\ 0 & 3k-6 \end{pmatrix} \tag{0.2}$$

For the rank of the matrix to be 1 it should've one non-zero row. make the elements of the 2^{nd} row zero.

$$\implies 3k - 6 = 0$$
$$\implies k = 2$$

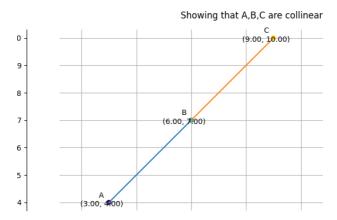


Fig. 0.1