

# Competitive Programming Handbook

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## 1 Templates and Boilerplates

### 1.1 Main C++ Boilerplate

```

1 // In the name of Allah, the Most Gracious, the Most Merciful
2 // C: FardinMahadi
3
4 #include <bits/stdc++.h>
5 #include <ext/pb_ds/tree_policy.hpp>
6 #include <ext/pb_ds/assoc_container.hpp>
7
8 using namespace __gnu_pbds;
9 using namespace std;
10
11 template<typename T> using ordered_set = tree<T, null_type, less<T>,
12     rb_tree_tag, tree_order_statistics_node_update>;
13
14 #define sp ' '
15 #define nl '\n'
16 #define F first
17 #define S second
18 #define ll long long
19 #define pb push_back
20 #define pf push_front
21 #define popb pop_back
22 #define popf pop_front
23 #define gcd(x,y) __gcd(x,y)
24 #define lcm(x,y) y*x/__gcd(x,y)
25 #define no cout << "NO" << nl
26 #define yes cout << "YES" << nl
27 #define all(a) (a.begin()),(a.end())
28 #define SUM(a) accumulate(all(a),0LL)
29 #define cinv(v) for(auto &i : v) cin >> i
30 #define coutv(v) for(auto &i : v) cout << i << sp
31 #define fixedpoint(x) cout << fixed << setprecision(x)
32 #define UNIQUE(X) (X).erase(unique(all(X)),(X).end())
33 #define print(v) for(auto x : v) cout << x << " "; cout << nl
34 #define SORT_UNIQUE(c) (sort(c.begin(),c.end()), c.resize(distance(c.begin(),unique(c.begin(),c.end()))))
35
36 // Enhanced Macros
37 #define min3(a,b,c) min(a,min(b,c))
38 #define max3(a,b,c) max(a,max(b,c))
39 #define min4(a,b,c,d) min(a,min(b,min(c,d)))
40 #define max4(a,b,c,d) max(a,max(b,max(c,d)))
41 #define sz(x) ((int)(x).size())
42 #define sqr(x) ((x)*(x))
43 #define ceildiv(a,b) ((a+b-1)/b)
44
45 // Debug Macros
46 #ifdef LOCAL
47 #define debug(x) cerr << #x << " = " << x << nl
48 #define debug2(x,y) cerr << #x << " = " << x << ", " << #y << " = " <<
49     y << nl

```

```

48 #define debug3(x,y,z)      cerr << #x << " = " << x << ", " << #y << " = " <<
    y << ", " << #z << " = " << z << nl
49 #define debugv(v)         cerr << #v << " = ["; for(auto x : v) cerr << x <<
    ", "; cerr << "]" << nl
50 #else
51 #define debug(x)
52 #define debug2(x,y)
53 #define debug3(x,y,z)
54 #define debugv(v)
55 #endif
56
57 // Constants
58 const double PI = acos(-1);
59 const int INF = 1e9 + 7;
60 const ll LINF = 1e18 + 7;
61 const int MOD = 1e9 + 7;
62 const int N = 1e5 + 5;
63
64 int n, m;
65
66 void Solve(int tc) {
67     // Your code here
68 }
69
70 int main() {
71     ios::sync_with_stdio(0);
72     cin.tie(0); cout.tie(0);
73
74     int t = 1;
75     cin >> t;
76     for (int tc = 1; tc <= t; tc++) Solve(tc);
77
78     return 0;
79 }

```

## 1.2 Binary Search Template

```

1 // Binary search on answer
2 ll binarySearch(ll left, ll right, function<bool>(ll) check) {
3     ll ans = right;
4     while (left <= right) {
5         ll mid = left + (right - left) / 2;
6         if (check(mid)) {
7             ans = mid;
8             right = mid - 1; // For minimum valid answer
9             // left = mid + 1; // For maximum valid answer
10        } else {
11            left = mid + 1; // For minimum valid answer
12            // right = mid - 1; // For maximum valid answer
13        }
14    }
15    return ans;
16 }

```

## 1.3 Binary Exponentiation

```

1 // Binary exponentiation (a^b) mod m
2 ll binpow(ll a, ll b, ll m = MOD) {
3     a %= m;
4     ll res = 1;
5     while (b > 0) {
6         if (b & 1) res = (res * a) % m;
7         a = (a * a) % m;
8         b >>= 1;
9     }
10    return res;
11 }

```

## 2 Data Structures

### 2.1 DSU (Disjoint Set Union)

```

1 // DSU with path compression and union by rank
2 class DSU {
3 private:
4     vector<int> parent, rank;
5 public:
6     DSU(int n) {
7         parent.resize(n+1);
8         rank.resize(n+1, 0);
9         for (int i = 0; i <= n; i++) parent[i] = i;
10    }
11
12    int find(int x) {
13        if (parent[x] != x) parent[x] = find(parent[x]);
14        return parent[x];
15    }
16
17    void unite(int x, int y) {
18        x = find(x), y = find(y);
19        if (x == y) return;
20        if (rank[x] < rank[y]) swap(x, y);
21        parent[y] = x;
22        if (rank[x] == rank[y]) rank[x]++;
23    }
24
25    bool same(int x, int y) {
26        return find(x) == find(y);
27    }
28 };

```

### 2.2 Segment Tree

```

1 // Segment Tree for range queries and updates
2 class SegmentTree {
3 private:
4     vector<ll> tree;
5     int n;
6
7     void build(vector<ll> &arr, int node, int start, int end) {
8         if (start == end) {
9             tree[node] = arr[start];
10        } else {
11            int mid = (start + end) / 2;
12            build(arr, 2*node, start, mid);
13            build(arr, 2*node+1, mid+1, end);
14            tree[node] = tree[2*node] + tree[2*node+1]; // Change operation
15        }
16    }
17
18    as needed
19 }

```

```

18 void update(int node, int start, int end, int idx, ll val) {
19     if (start == end) {
20         tree[node] = val;
21     } else {
22         int mid = (start + end) / 2;
23         if (idx <= mid) update(2*node, start, mid, idx, val);
24         else update(2*node+1, mid+1, end, idx, val);
25         tree[node] = tree[2*node] + tree[2*node+1];
26     }
27 }
28
29 ll query(int node, int start, int end, int l, int r) {
30     if (r < start || l > end) return 0; // Change identity element as
31     needed
32     if (l <= start && end <= r) return tree[node];
33     int mid = (start + end) / 2;
34     return query(2*node, start, mid, l, r) + query(2*node+1, mid+1, end, l
35     , r);
36 }
37
38 public:
39     SegmentTree(vector<ll> &arr) {
40         n = arr.size();
41         tree.resize(4*n);
42         build(arr, 1, 0, n-1);
43     }
44
45     void update(int idx, ll val) {
46         update(1, 0, n-1, idx, val);
47     }
48
49     ll query(int l, int r) {
50         return query(1, 0, n-1, l, r);
51     }
52 };

```

### 2.3 Fenwick Tree (BIT)

```

1 // Fenwick Tree (Binary Indexed Tree)
2 class FenwickTree {
3 private:
4     vector<ll> tree;
5     int n;
6
7 public:
8     FenwickTree(int size) {
9         n = size;
10        tree.resize(n+1, 0);
11    }
12
13    void update(int idx, ll delta) {
14        for (; idx <= n; idx += idx & -idx) {
15            tree[idx] += delta;
16        }
17    }
18 }

```

```

17 }
18
19 ll query(int idx) {
20     ll sum = 0;
21     for (; idx > 0; idx -= idx & -idx) {
22         sum += tree[idx];
23     }
24     return sum;
25 }
26
27 ll rangeQuery(int l, int r) {
28     return query(r) - query(l-1);
29 }
30 };

```

## 2.4 Trie

```

1 // Trie (Prefix Tree)
2 class Trie {
3 private:
4     struct Node {
5         vector<Node*> children;
6         bool isEnd;
7         Node() : children(26, nullptr), isEnd(false) {}
8     };
9     Node* root;
10
11 public:
12     Trie() { root = new Node(); }
13
14     void insert(string word) {
15         Node* curr = root;
16         for (char c : word) {
17             int idx = c - 'a';
18             if (!curr->children[idx]) {
19                 curr->children[idx] = new Node();
20             }
21             curr = curr->children[idx];
22         }
23         curr->isEnd = true;
24     }
25
26     bool search(string word) {
27         Node* curr = root;
28         for (char c : word) {
29             int idx = c - 'a';
30             if (!curr->children[idx]) return false;
31             curr = curr->children[idx];
32         }
33         return curr->isEnd;
34     }
35
36     bool startsWith(string prefix) {
37         Node* curr = root;

```

```

38         for (char c : prefix) {
39             int idx = c - 'a';
40             if (!curr->children[idx]) return false;
41             curr = curr->children[idx];
42         }
43         return true;
44     }
45 };

```

## 2.5 Sparse Table

```

1 // Sparse Table for RMQ (Range Minimum Query)
2 class SparseTable {
3 private:
4     vector<vector<ll>> table;
5     vector<int> log;
6
7 public:
8     SparseTable(vector<ll> &arr) {
9         int n = arr.size();
10        int maxLog = log2(n) + 1;
11        table.assign(n, vector<ll>(maxLog));
12        log.resize(n+1);
13
14        for (int i = 0; i < n; i++) table[i][0] = arr[i];
15
16        for (int j = 1; j < maxLog; j++) {
17            for (int i = 0; i + (1 << j) <= n; i++) {
18                table[i][j] = min(table[i][j-1], table[i + (1 << (j-1))][j-1]);
19            }
20        }
21
22        for (int i = 2; i <= n; i++) log[i] = log[i/2] + 1;
23    }
24
25    ll query(int l, int r) {
26        int j = log[r - l + 1];
27        return min(table[l][j], table[r - (1 << j) + 1][j]);
28    }
29 };

```

## 2.6 Ordered Set (PBDS)

```

1 #include <ext/pb_ds/tree_policy.hpp>
2 #include <ext/pb_ds/assoc_container.hpp>
3 using namespace __gnu_pbds;
4
5 template<typename T> using ordered_set = tree<T, null_type, less<T>,
6         rb_tree_tag, tree_order_statistics_node_update>;
7
8 // Usage:
9 ordered_set<int> os;

```

```

9 os.insert(5);
10 os.insert(2);
11 os.insert(7);
12 os.order_of_key(5); // Returns number of elements < 5
13 *os.find_by_order(1); // Returns element at index 1

```

## 3 Graph Algorithms

### 3.1 Graph Representation

```

1 // Graph representation - Adjacency list
2 vector<vector<int>> adj(N); // Unweighted
3 vector<vector<pair<int, int>>> adjWeighted(N); // Weighted: {node, weight}
4
5 // For directed graph, add edge once
6 // For undirected graph, add edge twice
7 void addEdge(int u, int v) {
8     adj[u].pb(v);
9     // adj[v].pb(u); // Uncomment for undirected
10 }
11
12 void addWeightedEdge(int u, int v, int w) {
13     adjWeighted[u].pb({v, w});
14     // adjWeighted[v].pb({u, w}); // Uncomment for undirected
15 }

```

### 3.2 DFS (Depth First Search)

```

1 // DFS - Depth First Search
2 vector<bool> visited(N, false);
3
4 void dfs(int u) {
5     visited[u] = true;
6     for (int v : adj[u]) {
7         if (!visited[v]) {
8             dfs(v);
9         }
10    }
11 }
12
13 // DFS with parent tracking
14 void dfs(int u, int parent) {
15     for (int v : adj[u]) {
16         if (v != parent) {
17             dfs(v, u);
18         }
19    }
20 }

```

### 3.3 BFS (Breadth First Search)

```

1 // BFS - Breadth First Search
2 vector<bool> visited(N, false);
3 vector<int> dist(N, -1);
4
5 void bfs(int start) {
6     queue<int> q;
7     q.push(start);

```

```

8   visited[start] = true;
9   dist[start] = 0;

10
11   while (!q.empty()) {
12       int u = q.front();
13       q.pop();

14       for (int v : adj[u]) {
15           if (!visited[v]) {
16               visited[v] = true;
17               dist[v] = dist[u] + 1;
18               q.push(v);
19           }
20       }
21   }
22 }
23

```

### 3.4 Dijkstra's Algorithm

```

1 // Dijkstra's Algorithm - Single source shortest path
2 vector<ll> dijkstra(int start, int n) {
3     vector<ll> dist(n+1, LINF);
4     dist[start] = 0;
5     priority_queue<pair<ll, int>, vector<pair<ll, int>>, greater<pair<ll, int>>> pq;
6     pq.push({0, start});

7
8     while (!pq.empty()) {
9         ll d = pq.top().F;
10        int u = pq.top().S;
11        pq.pop();

12        if (d > dist[u]) continue;

13        for (auto [v, w] : adjWeighted[u]) {
14            if (dist[u] + w < dist[v]) {
15                dist[v] = dist[u] + w;
16                pq.push({dist[v], v});
17            }
18        }
19    }
20
21    return dist;
22 }
23

```

### 3.5 Floyd-Warshall

```

1 // Floyd-Warshall - All pairs shortest path
2 vector<vector<ll>> floydWarshall(int n) {
3     vector<vector<ll>> dist(n+1, vector<ll>(n+1, LINF));

4
5     // Initialize distances
6     for (int i = 1; i <= n; i++) dist[i][i] = 0;
7     for (int u = 1; u <= n; u++) {

```

```

8         for (auto [v, w] : adjWeighted[u]) {
9             dist[u][v] = min(dist[u][v], (ll)w);
10        }
11    }

12    // Floyd-Warshall algorithm
13    for (int k = 1; k <= n; k++) {
14        for (int i = 1; i <= n; i++) {
15            for (int j = 1; j <= n; j++) {
16                if (dist[i][k] != LINF && dist[k][j] != LINF) {
17                    dist[i][j] = min(dist[i][j], dist[i][k] + dist[k][j]);
18                }
19            }
20        }
21    }

22    return dist;
23 }
24

```

### 3.6 Topological Sort

```

1 // Topological Sort using DFS
2 vector<bool> visited(N, false);
3 vector<int> topoOrder;

4
5 void dfsTopo(int u) {
6     visited[u] = true;
7     for (int v : adj[u]) {
8         if (!visited[v]) {
9             dfsTopo(v);
10        }
11    }
12    topoOrder.pb(u);
13 }

14
15 vector<int> topologicalSort(int n) {
16     topoOrder.clear();
17     fill(all(visited), false);
18     for (int i = 1; i <= n; i++) {
19         if (!visited[i]) dfsTopo(i);
20     }
21     reverse(all(topoOrder));
22     return topoOrder;
23 }

```

### 3.7 Cycle Detection

```

1 // Cycle detection in directed graph
2 vector<int> color(N, 0); // 0: white, 1: gray, 2: black

3
4 bool hasCycle(int u) {
5     color[u] = 1; // Gray
6     for (int v : adj[u]) {
7         if (color[v] == 1) return true; // Back edge found

```

```

8         if (color[v] == 0 && hasCycle(v)) return true;
9     }
10    color[u] = 2; // Black
11    return false;
12 }
13
14 // Cycle detection in undirected graph
15 bool hasCycleUndirected(int u, int parent) {
16     visited[u] = true;
17     for (int v : adj[u]) {
18         if (!visited[v]) {
19             if (hasCycleUndirected(v, u)) return true;
20         } else if (v != parent) {
21             return true;
22         }
23     }
24     return false;
25 }

```

```

34
35 // Second DFS on reverse graph
36 fill(all(visited), false);
37 vector<vector<int>> scc;
38 reverse(all(order));
39 for (int u : order) {
40     if (!visited[u]) {
41         component.clear();
42         dfs2(u, adjRev);
43         scc.pb(component);
44     }
45 }
46 return scc;
47 }

```

### 3.8 Strongly Connected Components (Kosaraju)

```

1 // Kosaraju's algorithm for Strongly Connected Components
2 vector<bool> visited(N, false);
3 vector<int> order, component;
4
5 void dfs1(int u) {
6     visited[u] = true;
7     for (int v : adj[u]) {
8         if (!visited[v]) dfs1(v);
9     }
10    order.pb(u);
11 }
12
13 void dfs2(int u, vector<vector<int>> &adjRev) {
14     visited[u] = true;
15     component.pb(u);
16     for (int v : adjRev[u]) {
17         if (!visited[v]) dfs2(v, adjRev);
18     }
19 }
20
21 vector<vector<int>> findSCC(int n) {
22     // Build reverse graph
23     vector<vector<int>> adjRev(n+1);
24     for (int u = 1; u <= n; u++) {
25         for (int v : adj[u]) adjRev[v].pb(u);
26     }
27
28     // First DFS
29     fill(all(visited), false);
30     order.clear();
31     for (int i = 1; i <= n; i++) {
32         if (!visited[i]) dfs1(i);
33     }

```

## 4 String Algorithms

### 4.1 KMP Algorithm

```

1 // KMP Algorithm for pattern matching
2 vector<int> buildLPS(string pattern) {
3     int m = pattern.length();
4     vector<int> lps(m, 0);
5     int len = 0, i = 1;
6
7     while (i < m) {
8         if (pattern[i] == pattern[len]) {
9             len++;
10            lps[i] = len;
11            i++;
12        } else {
13            if (len != 0) len = lps[len-1];
14            else { lps[i] = 0; i++; }
15        }
16    }
17    return lps;
18 }
19
20 vector<int> kmpSearch(string text, string pattern) {
21     vector<int> lps = buildLPS(pattern);
22     vector<int> matches;
23     int n = text.length(), m = pattern.length();
24     int i = 0, j = 0;
25
26     while (i < n) {
27         if (text[i] == pattern[j]) { i++; j++; }
28         if (j == m) {
29             matches.pb(i - j);
30             j = lps[j-1];
31         } else if (i < n && text[i] != pattern[j]) {
32             if (j != 0) j = lps[j-1];
33             else i++;
34         }
35     }
36     return matches;
37 }

```

### 4.2 Z-Algorithm

```

1 // Z-Algorithm for string preprocessing
2 vector<int> buildZ(string s) {
3     int n = s.length();
4     vector<int> z(n, 0);
5     int l = 0, r = 0;
6
7     for (int i = 1; i < n; i++) {
8         if (i <= r) z[i] = min(r - i + 1, z[i - l]);
9         while (i + z[i] < n && s[z[i]] == s[i + z[i]]) z[i]++;

```

```

10         if (i + z[i] - 1 > r) {
11             l = i;
12             r = i + z[i] - 1;
13         }
14     }
15     return z;
16 }
17
18 // Find all occurrences of pattern in text
19 vector<int> zSearch(string text, string pattern) {
20     string combined = pattern + "$" + text;
21     vector<int> z = buildZ(combined);
22     vector<int> matches;
23     int m = pattern.length();
24     for (int i = m + 1; i < combined.length(); i++) {
25         if (z[i] == m) matches.pb(i - m - 1);
26     }
27     return matches;
28 }

```

### 4.3 String Utilities

```

1 // String reverse
2 string reverseStr(string s) {
3     reverse(all(s));
4     return s;
5 }
6
7 // Check if string is palindrome
8 bool isPalindrome(string s) {
9     int n = s.length();
10    for (int i = 0; i < n/2; i++) {
11        if (s[i] != s[n-1-i]) return false;
12    }
13    return true;
14 }
15
16 // Convert string to lowercase
17 string toLower(string s) {
18     transform(all(s), s.begin(), ::tolower);
19     return s;
20 }
21
22 // Convert string to uppercase
23 string toUpper(string s) {
24     transform(all(s), s.begin(), ::toupper);
25     return s;
26 }
27
28 // Split string by delimiter
29 vector<string> split(const string &str, const string &delimiter) {
30     vector<string> tokens;
31     size_t start = 0, end, delimLength = delimiter.length();
32

```

```

33 while ((end = str.find(delimiter, start)) != string::npos) {
34     tokens.push_back(str.substr(start, end - start));
35     start = end + delimLength;
36 }
37 tokens.push_back(str.substr(start));
38 return tokens;
39 }

```

## 5 Mathematical Algorithms

### 5.1 GCD and LCM

```

1 // Recursive GCD
2 ll gcd(ll a, ll b) {
3     return b == 0 ? a : gcd(b, a % b);
4 }
5
6 // Efficient and overflow-safe LCM function
7 ll lcm(ll a, ll b) {
8     return (a / __gcd(a, b)) * b;
9 }

```

### 5.2 Extended Euclidean Algorithm

```

1 // Extended Euclidean Algorithm - returns gcd and coefficients
2 ll extgcd(ll a, ll b, ll &x, ll &y) {
3     if (b == 0) {
4         x = 1, y = 0;
5         return a;
6     }
7     ll x1, y1;
8     ll g = extgcd(b, a % b, x1, y1);
9     x = y1;
10    y = x1 - (a / b) * y1;
11    return g;
12 }
13
14 // Modular inverse using extended Euclidean
15 ll modInverse(ll a, ll m = MOD) {
16     ll x, y;
17     ll g = extgcd(a, m, x, y);
18     if (g != 1) return -1; // No inverse exists
19     return (x % m + m) % m;
20 }

```

### 5.3 Modular Arithmetic

```

1 // Modular arithmetic operations
2 ll modAdd(ll a, ll b, ll m = MOD) { return ((a % m) + (b % m)) % m; }
3 ll modSub(ll a, ll b, ll m = MOD) { return ((a % m) - (b % m) + m) % m; }
4 ll modMul(ll a, ll b, ll m = MOD) { return ((a % m) * (b % m)) % m; }
5 ll modDiv(ll a, ll b, ll m = MOD) { return modMul(a, modInverse(b, m), m); }

```

### 5.4 Sieve of Eratosthenes

```

1 // Sieve of Eratosthenes - Generate primes up to n
2 vector<bool> isPrime(N, true);
3 vector<int> primes;
4

```

```

5 void sieve(int n) {
6     isPrime[0] = isPrime[1] = false;
7     for (int i = 2; i * i <= n; i++) {
8         if (isPrime[i]) {
9             for (int j = i * i; j <= n; j += i) {
10                 isPrime[j] = false;
11             }
12         }
13     }
14     for (int i = 2; i <= n; i++) {
15         if (isPrime[i]) primes.pb(i);
16     }
17 }

```

## 5.5 Prime Factorization

```

1 // Prime factorization
2 vector<pair<ll, int>> factorize(ll n) {
3     vector<pair<ll, int>> factors;
4     for (ll i = 2; i * i <= n; i++) {
5         if (n % i == 0) {
6             int cnt = 0;
7             while (n % i == 0) {
8                 n /= i;
9                 cnt++;
10            }
11            factors.pb({i, cnt});
12        }
13    }
14    if (n > 1) factors.pb({n, 1});
15    return factors;
16 }

```

## 5.6 Euler Totient Function

```

1 // Euler Totient Function using sieve
2 vector<int> phi(N);
3
4 void eulerTotient(int n) {
5     for (int i = 1; i <= n; i++) phi[i] = i;
6     for (int i = 2; i <= n; i++) {
7         if (phi[i] == i) { // i is prime
8             for (int j = i; j <= n; j += i) {
9                 phi[j] -= phi[j] / i;
10            }
11        }
12    }
13 }

```

## 5.7 Combinatorics

```

1 // Factorial with mod
2 vector<ll> fact(N);
3
4 void precomputeFactorial(int n, ll m = MOD) {
5     fact[0] = 1;
6     for (int i = 1; i <= n; i++) {
7         fact[i] = (fact[i-1] * i) % m;
8     }
9 }
10
11 // nCr with mod
12 ll nCr(ll n, ll r, ll m = MOD) {
13     if (r > n || r < 0) return 0;
14     ll num = fact[n];
15     ll den = (fact[r] * fact[n-r]) % m;
16     return (num * modInverse(den, m)) % m;
17 }

```

## 5.8 Matrix Exponentiation

```

1 // Matrix multiplication
2 vector<vector<ll>> matMul(vector<vector<ll>> &a, vector<vector<ll>> &b, ll m = MOD) {
3     int n = a.size();
4     vector<vector<ll>> res(n, vector<ll>(n, 0));
5     for (int i = 0; i < n; i++) {
6         for (int j = 0; j < n; j++) {
7             for (int k = 0; k < n; k++) {
8                 res[i][j] = (res[i][j] + (a[i][k] * b[k][j]) % m) % m;
9             }
10        }
11    }
12    return res;
13 }
14
15 // Matrix exponentiation
16 vector<vector<ll>> matPow(vector<vector<ll>> base, ll exp, ll m = MOD) {
17     int n = base.size();
18     vector<vector<ll>> res(n, vector<ll>(n, 0));
19     for (int i = 0; i < n; i++) res[i][i] = 1; // Identity matrix
20
21     while (exp > 0) {
22         if (exp & 1) res = matMul(res, base, m);
23         base = matMul(base, base, m);
24         exp >>= 1;
25     }
26     return res;
27 }

```

## 6 STL Containers and Utilities

### 6.1 Vector

```

1 vector<int> v;
2 v.push_back(5);           // Add element
3 v.pop_back();             // Remove last element
4 v.size();                 // Get size
5 v.empty();                // Check if empty
6 v.clear();                // Clear all elements
7 sort(v.begin(), v.end()); // Sort
8 reverse(v.begin(), v.end()); // Reverse
9 v.resize(n, val);         // Resize with default value
10 v.insert(v.begin() + i, val); // Insert at position
11 v.erase(v.begin() + i);   // Erase at position
12 auto it = find(v.begin(), v.end(), val); // Find element

```

### 6.2 Map and Unordered Map

```

1 map<string, int> mp;
2 mp["key"] = value;        // Insert/update
3 mp.count("key");           // Check existence (0 or 1)
4 mp.find("key");            // Returns iterator
5 mp.erase("key");           // Erase by key
6 mp.size();                 // Number of elements
7 for (auto [key, val] : mp) { } // Iterate
8
9 unordered_map<string, int> ump; // Faster, no ordering

```

### 6.3 Set and Unordered Set

```

1 set<int> s;
2 s.insert(5);               // Insert
3 s.erase(5);                // Erase
4 s.count(5);                // Check existence
5 s.find(5);                 // Returns iterator
6 s.lower_bound(5);           // First element >= 5
7 s.upper_bound(5);           // First element > 5
8 s.size();
9
10 multiset<int> ms;           // Allows duplicates
11 ms.erase(ms.find(5));       // Erase one occurrence
12 ms.erase(5);                // Erase all occurrences
13
14 unordered_set<int> us;       // Faster, no ordering

```

### 6.4 Priority Queue

```

1 // Max heap (default)
2 priority_queue<int> pq;
3 pq.push(5);

```

```

4 pq.top();                  // Get max element
5 pq.pop();                  // Remove max element
6 pq.size();
7 pq.empty();
8
9 // Min heap
10 priority_queue<int, vector<int>, greater<int>> minpq;
11
12 // Custom comparator
13 auto cmp = [](int a, int b) { return a > b; };
14 priority_queue<int, vector<int>, decltype(cmp)> custompq(cmp);

```

### 6.5 Queue and Deque

```

1 queue<int> q;
2 q.push(5);                 // Add to back
3 q.pop();                   // Remove from front
4 q.front();                 // Get front element
5 q.back();                  // Get back element
6 q.size();
7 q.empty();
8
9 deque<int> dq;
10 dq.push_front(5);          // Add to front
11 dq.push_back(5);           // Add to back
12 dq.pop_front();            // Remove from front
13 dq.pop_back();             // Remove from back
14 dq.front();
15 dq.back();

```

### 6.6 Stack

```

1 stack<int> st;
2 st.push(5);                // Add to top
3 st.pop();                  // Remove from top
4 st.top();                  // Get top element
5 st.size();
6 st.empty();

```

### 6.7 Pair

```

1 pair<int, int> p = {1, 2};
2 p.first;                   // Access first element
3 p.second;                  // Access second element
4 p = make_pair(3, 4);
5
6 // Vector of pairs
7 vector<pair<int, int>> vp;
8 vp.push_back({1, 2});
9 sort(vp.begin(), vp.end()); // Sorts by first, then second

```

## 6.8 Common STL Algorithms

```

1 // Sorting
2 sort(v.begin(), v.end());           // Ascending
3 sort(v.begin(), v.end(), greater<int>()); // Descending
4 sort(v.begin(), v.end(), [](int a, int b) { return a > b; }); // Custom
5
6 // Binary search (requires sorted container)
7 binary_search(v.begin(), v.end(), val); // Returns bool
8 lower_bound(v.begin(), v.end(), val);   // First >= val
9 upper_bound(v.begin(), v.end(), val);   // First > val
10
11 // Other useful functions
12 max(a, b); min(a, b);
13 max_element(v.begin(), v.end());       // Returns iterator
14 min_element(v.begin(), v.end());
15 accumulate(v.begin(), v.end(), 0LL);   // Sum
16 count(v.begin(), v.end(), val);        // Count occurrences
17 find(v.begin(), v.end(), val);         // Find element
18 reverse(v.begin(), v.end());           // Reverse
19 unique(v.begin(), v.end());            // Remove consecutive duplicates
20 next_permutation(v.begin(), v.end());   // Next permutation
21 prev_permutation(v.begin(), v.end());   // Previous permutation

```

## 7 Miscellaneous Utilities

### 7.1 Grid Helpers

```

1 // 4-direction movement
2 int dx4[] = {-1, 0, +1, 0};
3 int dy4[] = {0, -1, 0, +1};
4
5 // 8-direction movement (including diagonals)
6 int dx8[] = {-1, -1, -1, 0, 0, +1, +1, +1};
7 int dy8[] = {-1, 0, +1, -1, +1, -1, 0, +1};
8
9 // Boundary check
10 inline bool in(int i, int j) {
11     return (0 <= i && i < n && 0 <= j && j < m);
12 }
13
14 // Grid traversal helper
15 void traverseGrid(int i, int j) {
16     for (int k = 0; k < 4; k++) { // Change to 8 for diagonal
17         int ni = i + dx4[k];
18         int nj = j + dy4[k];
19         if (in(ni, nj)) {
20             // Process cell (ni, nj)
21         }
22     }
23 }

```

### 7.2 Coordinate Compression

```

1 // Coordinate compression
2 vector<int> compress(vector<int> &arr) {
3     vector<int> sorted = arr;
4     sort(all(sorted));
5     sorted.erase(unique(all(sorted)), sorted.end());
6
7     vector<int> compressed;
8     for (int x : arr) {
9         int idx = lower_bound(all(sorted), x) - sorted.begin();
10        compressed.pb(idx);
11    }
12    return compressed;
13 }

```

### 7.3 Timing Utilities

```

1 #include <chrono>
2 using namespace std::chrono;
3
4 auto start_time = high_resolution_clock::now();
5 // Your code here
6 auto end_time = high_resolution_clock::now();

```

```

7 auto duration = duration_cast<microseconds>(end_time - start_time);
8 cout << "Time: " << duration.count() << " microseconds" << endl;

```

## 7.4 Merge Sort with Inversion Count

```

1 ll inversionCount = 0;
2
3 void merge(vector<int>& arr, int low, int mid, int high) {
4     vector<int> temp(high - low + 1);
5     int i = low, j = mid + 1, k = 0;
6     while (i <= mid && j <= high) {
7         if (arr[i] <= arr[j]) temp[k++] = arr[i++];
8         else {
9             temp[k++] = arr[j++];
10            inversionCount += (mid - i + 1); // Count inversions
11        }
12    }
13    while (i <= mid) temp[k++] = arr[i++];
14    while (j <= high) temp[k++] = arr[j++];
15    for (int idx = 0; idx < temp.size(); idx++) {
16        arr[low + idx] = temp[idx];
17    }
18 }
19
20 void mergeSort(vector<int>& arr, int low, int high) {
21     if (low < high) {
22         int mid = low + (high - low) / 2;
23         mergeSort(arr, low, mid);
24         mergeSort(arr, mid + 1, high);
25         merge(arr, low, mid, high);
26     }
27 }

```

## 7.5 Useful Constants and Macros

```

1 const double PI = acos(-1);
2 const int INF = 1e9 + 7;
3 const ll LINF = 1e18 + 7;
4 const int MOD = 1e9 + 7;
5 const int N = 1e5 + 5;
6
7 // Common macros already in boilerplate:
8 // sp, nl, F, S, ll, pb, popb, gcd, lcm, all, SUM, etc.

```