

**Habib University**  
**CSE 351 - Artificial Intelligence**  
**Fall' 2019**  
**Assignment 3**  
25 Points

**Objective:**

The objective of this assignment is to make student better understand the working of a collaborative filtering system to make recommendations. Students will gain hands-on experience of using gradient descent to perform matrix factorization.

You are implementing collaborative filtering to make recommendations to users  $U$  for items  $I$ . You decided to use a model based approach that applies matrix factorization to factorize a rating matrix ( $R$ ) into User features ( $P$ ) and Item features ( $Q$ ) such that,

$$P \times Q = \hat{R} \cong R$$

where  $P$  is a  $m \times k$  matrix and  $Q$  is  $k \times n$  matrix and  $m$ ,  $n$  and  $k$  represent no. of users, no. of items and no. of latent features respectively.

The predicted rating of an item  $j$  by user  $i$  is calculated as follows:

$$\hat{r}_{ij} = \sum_k p_{ik} q_{kj}$$

and error in this prediction is calculated as:

$$e_{ij}^2 = (r_{ij} - \sum_k p_{ik} q_{kj})^2$$

**Q1.1 – Computing gradients [5 points]**

You are applying gradient descent to minimize mean square error. Compute gradients and derive formulas to update  $p$  and  $q$  values.

**Q1.2 - Adding biases [5 points]**

There can be biases in user and item recommendations, which are handled by introducing user bias vector ( $b_U$ ) and item bias vector ( $b_I$ ). In the presence of these biases, rating  $r_{ij}$  is predicted as follows:

$$\hat{r}_{ij} = b_{u_i} + b_{i_j} + \sum_k p_{ik} q_{kj}$$

Derive formulas to update  $p$ ,  $q$ , and biases during gradient descent.

## Q 2 – Factorizing matrices using gradient descent [15 points]

In this question, you will implement gradient descent technique to perform matrix factorization. The code will be written in the attached python file (Ass3.py) that provides basic skeleton of your program.

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### Submission Instructions

Submissions will be made on LMS by the due date (announced on LMS). No email submission will be accepted. The submitted file should be in the form of a ZIP file named as **<studentid>\_Ass3** containing a pdf document for Q1 and python code for Q2.