

#### Faculty of Science

Course: CSCI 3070U: Analysis and Design of Algorithms

Assignment: #2

**Topic:** Sorting, Dynamic Programming, Greedy Algorithms

**Note:** This assignment is to be completed either individually or in a team of two students. Groups larger than two will not be permitted, because it is almost a guarantee that some student in the team is not meeting all the learning objectives.

### Part 1 (10 points)

Suppose you have a log of length L, marked to be cut in n different locations labeled  $1, 2, \ldots, n$ . The woodcutter will cut a given log of wood, at any place you choose, for **a price equal to the length of the given log**. For simplicity, let indices 0 and n + 1 denote the left and right endpoints of the original log of length L. Let  $d_i$  denote the distance of mark i from the left end of the log and assume that  $0=d_0 < d_1 < d_2 < ... < d_n < d_{n+1} = L$ . Determining the **sequence** of cuts to the log that will cut the log at all the n marked places and minimize your total payment. Choose the following strategies:

- A. Greedy algorithm picking the point closest to the center of log (**3 points**). This strategy is not optimum.
- B. Dynamic programming (**7 points**). The algorithm time-complexity is  $O(n^2)$ .

Use C, C++, Java, or Python to implement Part A and B (ask the instructor if you have another programming language in mind).

# Part 2 (5 points)

For this part of the assignment, you will implement a radix sort procedure for sorting numbers between 0 (inclusive) and 1,000,000 (exclusive) (i.e., 6-digit numbers).

You may find the following code (which determines the value of an arbitrary digit) useful:

```
function getDigit(num, digit) {
    working = num / 10<sup>digit-1</sup>;
    return working mod 10;
}
```

# Part 3 (5 points)

Write an implementation of Huffman coding, which is a greedy implementation of assigning prefix codes. This will require a program that does the following:

- 1. Read through a simple ASCII text file (passed as an argument), determining the frequency of each character in the file
- 2. Use these frequencies to calculate the optimal prefix codes for each character (Huffman)
  - Print a complete table of prefix codes for the characters in the document (print only characters with frequencies > 0)
- 3. Normally, you would then encode each character using its prefix code
  - However, actually implementing this requires some trick bit manipulation (which, for some languages, is difficult to do)
  - Instead, calculate the length of the entire document before and after using the prefix codes

Use C, C++, Java, or Python to implement the solution (ask the instructor if you have another programming language in mind).

#### **How to Submit**

Put your source code answers to part 1-3 into a ZIP file, called Assignment2\_FirstNameLastName\_StudentNum.zip (do not use .rar, .7z or other archival formats) and submit this file to Canvas.