

ENEL 476 – Assignment #3

Due on Thurs April 6 at 4 pm

Drop boxes on 2nd floor of ICT

An antenna with impedance $Z_L = 72 - j43 \Omega$ is connected to a lossless transmission line with impedance $Z_0 = 75 \Omega$. Use the Smith Chart to solve the following problems.

- Plot the normalized impedance, z_L
- Find the reflection coefficient, Γ .
- Find the standing wave ratio (VSWR, SWR or s).
- Find the shortest distances from the antenna to the location of the voltage maximum (V_{max}) and voltage minimum (V_{min}) on the transmission line.
- Indicate the locations of the short and open on the Smith Chart.
- The antenna is connected to transmission line of length of 0.625λ . What is Z_{in} at this location?
- A generator supplies 20 V and has internal impedance of $Z_g = 75 \Omega$. How much power is absorbed by the load connected to the generator and the 0.625λ line?

$$a) \quad z_L = \frac{72 - j43}{75}$$

$$= 0.96 - j0.573$$

$$b) \quad |\Gamma| = 0.28$$

$$\angle = -76^\circ$$

$$c) \quad S = 1.75 - 1.8$$

$$d) \quad V_{max} \text{ is located at } 0.25\lambda$$

$$V_{min} \text{ is located at } 0.5\lambda$$

$$Z_L \text{ is located at } 0.356\lambda$$

$$Z_L \rightarrow V_{max} = [(0.5 - 0.356) + 0.25]\lambda$$

$$= 0.394\lambda$$

$$Z_L \rightarrow V_{min} = 0.144\lambda$$

$$f) \quad 0.625\lambda = (0.5 + 0.125)\lambda$$

↑
notation

$$Z_L \rightarrow Z_{in} \Rightarrow 0.356\lambda$$

$$+ 0.125\lambda$$

$$\hline 0.481\lambda$$

$$Z_{in} = 0.575 - j0.08$$

$$Z_{in} = 75 Z_{in}$$

$$Z_{in} = 43.125 - j6 \Omega$$

$$g) \quad P_L = \frac{1}{2} |I_{in}|^2 \operatorname{Re}\{Z_{in}\}$$

$$I_{in} = \frac{10}{75 + 43.125 - j6}$$

$$= 0.168 + j0.0096$$

$$P_L = \frac{1}{2} (0.0283) (43)$$

$$P_L = 0.610 \text{ W}$$

Normalized Impedance Smith Chart

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