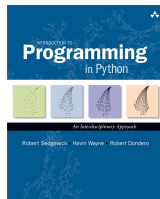


- [Intro to Programming](#)
 - [1. Elements of Programming](#)
 - [1.1 Your First Program](#)
 - [1.2 Built-in Types of Data](#)
 - [1.3 Conditionals and Loops](#)
 - [1.4 Arrays](#)
 - [1.5 Input and Output](#)
 - [1.6 Case Study: PageRank](#)
 - [2. Functions](#)
 - [2.1 Static Methods](#)
 - [2.2 Libraries and Clients](#)
 - [2.3 Recursion](#)
 - [2.4 Case Study: Percolation](#)
 - [3. OOP](#)
 - [3.1 Data Types](#)
 - [3.2 Creating Data Types](#)
 - [3.3 Designing Data Types](#)
 - [3.4 Case Study: N-Body](#)
 - [4. Data Structures](#)
 - [4.1 Performance](#)
 - [4.2 Sorting and Searching](#)
 - [4.3 Stacks and Queues](#)
 - [4.4 Symbol Tables](#)
 - [4.5 Case Study: Small World](#)
- [Intro to CS](#)
 - [0. Prologue](#)
 - [5. A Computing Machine](#)
 - [5.1 Data Representations](#)
 - [5.2 TOY Machine](#)
 - [5.3 TOY Instruction Set](#)
 - [5.4 TOY Programming](#)
 - [5.5 TOY Simulator](#)
 - [6. Building a Computer](#)
 - [6.1 Combinational Circuits](#)
 - [6.2 Sequential Circuits](#)
 - [6.3 Building a TOY](#)
 - [7. Theory of Computation](#)
 - [7.1 Formal Languages](#)
 - [7.2 Regular Expressions](#)

- [7.3 Finite State Automata](#)
- [7.4 Turing Machines](#)
- [7.5 Universality](#)
- [7.6 Computability](#)
- [7.7 Intractability](#)
- [7.8 Cryptography](#)
- [8. Systems](#)
 - [8.1 Library Programming](#)
 - [8.2 Compilers](#)
 - [8.3 Operating Systems](#)
 - [8.4 Networking](#)
 - [8.5 Applications Systems](#)
- [9. Scientific Computation](#)
 - [9.1 Floating Point](#)
 - [9.2 Symbolic Methods](#)
 - [9.3 Numerical Integration](#)
 - [9.4 Differential Equations](#)
 - [9.5 Linear Algebra](#)
 - [9.6 Optimization](#)
 - [9.7 Data Analysis](#)
 - [9.8 Simulation](#)

- Related Booksites



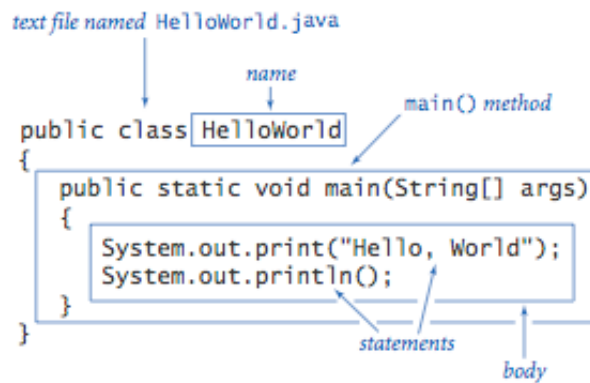
- [Web Resources](#)

- [FAQ](#)
- [Data](#)
- [Code](#)
- [Errata](#)
- [Appendices](#)
 - [A. Operator Precedence](#)
 - [B. Writing Clear Code](#)
 - [C. Gaussian Distribution](#)
 - [D. Java Cheatsheet](#)
 - [E. Matlab](#)
- [Lecture Slides](#)
- [Programming Assignments](#)

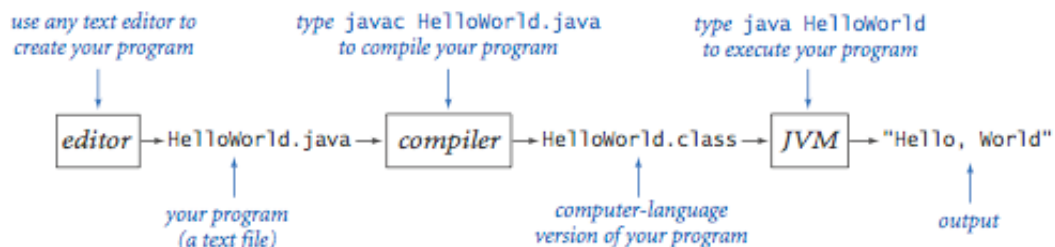
Appendix D: Java Programming Cheatsheet

This appendix summarizes the most commonly-used Java language features in the textbook. Here are the [APIs](#) of the most common libraries.

Hello, World.



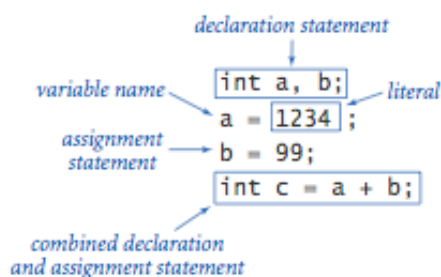
Editing, compiling, and executing.



Built-in data types.

type	set of values	common operators	sample literal values
<code>int</code>	integers	<code>+</code> <code>-</code> <code>*</code> <code>/</code> <code>%</code>	<code>99</code> <code>-12</code> <code>2147483647</code>
<code>double</code>	floating-point numbers	<code>+</code> <code>-</code> <code>*</code> <code>/</code>	<code>3.14</code> <code>-2.5</code> <code>6.022e23</code>
<code>boolean</code>	boolean values	<code>&&</code> <code> </code> <code>!</code>	<code>true</code> <code>false</code>
<code>char</code>	characters		<code>'A'</code> <code>'1'</code> <code>'%'</code> <code>'\n'</code>
<code>String</code>	sequences of characters	<code>+</code>	<code>"AB"</code> <code>Hello</code> <code>"2.5"</code>

Declaration and assignment statements.



Integers.

<i>values</i>	integers between -2^{31} and $+2^{31}-1$				
<i>typical literals</i>	1234 99 -99 0 1000000				
<i>operations</i>	add	subtract	multiply	divide	remainder
<i>operators</i>	+	-	*	/	%

<i>expression</i>	<i>value</i>	<i>comment</i>
5 + 3	8	
5 - 3	2	
5 * 3	15	
5 / 3	1	no fractional part
5 % 3	2	remainder
1 / 0		run-time error
3 * 5 - 2	13	* has precedence
3 + 5 / 2	5	/ has precedence
3 - 5 - 2	-4	left associative
(3 - 5) - 2	-4	better style
3 - (5 - 2)	0	unambiguous

Floating-point numbers.

<i>values</i>	real numbers (specified by IEEE 754 standard)				
<i>typical literals</i>	3.14159	6.022e23	-3.0	2.0	1.4142135623730951
<i>operations</i>	add	subtract	multiply	divide	
<i>operators</i>	+	-	*	/	

<i>expression</i>	<i>value</i>
3.141 + .03	3.171
3.141 - .03	3.111
6.02e23 / 2.0	3.01e23
5.0 / 3.0	1.6666666666666667
10.0 % 3.141	0.577
1.0 / 0.0	Infinity
Math.sqrt(2.0)	1.4142135623730951
Math.sqrt(-1.0)	NaN

Booleans.

<i>values</i>	true or false		
<i>literals</i>	true false		
<i>operations</i>	and	or	not
<i>operators</i>	&&		!

a	!a	a	b	a && b	a b
true	false	false	false	false	false
false	true	false	true	false	true
		true	false	false	true
		true	true	true	true

Comparison operators.

op	meaning	true	false
==	equal	2 == 2	2 == 3
!=	not equal	3 != 2	2 != 2
<	less than	2 < 13	2 < 2
<=	less than or equal	2 <= 2	3 <= 2
>	greater than	13 > 2	2 > 13
>=	greater than or equal	3 >= 2	2 >= 3

non-negative discriminant? `(b*b - 4.0*a*c) >= 0.0`
beginning of a century? `(year % 100) == 0`
legal month? `(month >= 1) && (month <= 12)`

Parsing command-line arguments.

<code>int Integer.parseInt(String s)</code>	<i>convert s to an int value</i>
<code>double Double.parseDouble(String s)</code>	<i>convert s to a double value</i>
<code>long Long.parseLong(String s)</code>	<i>convert s to a long value</i>

Math library.

public class Math

```
double abs(double a)           absolute value of a
double max(double a, double b) maximum of a and b
double min(double a, double b) minimum of a and b
```

Note 1: abs(), max(), and min() are defined also for int, long, and float.

```
double sin(double theta)      sine function
double cos(double theta)      cosine function
double tan(double theta)      tangent function
```

Note 2: Angles are expressed in radians. Use toDegrees() and toRadians() to convert.

Note 3: Use asin(), acos(), and atan() for inverse functions.

```
double exp(double a)          exponential (ea)
double log(double a)          natural log (loge a, or ln a)
double pow(double a, double b) raise a to the bth power (ab)

long round(double a)          round to the nearest integer
double random()               random number in [0, 1)
double sqrt(double a)         square root of a

double E                      value of e (constant)
double PI                     value of π (constant)
```

<i>expression</i>	<i>library</i>	<i>type</i>	<i>value</i>
Integer.parseInt("123")	Integer	int	123
Math.sqrt(5.0*5.0 - 4.0*4.0)	Math	double	3.0
Math.random()	Math	double	<i>random in [0, 1)</i>
Math.round(3.14159)	Math	long	3

The full [java.lang.Math API](http://docs.oracle.com/javase/7/docs/api/java/lang/Math.html).

Type conversion.

<i>expression</i>	<i>expression type</i>	<i>expression value</i>
"1234" + 99	String	"123499"
Integer.parseInt("123")	int	123
(int) 2.71828	int	2
Math.round(2.71828)	long	3
(int) Math.round(2.71828)	int	3
(int) Math.round(3.14159)	int	3
11 * 0.3	double	3.3
(int) 11 * 0.3	double	3.3
11 * (int) 0.3	int	0
(int) (11 * 0.3)	int	3

If and if-else statements.

<i>absolute value</i>	<code>if (x < 0) x = -x;</code>
<i>put x and y into sorted order</i>	<pre> if (x > y) { int t = x; y = x; x = t; } </pre>
<i>maximum of x and y</i>	<pre> if (x > y) max = x; else max = y; </pre>
<i>error check for division operation</i>	<pre> if (den == 0) System.out.println("Division by zero"); else System.out.println("Quotient = " + num/den); </pre>
<i>error check for quadratic formula</i>	<pre> double discriminant = b*b - 4.0*c; if (discriminant < 0.0) { System.out.println("No real roots"); } else { System.out.println((-b + Math.sqrt(discriminant))/2.0); System.out.println((-b - Math.sqrt(discriminant))/2.0); } </pre>

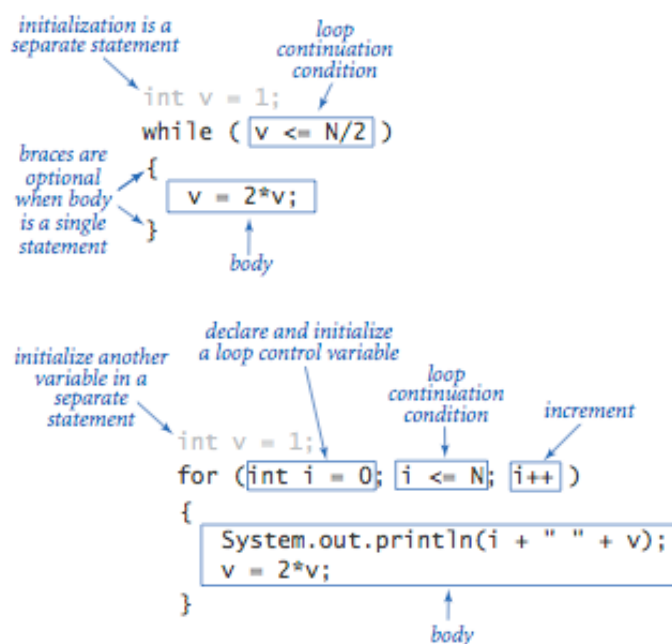
Nested if-else statement.

```

if (income < 0) rate = 0.0;
else if (income < 47450) rate = .22;
else if (income < 114650) rate = .25;
else if (income < 174700) rate = .28;
else if (income < 311950) rate = .33;
else rate = .35;

```

While and for loops.



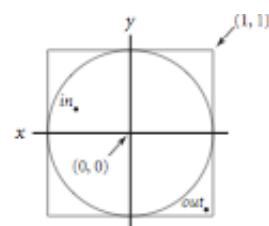
<i>print largest power of two less than or equal to N</i>	<pre>int v = 1; while (v <= N/2) v = 2*v; System.out.println(v);</pre>
<i>compute a finite sum ($1 + 2 + \dots + N$)</i>	<pre>int sum = 0; for (int i = 1; i <= N; i++) sum += i; System.out.println(sum);</pre>
<i>compute a finite product ($N! = 1 \times 2 \times \dots \times N$)</i>	<pre>int product = 1; for (int i = 1; i <= N; i++) product *= i; System.out.println(product);</pre>
<i>print a table of function values</i>	<pre>for (int i = 0; i <= N; i++) System.out.println(i + " " + 2*Math.PI*i/N);</pre>
<i>print the ruler function (see Program 1.2.1)</i>	<pre>String ruler = " "; for (int i = 1; i <= N; i++) ruler = ruler + i + ruler; System.out.println(ruler);</pre>

Break statement.

```
int i;
for (i = 2; i <= N/i; i++)
    if (N % i == 0) break;
if (i > N/i) System.out.println(N + " is prime");
```

Do-while loop.

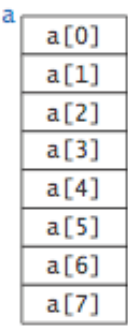
```
do
{
    x = 2.0*Math.random() - 1.0;
    y = 2.0*Math.random() - 1.0;
} while (Math.sqrt(x*x + y*y) > 1.0);
```



Switch statement.

```
switch (day)
{
    case 0: System.out.println("Sun"); break;
    case 1: System.out.println("Mon"); break;
    case 2: System.out.println("Tue"); break;
    case 3: System.out.println("Wed"); break;
    case 4: System.out.println("Thu"); break;
    case 5: System.out.println("Fri"); break;
    case 6: System.out.println("Sat"); break;
}
```


Arrays.



Compile-time initialization.

```
String[] suit = { "Clubs", "Diamonds", "Hearts", "Spades" };

String[] rank =
{
    "2", "3", "4", "5", "6", "7", "8", "9", "10",
    "Jack", "Queen", "King", "Ace"
};
```

Typical array-processing code.

<i>create an array with random values</i>	<pre>double[] a = new double[N]; for (int i = 0; i < N; i++) a[i] = Math.random();</pre>
<i>print the array values, one per line</i>	<pre>for (int i = 0; i < N; i++) System.out.println(a[i]);</pre>
<i>find the maximum of the array values</i>	<pre>double max = Double.NEGATIVE_INFINITY; for (int i = 0; i < N; i++) if (a[i] > max) max = a[i];</pre>
<i>compute the average of the array values</i>	<pre>double sum = 0.0; for (int i = 0; i < N; i++) sum += a[i]; double average = sum / N;</pre>
<i>copy to another array</i>	<pre>double[] b = new double[N]; for (int i = 0; i < N; i++) b[i] = a[i];</pre>
<i>reverse the elements within an array</i>	<pre>for (int i = 0; i < N/2; i++) { double temp = b[i]; b[i] = b[N-1-i]; b[N-i-1] = temp; }</pre>

Two-dimensional arrays.

	99	85	98
row 1 →	98	57	78
	92	77	76
	94	32	11
	99	34	22
	90	46	54
	76	59	88
	92	66	89
	97	71	24
	89	29	38
		column 2	

Compile-time initialization.

```
int[][] a =
{
    { 99, 85, 98, 0 },
    { 98, 57, 78, 0 },
    { 92, 77, 76, 0 },
    { 94, 32, 11, 0 },
    { 99, 34, 22, 0 },
    { 90, 46, 54, 0 },
    { 76, 59, 88, 0 },
    { 92, 66, 89, 0 },
    { 97, 71, 24, 0 },
    { 89, 29, 38, 0 },
    { 0, 0, 0, 0 }
};
```

Ragged arrays.

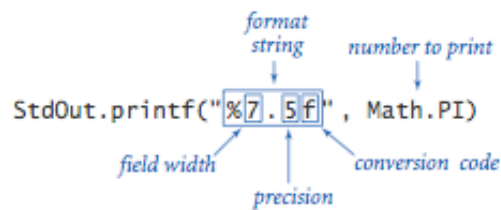
```
for (int i = 0; i < a.length; i++)
{
    for (int j = 0; j < a[i].length; j++)
        System.out.print(a[i][j] + " ");
    System.out.println();
}
```

Our standard output library.

public class StdOut	
void print(String s)	<i>print s</i>
void println(String s)	<i>print s, followed by newline</i>
void println()	<i>print a new line</i>
void printf(String f, ...)	<i>formatted print</i>

API for our library of static methods for standard output

The full [StdOut API](#).



Anatomy of a formatted print statement

type	code	typical literal	sample format strings	converted string values for output
int	d	512	<code>"%14d"</code> <code>"%-14d"</code>	<code>"512"</code> <code>"512"</code>
double	f e	1595.1680010754388	<code>"%14.2f"</code> <code>"%.7f"</code> <code>"%14.4e"</code>	<code>"1595.17"</code> <code>"1595.1680011"</code> <code>"1.5952e+03"</code>
String	s	"Hello, World"	<code>"%14s"</code> <code>"%-14s"</code> <code>"%-14.5s"</code>	<code>" Hello, World"</code> <code>"Hello, World "</code> <code>"Hello "</code>

Our standard input library.

`public class StdIn`

boolean	<code>isEmpty()</code>	<i>true if no more values, false otherwise</i>
int	<code>readInt()</code>	<i>read a value of type int</i>
double	<code>readDouble()</code>	<i>read a value of type double</i>
long	<code>readLong()</code>	<i>read a value of type long</i>
boolean	<code>readBoolean()</code>	<i>read a value of type boolean</i>
char	<code>readChar()</code>	<i>read a value of type char</i>
String	<code>readString()</code>	<i>read a value of type String</i>
String	<code>readLine()</code>	<i>read the rest of the line</i>
String	<code>readAll()</code>	<i>read the rest of the text</i>

API for our library of static methods for standard input

The full [StdIn API](#).

Our standard drawing library.

```
public class StdDraw
```

```

void line(double x0, double y0, double x1, double y1)
void point(double x, double y)
void text(double x, double y, String s)
void circle(double x, double y, double r)
void filledCircle(double x, double y, double r)
void square(double x, double y, double r)
void filledSquare(double x, double y, double r)
void polygon(double[] x, double[] y)
void filledPolygon(double[] x, double[] y)

void setXscale(double x0, double x1)    reset x range to (x0, x1)
void setYscale(double y0, double y1)    reset y range to (y0, y1)
void setPenRadius(double r)             set pen radius to r
void setPenColor(Color c)               set pen color to c
void setFont(Font f)                    set text font to f
void setCanvasSize(int w, int h)        set canvas to w-by-h window
void clear(Color c)                     clear the canvas; color it c
void show(int dt)                       show all; pause dt milliseconds
void save(String filename)              save to a .jpg or w.png file

```

Note: Methods with the same names but no arguments reset to default values.

API for our library of static methods for standard drawing

The full [StdDraw API](#).

Our standard audio library.

```
public class StdAudio
```

```

void play(String file)                  play the given .wav file
void play(double[] a)                   play the given sound wave
void play(double x)                     play sample for 1/44100 second
void save(String file, double[] a)      save to a .wav file
double[] read(String file)              read from a .wav file

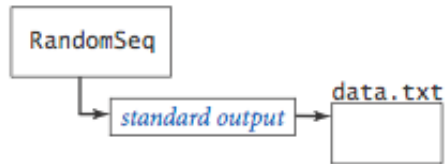
```

API for our library of static methods for standard audio

The full [StdAudio API](#).

Redirection and piping.

```
java RandomSeq 1000 > data.txt
```



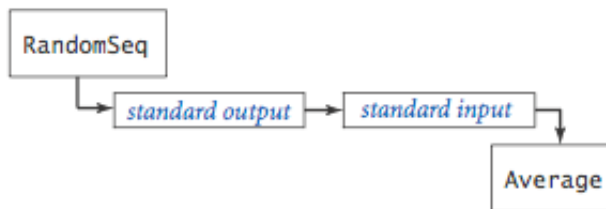
Redirecting standard output to a file

```
java Average < data.txt
```



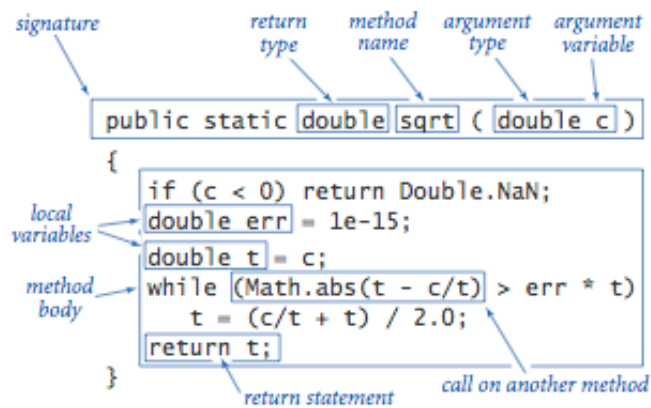
Redirecting from a file to standard input

```
java RandomSeq 1000 | java Average
```



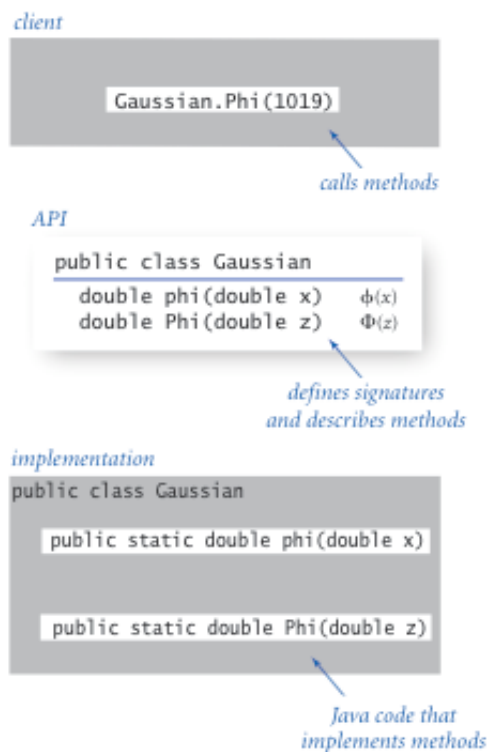
Piping the output of one program to the input of another

Functions.



<i>absolute value of an int value</i>	<pre> public static int abs(int x) { if (x < 0) return -x; else return x; } </pre>
<i>absolute value of a double value</i>	<pre> public static double abs(double x) { if (x < 0.0) return -x; else return x; } </pre>
<i>primality test</i>	<pre> public static boolean isPrime(int N) { if (N < 2) return false; for (int i = 2; i <= N/i; i++) if (N % i == 0) return false; return true; } </pre>
<i>hypotenuse of a right triangle</i>	<pre> public static double hypotenuse(double a, double b) { return Math.sqrt(a*a + b*b); } </pre>
<i>Harmonic number</i>	<pre> public static double H(int N) { double sum = 0.0; for (int i = 1; i <= N; i++) sum += 1.0 / i; return sum; } </pre>
<i>uniform random integer in [0, N)</i>	<pre> public static int uniform(int N) { return (int) (Math.random() * N); } </pre>
<i>draw a triangle</i>	<pre> public static void drawTriangle(double x0, double y0, double x1, double y1, double x2, double y2) { StdDraw.line(x0, y0, x1, y1); StdDraw.line(x1, y1, x2, y2); StdDraw.line(x2, y2, x0, y0); } </pre>

Libraries of functions.



Our standard random library.

<code>public class StdRandom</code>	
<code>int uniform(int N)</code>	<i>integer between 0 and N-1</i>
<code>double uniform(double lo, double hi)</code>	<i>real between lo and hi</i>
<code>boolean bernoulli(double p)</code>	<i>true with probability p</i>
<code>double gaussian()</code>	<i>normal, mean 0, standard deviation 1</i>
<code>double gaussian(double m, double s)</code>	<i>normal, mean m, standard deviation s</i>
<code>int discrete(double[] a)</code>	<i>i with probability a[i]</i>
<code>void shuffle(double[] a)</code>	<i>randomly shuffle the array a[]</i>

Our standard statistics library.

<code>public class StdStats</code>	
<code>double max(double[] a)</code>	<i>largest value</i>
<code>double min(double[] a)</code>	<i>smallest value</i>
<code>double mean(double[] a)</code>	<i>average</i>
<code>double var(double[] a)</code>	<i>sample variance</i>
<code>double stddev(double[] a)</code>	<i>sample standard deviation</i>
<code>double median(double[] a)</code>	<i>median</i>
<code>void plotPoints(double[] a)</code>	<i>plot points at (i, a[i])</i>
<code>void plotLines(double[] a)</code>	<i>plot lines connecting points at (i, a[i])</i>
<code>void plotBars(double[] a)</code>	<i>plot bars to points at (i, a[i])</i>

Using an object.

declare a variable (object name)
invoke a constructor to create an object

```
Charge c1;
```


object name

```
c1 = new Charge(.51, .63, 21.3) ;
```



```
double v = c1.potentialAt(x, y) ;
```


invoke an instance method that operates on the object's value

Creating an object.

Instance variables.

```
public class Charge
{
    private final double rx, ry;
    private final double q;
    .
    .
}
```

instance variable declarations
modifiers
Instance variables

Constructors.

```
public Charge ( double x0 , double y0 , double q0 )
{
    rx = x0;
    ry = y0;
    q = q0;
}
```

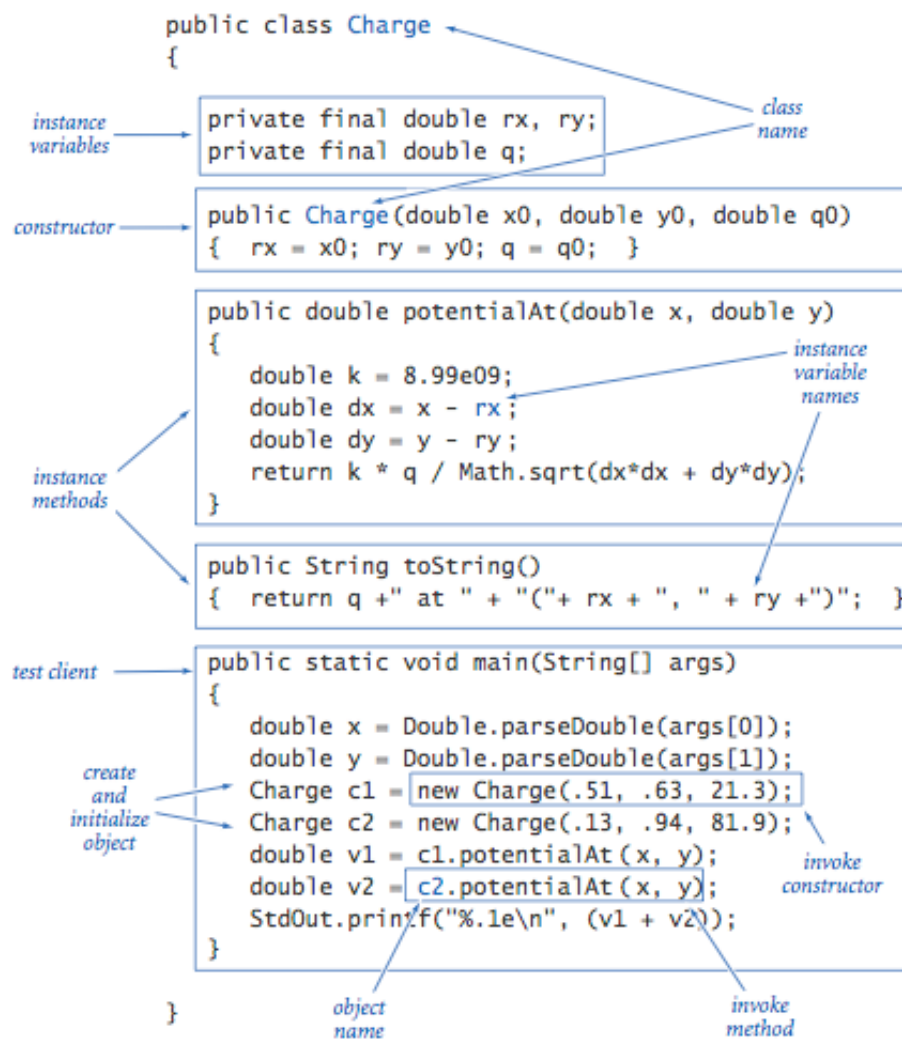
access modifier
no return type
constructor name (same as class name)
argument variables
signature
instance variable names
body
Anatomy of a constructor

Instance methods.

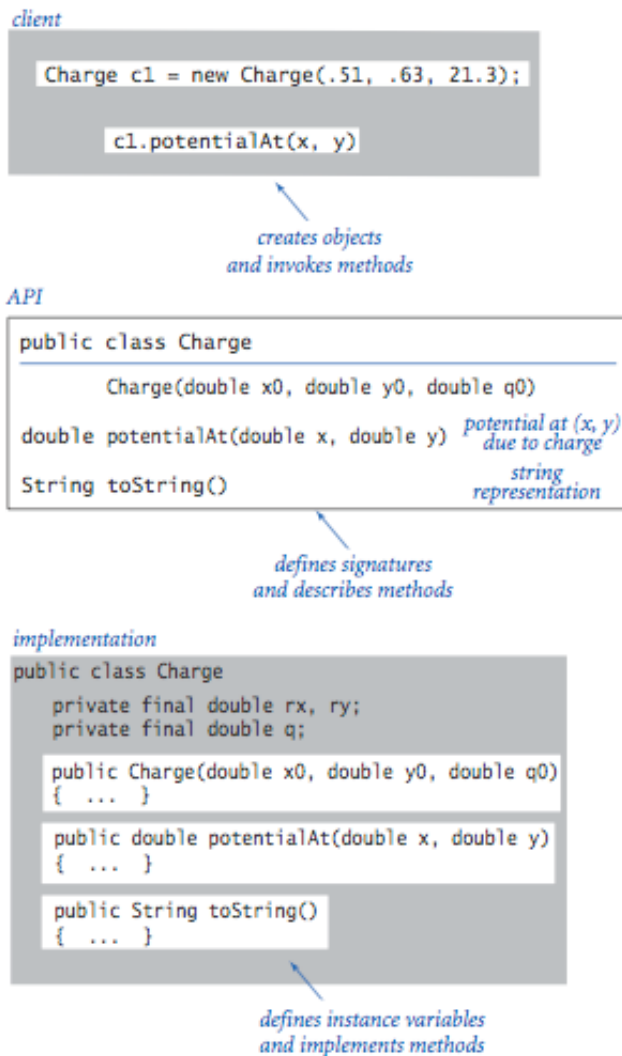
```
public double potentialAt ( double x , double y )
{
    double k = 8.99e09;
    double dx = x - rx;
    double dy = y - ry;
    return k * q / Math.sqrt(dx*dx + dy*dy);
}
```

access modifier
return type
method name
argument variables
signature
local variables
argument variable name
instance variable name
call on a static method
local variable name
Anatomy of an instance method

Classes.



Object-oriented libraries.



Java's String data type.

public class String (Java string data type)

String(String s)	create a string with the same value as s
int length()	string length
char charAt(int i)	i th character
String substring(int i, int j)	i th through (j-1) st characters
boolean contains(String sub)	does string contain sub as a substring?
boolean startsWith(String pre)	does string start with pre?
boolean endsWith(String post)	does string end with post?
int indexOf(String p)	index of first occurrence of p
int indexOf(String p, int i)	index of first occurrence of p after i
String concat(String t)	this string with t appended
int compareTo(String t)	string comparison
String replaceAll(String a, String b)	result of changing a's to b's
String[] split(String delim)	strings between occurrences of delim
boolean equals(String t)	is this string's value the same as t's?

The full [java.lang.String API](http://introcs.cs.princeton.edu/java/11cheatsheet/).

```
String a = "now is ";
String b = "the time ";
String c = "to"
```

<i>call</i>	<i>value</i>
a.length()	7
a.charAt(4)	i
a.substring(2, 5)	"w i"
b.startsWith("the")	true
a.indexOf("is")	4
a.concat(c)	"now is to"
b.replace('t','T')	"The Time "
a.split(" ")[0]	"now"
a.split(" ")[1]	"is"
b.equals(c)	false

Note: the [java.lang.StringBuilder](#) API is similar, but `StringBuilder` supports some operations more efficiently than `String` (notably, string concatenation) and some operations less efficiently (notably, substring extraction).

Java's Color data type.

```
public class java.awt.Color
```

	<code>Color(int r, int g, int b)</code>	
<code>int</code>	<code>getRed()</code>	<i>red intensity</i>
<code>int</code>	<code>getGreen()</code>	<i>green intensity</i>
<code>int</code>	<code>getBlue()</code>	<i>blue intensity</i>
<code>Color</code>	<code>brighter()</code>	<i>brighter version of this color</i>
<code>Color</code>	<code>darker()</code>	<i>darker version of this color</i>
<code>String</code>	<code>toString()</code>	<i>string representation of this color</i>
<code>boolean</code>	<code>equals(Color c)</code>	<i>is this color's value the same as c's?</i>

The full [java.awt.Color API](#).

Our input library.

```
public class In
```

	<code>In()</code>	<i>create an input stream from standard input</i>
	<code>In(String name)</code>	<i>create an input stream from a file or website</i>
<code>boolean</code>	<code>isEmpty()</code>	<i>true if no more input, false otherwise</i>
<code>int</code>	<code>readInt()</code>	<i>read a value of type int</i>
<code>double</code>	<code>readDouble()</code>	<i>read a value of type double</i>
	<code>...</code>	

Note: All operations supported by `StdIn` are also supported for `In` objects.

The full [In API](#).

Our output library.

```
public class Out
```

<code>Out()</code>	<i>create an output stream to standard output</i>
<code>Out(String name)</code>	<i>create an output stream to a file</i>
<code>void print(String s)</code>	<i>print s to the output stream</i>
<code>void println(String s)</code>	<i>print s and a newline to the output stream</i>
<code>void println()</code>	<i>print a newline to the output stream</i>
<code>void printf(String f, ...)</code>	<i>formatted print to the output steam</i>

The full [Out API](#).

Our picture library.

```
public class Picture
```

<code>Picture(String filename)</code>	<i>create a picture from a file</i>
<code>Picture(int w, int h)</code>	<i>create a blank w-by-h picture</i>
<code>int width()</code>	<i>return the width of the picture</i>
<code>int height()</code>	<i>return the height of the picture</i>
<code>Color get(int x, int y)</code>	<i>return the color of pixel (x, y)</i>
<code>void set(int x, int y, Color c)</code>	<i>set the color of pixel (x, y) to c</i>
<code>void show()</code>	<i>display the image in a window</i>
<code>void save(String filename)</code>	<i>save the image to a file</i>

The full [Picture API](#).

Compile-time and run-time errors.

Here's a [list of errors](#) compiled by Mordechai Ben-Ari. It includes a list of common error message and typical mistakes that give rise to them.

Last modified on February 17, 2013.

Copyright © 2002–2012 [Robert Sedgewick](#) and [Kevin Wayne](#). All rights reserved.