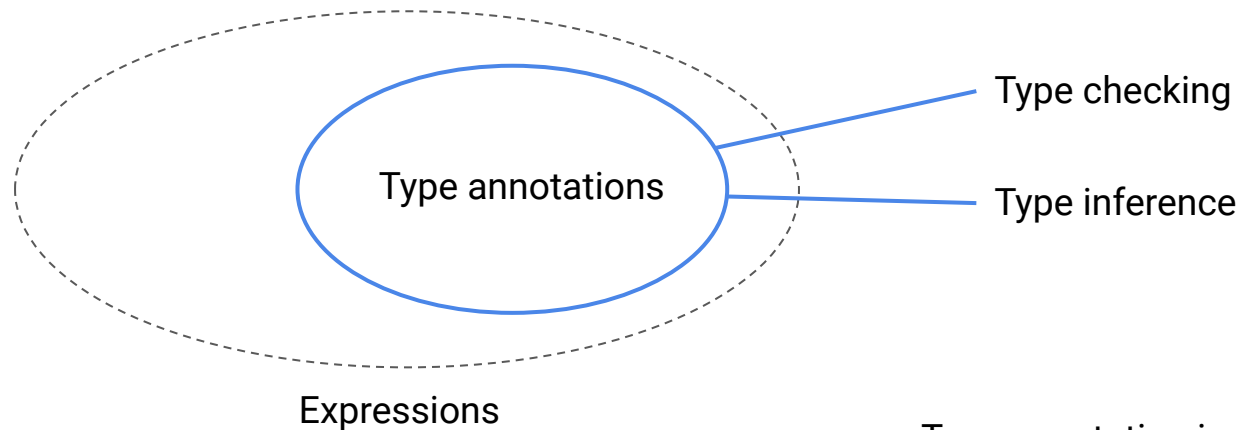


# Elements of Type Systems

# Elements of Type Systems



Type annotation is part of the syntax of the programming language.

# Type annotation over expressions

Concrete types

- Complete descriptions of the data.
- Allows construction of new instances in memory.

Abstract types

- Partial description of data
- Only applicable to data already constructed in memory.

# Type annotations

## Basic types

- Physical data layout in memory

## Concrete class

- Composite data layout
- Access by members and methods

## Extension and Composition

- Building more complex types using existing types

## Abstract classes

- Functional specification of data
- Partially concrete specs

## Interfaces

- Purely abstract with no concrete specs
- Spec on both field and methods
- Default method implementation

## Generics

- Composite types with type parameters

# Function Types

- A function is described by function types.
- A function type describes the types of the parameters and the type of the return value.



# Some Types

## Basic types

- Boolean: 1B
- Byte: 1B
- Char: 2B
- Int and UInt: 4B
- Int64 and UInt: 8B
- Float32
- Float64 and Double: 8B

They are not data, but description of some data to be created or manipulated during runtime of the code.

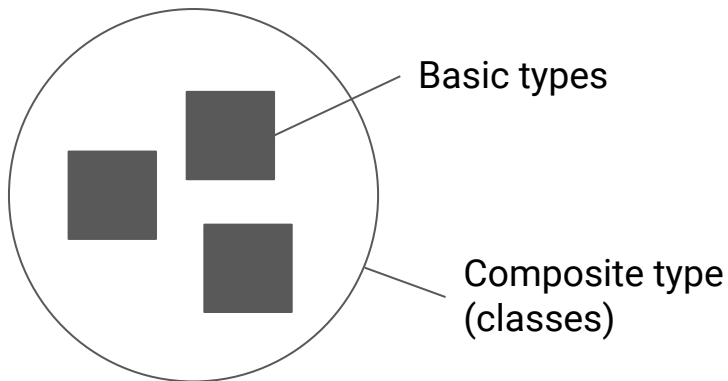
1. Data are instances of types.
2. Evaluation is performed on instances of types, not the types themselves.
3. Evaluation only occurs when the expression passes type checking.

All basic types are provided by programming language - not the program. So, we cannot define any additional basic types.

# Concrete Classes

## Examples

- String
- BigDecimal



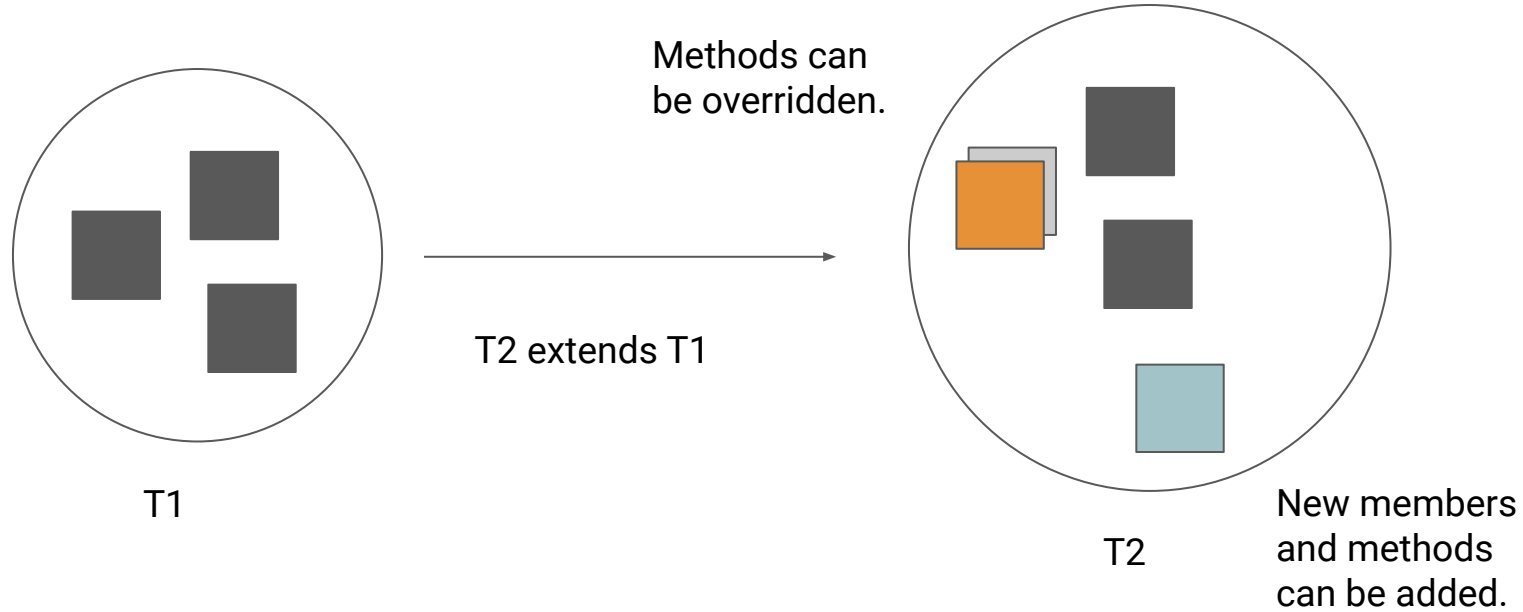
Objects are instances of classes.

How do we access parts of an object?

- Members (aka fields, properties, ...)
- Methods

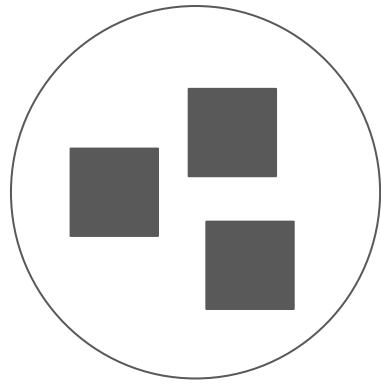
Programs can define many concrete classes.

# Extension





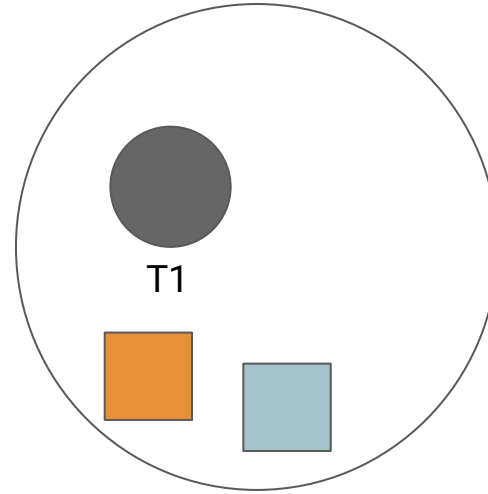
# Composition



T1

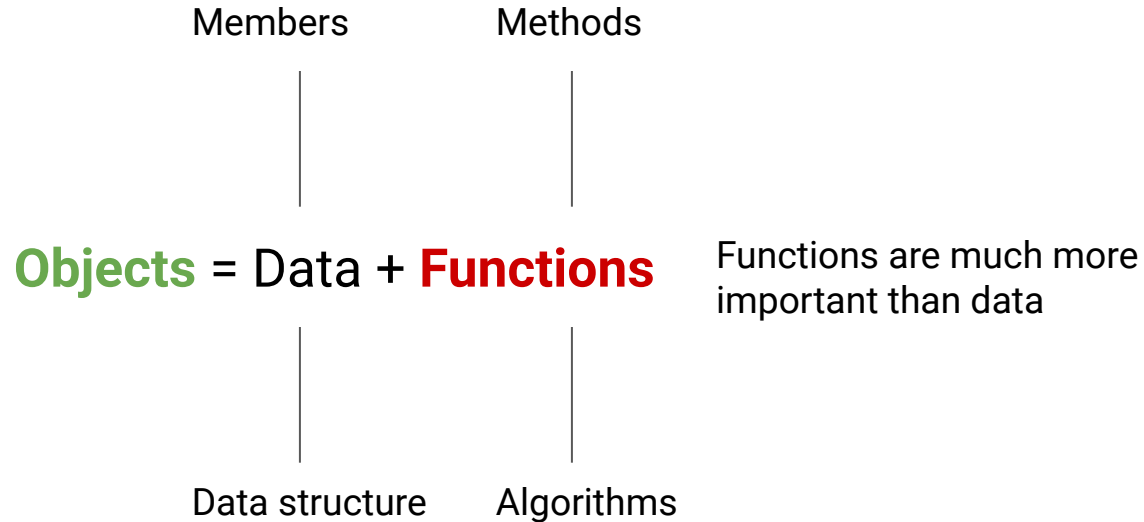


T2 is a  
composition of T1  
with other types



T2

# Object-oriented programming



# Functional specification of data

We specify objects by the members and methods they **should** have.

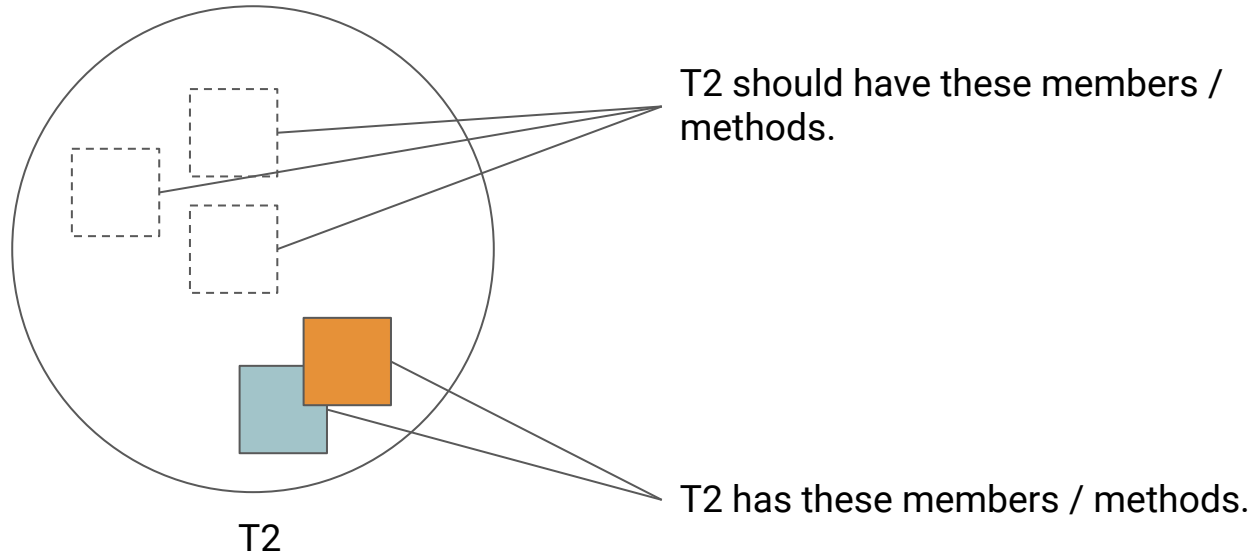
A student in CSCI3055U **should** be able to program in Clojure.

*This is an abstract specification on objects.*

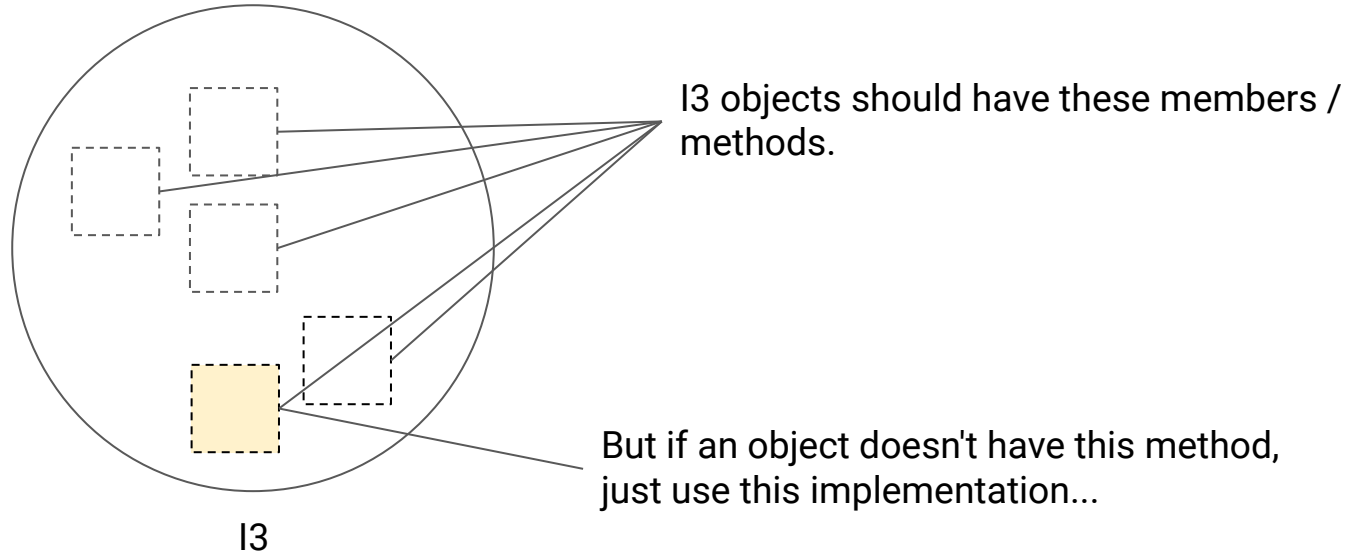
A student in CSCI3055U **writes** Clojure code like this ...

*This is a concrete description of objects.*

# Abstract Classes: concrete and abstract



# Interfaces: 100% abstract (sort of)



# Generics

Consider a data structure: **List**.

- **List** of *what?*
- But all lists have a common set of methods and members
  - `List.add( __ )`
  - `List.get(i)`
  - `List.size`
- Using generics, we can still describe **List** as a type without knowing *what* is.

# Generics with type parameters

Let  $T$  be a type.

List of  $T$  is a type that has the following methods:

- `add(thing: T)`
- `get(index: Integer) -> T`
- `size: Integer`
- $T$  is a type parameter.
- $T$  is used to describe **List**.
- This makes **List** a generic type, with one type parameter  $T$ .

`List<T>` means List of  $T$  things.

# Multiple type parameters

Consider HashMap as a type. It has two type parameters: one for the keys of the hashmap, and another for the values: K, V.

HashMap of <K, V>

- add(key: K, value: V)
- get(key: K) -> V
- size: Integer