

# Assignment 3

## 2023-April

### Session-04-10-2023-shift:2-1-15

EE24BTECH11049  
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#### MCQ

1) If the coefficients of  $x$  and  $x^2$  in  $(1+x)^p (1-x)^q$  are 4 and  $-5$  respectively, then  $2p+3q$  is equal to

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- a) 60                      b) 63                      c) 66                      d) 69

2) let  $A = \{2, 3, 4\}$  and  $B = \{8, 9, 12\}$ . . Then the number of elements in the relation  $R = \{((a_1, b_1), (a_2, b_2)) \in (A \times B, A \times B) : a_1 \text{ divides } b_2 \text{ and } a_2 \text{ divides } b_1\}$  is

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- a) 18                      b) 24                      c) 12                      d) 36

3) Let time image of the point  $\mathbf{P}(1, 2, 6)$  n the plane passing through the points  $\mathbf{A}(1, 2, 0)$ ,  $\mathbf{B}(1, 4, 1)$  and  $\mathbf{C}(0, 5, 1)$  be  $\mathbf{Q}(\alpha, \beta, \gamma)$ . Then  $(\alpha^2 + \beta^2 + \gamma^2)$  is equal to

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- a) 70                      b) 76                      c) 62                      d) 65

4) The statement  $\sim [p \vee (\sim (p \wedge q))]$  is equivalent to

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- a)  $(\sim (p \wedge q)) \wedge q$     b)  $\sim (p \vee q)$                       c)  $\sim (p \wedge q)$                       d)  $(p \wedge q) \wedge (\sim)$

5) let

$$S = \left\{ x \in \left( -\frac{\pi}{2}, \frac{\pi}{2} \right) : 9^{1-\tan^2 x} + 9^{\tan^2 x} = 10 \right\} \text{ and } b = \sum_{x \in S} \tan^2 \left( \frac{x}{3} \right),$$

then  $\frac{1}{6}(\beta - 14)^2$  is equal to

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a) 16

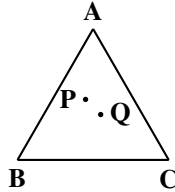
b) 32

c) 8

d) 64

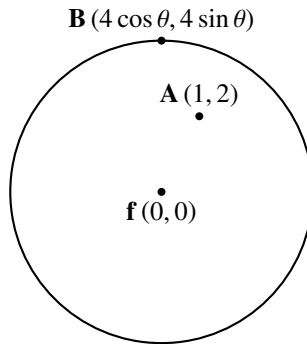
- 6) If the points **P** and **Q** are respectively the circumcenter and the orthocentre of a  $\triangle ABC$ , the  $\overline{PA} + \overline{PB} + \overline{PC}$  is equal to

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a)  $2\overline{QP}$ b)  $\overline{QP}$ c)  $2\overline{PQ}$ d)  $\overline{PQ}$ 

- 7) Let **A** be the point  $(1, 2)$  and **B** be any point on the curve  $x^2 + y^2 = 16$ . **f** the centre of the locus of the point **P**, which divides the line segment **AB** in the ratio  $3 : 2$  is the point **C**  $(\alpha, \beta)$  then the length of the line segment **AC** is

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a)  $\frac{6\sqrt{5}}{5}$ b)  $\frac{2\sqrt{5}}{5}$ c)  $\frac{3\sqrt{5}}{5}$ d)  $\frac{4\sqrt{5}}{5}$ 

- 8) Let  $m$  be the mean and  $\sigma$  be the standard deviation of the distribution

$x_i$	0	1	2	3	4	5
$f_i$	$k + 2$	$2k$	$k^2 - 1$	$k^2 - 1$	$k^2 + 1$	$k - 3$

where  $\sum f_i = 62$ . If  $[x]$  denotes the greatest integer  $\leq x$ , then  $[\mu^2 + \sigma^2]$  is equal to  
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- a) 8                      b) 7                      c) 6                      d) 9

9) If  $S_n = 4 + 11 + 21 + 34 + 50 + \dots$  to  $n$  terms, then  $\frac{1}{60} (S_{29} - S_9)$   
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- a) 220                      b) 227                      c) 226                      d) 223

10) Eight persons are to be transported from city  $A$  to city  $B$  in three cars different makes. If each car can accommodate at most three persons, then the number of ways, in which they can be transported, is  
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- a) 1120                      b) 560                      c) 3360                      d) 1680

11) If

$$A = \frac{1}{5!6!7!} \begin{pmatrix} 5! & 6! & 7! \\ 6! & 7! & 8! \\ 7! & 8! & 9! \end{pmatrix},$$

then  $|\text{adj}(\text{adj}(2A))|$  is equal to

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- a)  $2^{16}$                       b)  $2^8$                       c)  $2^{12}$                       d)  $2^{20}$

12) Let the number  $(22)^{2022} + (2022)^{22}$  leave the remainder  $\alpha$  when divided by 3 and  $\beta$  when divided by 7. Then  $(\alpha^2 + \beta^2)$  is equal to  
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- a) 13                      b) 20                      c) 10                      d) 5

13) let

$$g(x) = f(x) + f(1-x) \text{ and } f^n(x) > 0, x \in (0, 1).$$

If  $g$  is decreasing in the interval  $(0, \alpha)$  and increasing in the interval  $(\alpha, 1)$ , then

$$\tan^{-1}(2\alpha) + \tan^{-1}\left(\frac{\alpha+1}{\alpha}\right)$$

is equal to

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- a)  $\frac{5\pi}{4}$                       b)  $\pi$                       c)  $\frac{3\pi}{4}$                       d)  $\frac{3\pi}{2}$

14) For  $\alpha, \beta, \gamma, \delta \in \mathbf{N}$ , if

$$\int \left( \left( \frac{x}{e} \right)^{2x} + \left( \frac{e}{x} \right)^{2x} \right) \log_e x \, dx = \frac{1}{\alpha} \left( \frac{x}{e} \right)^{\beta x} - \frac{1}{\gamma} \left( \frac{e}{x} \right)^{\delta x} + C, \text{ where } e = \sum_{n=0}^{\infty} \frac{1}{n!}$$

and  $C$  is constant of integration, then  $\alpha + 2\beta + 3\gamma - 4\delta$  is equal to

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a) 4

b)  $-4$

c)  $-8$

d) 1

15) Let  $f$  be a continuous function satisfying

$$\int_0^{t^2} (f(x) + x^2) dx = \frac{4}{3}t^3, \forall t > 0.$$

Then  $f\left(\frac{\pi^2}{4}\right)$  is equal to

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a)  $-\pi^2\left(1 + \frac{\pi^2}{16}\right)$

b)  $\pi\left(1 - \frac{\pi^3}{16}\right)$

c)  $-\pi\left(1 + \frac{\pi^3}{16}\right)$

d)  $\pi^2\left(1 - \frac{\pi^3}{16}\right)$