

Area Under Curves and Volume of Revolving a Curve

Problem Statement

Definite Integrals via Numerical Methods

This relates to definite integration via numerical methods.

Consider the algebraic expression given by:

$$(a_1)x^{b_1} + (a_2)x^{b_2} + (a_3)x^{b_3} \dots (a_n)x^{b_n}$$

For the purpose of numerical computation, the area under the curve $y = f(x)$ between the limits a and b can be computed by the [Limit Definition of a Definite Integral](#).

Some background about [areas and volume computation](#).

Using equal Sub-Intervals of length = 0.001, you need to

1. Evaluate the area bounded by a given polynomial function of the kind described above, between given limits L and R .
2. Evaluate the volume of the solid obtained by revolving this polynomial curve around the X-Axis.

A relative error margin of 0.01 will be tolerated.

Input Format

First line will contain N integers separated by spaces, which are the values of $a_1, a_2 \dots a_N$.

Second Line will contain N integers separated by spaces, which are the values of $b_1, b_2 \dots b_N$.

The third Line will contain two space separated integers, L, R , which are the lower and upper limits of the range in which integration needs to be performed.

Constraints

$$-1000 \leq a \leq 1000$$

$$-20 \leq b \leq 20$$

$$1 \leq L < R \leq 20$$

Output Format

The first Line will contain the area between the curve and the x-axis, bound between the specified limits.

The second Line will contain the volume of the solid obtained by rotating the curve around the x-axis, between the specified limits.

Sample Input

```
1 2 3 4 5
6 7 8 9 10
1 4
```

Explanatory Note

The algebraic expression represented by

$$(1)x^6 + (2)x^7 + (3)x^8 + (4)x^9 + (5)x^{10}$$

We need to find the area of the curve enclosed under this curve, between the limits $x=1$ and 4. And, we also need to find the volume of the solid formed by revolving this curve around the x-axis between the limits $x = 1$ and 4.

Sample Output

```
2435300.3
26172951168940.8
```

Scoring

All test cases are weighted equally. You need to clear all the tests in a test case.