EE24BTECH11049

1 MCQ

1) The integral

$$\int_0^{\frac{\pi}{4}} \frac{136 \sin x}{3 \sin x + 5 \cos x} \, dx$$

is equal to:

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a)
$$3\pi - 10\log_e(2\sqrt{2}) + 10\log_e 5$$

b) $3\pi - 50\log_e 2 + 20\log_e 5$
c) $3\pi - 30\log_e 2 + 20\log_e 5$
d) $3\pi - 25\log_e 2 + 10\log_e 5$

c)
$$3\pi - 30 \log_{e} 2 + 20 \log_{e} 5$$

b)
$$3\pi - 50 \log_e 2 + 20 \log_e 5$$

d)
$$3\pi - 25 \log_e 2 + 10 \log_e 3$$

2) If y = y(x) is the solution of the differential equation

$$\frac{dy}{dx} + 2y = \sin(2x),$$

 $y(0) = \frac{3}{4}$, then $y(\frac{\pi}{8})$ is equal to:

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a)
$$e^{\frac{\pi}{8}}$$

b)
$$e^{-\frac{\pi}{8}}$$
 c) $e^{\frac{\pi}{4}}$

c)
$$e^{\frac{\pi}{4}}$$

d)
$$e^{-\frac{\pi}{4}}$$

3) Let two straight line drawn from the origin **O** intersect the line 3x + 4y = 12 at the points **P** and **Q** such that $\triangle OPQ$ is an isosceles triangle and $\angle POQ = 90^{\circ}$. If $l = \mathbf{OP}^2 + \mathbf{PQ}^2 + \mathbf{QO}^2$, then the greatest integer less than or equal to l is:

(2024-Apr)

b) 48

c) 42

d) 46

4) If the function

$$f(x) = \frac{\sin 3x + \alpha \sin x - \beta \cos 3x}{x^3}, x \in \mathbf{R}$$

is continuous at x = 0, then f(0) is equal to:

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$$a) -4$$

d)
$$-2$$

5) consider the following statements:

Statement I: For any two complex numbers z_1, z_2 ,

$$(|z_1| + |z_2|) \left| \frac{z_1}{|z_1|} + \frac{z_2}{|z_2|} \right| \le 2(|z_1| + |z_2|), \text{ and}$$

Statement II: If x, y, z and three distinct complex numbers and

a, b, c are three positive real numbers such that

$$\frac{a}{|y-z|} = \frac{b}{|z-x|} = \frac{c}{|x-y|}, \text{ then}$$

$$\frac{a^2}{y-z} + \frac{b^2}{z-x} + \frac{c^2}{x-y} = 1.$$

Between the above two statements:

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- a) statement I is correct but statement II is incorrect.
- b) both statement I and statement II are correct.
- c) statement I is incorrect but statement II is correct.
- d) both statement I and statement II are incorrect.

2 INTEGER

1) Let a_1, a_2, a_3, \ldots be in arithmetic progression progression of positive terms. Let

$$A_k = a_1^2 - a_2^2 + a_3^2 - a_4^2 + \dots + a_{2k-1}^2 - a_{2k}^2.$$

If $A_3 = -153$, $A_5 = -435$ and $a_1^2 + a_2^2 + a_3^2 = 66$, then $a_{17} - A_7$ is equal to _____ (2024-Apr)

- 2) Suppose **AB** is focal chord of the parabola $y^2 = 12x$ of length l and slope $m < \sqrt{3}$, If the distance of the chord **AB** from the origin is d, then ld^2 is equal to _____
- 3) The number real roots of the equation |x||x+2|-5|x+1|-1=0 is _____(2024-Apr)
- 4) If

$$S = \{a \in \mathbf{R} : |2a - 1| = 3[a] + 2\{a\}\}, A = 72\sum_{a \in S} a,$$

where [t] denotes the greatest integer less than or equal to t and $\{t\}$ represents the fractional part of t, then A is equal to _____

5) Let $\mathbf{\bar{a}} = \hat{i} - 3\hat{j} + 7\hat{k}$, $\mathbf{\bar{b}} = 2\hat{i} - \hat{j} + \hat{k}$ and $\mathbf{\bar{c}}$ be a vector such that $(\mathbf{\bar{a}} + 2\mathbf{\bar{b}}) \times \mathbf{\bar{c}} = 3(\mathbf{\bar{c}} \times \mathbf{\bar{a}})$. If $\bar{\mathbf{a}}.\bar{\mathbf{c}} = 130$, then $\bar{\mathbf{b}}.\bar{\mathbf{c}}$ is equal to ____

(2024-Apr)

6) The area of the region enclosed by the parabolas $y = x^2 - 5x$ and $y = 7x - x^2$ is

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7) let f be a differentiable function in the interval $(0, \infty)$ such that f(1) = 1 and

$$\lim_{t\to x}\frac{t^2f\left(x\right)-x^2f\left(t\right)}{t-x}=1, \forall x>0.$$

Then 2f(2) + 3f(3) is equal to _____

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8) If the constant term in the expansion of

$$(1+2x-3x^3)(\frac{3}{2}x^2-\frac{1}{3x})^9$$

is p, then 108p is equal to _____

(2024-Apr)

- 9) From a lot of 10 items, which include 3 defective items, a sample of 5 items is drawn at random. Let the random variable X denote the numbers of defective items in the sample. If the variance of X is σ , then $96\sigma^2$ is equal to _____
 - (2024-Apr)
- 10) The number of ways of getting sum 16 on throwing a dice four times is $\underline{\hspace{1cm}}$ (2024-Apr)