1)
$$x = v \cos\theta$$
 $y = u \sin\theta$
 $y = u$

$$\dot{e}_{x} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 10 \end{bmatrix} e_{x} + \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} e_{u}, \text{ where, } e_{x} = X - X_{d}, e_{u} = u - ud$$

$$e_{x} = \begin{bmatrix} X - 10t \\ Y - 2 \\ \theta - 0 \end{bmatrix}, e_{u} = \begin{bmatrix} V - 10 \\ \omega - 0 \end{bmatrix}$$

using pole placement techique we find the desired K (gain) which places the poles in a stable LHS of the imaginary axis. K is calculated as *K=[5000,200,300;1000,200,300] Also, by using the reachability matrix we see that the system is trul rank and controllable.

$$\begin{aligned} & \text{Fank} \left(\left[\overrightarrow{B} \right] AB \right) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 10 \\ 0 & 1 & 0 & 0 \end{bmatrix} \\ & \text{vank} = 3 \\ & u = -k e_{x} + u_{d} - xu = -\begin{bmatrix} 5000 & 200 & 300 \\ 1000 & 200 & 300 \end{bmatrix} \begin{bmatrix} x - x_{d} \\ y - y_{d} \\ \theta - \theta_{d} \end{bmatrix} + \begin{bmatrix} v_{d} \\ \omega_{d} \end{bmatrix} \\ & u = \begin{bmatrix} V \\ U \end{bmatrix} = \begin{bmatrix} u_{1} \\ u_{2} \end{bmatrix}$$

$$\begin{aligned} u &= \begin{bmatrix} V \\ U \end{bmatrix} = \begin{bmatrix} u_{1} \\ u_{2} \end{bmatrix} \\ & u = -\begin{bmatrix} 5000(x - 10t) + 200(y - 2) + 300(\theta) \\ 1000(x - 10t) + 200(y - 2) + 300(\theta) \end{bmatrix} + \begin{bmatrix} 10 \\ 0 \end{bmatrix}$$

$$\end{aligned}$$

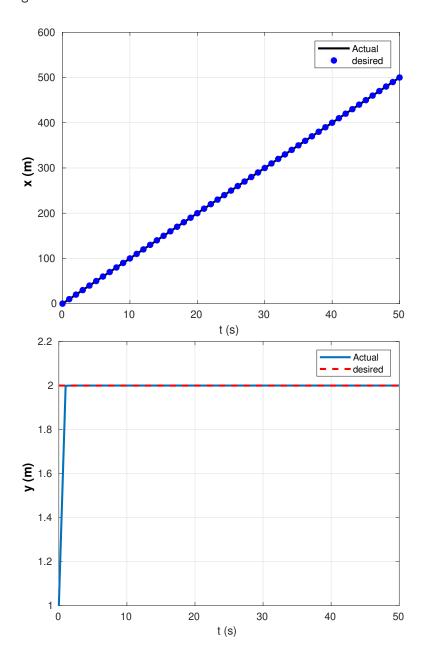
$$\begin{aligned} &\text{Feedback} \end{aligned}$$

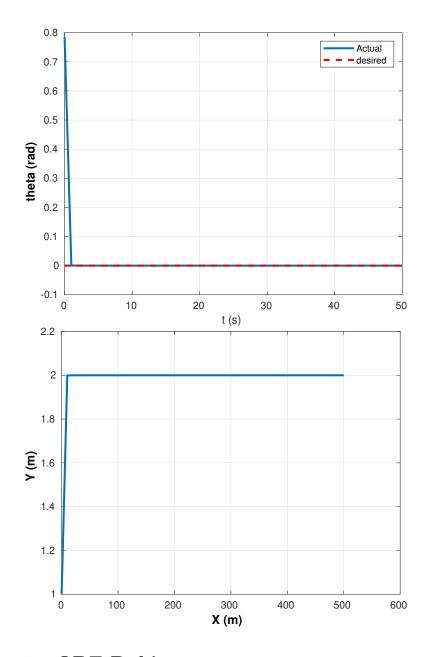
$$\end{aligned}$$

Farid Tavakkolmoghaddam HW4

```
%Steering control
clear; close all; clc
T=50;
x0 =[0;1;pi/4]; % Feel free to change the initial state and sampling horizon.
% design steering control to follow a straight lane while maintaining a given velocity
% the lateral position yr= 2;
%TODO: param is the additional parameter to pass to the ode function.
[T,X] = ode45(@(t,x) ode_dubins(t,x), (0:T), x0);
tt=0:1:50;
XX=10*tt; % desired trajectory x
YY=2*ones(1,51); % desired trajectory y
thetta=2*zeros(1,51); % desired trajectory y
% plot your state trajectories for both 1 and 2, using the following code or else.
figure
title(' X position vs. time')
plot(T,X(:,1),'k',tt,XX,'b*','LineWidth',2);
xlabel('t (s)');
ylabel('x (m)','FontSize',12,'FontWeight','bold','Color','k');
legend('Actual','desired')
grid
figure
title(' Y position vs. time')
plot(T,X(:,2),tt,YY,'r--','LineWidth',2);
xlabel('t (s)');
ylabel('y (m)','FontSize',12,'FontWeight','bold','Color','k');
legend('Actual','desired')
grid
figure
title(' Orientation vs. time')
plot(T,X(:,3),tt,thetta,'r--','LineWidth',2);
xlabel('t (s)');
ylabel('theta (rad)','FontSize',12,'FontWeight','bold','Color','k');
legend('Actual','desired')
grid
```

```
figure ('name','X v.s y')
title(' x vs. y')
plot(X(:,1), X(:,2),'LineWidth',2)
xlabel('X (m)','FontSize',12,'FontWeight','bold','Color','k');
ylabel('Y (m)','FontSize',12,'FontWeight','bold','Color','k');
grid
```





1 ODE Dubins

article graphicx color

Contents

 $\bullet\,$ TODO: Here is the code for control input.

- the controller needs to provide control input: linear velocity and
- steering angle: v, delta

```
function dz = ode_dubins(t,z)
% use z for [x,y,theta]
dz =zeros(3,1);
```

TODO: Here is the code for control input.

the controller needs to provide control input: linear velocity and

steering angle: v, delta

```
% step 1: calculate the value of deviation variables given the
\% desired state and input and the actual state, exacted from z.
v_d = 10;
w_d = 0;
u_d = [v_d ; w_d];
y_d = 2;
theta_d = 0;
v_r = 10;
x_d = [v_r*t; y_d ; theta_d];
e_x = z - x_d;
% de_x = dx - dx_d;
% step 2: based on the feedback controller, calculate the e_u=
% [e_v, e_w].
k=[5000 200 300;
    1000 200 300];
e_u = -k*e_x;
% step 3: based on the relation between u and e_u, derive the
% desired input v, and w.
% e_u = u - u_d; --> u = e_u + u_d
u = -k*e_x + u_d;
v = u(1);
w = u(2);
theta= z(3);
dz(1) = v*cos(theta);
dz(2) = v*sin(theta);
dz(3) = w;
```

```
Not enough input arguments.
```

```
Error in ode_dubins (line 18)
x_d = [v_r*t; y_d ;theta_d];
```

end