

# Online Tutorial #01 - FM Demodulation - PLL - Part I

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12:01 PM

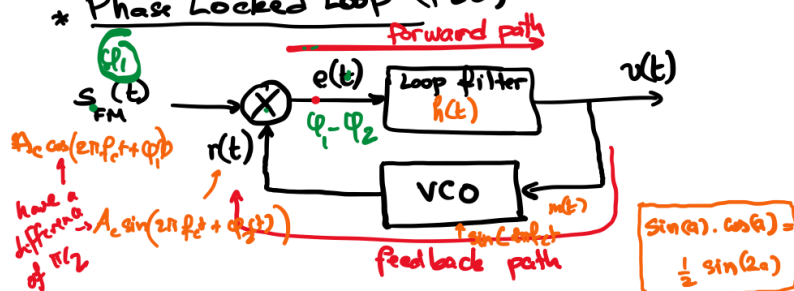
Objective: to use a system that takes  $s_{FM}(t)$  as input and returns  $m(t)$  as output.

$$s_{FM}(t) = A_c \cos\left(2\pi f_c t + 2\pi k_f \int_0^t m(\tau) d\tau\right)$$

$\xrightarrow{\varphi_1(t)}$  System  $\rightarrow m(t) \approx \frac{d\varphi_1(t)}{dt}$

$$\varphi_1(t) = 2\pi k_f \int_0^t m(\tau) d\tau$$

\* Phase Locked Loop (PLL):



if  $v(t) = m(t)$  then  $r(t)$  is a FM signal similar to  $s_{FM}(t)$  but with  $\pi/2$  phase difference.

In that case,  $e(t)$  will not have low frequency components and the loop converges to the desired output.

if  $v(t) \neq m(t)$  then  $r(t)$  is a FM signal that is different than  $s_{FM}(t)$ .

In that case,  $e(t)$  will have a low freq. component  $\rightarrow v(t)$  will change to get closer to  $m(t)$

$$\sin(a) \cos(b) = \frac{1}{2} [\sin(a+b) + \sin(a-b)]$$

high freq.      low freq.

PLL can be seen as a negative feedback system on the phases.

To analyze this system, we make two assumptions:

- 1- the VCO frequency is exactly the same as the center frequency of the FM signal.
- 2- there is a  $\pi/2$  phase shift between the unmodulated carrier of the VCO and the unmodulated carrier of the FM signal.