

Student ID: _____

March 14, 2018 – 9:00 AM

Duration: 50 minutes

**ENEL 471 - Winter 2018
2nd Midterm Exam**

Notes:

- This exam is closed book and closed notes.
- Non-programmable calculators are allowed.
- The exam duration is 50 minutes.
- The exam is composed of 2 Problems and 5 pages. All the problems are independent.
- Please write your name and ID# in each page

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Problem 1 [10 pts]

The sinusoidal modulating wave:

$$m(t) = 2\cos(6000\pi t)$$

is applied to a phase modulator with phase sensitivity $k_p = 0.1$ radian per volt. The unmodulated carrier wave has frequency $f_c = 1$ MHz and amplitude $A_c = 1$ volt.

- a- Determine the instantaneous frequency of this PM signal and sketch it versus time.
- b- Determine the time domain expression of this PM signal and sketch it versus time.
- c- Determine the maximum frequency deviation Δf and the modulation index β .
- d- Determine the expression of the frequency spectrum of the resulting PM signal and sketch it. **Show all amplitudes and frequencies of interest.**
- e- Construct a phasor diagram of this PM modulated signal.

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Problem 2 [10 pts]

A carrier wave of amplitude $A_c = 2$ volt and frequency $f_c = 100$ kHz is FM modulated by the message $m(t) = A_m \cos(2f_m \pi t)$, where $A_m = 1$ volt and $f_m = 1$ kHz. The frequency sensitivity of the FM modulator is k_f is 2 kHz per volt.

- What is the time domain expression of the FM modulated signal?
- Determine the maximum frequency deviation Δf and the modulation index β
- Determine the transmission bandwidth of this FM signal using Caron's rule.
- Determine the bandwidth by transmitting only those side frequencies whose amplitude exceed 1 percent of the unmodulated carrier amplitude. (Use the table below)
- Sketch the frequency spectrum of the modulated signal. **Show only the sidebands within the bandwidth calculated in d-. Indicate all the frequencies and amplitudes of interest.** (Use the table below)

Values of the Bessel Functions $J_n(\beta)$

	$\beta = 1$	$\beta = 2$	$\beta = 3$	$\beta = 4$
$n = 0$	0.7652	0.2239	-0.2601	-0.3971
$n = 1$	0.4401	0.5767	0.3391	-0.066
$n = 2$	0.1149	0.3528	0.4861	0.3641
$n = 3$	0.0196	0.1289	0.3091	0.4302
$n = 4$	0.0025	0.034	0.132	0.2811
$n = 5$		0.007	0.043	0.1321
$n = 6$		0.0012	0.0114	0.0491
$n = 7$			0.0025	0.01518
$n = 8$				0.004

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Trigonometric Identities

$$\cos(a + b) = \cos(a)\cos(b) - \sin(a)\sin(b)$$

$$\cos(a - b) = \cos(a)\cos(b) + \sin(a)\sin(b)$$

$$\sin(a + b) = \sin(a)\cos(b) + \cos(a)\sin(b)$$

$$\sin(a - b) = \sin(a)\cos(b) - \cos(a)\sin(b)$$

$$\cos(a)\cos(b) = \frac{1}{2}[\cos(a - b) + \cos(a + b)]$$

$$\sin(a)\sin(b) = \frac{1}{2}[\cos(a - b) - \cos(a + b)]$$

$$\sin(a)\cos(b) = \frac{1}{2}[\sin(a + b) + \sin(a - b)]$$

$$\cos\left(a + \frac{\pi}{2}\right) = -\sin(a)$$

$$\cos\left(a - \frac{\pi}{2}\right) = \sin(a)$$

$$\sin\left(a + \frac{\pi}{2}\right) = \cos(a)$$

$$\sin\left(a - \frac{\pi}{2}\right) = -\cos(a)$$

Taylor series first order approximation of trigonometric functions

If $a \ll 1$ rad

Then: $\cos(a) \simeq 1$

$$\sin(a) \simeq a$$

Properties of the Bessel Functions of the First Kind

$$J_n(\beta) = \frac{1}{2\pi} \int_{-\pi}^{\pi} \exp(j\beta \sin(\theta) - jn\theta) d\theta$$

$$J_{-n}(\beta) = (-1)^n J_n(\beta)$$