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10

11 **Contributors:**

- 12 Adalberto C. Farias, UFPE
- 13 Alexandre C. Mota, UFPE
- 14 André Didier, UFPE
- 15 Jim Woodcock, UK

16 **Editors:**

- 17 Alexandre C. Mota, UFPE

18 **Reviewers:**

- 19 Luis Couto, AU
- 20 Richard Payne, NCL
- 21 Ken Pierce, NCL
- 22 Adrian Larkham, Atego

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1 Introduction

Model checking [CGP99] is an automatic technique aiming to verify whether the relation $M \models f$ holds, where M is a model (in general some kind of Labelled Transition System, like a Kripke structure) of some formal language L and f is a temporal logic formula. The process algebra CSP [Ros10] has introduced another way of performing model checking, named refinement checking. The idea is to verify that the refinement relation $M_f \sqsubseteq M$ (M refines M_f) holds, where both M and M_f are models of a same language and M_f is the most non-deterministic model known to satisfy f .

Traditionally, a model checker is a tool that implements search procedures derived from the relation $M \models f$ (or from a refinement theory). These search procedures and representations of M and f are very specialized algorithms and data structures aiming at achieving the best space and time complexities possible. Because of this, it is not common to find model checkers for rich-state space languages (that use elaborate data structures). The best performing model checkers use very primitive data structures like natural numbers and arrays, and avoid sets, sequences, functions, etc.

This way of developing model checkers creates a gap between theory and practice, particularly for rich state languages that are more appropriate to model and reason about systems of systems. One of the problems is related to the guarantee of creating the right model M from the semantics (usually the Structured Operational Semantics, or simply SOS) of the language L . Another is whether the search procedure to check $M \models f$ (or $M_f \sqsubseteq M$) is correct. Finally, this restricts the kinds of formal languages that can have their own model checkers.

CML is the COMPASS Modelling Language, the first language specifically designed for modelling and analysing Systems of Systems (SoS). It is based on the following baseline languages: VDM [ABH⁺95], CSP [Ros10], and Circus [WC02]. It is fully described in deliverables D23.2 (syntax) and D23.3 (semantics). CML has a rich and heterogeneous semantics in the sense of combining several different paradigms with a rich state space. Developing a correct model checker for such a language is daunting. Thus instead of focusing on the best space and time complexities when creating such a model checker, we need first to focus on the most abstract and elegant implementation infra-structure to create a correct model checker for CML. This is the main goal of this deliverable.

The very recent technology developed by Microsoft Research, known as FORMULA [JSD⁺09] (Formal Modelling Using Logic Programming and Analysis), seems to be an appropriate candidate to provide the right abstraction and elegance

91 to implement a model checker able to handle the heterogeneity and rich-state fea-
92 tures exhibited by CML. It is based on the Constraint Programming Paradigm [RvBW06]
93 and Satisfiability Modulo Theory (SMT) solving provided by Z3 [DMB08].

94 The purpose of this deliverable is to present how a model checker for CML that
95 conforms to its SOS was created, and how a feasibility study was performed to
96 test the ability of FORMULA to capture and analyse CML specifications using
97 the COMPASS CML tool.

98 As our model checker is provided through the COMPASS CML tool, we start this
99 deliverable in Section 2 by presenting a user guide towards this tool (reusing some
100 basic context of the COMPASS CML tool [CMLC13]). We cover installation pro-
101 cedures and requirements, usage of the tool and some illustrative examples.

102 After the practical aspect of our contribution, we present the more theoretical
103 contribution. As CML can be seen as a combination between a behavioural (CSP
104 language) and state-based (VDM language) parts, we consider the effort to create
105 a CSP model checker based on the FORMULA technology in Section 3. In this
106 section we give a brief introduction to FORMULA, present the SOS of CSP (this
107 is just to show how close is the description in FORMULA from its pure theoretical
108 SOS counterpart), present details about CSP refinement checking and finally the
109 model checker script written in FORMULA.

110 A CML model checker is the logical following step and it is considered in Sec-
111 tion 4. We show how to incorporate the state-aspect of VDM to the previous
112 considered behavioural-aspect of CSP. To this end, we present and discuss about
113 the types supported by FORMULA and how the VDM Mathematical toolkit is
114 supported. Some state-aspects are directly supported while others are interpreted.
115 For those that are interpreted, we provide a FORMULA solution to a subset of
116 them. The CML model checker has been implemented as an Eclipse plugin whose
117 architecture and implementation are detailed in Section 5.

118 In Section 6 we discuss about the advantages and disadvantages to create a model
119 checker for CML using the FORMULA framework and other alternatives.

120 This deliverable ends by presenting some related work in Section 7, and conclu-
121 sions and future work in Section 8.

122 Complementary material, concerning the formal semantics of FORMULA and the
123 relationship between first-order logic formulations of deadlock, livelock, nonde-
124 terminism and traces refinement analyses and FORMULA rules and queries, can
125 be found in Appendices A and B, respectively. In Appendix C we present some
126 key examples and the quantitative part of our feasibility study.

2 User Guide

This section provides essential information for the users of the CML model checker. Before using the model checker we suggest reading the main documentation about the entire COMPASS IDE tool [CMLC13]. This is useful to make the user familiar with the resources provided by the IDE as well as to understand basic activities like creating CML projects, editing files, compilation errors and type checking errors, for example, as they have to be performed prior to the model checking itself.

2.1 Installation

The CML model checker is developed over the Microsoft FORMULA (Formal Modelling Using Logic Analysis) tool and GraphViz. The first is used as the main engine to analyse CML specifications whereas the second is used to build the counterexample found by the analysis.

The steps to install and put the CML model checker to work are listed as follows:

1. Download and install the Microsoft FORMULA tool. It is available at <http://research.microsoft.com/en-us/um/redmond/projects/formula/>. Although the tool is free, it requires the Microsoft Visual Studio¹ installed. This makes the current version of the CML model checker platform dependent as the underlying framework is from Microsoft.
2. Download and install the GraphViz software. Graphviz is open source graph visualization software. It allows one to write several kinds of graphs (in a text file) and generate graphical output in several formats to be presented. GraphViz is available at <http://www.graphviz.org/> and can be installed in several platforms. The CML model checker uses specifically the `dot.exe` program, which provides compilation from a textual description to several formats. We use the SVG format that is vectorial and accepted by most of Web browsers.
3. Download and install the COMPASS IDE tool. The COMPASS tool containing all features is available at <http://build.compass-research.eu/builds/compass-devel/>. We recommend to use the latest release of the tool.

¹<http://www.microsoft.com/visualstudio>.

2.2 Using the CML model checker

This section introduces the CML model checker. We show how to invoke its functionalities and which components are available to the user.

The model checker functionalities are available through the CML Model Checker perspective (see Figure 1), or MC perspective, which is composed by the CML Explorer (1), the CML Editor (2), the Outline view (3), the internal Web browser (to show the counterexample when invoked) and two further specific views: the CML MC List view (4) to show the overall result of the analysis and the MC Progress view (5) to show the execution progress of the analysis.

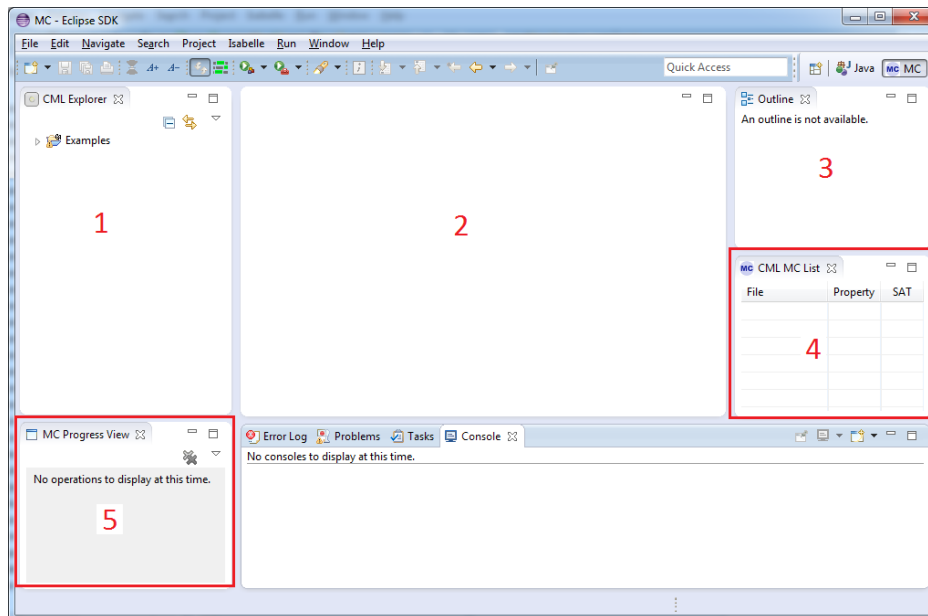


Figure 1: CML Model Checker Perspective

At startup, the CML model checker plugin checks (by using the PATH environment variable of your system) if the installation of FORMULA and GraphViz are working properly. For each problem found at startup, the COMPASS tool shows a warning as illustrated in Figure 2.

The analysis of a CML file is invoked through the context menu when the CML or the MC perspective are active (see Figure 3).

Select the CML file to be analysed. Then, Right click -> Model check -> Property to be checked. The analysis is performed and the information is shown in different views. The MC list view shows a ✓ or an X as result

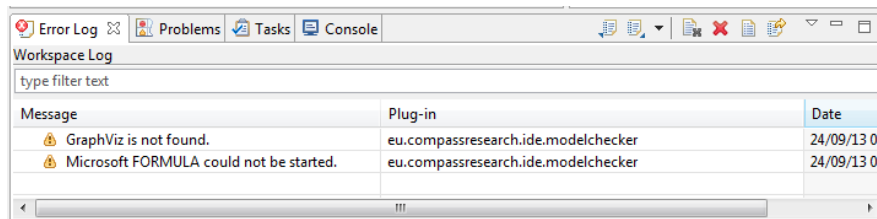


Figure 2: Warning about auxiliary software at startup

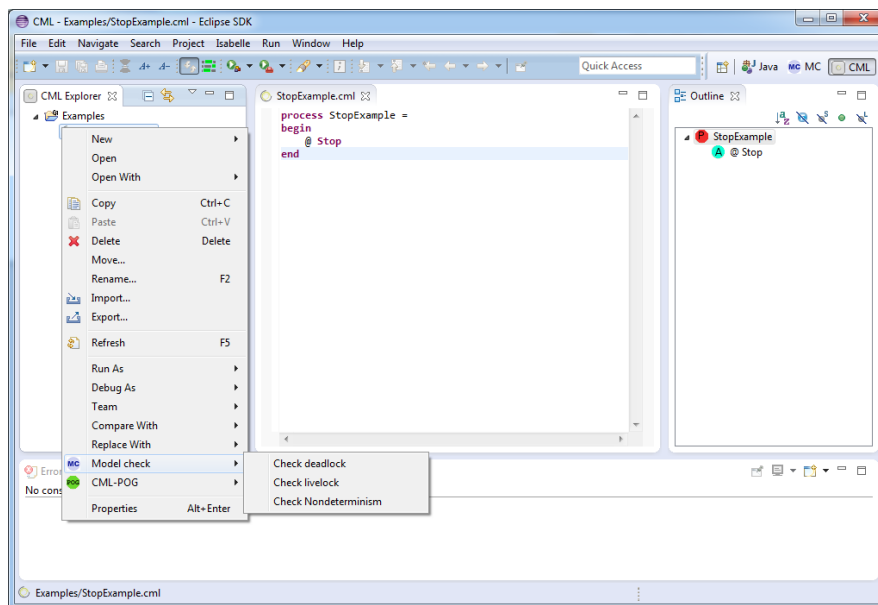


Figure 3: The Model Checker Context Menu

177 of the overall analysis (meaning satisfiable or unsatisfiable, respectively). More-
 178 over, if the model is satisfiable, the trace validating the property can be viewed by
 179 a double click in the item of the MC list view.

180 It is worth noting that if FORMULA (or GraphViz) is not available and the user
 181 requires its use, the COMPASS tool shows appropriate messages like in Fig-
 182 ure 4.

183 The model checker analysis uses an auxiliary folder (`generated\modelchecker`)
 184 to originate the FORMULA file (with extension `.4ml`). This file is loaded in the
 185 FORMULA tool to be analysed. Based on the result, the model checker plugin
 186 generates a GraphViz file (with extension `.gv`), compiles it (using `dot.exe`) to
 187 a graph file (with extension `.svg`) and shows it in the internal browser of Eclipse.
 188 All these steps are performed automatically.

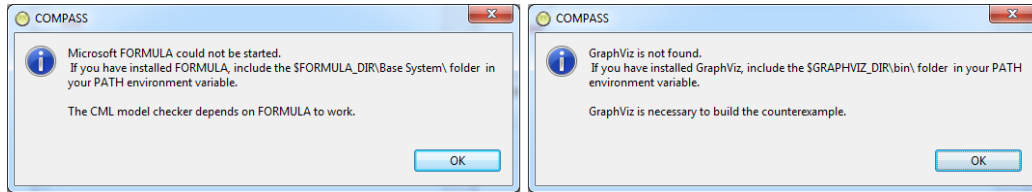


Figure 4: Messages when auxiliary software are not installed but are invoked

189 The initial state of the graph is double circled; intermediate states are simply cir-
 190 cled; and the deadlocked state (or other special states related to properties ver-
 191 ification) has a different colour (a red tone). Each state has a number and an
 192 information (hint) about the bindings (from variables to values), the name of the
 193 owner process, and the current context (process fragment). To see the internal
 194 information of each state just put the cursor over the state number.

195 Similarly, transitions are labelled with the corresponding event and also have a
 196 hint showing the source and the target states. This feature is useful to provide
 197 information about which rule (of the structured operational semantics) was ap-
 198 plied.

199 The internal graph builder of the model checker considers the shortest path that
 200 makes the analysed file satisfiable. Thus, although there might be other counterex-
 201 amples, it shows the shortest one.

202 2.2.1 Supported Constructs

203 Currently, the model checker is able to analyse CML files containing the fol-
 204 lowing constructs: channel declarations, action declarations, action (Skip, Stop,
 205 Chaos, Div, communication, guarded, sequential composition, external choice, in-
 206 ternal choice), replicated action (sequential composition, external choice, internal
 207 choice), type declaration, operators ($<$, $<=$, $>$, $>=$, $=$) in guards involving con-
 208 stant values, variable declaration (in actions) and assignment over it, state declara-
 209 tion (used only in action paragraph), operation declarations (without no qualifiers
 210 neither frames), process declaration, generalised parallelism. The use of auxiliary
 211 actions (with local variables) is also possible.

212 2.3 Examples

213 This section presents some examples of CML specifications and their analysis
 214 using the model checker. The examples are available in the COMPASS SVN

215 repository. We recommend that you download and try them. The following figures
 216 are intuitive and show the analysis result for some examples.

217 Immediate Deadlock

218 The CML file `action-stop.cml` is the most simple deadlock process. Fig-
 219 ures 5 and 6 show the result of its analysis and the corresponding graph. It is
 220 worth noting that the generated files can be viewed by refreshing the project (as
 221 illustrated in the CML explorer in Figure 6). The user can see the content of all
 222 files (`.4ml`, `.gv` and `.svg`) as they are text files.

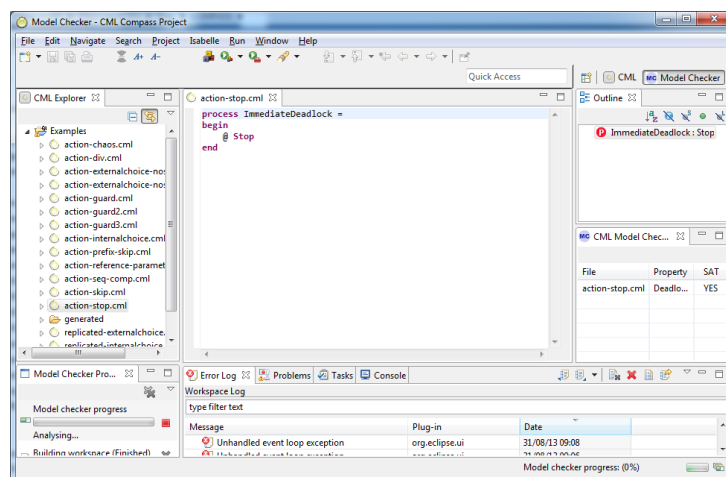


Figure 5: An immediate deadlock example

223 When the analysed file is unsatisfiable, and the user tries to see the graph, the
 224 model checker plugin returns a message indicating that the graph is available only
 225 for satisfiable models (Figure 7).

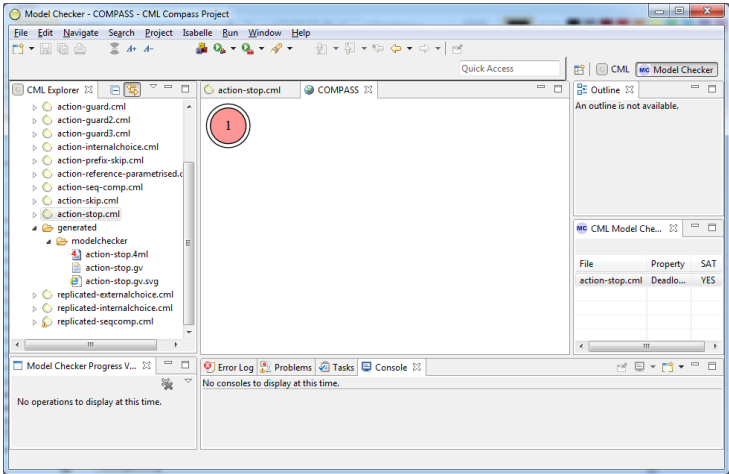


Figure 6: An immediate deadlock example

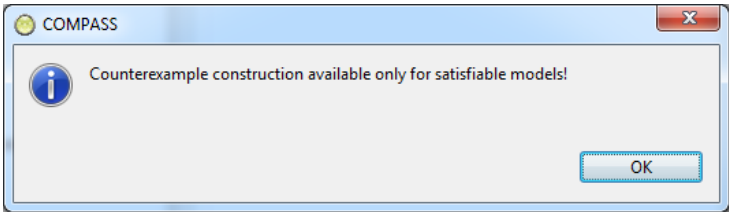


Figure 7: Message when the graph is not available

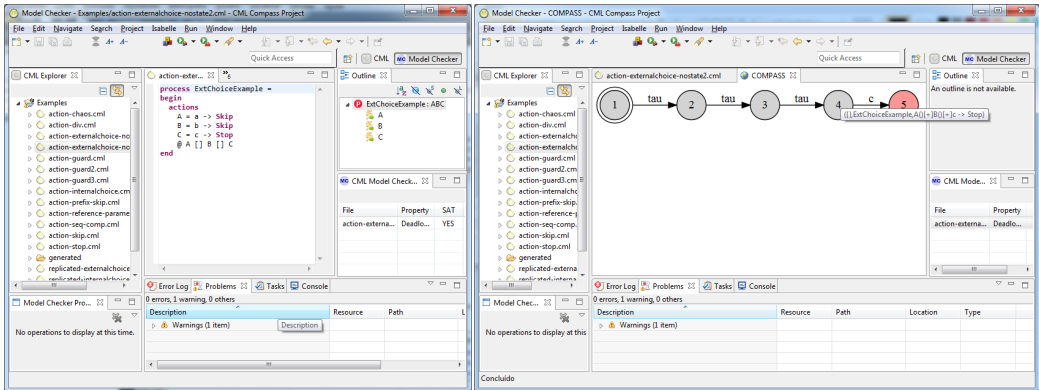


Figure 8: An external choice example

226 3 CSP embedding in FORMULA

227 This section provides information about the underlying infrastructure used by the
228 CML model checker. We first introduce the FORMULA tool and its language to
229 clarify such a framework and its constructs. Then we present the encoding of CML
230 in the language of FORMULA. We start by showing the embedding for CSP and
231 then evolve such a representation by including data manipulation to contemplate
232 VDM constructs.

233 3.1 FORMULA Framework

234 The Microsoft FORMULA (Formal Modelling Using Logic Programming and
235 Analysis) tool encompasses several facets to provide a framework to (abstractly)
236 reason about models and analysis:

- 237 1. A modern formal specification language that follows the principles of model-
238 based development (MBD). The language of FORMULA is based on alge-
239 braic data types (ADTs) and strongly-typed constraint logic programming
240 (CLP). It supports concise specifications of abstractions (in a Prolog-like
241 style) and model transformations.
- 242 2. Use of SMT (Satisfiability Modulo Theories) solving. The automatic inte-
243 gration with the Z3 SMT solver is useful to make automatic analysis and
244 instantiations inside FORMULA. This brings the advantage of providing
245 model finding and design space exploration facilities, in which FORMULA
246 can be used to construct system models satisfying complex domain con-
247 straints.

248 The main elements of a FORMULA specification are:

- 249 • *Domains*: used to create abstractions of real-world problems in a way very
250 similar to Prolog (with facts, rules, and queries);
- 251 • *Facts*: n -ary relations or constructors ($n \geq 1$), completely instantiated.
252 They can be primitive or not. Only primitive facts can be used within (par-
253 tial) models (given as initial facts). On the other hand, primitive facts cannot
254 be used as head of rules because they cannot be derived from other facts;
- 255 • *Rules*: they have the same role as in Prolog, except that rules cannot leave
256 unbounded the elements used in the head. A FORMULA rule has the format
257 LHS :- RHS, where the left-hand side (LHS) is the head and the right-hand
258 side (RHS) is the body of the rule (a list of facts used to derive the LHS). For

every element X used in the LHS, we must have some constructor $\text{Cons}(X)$ in the RHS to constrain the possible values of X ; FORMULA can only build the head from the elements of the body (bottom-up approach);

- *Queries*: quantifier-free formulae in terms of constructors of the language. The special query `conforms` combines other queries using logical operators and is used as the main goal to validate a model in a domain. When a (partial) model is inspected in FORMULA, the `conforms` clause is the starting point of the searching procedure. If it is not possible to find an instance that satisfies this special query, the (partial) model is said to be Unsatisfiable;
- *(Partial) models*: these are possible instances of domains. The main distinction between models and partial models are that models are closed instances and partial models are open (to be closed/instantiated by the solver) instances.

Although domains have similar elements like Prolog programs, they work differently. Prolog uses rules as starting points of the searching procedure and stops at facts (a top-down approach), whereas FORMULA uses (primitive) facts as starting points to create new facts (a bottom-up approach). Figure 9 illustrates the work performed by FORMULA in an analysis. It takes the main goal (`conforms` clause) and the facts given in a (partial) model as starting point. From the (initial) base of facts and the RHS of domain rules, FORMULA tries to generate other facts (according to the LHS of domain rules). If the new base of facts satisfies the main goal, the model is SAT (satisfiable). Otherwise, FORMULA keeps generating new facts again until the base of facts stops increasing (a bottom-up fixed point based search). At the end of this iterative generation, if the goal cannot be satisfied, the model is UNSAT (unsatisfiable). Furthermore, if any SMT-solving activity (instantiation, evaluation, etc.) is required, FORMULA invokes Z3 automatically.

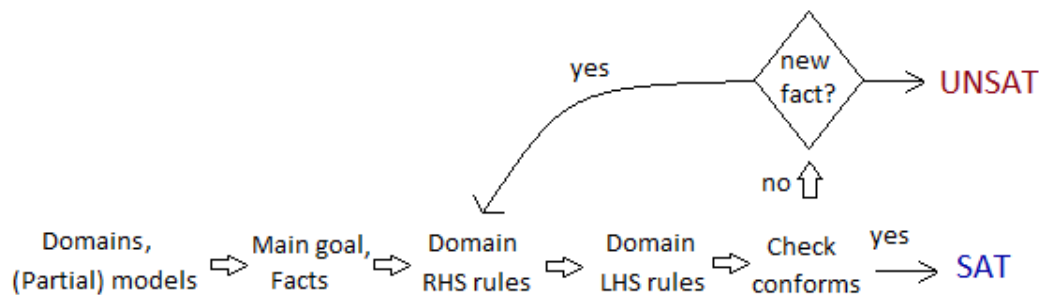


Figure 9: Iterative analysis of FORMULA

When open facts are used in partial models, they activate the symbolic execution algorithm inside FORMULA that creates symbolic derived facts (head of rules). If a rule (head) is bound only by previous derived facts, this can create an infinite loop in the symbolic execution algorithm of FORMULA and making the search diverges. Therefore it is advised to have at least one primitive fact in the body of a rule to avoid infinite application of such a rule. This creates a bounded analysis similar to what is done in bounded model checking [BCCZ99, AMP09]. Therefore our CML model checker can have infinite predicates and communications but not infinite states. That is, we aim at creating finite symbolic labelled transition systems as we will see later in Section 3.4.

3.1.1 A simple example

We illustrate the work of FORMULA using an example that captures the essence of a basic digraph (see Figure 10).

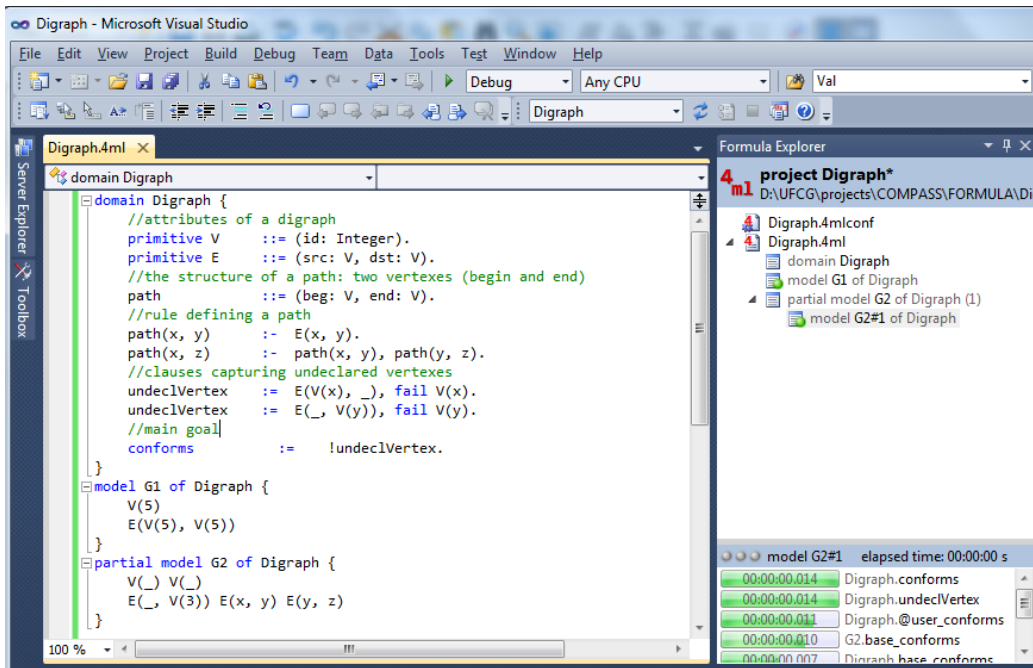


Figure 10: FORMULA snapshot model analysis

A digraph is modelled as a domain containing a set of vertexes (V) and a set of edges (E). The qualifier `primitive` indicates that vertexes and edges cannot be generated during the analysis (however their values can be instantiated). The rule `path` links vertexes where there is a single edge or several edges. By using the definition

of path, FORMULA is able to find a path between two vertexes (if it exists) by building paths between intermediate vertexes. The query `undeclVertex` establishes constraints upon the domain; it captures undeclared vertexes by checking if the first ($E(V(x), _)$) or the second ($E(_, V(y))$) components of edges have not been declared as vertexes (`fail(V(x))` and `fail(V(y))`, respectively). Finally, the `conforms` query defines the main goal: a valid graph cannot have undeclared vertexes.

We use two models to check instances of the domain `Digraph`. The model `G1` defines a digraph with one vertex (`V(5)`) and a self-edge. As it has no undeclared vertexes, FORMULA detects its conformance with the `Digraph` domain (satisfiable). Concerning the partial model `G2`, there are three edges and two vertexes (some are left undetermined). These elements play the role of parameters to be instantiated by FORMULA to make `G2` satisfiable. In this case, FORMULA found the instances `V(3)` and `V(-103701)` and used `V(3)` to validate the edge with the first vertex undetermined ($E(V(3), V(3))$). The value `-103701` is arbitrary and was generated only because there are two given vertexes in `G2`. If we remove one vertex, only `V(3)` is used. In this sense, FORMULA works as a symbolic executor, expanding its base of facts as much as necessary. This fits well the purposes of LTS generation.

3.2 Structured Operational Semantics of CSP

Although there are three formal semantics for CSP (algebraic, operational and denotational), we focus on the operational semantics [Ros10] as it is closer to the purpose of automatic verification via model checking: it defines the behaviour of a process as a labelled transition system (LTS). Formally, an LTS is a tuple $(S, S_0, T, \Sigma^{\check, \tau})$, where S is a set of states, S_0 is an initial state ($S_0 \in S$), T is a transition relation over $S \times \Sigma^{\check, \tau} \times S$, and $\Sigma^{\check, \tau}$ is the set of all possible events; visible events are represented by Σ and the special events \check and τ are used to semantically represent successful termination and internal actions, respectively. The representation $\Sigma^{\check, \tau}$ stands for $\Sigma \cup \{\check, \tau\}$.

According to [Plo81], the structured (or structural) operational semantics (SOS) of a language is an operational method of specifying semantics based on syntactic transformations and simple operations on discrete data. The occurrence of such operations is associated to elementary steps (firing rules) and recorded as transitions (or moves). This means that the LTS corresponding to a specification (or program) P written in a language L can be generated by applying the firing rules of L on each syntactic fragments (BNF) of P . A firing rule has the format:

$$\frac{\text{premises}}{\text{conclusion}}, (\text{conditions})$$

340 In the above format, the *conclusion* is mandatory. The rest is optional and depends
 341 on the language constructors involved as well as the kind of semantics the designer
 342 is intending to give. When premises are absent, the rule is said to be an *axiom*. A
 343 generic example of a firing rule is given as follows.

$$344 \quad \frac{p_1^1 \longrightarrow p_1', \dots, p_n \longrightarrow p_n'}{Op(p_1, \dots, p_n) \longrightarrow Op(p_1', \dots, p_n')}, C(p_1, \dots, p_n)$$

345 where $Op(p_1, \dots, p_n)$ and $Op(p_1', \dots, p_n')$ are constructors of the language follow-
 346 ing its BNF, and p_1, \dots, p_n are its operands. The predicate $C(p_1, \dots, p_n)$ states
 347 the conditions under which such a rule can be applied beyond the premises. That
 348 is, the premises act as a pattern condition and $C(p_1, \dots, p_n)$ as a boolean and more
 349 general condition. Moreover, it can be the case of certain fragments of a language
 350 does not have an associated firing rule (as it is the case of CSP).

351 The embedding of CSP has been designed in such a way that it directly follows its
 352 structured operational semantics (SOS). This leads to a very intuitive way of cre-
 353 ating semantics-preserving model checkers. This is very important in our context
 354 because CML is intended to be a heterogeneous language integrating behaviour,
 355 state, time, mobility, probability, etc.

356 The language CSP is based on the notion of processes and (communication) events.
 357 A process is an independent self-contained entity with particular interfaces through
 358 which it interacts with its environment (the context outside the process). An event
 359 describes a particular kind of atomic and indivisible action that can be performed
 360 by the process. The set of all events a process can perform is known as the alpha-
 361 bet of the process. Our current embedding of CSP in FORMULA considers the
 362 most common constructs of CSP given by the following syntax:

$Proc ::=$	$Stop$	(Deadlock)
	$ Skip$	(Successful termination)
	$ a \rightarrow Proc$	(Prefix)
	$ Proc \sqcap Proc$	(Internal choice)
	$ Proc \square Proc$	(External choice)
	$ Proc \triangleleft g \triangleright Proc$	(Conditional choice)
363	$ g \& Proc$	(Boolean guard)
	$ Proc \parallel_x Proc$	(Generalised parallelism)
	$ Proc \setminus X$	(Hiding)
	$ Proc Proc$	(Interleaving)
	$ Proc; Proc$	(Sequential composition)
	$ \mu Y \bullet F(Y)$	(Recursion)
	$ ProcCall$	(Process call)

364 The primitive processes *Stop* and *Skip* denote, respectively, immediate deadlock
 365 (as a broken system) and successful termination (it does nothing besides terminat-
 366 ing); while *Stop* communicates no event, whereas *Skip* communicates a special
 367 event \checkmark (tick) before terminating. The *prefix* process $a \rightarrow P$ offers the event a
 368 to its environment, and after its occurrence, it behaves as P . When values may
 369 be exchanged between processes, we use the constructs $c!exp$ (to send the value
 370 corresponding to expression exp) and $c?x$ (to receive a value and store it in the
 371 variable x) in place of the event a . The *internal choice* $P \sqcap Q$ behaves as P
 372 or Q , but the choice is arbitrary (an internal and nondeterministic decision). The
 373 *external choice* $P \square Q$ behaves as P or Q where the choice is made by the en-
 374 vironment (that is, the context outside P and Q decides which of P or Q should
 375 evolve). The *conditional choice* $P \triangleleft g \triangleright Q$ denotes a process that behaves as
 376 P if the condition guard g is true, or as Q otherwise. The *guarded choice* $g \& P$
 377 is equivalent to $P \triangleleft g \triangleright Stop$. The process $P \parallel_x Q$ stands for the *generalised*
 378 *parallel composition* of the processes P and Q with synchronisation set X . This
 379 states that the processes P and Q must progress together for events that belong to
 380 X (that is, they must engage on the same events). On the other hand, for events
 381 outside X , if these events are different each process can evolve independently;
 382 otherwise, just one of them evolves (after a nondeterministic choice). The process
 383 $P ||| Q$ establishes an *interleaved* execution where P and Q are executed inde-
 384 pendently; this construct is similar to a parallelism with empty synchronisation
 385 set (that is, $P || Q$). The sequential composition $P; Q$ represents a process that
 386 behaves as P until P terminates successfully, and then the composition behaves
 387 as Q . The process $\mu Y \bullet F(Y)$ represents a recursive process where F is any
 388 CSP term involving Y . When Y occurs we replace it by $\mu Y.F(Y)$ again (un-

fold). Finally, the *ProcCall* construct denotes any process call possibly involving parameters.

The semantic rules of CSP follow the Plotkin's style [Plo81] and are presented by the firing rules of Figure 11. The special state Ω is a semantic element that represents a state with no outgoing transition (a final state). It corresponds to the behaviour of *Stop* (a deadlock process performs no action at all and, therefore, has no associated transition). The process *Skip* can perform a single action \checkmark , after which it does nothing more; this corresponds to a \checkmark -transition leading to Ω (rule *termination*).

The transition rule for the prefix operator is represented by rule *prefix*; it states that an initially accepted event a (where $a \in A$) is performed and the following behaviour is determined by replacing the occurrences of x by a in the process P , where the event a possibly involves data communication. The internal choice can originate two transitions where the process decides (by an internal action) to behave as one of its parts. The special event τ represents such a decision.

The external choice operator has two main situations that originate several transitions. If there is a possible internal progress in any constituent process (the premises of the external choice τ rule), the external choice also evolves by performing an internal action. Otherwise, the external choice evolves by behaving as one of its constituent parts (stated in the premises of the external choice Σ rule). The conditional and the guarded choices have no explicit transition rules because they are rewritten to one of the other cases. The behaviour of $P \langle g \rangle Q$ is defined by P or Q ; this decision is determined by evaluating the boolean guard g and, hence, does not originate a specific transition. The behaviour of $g \& P$ is similar to $P \langle g \rangle \text{Stop}$ and has no transition for evaluating the guard g .

The generalised parallelism has different situations for originating transitions. If any constituent process can evolve by an internal action, the parallelism also does so accordingly (the *parallelism* τ rule). When the constituent parts want to perform different events that do not belong to the synchronisation set, they evolve asynchronously and the parallelism can progress by evolving both of its constituent parts independently (the *async-parallelism* rule). On the other hand, if both constituent processes offer the same event (from the synchronisation set), then there is a synchronous progress (the *sync-parallelism* rule). Finally, if one process in the parallelism terminates the entire combination waits for the other process terminate as well. And only if both terminate, the entire combination performs a \checkmark -action and leads to the final state Ω (the *dist-term-parallelism* rule). Note that a deadlock might occur if one process terminates and the other wants to synchronise with it.

$$\begin{array}{c}
\frac{}{\overline{Skip} \xrightarrow{\checkmark} \Omega} \quad (\text{termination}) \\
\\
\frac{}{\overline{x:A \rightarrow P(x)} \xrightarrow{a} P[a/x]} \quad (a \in A) \quad (\text{prefix}) \\
\\
\frac{}{\overline{P \sqcap Q} \xrightarrow{\tau} P} \quad \frac{}{\overline{P \sqcap Q} \xrightarrow{\tau} Q} \quad (\text{internal choice}) \\
\\
\frac{P \xrightarrow{\tau} P'}{\overline{P \sqcap Q} \xrightarrow{\tau} P' \sqcap Q} \quad \frac{Q \xrightarrow{\tau} Q'}{\overline{P \sqcap Q} \xrightarrow{\tau} P \sqcap Q'} \quad (\text{external choice } \tau) \\
\\
\frac{P \xrightarrow{a} P'}{\overline{P \sqcap Q} \xrightarrow{a} P'} \quad (a \neq \tau) \quad \frac{Q \xrightarrow{a} Q'}{\overline{P \sqcap Q} \xrightarrow{a} Q'} \quad (a \neq \tau) \quad (\text{external choice } \Sigma) \\
\\
\frac{P \xrightarrow{\tau} P'}{\overline{P \parallel_X Q} \xrightarrow{\tau} P' \parallel_X Q} \quad \frac{Q \xrightarrow{\tau} Q'}{\overline{P \parallel_X Q} \xrightarrow{\tau} P \parallel_X Q'} \quad (\text{parallelism } \tau) \\
\\
\frac{P \xrightarrow{a} P'}{\overline{P \parallel_X Q} \xrightarrow{a} P' \parallel_X Q} \quad (a \in \Sigma \setminus X) \quad \frac{Q \xrightarrow{a} Q'}{\overline{P \parallel_X Q} \xrightarrow{a} P \parallel_X Q'} \quad (a \in \Sigma \setminus X) \quad (\text{async-parallelism}) \\
\\
\frac{P \xrightarrow{a} P' \quad Q \xrightarrow{a} Q'}{\overline{P \parallel_X Q} \xrightarrow{a} P' \parallel_X Q'} \quad (a \in X) \quad (\text{sync-parallelism}) \\
\\
\frac{P \xrightarrow{\checkmark} P'}{\overline{P \parallel_X Q} \xrightarrow{\tau} \Omega \parallel_X Q} \quad \frac{Q \xrightarrow{\checkmark} Q'}{\overline{P \parallel_X Q} \xrightarrow{\tau} P \parallel_X \Omega} \quad \frac{}{\overline{\Omega \parallel_X \Omega} \xrightarrow{\checkmark} \Omega} \quad (\text{dist-term-parallelism}) \\
\\
\frac{P \xrightarrow{a} P'}{\overline{P \setminus A} \xrightarrow{\tau} P' \setminus A} \quad (a \in A) \quad \frac{P \xrightarrow{a} P'}{\overline{P \setminus A} \xrightarrow{a} P' \setminus A} \quad (a \notin A) \quad (\text{hiding}) \\
\\
\frac{P \xrightarrow{\checkmark} P'}{\overline{P \setminus A} \xrightarrow{\checkmark} \Omega} \quad (\text{hiding } \checkmark) \\
\\
\frac{P \xrightarrow{a} P'}{P;Q \xrightarrow{a} P';Q} \quad (a \neq \checkmark) \quad \frac{P \xrightarrow{\checkmark} P'}{P;Q \xrightarrow{\tau} Q} \quad (\text{sequential composition}) \\
\\
\frac{}{\overline{\mu Y \bullet F(Y)} \xrightarrow{\tau} F[(\mu Y \bullet F(Y))/Y]} \quad (\text{recursion})
\end{array}$$

Figure 11: Firing rules for CSP

427 The transitions of the hiding $P \setminus A$ are the same transitions of P with a subtle
 428 change: for all events from A , the event is hidden and originates a τ -transition
 429 (the *hiding* rule). Furthermore, independently of the performed event, the set of
 430 events to be hidden is propagated to the following behaviour. In the case where
 431 the process terminates the hiding also does so (the *hiding* \checkmark rule). The interleave
 432 operator has no firing rule because it is equivalent to a parallelism with an empty
 433 synchronisation set.

434 The *sequential composition* rule states that if the first process terminates success-
 435 fully, the composition behaves as the second process; otherwise, only the first
 436 process evolves in the composition. The usual unfold of a recursion is represented
 437 by a τ -transition where the bounded variable is replaced in the original expres-
 438 sion by the entire recursive definition again. The transition for a process call is
 439 not necessary as it simply corresponds to the execution of any (already) defined
 440 rule.

441 3.3 CSP Refinement Checking

442 Model checking is an automatic technique to investigate whether a property f is
 443 valid in a given model M , or simply $M \models f$. In general, the model M describes
 444 the behavior of some concurrent language L and the property f is written using
 445 some fragment of temporal logic (TL). It is normally implemented as a black box
 446 containing very optimised algorithms (in terms of space and time) that traverse the
 447 model M (a graph). Nevertheless, this satisfaction relation can also be checked
 448 via refinement, which is the focus of this work. That is, one can use another model
 449 M_f (the model M_f is known—or built in such a way—to satisfy the property f
 450 in the most nondeterministic possible way) as a way of checking that the model
 451 M satisfy a property f ; in this case, it is formally represented as $M_f \sqsubseteq M$. This
 452 is the strategy used in CSP, where both models (M_f and M) can be compared
 453 with respect to three main models: traces (\mathcal{T}), failures (\mathcal{F}) or failures-divergences
 454 (\mathcal{FD}). These models are defined by the denotational semantics of CSP. However,
 455 due to the congruence between the operational and the denotational semantics²,
 456 we can also check CSP refinements by using the operational semantics.

457 We focus on traces refinement to simplify our presentation and because it is
 458 the simplest denotational model that allows us to check the properties we im-
 459 plemented in this work. The extension of our model checker to deal with the
 460 standard failures-divergences requires a more elaborate embedding of properties

²This congruence for CSP models is stated in [Ros10]. However, the work reported in [HJ98] shows how one can obtain such a congruence in general.

(FORMULA queries) to capture failures and divergences of the generated LTS, but it is feasible and achievable from the infra-structure we create for traces analysis. In particular, we will see later that with the current infra-structure we already perform deadlock (this requires the stable failures semantics of CSP in the FDR model checker) and livelock (this requires the stable failures-divergences semantics in FDR) analyses because all complementary information can be inferred from the traces.

Concerning the traces model, for each fragment of the CSP language it is defined the traces it can produce by using the function $traces: Process \rightarrow (\Sigma^{\check{\cdot}, \tau})$ from the denotational semantics of CSP. Some examples of traces calculation are listed as follows.

- $traces(STOP) = \{\langle \rangle\};$
- $traces(SKIP) = \{\langle \rangle, \langle \surd \rangle\};$
- $traces(a \rightarrow P) = \{\langle \rangle\} \cup \{\langle a \rangle \frown s \mid a \in A \wedge s \in traces(P)\};$
- $traces(a?x \rightarrow P) = \{\langle \rangle\} \cup \{\langle a.v \rangle \frown s \mid v \in T_a \wedge s \in traces(P[v/x])\};$
- $traces(P \sqcap Q) = traces(P) \cup traces(Q);$
- $traces(P \sqcup Q) = traces(P) \cup traces(Q);$
- $traces(P \setminus A) = \{s \setminus A \mid s \in traces(P)\};$

The function $traces$ provides the set of histories (or performed actions) a process can exhibit. Based on it, the refinement relation for the traces model ($\sqsubseteq_{\mathcal{T}}$) is easily defined:

$$P \sqsubseteq_{\mathcal{T}} Q \equiv traces(Q) \subseteq traces(P)$$

According to the definition of traces refinement, a process Q traces refines another process P whether Q produces at least the same traces as P . This can also be captured by comparing the executions of P and Q , according to their operational semantics. We use this strategy in our work. That is, instead of creating sets of sequences of events as in the traces function, we walk through the event-annotated transitions in a somewhat similar way like the model checker FDR.

3.4 Capturing CSP SOS in FORMULA

Work on model checking assumes that M is given and focuses on formally describing what $M \models f$ means, or how to check f by traversing M . For languages whose syntax are closer to an LTS, such as LTSA [MK99] or Petri Nets [Mur89],

the model M is easily achievable and (usually) is correct. Nevertheless, for languages such as CSP [Ros10], PROMELA [GM99] and Circus [WCF05], creating a model checker by a direct programming approach can be too error-prone, as the model M can be wrong and the tool concentrates on analysing it assuming the SOS of L . In particular our first effort towards creating a Circus model checker aimed at using Perfect Developer [Cro03]. however, the results were restrict and very difficult to maintain. This was expected because this approach is still programmatic, although Perfect Developer has formal development support.

In practice, most model checkers create M from L using some black-box implementation susceptible to programming errors. However, if the model M is systematically created from the SOS of L (that is, $M \in SOS\{L\}$) the model checker becomes a semantics-preserving model checker for L relative to the semantics of the framework used to encode the SOS of L .

In this section we show how to systematically capture the firing rules of the CSP SOS in FORMULA so that the LTS is directly derived from a conceptual (and formal) model similar to Leuschel [Leu01] and Verdejo [VMO02]. This systematic capture can be automated. The representation proposed by Corradini [CHM00] is an abstract and intuitive description for structured operational semantics. As long as it works as a Domain Specific Language (DSL), our strategy can be adapted to derive a FORMULA script (the model checker) from a SOS description.

The semantics of a complex language might have several aspects, such as, for example, data aspects and control (or concurrency). The ideal situation to guarantee full correctness about a possible encoding of a language semantics into a programming framework is a one-to-one mapping from each syntactic fragment of the language to its meaning (or interpretation) using the constructors of the programming framework. This is called a deep semantics embedding.

Sometimes, however, the semantics of part of the source language is close to the one available in the framework. This is frequently the case of data aspects, where the framework already provides the means to deal with arithmetic expressions, known data types (natural, integer, real numbers and strings), sets, relations, sequences, and so on. When a language semantics is captured in this way, we say that such a semantics was a shallow embedding in the programming framework.

3.4.1 Basic Shallow Embedding in FORMULA

We propose a way to capture the structured operational semantics of CSP using a so-called hybrid semantics embedding in which behavioural aspects are captured

in a deep embedding way and data aspects are not interpreted as much as possible (For those that we cannot find a direct mapping we follow a deep embedding as well. This is used for supporting for sets, sequences, and mappings of VDM in FORMULA). They are simply mapped to the available elements, yielding a shallow embedding. Although FORMULA provides basic data types (Integer, Natural, Real, String), more complex types (like sets, relations, functions, sequences, bags, etc.) are absent and the mapping is not so direct. The domain `ShallowEmbedding` shows the mappings for basic types and for sequence type.

```

538 domain ShallowEmbedding {
539   // Types
540   primitive UNDEF    ::= {undef}.    //a default value for all types
541   primitive Int      ::= (Integer).   //integers
542   primitive Nat      ::= (Natural).   //naturals
543   primitive Str      ::= (String).    //strings
544   primitive IR       ::= (Real).      //reals
545   primitive Seq      ::= (SeqDef).    //sequence
546   EmptySeq          ::= {empty}.
547   primitive SeqCont  ::= (head:Types,tail:SeqDef).
548   SeqDef            ::= EmptySeq + SeqCont.
549   Types             ::= Int + Nat + IR + Str + Seq.
550   aSeq              ::= (SeqRest).
551
552   // Some relational operators
553   primitive EQ       ::= (x:Types,y:Types). //equal
554   primitive NEQ      ::= (x:Types,y:Types). //not equal
555   primitive LT       ::= (x:Types,y:Types). //less than
556   primitive GT       ::= (x:Types,y:Types). //greater than
557   bExps              ::= EQ + NEQ + LT + GT.
558 }

```

The most basic types—integer (`Int`), natural (`Nat`), real (`IR`) and string (`Str`)—are directly mapped to their corresponding types in FORMULA. The type `UNDEF` is defined to provide a default value for variables declared but not initialised with a specific value of its type. The sequence type (`Seq`) is defined by another constructor (`SeqDef`) that is the union of two types (inductively defining a sequence). The constructor `EmptySeq` defines an empty sequence and `SeqCont` defines a non-empty sequence as a tuple containing a head and a tail. Finally, all types are defined by the union of the basic types and `Seq`. The (derived) constructor `aSeq` is used just to provide a way of generating sequences during the analysis.

Each relational operation (`EQ`, `NEQ`, `LT`, `GT`) is intuitively modelled as a pair containing the operands. At the end, the constructor `bExps` uses union of types to capture all possible relational expressions to be used in our encoding.

571 User Defined Types in FORMULA

572 The support of FORMULA for type union allows one to extend type definitions in
573 a quite flexible way. For example, the following CSP datatype definition

574 *datatype ANSWER = OK|ERROR*
575 *nametype POINT = Int.Int*

576 is captured in FORMULA as follows

```
577 domain ShallowEmbedding {
578   // Types
579   primitive Int      ::= (Integer). //integers
580   primitive Nat      ::= (Natural). //naturals
581   primitive Str      ::= (String).  //strings
582   primitive IR       ::= (Real).    //reals
583   primitive Seq      ::= (SeqDef).   //sequence
584   EmptySeq          ::= {empty}.
585   primitive SeqCont  ::= (head:Types,tail:SeqDef).
586   SeqDef            ::= EmptySeq + SeqCont.
587
588   //Defining the new types
589   primitive ANSWER ::= {OK,ERROR}
590   primitive POINT  ::= (Integer,Integer).
591
592   //Extending the pre-defined types
593   Types            ::= Int + Nat + IR + Str + Seq + ANSWER + POINT.
594 }
```

595 Both types are represented by primitive constructs (as all pre-defined types also
596 are). However, types defined by using explicit values are captured by sets of values
597 in FORMULA, whereas types defined by combining existing types with the CSP
598 “.” type operator³ are represented as tuples.

599 After representing each new type individually, the union of all types is adjusted
600 to include the new types. This makes them available in the general scope of the
601 FORMULA script.

602 3.4.2 CSP Syntax in FORMULA

603 The CSP SOS is captured as in the real scenario: the syntax and semantics are
604 described in two separated domains: syntax and semantics. The former defines
605 the structures (building blocks) necessary to represent CSP constructs for events
606 and processes, according to its BNF grammar given in Section 3.2.

```
607 domain CSP_Syntax includes ShallowEmbedding {
608   SpecialEvents      ::= {tick,tau}.
609   primitive BasicEv  ::= (name:String).
```

³This operator means cartesian product or tuple construction.

```

610 primitive CommEv      ::= (name:String,data:Types) .
611 Sigma                 ::= BasicEv + CommEv.
612 SigmaTickTau          ::= Sigma + SpecialEvents.
613 BasicProcess          ::= {Stop,Skip}.
614 primitive Prefix      ::= (ev:Sigma,proc:CSPPProcess) .
615 primitive iChoice     ::= (lProc:CSPPProcess,rProc:CSPPProcess) .
616 primitive eChoice     ::= (lProc:CSPPProcess,rProc:CSPPProcess) .
617 primitive bChoice     ::= (cond:bExps,lProc:CSPPProcess,rProc:CSPPProcess) .
618 primitive seqC        ::= (lProc:CSPPProcess,rProc:CSPPProcess) .
619 primitive hide        ::= (proc:CSPPProcess,hideS:String) .
620 primitive par         ::= (lProc:CSPPProcess,SyncS:String,rProc:CSPPProcess) .
621 NoPar                 ::= {nopar}.
622 SPar                  ::= (Types) .
623 DPar                  ::= (p1:Types,p2: Types) .
624 Param                 ::= NoPar + SPar + DPar.
625 primitive proc        ::= (name : String, p: Param) .
626 CSPPProcess           ::= BasicProcess + Prefix + iChoice + eChoice +
627                        bChoice + seqC + hide + par + proc.
628 }

```

Events are represented by different constructs. The special events \checkmark and τ are represented by the element `SpecialEvents`. The visible events (from Σ) are classified as basic events (`BasicEv` does not have communication values) and communication events (`CommEv` involves communication values); the union of these types defines the entire set `Sigma`. The element representing $\Sigma^{\checkmark,\tau}$ (`SigmaTickTau`) is obtained by the union of `Sigma` and `SpecialEvents`.

The representation of processes starts by the primitive processes *Stop* and *Skip*. They are captured by the element `BasicProcess`. The `Prefix` is represented as a pair of an event (from `Sigma`) and a next behaviour (a process). Internal and external choices are respectively represented by the constructors `iChoice` and `eChoice`; each of them is composed by a left and a right processes. The conditional choice constructor (`bChoice`), on the other hand, has three components: a boolean condition, a process defining the behaviour if the condition is valid and another process defining the behaviour if the condition is invalid. The constructor for sequential composition (`seqC`) is defined as a pair containing the first and the second processes. The hiding (`hide`) is represented by a constructor containing a process and a set of events to be hidden (represented as a string). This is a design decision used to avoid interpretation of set operations in FORMULA; the necessary information over sets (membership, inclusion, etc.) is given as initial facts to improve the performance of FORMULA. We discuss more about this in Section 3.4.3.

The parameters are defined by a construct representing no parameters (`NoPar` contains only the element `nopar`), one parameter (`SPar` can be of any type previously defined) or two parameters (`DPar` is a pair). The type `Param` is just a union of those types. A process call is represented by a constructor (`proc`) that contains a process name and its parameters. Finally, the constructor `CSPPProcess` defines

655 (syntactically) all possible processes.

656 3.4.3 Deep Embedding of CSP SOS in FORMULA

657 Concerning the deep embedding, where the behavioural aspects are completely
658 interpreted in FORMULA, we use an approach similar to those in the litera-
659 ture [Leu01, VMO02]: one-to-one mapping for each firing rule. Before showing
660 these mappings we start by addressing the underlying LTS structure: states, events
661 and transitions.

```
662 | domain CSP_Syntax includes ShallowEmbedding {  
663 |   State ::= (p:CSPProcess).  
664 |   trans ::= (source:State, event:SigmaTickTau, target:State).  
665 | }
```

666 The constructor `State` captures any possible state (or context) of a CSP process
667 during its execution directly from the syntax domain. A transition is intuitively
668 captured by the constructor `trans` as a triple containing a `source` state, an
669 event (captured as presented in the previous section) as label and a `target`
670 state. Note that these constructors are derived because these elements will be gen-
671 erated during the LTS construction. This LTS construction is the main bottleneck
672 of our CML model checker. As FORMULA is interpreted and to build the LTS
673 we have to interpret several rules iteratively, this takes a considerable amount of
674 time. We point out this as a future extension of this work by deriving an opti-
675 mised implementation from the FORMULA script using Python or Haskell, for
676 example.

677 Now we start by showing the representation of each firing rule for CSP in terms
678 of FORMULA transitions and states.

679 **No Transition** In some languages, there are terminal symbols in the sense of
680 their definitions do not involve the creation of transitions, but just states with no
681 outgoing transitions. In CSP, for instance, Ω and *STOP* represent a same state
682 meaning deadlock, from where there is no progress. We represent this state in
683 FORMULA by `State(Stop)`

684 **Dynamic Creation of States** The existence of a transition between states re-
685 quires the existence of the source state and causes the (dynamic) creation of the
686 target state (the initial state of a new transition). This is achieved by the gen-
687 eral rule `State(nS) :- trans(State(iS), ev, State(nS))`. This

rule is important to provide a way of creating an entire path (sequence of transitions).

Skip Recall from Figure 11 the firing rule for *Skip*:

$$\overline{Skip \xrightarrow{\checkmark} \Omega}$$

Its translation into FORMULA is quite intuitive as *Skip* performs \checkmark event and leads the system to Ω . We just replace the source and the target states with their respective representations to obtain a \checkmark -transition as follows.

```
trans(State(Skip), tick, State(Stop)) :- State(Skip).
```

Prefix The prefix has the following firing rule:

$$\overline{x : A \rightarrow P(x) \xrightarrow{a} P[a/x]} (a \in A)$$

Its representation in FORMULA is also intuitive as it simply creates a transition labelled with an event to the next behaviour (state):

```
trans(State(Prefix(a,P)), a, State(P)) :- State(Prefix(a,P)).
```

Internal choice The firing rules for the internal choice originate two transitions

$$\overline{P \sqcap Q \xrightarrow{\tau} P} \quad \overline{P \sqcap Q \xrightarrow{\tau} Q}$$

Their translation originates the following elements in FORMULA:

```
//It creates following states
State(P) :- State(iChoice(P,Q)).
State(Q) :- State(iChoice(P,Q))

//It creates the corresponding transitions
trans(State(iChoice(P,Q)), tau, State(P)) :- State(iChoice(P,Q)).
trans(State(iChoice(P,Q)), tau, State(Q)) :- State(iChoice(P,Q)).
```

The existence of an internal choice needs to create the following states and their corresponding transitions.

711 **External choice** The external choice rules with internal progress are given by:

$$\frac{P \xrightarrow{\tau} P'}{P \sqcap Q \xrightarrow{\tau} P' \sqcap Q} \quad \frac{Q \xrightarrow{\tau} Q'}{P \sqcap Q \xrightarrow{\tau} P \sqcap Q'}$$

712 Their representations in FORMULA are given as follows:

```

713 //It creates states for the constituent parts
714 State(P) :- State(eChoice(P,Q)).
715 State(Q) :- State(eChoice(P,Q))
716
717 trans(State(eChoice(P,Q)),tau,State(eChoice(P_,Q))) :-
718     State(eChoice(P,Q)),trans(State(P),tau,State(P_)).
719 trans(State(eChoice(P,Q)),tau,State(eChoice(P,Q_))) :-
720     State(eChoice(P,Q)),trans(State(Q),tau,State(Q_)).

```

721 Similarly to the previous operator, we also need to create the constituent states
722 for external choice. Note that the premises are added to the right-hand side of the
723 corresponding FORMULA code as they are necessary to generate the transition.
724 The firing rules with antecedent and conditions over the events are given by

$$\frac{P \xrightarrow{a} P'}{P \sqcap Q \xrightarrow{a} P'} (a \neq \tau) \quad \frac{Q \xrightarrow{a} Q'}{P \sqcap Q \xrightarrow{a} Q'} (a \neq \tau)$$

725 Their translations produce rules containing the premises and the conditions in the
726 right-hand side.

```

727 trans(State(eChoice(P,Q)),ev,State(P_)) :-
728     State(eChoice(P,Q)),trans(State(P),ev,State(P_)),ev!=tau.
729 trans(State(eChoice(P,Q)),ev,State(Q_)) :-
730     State(eChoice(P,Q)),trans(State(Q),ev,State(Q_)),ev!=tau.

```

731 **Parallelism** The firing rules for parallelism with internal progress are given
732 by:

$$\frac{P \xrightarrow{\tau} P'}{P \parallel_X Q \xrightarrow{\tau} P' \parallel_X Q} \quad \frac{Q \xrightarrow{\tau} Q'}{P \parallel_X Q \xrightarrow{\tau} P \parallel_X Q'}$$

733 They are translated into

```

734 // Required by the premises.
735 State(P) :- State(par(P, X, Q)).
736 State(Q) :- State(par(P, X, Q)).
737
738 trans(State(par(P, X, Q)), tau, State(par(P_, X, Q))) :-
739   trans(State(P), tau, State(P_)), State(par(P, X, Q)).
740 trans(State(par(P, X, Q)), tau, State(par(P, X, Q_))) :-
741   trans(State(Q), tau, State(Q_)), State(par(P, X, Q)).

```

742 The rules of asynchronous parallelism are given by

$$\frac{P \xrightarrow{a} P'}{P \parallel_X Q \xrightarrow{a} P' \parallel_X Q} (a \in \Sigma \setminus X) \quad \frac{Q \xrightarrow{a} Q'}{P \parallel_X Q \xrightarrow{a} P \parallel_X Q'} (a \in \Sigma \setminus X)$$

743 Note that both have a membership condition to activate the rule. In FORMULA,
 744 we avoid this membership interpretation and use FORMULA's base of facts it-
 745 self as a set. Thus we define a special constructor `lieIn(..., ...)` that
 746 characterises when some element `a` lies in a set `X` by simply existing the fact
 747 `lieIn(a, X)`. Otherwise, we have `fail lieIn(a, X)`. The definition of `lieIn`
 748 and the translation of the asynchronous parallelism are presented as follows.

```

749 lieIn ::= (ev:Sigma, set:String).
750
751 trans(State(par(P, X, Q)), a, State(par(P_, X, Q))) :-
752   State(par(P, X, Q)), a != tau, a != tick,
753   trans(State(P), a, State(P_)), fail lieIn(a, X).
754 trans(State(par(P, X, Q)), a, State(par(P, X, Q_))) :-
755   State(par(P, X, Q)), a != tau, a != tick,
756   trans(State(Q), a, State(Q_)), fail lieIn(a, X).

```

757 The firing rule for synchronous parallelism is simpler

$$\frac{P \xrightarrow{a} P' \quad Q \xrightarrow{a} Q'}{P \parallel_X Q \xrightarrow{a} P' \parallel_X Q'} (a \in X)$$

758 Two processes evolve together only if they agree in the same event that lies in the
 759 synchronisation set. The translation produces:

```

760 trans(State(par(P, X, Q)), ev, State(par(P_, X, Q_))) :-
761   State(par(P, X, Q)), ev != tau, ev != tick, lieIn(ev, X),
762   trans(State(P), ev, State(P_)), trans(State(Q), ev, State(Q_)).

```

763 Recall the firing rules for parallelism that deal with distributed termination.

$$\frac{P \xrightarrow{\checkmark} P'}{P \parallel_X Q \xrightarrow{\tau} \Omega \parallel_X Q'} \quad \frac{Q \xrightarrow{\checkmark} Q'}{P \parallel_X Q \xrightarrow{\tau} P \parallel_X \Omega} \quad \frac{}{\Omega \parallel_X \Omega \xrightarrow{a} \Omega}$$

764 They exist only to force both processes terminate together. In our embedding, we
765 just need a rule for the distributed termination.

766 `| trans(s,tick,State(Stop)) :- s is State(par(Skip,X,Skip)).`

767 **Hiding** The firing rules for hiding are given by

$$\frac{P \xrightarrow{a} P'}{P \setminus A \xrightarrow{\tau} P' \setminus A} (a \in A) \quad \frac{P \xrightarrow{a} P'}{P \setminus A \xrightarrow{a} P' \setminus A} (a \notin A) \quad \frac{P \xrightarrow{\checkmark} P'}{P \setminus A \xrightarrow{\checkmark} \Omega}$$

768 They are translated into

```
769 //Required by the premises
770 State(P) :- State(hide(P, X)).
771
772 trans(State(hide(P,X)),tau,State(hide(P_,X))) :-
773   State(hide(P,X)),ev!=tick,lieIn(ev, X),
774   trans(State(P),ev,State(P_)).
775 trans(State(hide(P,X)),ev,State(hide(P_,X))) :-
776   State(hide(P,X)),ev!=tick,fail lieIn(ev, X),
777   trans(State(P),ev,State(P_)).
778 trans(State(hide(P,X)),tick,State(Stop)) :-
779   State(hide(P,X)),trans(State(P),tick,State(P_)).
```

780 **Sequential composition** The following firing rules describe the behaviour of
781 the sequential composition operator

$$\frac{P \xrightarrow{a} P'}{P; Q \xrightarrow{\tau} P'; Q} (a \neq \checkmark) \quad \frac{P \xrightarrow{\checkmark} P'}{P; Q \xrightarrow{\tau} Q}$$

782 The translation to FORMULA produces

```
783 //Required by the premises
784 State(P) :- State(seqC(P, Q)).
785
786 trans(State(seqC(P,Q)),ev,State(seqC(P_,Q))) :- ev!=tick,
787   State(seqC(P,Q)),trans(State(P),ev,State(P_)).
788 trans(State(seqC(P,Q)),tau,State(Q)) :- State(seqC(P, Q)),
789   trans(State(P),tick,State(P_)).
```

790 **Recursion** The firing rule for recursion is given by

$$\frac{}{\mu Y \bullet F(Y) \xrightarrow{\tau} F[\mu Y \bullet F(Y)/Y]}$$

791 The μ construct is just a way to call the process again. This is expressed in FOR-
 792 MULA as a process call in the body of the process. Furthermore, we need more
 793 constructors to deal with this. The following code is the translation for recursive
 794 processes.

```
795 ProcDef ::= (name:String,params:Param,proc:CSPProcess) .
796 trans (State (proc (P,pP)),tau,State (PBody)) :-
797   State (proc (P,pP)),ProcDef (P,pP,PBody),State (PBody) .
798 State (PBody) :- State (proc (P,pP)),ProcDef (P,pP,PBody) .
```

799 The constructor `ProcDef` (meaning Process Definition and a way of encoding
 800 CSP equations as $P(X) = PBody$) is a way of describing in FORMULA all
 801 processes that are defined in a CSP specification. It contains a name (of type
 802 `String`), a parameter (of type `Param`) and the process body itself (of type
 803 `CSPProcess`). The initial state of the firing rule is $\mu Y \bullet F(Y)$. This is cap-
 804 tured in FORMULA by `State (proc (P,pP))`, where `pP` are the possible ac-
 805 tual parameters of `P`. However the new state $P[\mu p.P/p]$ needs two FORMULA
 806 facts to work accordingly: `ProcDef (P,pP,PBody)` (the creation of the new
 807 process body substituting all arguments with the values provided by the actual
 808 parameters `pP`) and `State (PBody)` (the state building block corresponding to
 809 this new process body). As the new state is used in the right-hand side of the
 810 previous rule, it must be created beforehand. That is the reason we need the rule
 811 `State (PBody) :- . . .`. Note that its right-hand side is almost the same as the
 812 transition rule, except that here we are creating the state to be used there (a cre-
 813 ation only when the actual parameter is available).

814 3.4.4 Capturing CSP Channels in FORMULA

815 In CSP channels are useful to define events (or set of events). In FORMULA chan-
 816 nels have a similar purpose. For events without data communication, the existence
 817 of an event (`BasicEv ("ch")`, for example) makes implicit the existence of a
 818 channel `ch`. This means that the CSP channel declaration

```
819 channel ev
```

820 has no corresponding FORMULA code.

Nevertheless, as FORMULA uses SMT solving to instantiate values, events involving data communication have a different purpose: providing basic facts (probably with uninstantiated values) so that FORMULA can instantiate values to be used in communications. This approach provides a powerful abstraction mechanism for data values. For example, the following channel declaration

```
channel in : Int
```

is represented in FORMULA by

```
primitive Channel ::= (chName:String,chType:Types).
```

The representation is intuitive and contains channel's name and the supported communication type. The `primitive` qualifier establishes that a channel in FORMULA must be given in the partial model. Moreover, all constructors involving the communicated type depend on the corresponding FORMULA channel. For example, the following CSP code shows a process that uses a communication event involving values from an infinite domain

```
channel in : Int
P = in?x → Skip
```

Its translation to FORMULA produces the following code

```
//Inside the semantic domain of the problem
trans(So, CommEv("in", Int(x)), State(Skip)) :- So is State(CommEv("in", Int(x))),
                                                Channel("in", Int(x)).

//Inside the partial model of the problem
Channel("in", Int(_))
```

It is worth noting that the transition for the prefix construct has already been defined in the semantic domain. However, such a definition works only for basic events (without communication values) or events involving an already known (constant) communication values. When communication values need to be instantiated the channel declaration is necessary as premise to create a transition (or any other element) that depends on it. Furthermore, these codes are placed in different parts of the FORMULA script: the semantic domain contains the rule to generate a new transition, and the partial model contains the fact corresponding to the channel declaration. This separation occurs because the semantic domain manipulates dynamic information whereas the partial model provides all the necessary static information to make FORMULA work. This is also discussed in Section 3.4.7.

857 3.4.5 Classical Properties in FORMULA

858 Recall from Section 3.3 that model checking is basically stated as a possible walk-
 859 through (breath-first, etc.) in a given LTS. For CSP, such a check includes some
 860 classical properties like deadlock, livelock, and nondeterminism. Other properties
 861 are checked via explicit refinement⁴.

862 For each domain instance (or model) to be analysed, we must be able to inform
 863 which process will be analysed. This is achieved by adding a new constructor
 864 with this purpose.

```
865 domain CSP_Semantics extends CSP_Syntax{
866   ...
867   // to allow informing the process to be analysed
868   primitive GivenProc ::= (name:String).
869   State(body) :- GivenProc(name), ProcDef(name,params,body) .
870 }
```

871 The constructor `GivenProc` allows one to inform which process (actually only
 872 its name) will be analysed. Based on that information and on the corresponding
 873 process definition, we are able to create the first state and then start the creation
 874 of the entire LTS (dynamic states and transitions).

875 Once the LTS has been created, we can define queries (partial model) capturing
 876 properties over the LTS. It is worth noting however that FORMULA only presents
 877 a successful analysis when a query is satisfiable; this exactly corresponds to the
 878 counterexample provided by model checkers. Therefore, if one wants to find a
 879 counterexample in FORMULA, the properties must be stated in such a way that
 880 they aim at finding the conterexample. That is, instead of checking for deadlock-
 881 freedom we are interested in finding a possible deadlock; the same idea is used
 882 to the other classical properties. The encoding of each classical property in FOR-
 883 MULA is almost direct and based on its definition. As introduced later on in
 884 this section, the following formal descriptions assume a relation *Reachable(s)*
 885 that holds only whether there is a path from the process equation (definition) to a
 886 semantic state *s*.

- 887 • Deadlock - a process is deadlocked if it reaches some state from which it
 888 goes nowhere. Furthermore, such a state is not reached by a \checkmark -transition
 889 (successful termination). This is formally stated by,

$$890 \quad \exists s : State \bullet \neg \exists t : Transition \bullet Reachable(s) \wedge t = (s, ev, s'),$$

⁴Deadlock, livelock and nondeterminism are also checked via refinement. However, the process exhibiting the desirable property is internally defined in FDR and compared with the process given by the user.

891 where *Reachable* captures all reachable states of the analysed system;

892 • Livelock - a process has a livelock if it can perform a τ -loop (a loop of
893 internal or τ -transitions). This is formalised by

$$894 \quad \neg \exists p: \text{TauPath} \bullet \text{Reachable}(s) \wedge p = (s, s),$$

895 where *TauPath* represents a sequence of one or more invisible transitions
896 between two states.

897 • Nondeterminism - a process is nondeterministic if it decides to accept or
898 reject the same event. This is similar to say that there are two transitions
899 with the same event from the same state leading to states (with different
900 initial acceptances). A formalisation of nondeterminism is given by

$$901 \quad \exists t_1, t_2 : \text{Transition} \bullet t_1 = (s, ev, s_1) \wedge t_2 = (s, ev, s_2) \wedge s_1 \neq s_2 \wedge$$

$$902 \quad \text{Reachable}(s_1) \wedge \text{Reachable}(s_2);$$

903 It is worth pointing out that the above properties are checked by FDR using re-
904 finement. That is, processes are analysed against some standard processes that
905 exhibit the desirable properties. Furthermore, FDR checks for deadlock-freedom,
906 livelock-freedom and determinism, whereas we check the existence of deadlock,
907 livelock and nondeterminism. this is due to the purpose of FORMULA queries
908 and because it is easy to find the counterexample.

909 Before performing the real check of a refinement, FDR generates the LTSs of both
910 processes⁵ and applies a *normalisation* to the specification, in the sense that the
911 structure of the LTS is changed for optimization. Afterwards, it compares its LTS
912 of the specification with that of the implementation. The chosen model (\mathcal{T} , \mathcal{F} or
913 \mathcal{FD}) determines which kind of information the LTS structure contains.

914 Concerning determinism checking FDR works differently. As deterministic pro-
915 cesses are the maximal ones under refinement, and the nondeterministic choice
916 of all deterministic processes is Chaos, one cannot check the determinism of a
917 process P by refinement checking it against some specification in any model X :
918 $\text{Spec} \sqsubseteq_X P$. Instead, FDR uses an algorithm that analyses the internal structure
919 of P (it indeed extracts specific transitions of P). This cannot be reproduced using
920 the refinement function of FDR. A detailed description of this algorithm can be
921 found in [Ros10].

922 Our approach, on the other hand, works directly on the LTS and uses the high level

⁵For processes (specification and implementation) involving parallelism, there is a previous *compilation* stage, where FDR identifies the parallel components and compiles these to explicit state machines to make the comparison easier.

support of FORMULA queries. This makes the check of properties much more close to their definition, as the FORMULA language corresponds to first-order logic. This also shows how powerful is FORMULA to abstract away programmatic details.

The most natural way to capture properties is using clauses establishing constraints over the LTS (built according to the semantic domain rules). To avoid polluting the semantic domain, we use domain extension and define auxiliary definitions and the corresponding clause to each property.

```

931 domain CSP_Properties extends CSP_Semantics {
932   //Determining a reachable state
933   reachable      ::= (fS:State) .
934   reachable(State(PBody)) :- GivenProc(P), ProcDef(P, pPar, PBody) .
935   reachable(Q)    :- GivenProc(P), ProcDef(P, pPar, PBody), trans(State(PBody), _, Q) .
936   reachable(Q)    :- reachable(R), trans(R, _, Q) .
937
938   //A path of tau-transitions between two states
939   tauPath        ::= (iS:State, fS:State) .
940   tauPath(P, Q)  :- trans(P, tau, Q) .
941   tauPath(P, Q)  :- tauPath(P, S), tauPath(S, Q) .
942
943   //The acceptances of a process in a given state
944   accepts        ::= (iS:State, ev:SigmaTickTau) .
945   accepts(P, ev) :- trans(P, ev, _), ev != tau .
946   accepts(P, ev) :- trans(P, tau, R), accepts(R, ev) .
947
948   //Capturing deadlock
949   Deadlock := trans(_, _, L), fail trans(L, _, _), fail trans(_, tick, L), reachable(L) .
950
951   //Capturing livelock
952   Livelock  := reachable(L), tauPath(L, L) .
953
954   //Capturing nondeterminism
955   Nondeterminism := trans(L, ev, S1), trans(L, ev, S2), S1 != S2, ev1 != tau,
956   accepts(S1, ev1), fail accepts(S2, ev1), reachable(S1), reachable(S2) .

```

The rule `reachable` captures any state that is reachable by the analysed process. Based on the main process (`GivenProc(P)`) and on its definition (that is, `ProcDef(P, pPar, PBody)`), we calculate all reachable states (starting at `State(PBody)`) by using reflexive-transitive closure: the main process itself is reachable, all main state's neighbour are reachable, and all neighbour of a reachable state is also reachable.

The rule `tauPath` is a FORMULA description to represent a sequence (possibly unitary) of τ -transitions between two states. It is defined in terms of transitive closure.

The rule `accepts` captures the initial acceptances (only visible events) of a process in a given state/context. Thus, `accepts(P, ev)` means the analysed process accepts the visible event `ev` in a state `P` (possibly performing τ -transitions

969 before `ev`).

970 Each property is almost a direct transcription from its definition considering the
 971 structure of the generated LTS and some auxiliary rule. A deadlock, for ex-
 972 ample, is found if there is an arbitrary (and reachable) state `L`, reached by a
 973 transition (`trans(_, _, L)`) that does not mean successful termination (`fail`
 974 `trans(_, tick, L)`) and from where there is no outgoing transition (`fail`
 975 `trans(L, _, _)`).

976 On the other hand, a livelock is intuitively defined by the existence of a `tauPath`
 977 from a reachable state to itself (`reachable(L), tauPath(L, L)`). This is a
 978 very simple way to capture the notion of a τ -loop (a cycle containing only τ -
 979 transitions).

980 The nondeterminism is captured by checking the existence of two transitions with
 981 a same event (possibly τ -transitions) from the same state `L` (`trans(L, ev, S1)`
 982 and `trans(L, ev, S2)`) leading to different states (`S1 != S2`) in which the pro-
 983 cess can accept (`accepts(S1, ev1)`) or reject (`fail accepts(S1, ev1)`)
 984 the same visible event (`ev1 != tau`). The remaining facts `reachable(S1)`
 985 and `reachable(S2)` are necessary to guarantee that `S1` and `S2` are reachable
 986 by the analysed process. Actually, when finding states (wider contexts) that de-
 987 pend on simpler states (narrower contexts), FORMULA generates auxiliary tran-
 988 sitions for narrower contexts as premises for the transitions for the wider contexts.
 989 Nevertheless, the query must consider only the wider contexts as they actually
 990 represent the LTS of the analysed process. For example, in the analysis of the
 991 process $(a \rightarrow SKIP) \backslash a$, FORMULA generates the transitions

```
992 trans(State(Prefix(BasicEv("a"), Skip)), BasicEv("a"), State(Skip)),
993 trans(State(Skip), tick, State(Stop)),
994 trans(State(hide(Prefix(BasicEv("a"), Skip), "{a}")), tau, State(hide(Skip, "{a}"))),
995 trans(State(hide(Skip, "{a}")), tick, State(Stop)).
```

996 However, the first and the second transitions are just premises for the third and
 997 fourth transitions (the real transitions of the original process), respectively. Hence,
 998 they must be discarded by the nondeterminism property query.

999 3.4.6 Refinement Checking in FORMULA

1000 Recall from Section 3.3 that traces refinement (\sqsubseteq_T) is defined as

$$1001 \quad P \sqsubseteq_T Q \equiv \text{traces}(Q) \subseteq \text{traces}(P)$$

1002 where the function *traces* comes from the denotational semantics.

1003 In terms of LTS analysis, traces calculation uses the transitive closure on the tran-
 1004 sitions from the initial state of the process being analysed to a certain end state.
 1005 In FORMULA, the transitive close is easily obtained by connecting the final state
 1006 of a transition with the initial state of another transition. However, we have to
 1007 consider this approach for two processes (P and Q) that will be compared and
 1008 use an on demand LTS creation and comparison. Therefore, from the negation
 1009 of $traces(Q) \subseteq traces(P)$, it suffices we can find some end state of the process
 1010 Q that cannot be achieved by process P or that it is achieved by different events.
 1011 In other words, we evolve both processes together on demand (recording the se-
 1012 quence of performed events) and check if the refinement is invalid. In this case,
 1013 we finish the LTSs construction (because we have found a counterexample).

1014 It is worth pointing out that in the traces model, invisible events do not make
 1015 sense. Moreover, tools like FDR and PAT optimize the LTS walkthrough process
 1016 by applying a normalisation step in the specification. Thus, the resulting LTS is
 1017 changed for optimization. In FORMULA we do that simultaneously through the
 1018 comparison between specification and implementation.

1019 In our refinement checking implementation in FORMULA we extend the proper-
 1020 ties domain⁶ by defining two objects of it: specification (`Spec`) and implemen-
 1021 tation (`Impl`). This is a resource of FORMULA that allows both usual domain
 1022 extension features as well as using renamed instances of a same domain. The
 1023 constructor `CEPath` has the purpose of detecting if a given event has been per-
 1024 formed by the specification just before a given final state (Q); it also discards
 1025 previous τ -transitions. As we analyse simultaneously two processes, the structure
 1026 of the counterexample (`C_EX`) should contain the initial states of both specification
 1027 and implementation, an event, and the final states of both specification and imple-
 1028 mentation. The rules for building the counterexample will be explained by cases
 1029 later. And the clause `counterexample` clause defines a valid counterexample
 1030 (representing a witness of an invalid refinement). Provided that the main process
 1031 (`GivenProc`) and its corresponding definition (`ProcDef`) are defined for both
 1032 specification and implementation, the counter example must have in its first transi-
 1033 tion calls to those processes (`proc(P, Ppar)`) and (`proc(Q, Qpar)`) as initial
 1034 states. And the final states of a valid counter example must have `State(Stop)`
 1035 as final state for both specification and implementation. The inclusion of such fi-
 1036 nal states in the counterexample happens when a situation violating the refinement
 1037 is found during its construction.

```
1038 domain TrRefinement extends CSP_Properties as Spec, CSP_Properties as Impl{
1039
1040   CEPath ::= (iS:Spec.State, event:Spec.SigmaTickTau, fS:Spec.State) .
```

⁶This is due to the reuse of the `tauPath` constructor. We could also extend the semantic domain and (re) define a constructor to capture τ -path between two states.

```

1041 C_EPath(P, ev, Q)      :- Spec.trans(P, ev, Q), ev != tau.
1042 C_EPath(P, ev2, Q)    :- Spec.tauPath(P, S), Spec.trans(S, ev2, Q), ev2 != tau.
1043
1044 //The counterexample structure
1045 C_Ex := (spec:Spec.State, impl:Impl.State, event:Impl.SigmaTickTau,
1046         specNext:Spec.State, implNext:Impl.State) .
1047
1048 //Rules for counterexample construction
1049 // Counterexample definition
1050 counterExample :=
1051   Spec.GivenProc(P), Spec.ProcDef(P, Ppar, PBody),
1052   Impl.GivenProc(Q), Impl.ProcDef(Q, Qpar, QBody),
1053   C_Ex(Spec.State(proc(P, Ppar)), Impl.State(proc(Q, Qpar)), _, _, _),
1054   C_Ex(_, _, _, Spec.State(Stop), Impl.State(Stop)) .
1055
1056 //The main goal
1057 conforms      := counterExample.
1058 }

```

Now we explain the construction of the counterexample by detailing all situations we must capture on demand. In the first situation we consider the creation of the first transition. It is a simple case, as we just use process calls as initial states and an internal action to recover the bodies (states) of each process. This is possible as long as the main processes and their definitions are available in the base of facts.

```

1065 //Building the first transition
1066 C_Ex(Spec.State(proc(P, pP)), Impl.State(proc(Q, pQ)), tau,
1067      Spec.State(PBody), Impl.State(QBody)) :-
1068   Spec.GivenProc(P), Spec.ProcDef(P, pP, PBody),
1069   Impl.GivenProc(Q), Impl.ProcDef(Q, pQ, QBody) .

```

The second situation is the simplest situation and discards internal actions performed by the implementation. As long as there is a previous record in the counterexample structure leading the implementation to a state $S \perp Q$, and from that state there is a τ -transition, we simply discard it and evolve only the implementation in the counterexample structure.

```

1075 //Tau transitions in the implementation are discarded.
1076 C_Ex(S0P, S0Q, ev, S1P, S2Q) :- C_Ex(S0P, S0Q, ev, S1P, S1Q), Impl.trans(S1Q, tau, S2Q) .

```

The third situation handles different sizes in traces of both specification and implementation. Actually, we need to detect if the implementation has a lengthier trace than the specification; that is, the implementation performs a visible event and the specification does not perform any visible event (in the future).

```

1081 //Implementation has a lengthier trace
1082 C_Ex(S0P, S0Q, evI, Spec.State(Stop), Impl.State(Stop)) :-
1083   Impl.trans(S0Q, evI, _) , evI != tau, evI != tick, C_Ex(_, _, _, S0P, S0Q) ,
1084   fail C_EPath(S0P, _, _) .

```


1085 The fourth situation deals with the case where both specification and implemen-
 1086 tation want to perform visible but different events. This represents an invalid
 1087 refinement situation and we record the event performed by the implementation
 1088 and stop the counterexample construction. As long as there is a record on the
 1089 counterexample leading to $S0P$ and $S0Q$, from which the implementation evolves
 1090 via a specific visible event that is not the same event used by the specification to
 1091 evolve, we record the event performed by the implementation as the final event
 1092 of the counterexample. Note that these rules are the same, except for the event.
 1093 This is necessary because FORMULA does not allow direct comparison between
 1094 events of the specification and of the implementation. The last case concerns suc-
 1095 cessful termination only in the implementation: if the implementation is ready to
 1096 terminate successfully and the specification does not terminate (in the future), we
 1097 record the \checkmark event as the last event in the counterexample.

```

1098 //Different events originate the final transition.
1099 C_Ex(S0P,S0Q,evI,Spec.State(Stop),Impl.State(Stop)) :-
1100   Impl.trans(S0Q,evI,_,C_Ex(_,_,_,S0P,S0Q),
1101   evI=Impl.BasicEv(name),
1102   fail CEPath(S0P,Spec.BasicEv(name),_).
1103
1104 C_Ex(S0P,S0Q,evI,Spec.State(Stop),Impl.State(Stop)) :-
1105   Impl.trans(S0Q,evI,_,C_Ex(_,_,_,S0P,S0Q),
1106   evI=Impl.CommEv(name,data),
1107   fail CEPath(S0P,Spec.CommEv(name,data),_).
1108
1109 //For the case where impl performs tick
1110 C_Ex(S0P,S0Q,tick,Spec.State(Stop),Impl.State(Stop)) :-
1111   Impl.trans(S0Q,tick,_,C_Ex(_,_,_,S0P,S0Q),
1112   fail CEPath(S0P,tick,_).

```

1113 Finally, the last situation captures equal events performed by specification and im-
 1114 plementation and records it in the counterexample structure. It is worth noting that
 1115 we use the constructor `CEPath` to check if the specification performs the event
 1116 because we have to discard τ -transitions in such a check. Due to the impossibility
 1117 of comparing events of the specification and of the implementation directly the
 1118 rule is duplicated for different events.

```

1119 // Equal events were performed. Just record it.
1120 C_Ex(S0P,S0Q,evI,S1P,S1Q) :- CEPath(S0P,evS,S1P),
1121   Impl.trans(S0Q,evI,S1Q),evI=Impl.BasicEv(name),
1122   evS=Spec.BasicEv(name),C_Ex(_,_,_,S0P,S0Q),evI!=tau.
1123
1124 C_Ex(S0P,S0Q,evI,S1P,S1Q) :- CEPath(S0P,evS,S1P),
1125   Impl.trans(S0Q,evI,S1Q),evI=Impl.CommEv(name,data),
1126   evS=Spec.CommEv(name,data),C_Ex(_,_,_,S0P,S0Q),evI!=tau.

```


1127 3.4.7 Using the model checker directly in Visual Studio

1128 The framework FORMULA allows two execution modes: inside Microsoft Visual
 1129 Studio and command line based. In both modes one has to provide the entire
 1130 encoding of CSP semantics as well as the encoding of the process to be analysed.
 1131 The latter consists of extending (using simple inclusion) the properties domain (if
 1132 one wants to check classical properties) or the refinement domain (if one wants
 1133 to check traces refinement), and determining the main process and all necessary
 1134 facts in a partial model. In case of refinement checking, the domain and the partial
 1135 model contain necessary information for both specification and implementation.
 1136 For example, let us consider the analysis of a simple process P given by $a \rightarrow$
 1137 $Skip \sqcap b \rightarrow Stop$ and the refinement check between P and another process Q
 1138 given by $a \rightarrow Skip \sqcap b \rightarrow Stop$. We perform deadlock check for both of them
 1139 and the refinement $P \sqsubseteq_{\mathcal{T}} Q$. The encoding for each process is presented as
 1140 follows.

```

1141 //Domain and partial model defining P
1142 domain PDomain includes CSP_Properties {
1143   ProcDef("P", nopar, eChoice(Prefix(BasicEv("a"), Skip),
1144                                   Prefix(BasicEv("b"), Stop))).
1145   conforms := CSP_Properties.Deadlock.
1146 }
1147 partial model P of PDomain{
1148   GivenProc("P")
1149 }
1150
1151 //Domain and partial model defining Q
1152 domain QDomain includes CSP_Properties {
1153   ProcDef("Q", nopar, iChoice(Prefix(BasicEv("a"), Skip),
1154                                   Prefix(BasicEv("b"), Stop))).
1155   conforms := CSP_Properties.Deadlock.
1156 }
1157 partial model Q of PDomain{
1158   GivenProc("Q")
1159 }

```

1160 For the process P we have a domain (PDomain) and a corresponding partial
 1161 model (P). The domain contains a process definition representing a CSP definition
 1162 for the process P as well as the deadlock check as the main goal. On the other
 1163 hand, the partial model contains only a fact to establish P as the process to be
 1164 analysed. The process Q is encoded similarly. We point out that this encoding
 1165 allows the definition of auxiliary processes in the domain as the main process is
 1166 only informed in the partial model. This is an important resource to follow a
 1167 modular description of a CSP specification.

1168 Concerning the refinement, the encoding in FORMULA is given as follows.

```

1169 domain PRefQDomain includes TrRefinement {

```

```
1170 Spec.ProcDef("P", nopar, eChoice(Prefix(BasicEv("a"), Skip),
1171                                   Prefix(BasicEv("b"), Stop))) .
1172 Impl.ProcDef("Q", nopar, iChoice(Prefix(BasicEv("a"), Skip),
1173                                   Prefix(BasicEv("b"), Stop))) .
1174 conforms := TrRefinement.conforms.
1175 }
1176 partial model PRefQ of PRefQDomain{
1177   Spec.GivenProc("P")
1178   Impl.GivenProc("Q")
1179 }
```

1180 The refinement is also represented by a domain and a corresponding partial model.
1181 The domain contains two process definitions establishing the specification and the
1182 implementation. Moreover, the conforms clause is defined as the main goal of the
1183 `TrRefinement` domain, which checks for the existence of a valid counterexample.
1184 The partial model just defined the main processes of the specification and of
1185 the implementation. Similarly to the previous encoding, this also allows the use
1186 of auxiliary processes for the specification and the implementation.

4 CML embedding in FORMULA

The embedding of CSP in FORMULA, detailed in Section 3 and shows how to build a model checker for CSP based on the its operational semantics. Such an embedding is important mainly because it can be reused in the context of CML. That is, the CML embedding is reuses the CSP embedding with some adjustments and extensions to include more behavioural aspects and data aspects as well. This allows one to create model checkers in a gradual approach.

We present the CML embedding as an extension of the embedding presented in Section 3. We start by showing how to deal with some data aspects and then present the new behavioural constructs and adjustment of those reused from the CSP embedding. We also point out that our embedding follows the structured operational semantics of CML of the deliverable D23.3 [BCC⁺13].

4.1 State and variables in FORMULA

In CML, states and local variables are similar to Circus, where they become available for manipulation in a specific scope. The most common FORMULA structure to represent a set of components (state and variables) together is a tuple. However, as they vary from specification to specification we have used a recursive structure to represent them: *bindings* (that is, mappings from variables to values). The immediate consequence of such a modelling is the existence of a specific value to be used in components that have been declared but not initialised yet. Such a value (*undef*) is defined in the types definition section of the FORMULA embedding.

```

1209 domain AuxiliaryDefinitions {
1210   //Types
1211   UNDEF      ::= {undef}.    //it works like a bottom value for all types
1212   primitive Int ::= (v:Integer).
1213   ...
1214   Types      ::= UNDEF + Int + ...
1215   ...
1216 }

```

The representation of bindings is introduced as follows.

```

1218 // Bindings
1219 NullBind      ::= { nBind }.
1220 primitive SingleBind ::= (name: String, val: Types).
1221 primitive BBinding ::= (b: SingleBind, rest: Binding).
1222 Binding       ::= NullBind + BBinding.
1223
1224 // Operations over bindings.

```

```
1225 //fetches the single bind containing the variable var
1226 fetch ::= (var: String, bind: Binding, b: SingleBind).
1227
1228 //updates the old binding by replacing (or adding) a new single binding to it
1229 upd   ::= (old: Binding, b: SingleBind, new: Binding).
1230
1231 //removes the single binding associated to var from the old binding
1232 del   ::= (old: Binding, var: String, new: Binding).
```

1233 The value `nBind` denotes the null (or empty) binding (base case). The constructor
1234 `SingleBind` represents a tuple (var, val) maintaining the association of a value
1235 (val) to a variable (var) . The constructor `BBinding` represents the inductive
1236 case of bindings. Its structure is similar to a list definition: a single bind is the head
1237 and another binding is the rest (tail) of the structure. Both empty and non-empty
1238 bindings are represented together as the type `Binding`. With this representation,
1239 specifications containing (without initialising) none, one (variable $x : int$) or two
1240 variables $(x : int$ and $y : int)$ have bindings, respectively given by

```
1241 nBind,
1242 BBinding(SingleBind("x", undef), nBind),
1243 BBinding(SingleBind("x", undef),
1244          BBinding(SingleBind("y", undef), nBind))
```

1245 Concerning binding manipulation, we use representations for the operations of
1246 updating, deleting and fetching. Each operation is represented as a relation whose
1247 facts are created on demand to activate semantic rules that depend on it.

1248 Consider the following CML specification

```
1249 channels
1250 choose, out : int
1251
1252 process P =
1253 begin
1254   state v : int := 2
1255   actions
1256     TEST = (dcl x : int @ (x := 4;
1257                        choose.x -> out.(x+v) -> Skip))
1258   @ TEST
1259 end
```

1260 Its initial binding must contain the bindings $(v, 2)$ and $(x, undef)$ as the vari-
1261 able x is initiated only when the assignment $x := 4$ is executed. This changes
1262 dynamically the binding structure.

```
1263 BBinding(SingelBind("v",2),
1264           BBinding(SingelBind("x",undef),nBind))
```

1265 It is worth pointing out that the notion of bindings must be carried out along the
1266 LTS. To make this possible, we extend the `State` constructor to include such an
1267 information as follows:

```
1268 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1269   ...
1270   // Including binding information into State
1271   State ::= (b: Binding, procName: String, p: CMLProcess).
1272   ...
1273 }
```

1274 4.2 User Defined Types in FORMULA

1275 The representation for type definitions in FORMULA is quite intuitive. For ex-
1276 ample, consider the following type declaration in CML

```
1277 types
1278   Index = nat
1279   inv i == i in set {0,1}
1280   Money = nat
1281   inv m == m in set {0..5}
```

1282 It introduces the new types `Index` and `Money` whose invariants limit their val-
1283 ues to the sets `0, 1` and `0..5`, respectively. The most natural way to represent
1284 these types in FORMULA is by extending the existing types and using constraints
1285 (clauses) over them (in the domain of the analysed process) to be considered in
1286 all models of the specification domain. Thus, the resulting embedding is given as
1287 follows

```
1288 domain AuxiliaryDefinitions {
1289   //Types
1290   UNDEF      ::= {undef}. //it works like a bottom value for all types
1291   primitive Int ::= (v:Integer).
1292   ...
1293   primitive Index ::= (Natural).
1294   primitive Money ::= (Natural).
1295   ...
1296   Types      ::= UNDEF + Int + ... + Index + Money.
1297   ...
1298 }
1299
1300 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1301   ...
1302 }
```

```
1303
1304 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1305   ...
1306 }
1307
1308 domain CML_PropertiesSpec extends CML_SemanticsSpec {
1309   ...
1310 }
1311
1312 domain DependentDomain includes CML_PropertiesSpec {
1313   ...
1314   //capturing the constraints defined by invariants over types
1315   badIndex := Index(i), i != 0.
1316   badIndex := Index(i), i != 1.
1317   badMoney := Money(m), m > 5.
1318
1319   conforms := !badIndex & !badMoney & ...
1320
1321 }
```

1322 It is worth noting that our FORMULA constraints are indeed negation of the in-
1323 variants. This is more suitable to FORMULA and simplifies the embedding.

1324 4.3 User Defined Values in FORMULA

1325 The representation for user defined values in FORMULA is simpler than user
1326 defined types. As they are intended to establish global values (constants), they
1327 are represented as primitive constructors, whose real values are given in the
1328 partial model. For example, consider the following CML code

```
1329 values
1330   N : nat = 10
1331   V : nat = 20
```

1332 Its conversion originates the following FORMULA code

```
1333 partial model StartProcModel of DependentDomain {
1334   ...
1335   N(10)
1336   V(20)
1337   ...
1338 }
```

1339 The translation of each CML element that uses N and V must use these facts in
1340 some way.

4.4 CML Specific Processes Fragments

Although CML reuses some constructs of CSP, some of them are adjusted and new constructs are available only in CML. This section can be viewed as an extension of Section 3.4. The translation follows the structured operational semantics rules of CML presented in [BCC⁺13]. Furthermore, in Section 3.4 we did not consider state (and variables) information. This is handled in CML by using the notion of *bindings* (mappings from variables to values) – an extra information inserted in the state of the generated LTS. This design has been important to create the CML model checker from the CSP one. Hence, the constructs presented in Section 3.4 implicitly manipulate empty bindings.

4.4.1 Div and Chaos

The Div process originates a transition to itself to represent an auto-loop of invisible transitions. Its translation to FORMULA extends the syntax of basic processes to include Div and the semantics domain to include the corresponding transition. Concerning Chaos it is only represented as a basic process with no corresponding transition.

```
domain CML_SyntaxSpec includes AuxiliaryDefinitions {
  ...
  BasicProcess ::= {Stop, Skip, Chaos, Div}.
  ...
}
domain CML_SemanticsSpec extends CML_SyntaxSpec {
  ...
  //Div
  trans(iS,tau,iS) :- iS is State(st,pN,Div).
  ...
}
```

4.4.2 Input and Output

Inputs and outputs are handled uniformly by using a generic representation for communication involving values. In the syntax domain, IOComm is a constructor that handles the real value to be communicated. IOCommDef is a constructor to make the corresponding changes in the bindings and CommEv is the event to be present in transitions.

```
domain CML_SyntaxSpec includes AuxiliaryDefinitions {
  ...
  primitive IOComm ::= (id: Natural, chName: String, chExp:String, val: Types).
  primitive CommEv ::= (chName: String, chExp:String, val: Types).
```

```

1379 | IOCommDef      ::= (id: Natural, exp: Types, st: Binding, st_: Binding).
1380 | Sigma         ::= BasicEv + CommEv + IOComm.
1381 | ...
1382 | }

```

Concerning the firing rules, we have different rules. For events without communication values, we create a transition whose event is `BasicEv`. When values are involved, we need to obtain values from a channel (using the constructor `Channel`) or from the bindings (using `fetch`). The link between `IOComm` and `IOCommDef` is essential for separating values from the process body. `IOCommDef` is responsible to handle the value and give it to `IOComm`. After that a new `CommEv` is created as the label of the transition.

```

1390 | domain CML_SemanticsSpec extends CML_SyntaxSpec {
1391 |   ...
1392 |   // communications
1393 |   State(st,pN,P),
1394 |   trans(State(st,pN,Prefix(BasicEv(a),P)),BasicEv(a),State(st,pN,P)) :-
1395 |     State(st,pN,Prefix(BasicEv(a),P)).
1396 |
1397 |   State(st_,pN,P),
1398 |   trans(ini, CommEv(chName,chExp, chType),State(st_,pN,P)) :-
1399 |     ini is State(st,pN,Prefix(IOComm(id,chName,chExp,chType),P)),
1400 |     Channel(chName,chType), IOCommDef(id,chType,st,st_).
1401 |
1402 |   State(st_,pN,P),
1403 |   trans(ini,CommEv(chName,chExp,v), State(st_,pN,P)):-
1404 |     ini is State(st,pN,Prefix(IOComm(id,chName,chExp,chType),P)),
1405 |     Channel(chName,chType1), chType1 != v, IOCommDef(id,chType,st1,st_),
1406 |     fetch(chExp,_,v).
1407 |   ...
1408 | }

```

4.4.3 Variable Block

Variable block is also implemented in CML by extending the syntactical domain to include a new process fragment and by translating the corresponding operational semantic rules as follows.

```

1413 | domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1414 |   ...
1415 |   primitive var ::= (name: String, tName: String, p: CMLProcess).
1416 |   primitive let ::= (name: String, p: CMLProcess).
1417 |   ...
1418 |   CMLProcess := ... + var + let.
1419 | }
1420 |
1421 | domain CML_SemanticsSpec extends CML_SyntaxSpec {
1422 |   ...
1423 |   // variable block begin
1424 |   trans(iS,tau,State(st,pName,let(nx,pBody))) :-
1425 |     iS is State(st, pName, var(nx, xT, pBody)).

```



```

1426
1427 // variable block visible
1428 State(st, pName, P) :- State(st,pName,let(x, P)).
1429 trans(iS, ev, State(st_, pName,let(x,P_))) :-
1430     iS is State(st,pName, let(x,P)),
1431     trans(State(st,pName, P), ev, State(st_,pName, P_)).
1432
1433 // variable block end
1434 trans(iS, tau, State(st_,pName,Skip)) :-
1435     iS is State(l,st,pName,let(x,Skip)), del(_,vName,st_).
1436 ...
1437 }

```

1438 4.4.4 Sequence

1439 CML sequence has almost the same meaning as sequential composition in CSP. In
1440 terms of FORMULA, this correspondence is also true. Thus, there is a constructor
1441 in the syntax domain and the rules in the semantic domain.

```

1442 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1443     ...
1444     //Similar to CSP but it uses CMLProcesses
1445     primitive seqC ::= (lProc : CMLProcess, rProc : CMLProcess).
1446     ...
1447 }
1448
1449 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1450     ...
1451     // sequence progress
1452     State(st,pN,P) :- State(st,pN,seqC(P,Q)), P != Skip.
1453     State(st_,pN,seqC(P_,Q)),
1454     trans(iS,ev,State(st_,pN,seqC(P_,Q))) :- iS is State(st,pN,seqC(P,Q)),
1455         trans(State(st,pN,P),ev,State(st_,_,P_)).
1456
1457     //sequence end
1458     State(st,pN,Q),
1459     trans(iS,tau,State(st,pN,Q)) :- iS is State(st,pN,seqC(Skip,Q)).
1460     ...
1461 }

```

1462 4.4.5 Nondeterministic Choice

1463 The CML nondeterministic choice has almost the same meaning as the internal
1464 choice in CSP. In the FORMULA script we have a constructor in the syntax do-
1465 main and the rules in the semantic domain.

```

1466 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1467     ...
1468     //Similar to CSP but it uses CMLProcesses
1469     primitive iChoice ::= (lProc : CMLProcess, rProc : CMLProcess).
1470     ...

```

```

1471 }
1472
1473 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1474   ...
1475   // nondeterministic choice left
1476   State(st, pN, P),
1477   trans(State(st, pN, iChoice(P, Q)), tau, State(st, pN, P)) :-
1478     State(st, pN, iChoice(P, Q)).
1479
1480   // nondeterministic choice right
1481   State(st, pN, Q),
1482   trans(State(st, pN, iChoice(P, Q)), tau, State(st, pN, Q)) :- State(st, pN, iChoice(P, Q))
1483   ).
1484   ...
1485 }

```

1486 4.4.6 Guard

1487 The translation of the CML guard construct establishes a process fragment (syntax) to allow such a construct in FORMULA and semantic rules that depend on
 1488 the evaluation of some boolean expression. The evaluation of boolean expression
 1489 is performed by reusing the built-in FORMULA support, where relational and
 1490 boolean expressions are directly converted in conditions that enable the creation
 1491 of a valid (guardDef) or invalid (guardNDef) guard definition. Guard definitions
 1492 are useful to provide a way to FORMULA to know which behaviour to
 1493 follow based on the guard evaluation.

```

1495 domain AuxiliaryDefinitions{
1496   ...
1497   //Guard evaluation to handle boolean expression evaluation
1498   guardDef      ::= (id: Natural, st: Binding).
1499   guardNDef     ::= (if: Natural, st: Binding).
1500 }

```

1501 The syntax domain is also adjusted to include CML guards as a process fragment.
 1502 In this case, we define a general constructor for conditional choice to provide a
 1503 uniform way to deal with guard and conditional choices in CML.

```

1504 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1505   ...
1506   //Similar to CSP but it uses CMLProcesses
1507   primitive condChoice ::= (id: Natural, procTrue: CMLProcess, procFalse:
1508     CMLProcess).
1509   ...
1510 }

```

1511 Concerning the semantic domain we define the following firing rules.

```

1512 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1513   ...
1514   // conditional choice
1515   State(st, pN, p),

```

```

1516   trans(iS,tau,State(st,pN,p)) :- iS is State(st,pN,condChoice(condId,p,q)),
1517                                   guardDef(condId,st).
1518   State(st,pN,q),
1519   trans(iS,tau,State(st,pN,q)) :- iS is State(st,pN,condChoice(condId,p,q)),
1520                                   guardNDef(condId, st).
1521   ...
1522 }

```

Note that the rule for conditional choice is replicated and it depends on the existence of a `guardDef` or `guardNDef`. These facts are created in the domain of the process being analysed according to the condition to be evaluated. For example, consider the following action

```

1527   P = [2 > 1] & Skip

```

Its translation to FORMULA originates a process definition whose conditional choice can behave as `Skip` or `Stop`. The expression to be evaluated is translated directly to FORMULA and is a premise to create a `guardDef` fact that will trigger the correct conditional choice rule.

```

1532 domain DependentDomain extends CML_PropertiesSpec {
1533   ...
1534   ProcDef("P", nopar, condChoice(1, Skip, Stop)).
1535   guardDef(1, nBind) :- 2 > 1.
1536   ...
1537 }

```

4.4.7 External Choice

CML contains two operators for external choice: `[]` and `[+]`. They are respectively represented in formula by `eChoice` and `extraChoice`. The firing rule for `[]` establishes a transition in which the associated binding is copied to each constituent process and the operator changes to `[+]`. The firing rules for `[+]` define the real behaviour of the external choice. The definition of `extraChoice` and the rules of external choice are described as follows:

```

1545 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1546   ...
1547   extraChoice ::= (lSt: Binding, lProc: CMLProcess, rSt: Binding, rProc:
1548                   CMLProcess).
1549   ...
1550   CMLProcess := ... + extraChoice.
1551 }
1552
1553 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1554   ...
1555   // P [] Q (external choice begin)
1556   State(st,name,P),
1557   State(st,name,Q),
1558   State(nBind,name,extraChoice(st,P,st,Q)),

```

```

1559   trans (iS,tau,State (nBind,name,extraChoice (st,P,st,Q))) :-
1560       iS is State (st,name,eChoice (P,Q)) .
1561
1562   //external choice skip
1563   State (st1,name,Skip) ,
1564   trans (iS,tau,State (st1,name,Skip)) :-
1565       iS is State (st,name,extraChoice (st1,Skip,st2,_)) .
1566   State (st2,name,Skip) ,
1567   trans (iS,tau,State (st2,name,Skip)) :-
1568       iS is State (st,name,extraChoice (st1,_,st2,Skip)) .
1569
1570   //external choice silent
1571   State (st3,pName_,P_) ,
1572   State (st,pN,extraChoice (l,st3,P_,st2,Q)) ,
1573   trans (iS,tau,State (st,pN,extraChoice (l,st3,P_,st2,Q))) :-
1574       iS is State (st,pN,extraChoice (st1,P,st2,Q)) ,
1575       trans (State (st1,pName,P) ,tau,State (st3,pName_,P_)) .
1576
1577   State (st3,qName_,Q_) ,
1578   State (st,pN,extraChoice (st1,P,st3,Q_)) ,
1579   trans (iS,tau,State (st,pN,extraChoice (st1,P,st3,Q_))) :-
1580       iS is State (st,pN,extraChoice (st1,P,st2,Q)) ,
1581       trans (State (st2,qName,Q) ,tau,State (st3,qName_,Q_)) .
1582
1583   //external choice end
1584   State (st3,pName,P_) ,
1585   trans (iS,ev,State (st3,pN,P_)) :-
1586       iS is State (st,pN,extraChoice (st1,P,st2,Q)) ,
1587       trans (State (st1,pName,P) ,ev,State (st3,pName,P_)) ,ev != tau .
1588   State (st3,qName,Q_) ,
1589   trans (iS,ev,State (st3,pN,Q_)) :-
1590       iS is State (st,pN,extraChoice (st1,P,st2,Q)) ,
1591       trans (State (st2,qName,Q) ,ev,State (st3,qName,Q_)) ,ev != tau .
1592   ...
1593 }

```

1594 4.4.8 Parallel

1595 In a similar way to the external choice, parallelism in CML is represented by two
1596 constructors: one for the begin and another for independent, synchronised and end
1597 (following the terminology introduced in the Deliverable D23.3). Thus, we use a
1598 syntactical (`parll`) and a semantic (`par`) operators.

1599 We also had to provide implementation for merging bindings to be used by the
1600 parallel. The syntax domain contain these definitions.

```

1601 domain AuxiliaryDefinitions{
1602   ...
1603   primitive Set      ::= (SetDef) .    //sequence
1604   EmptySet           ::= {empty} .
1605   primitive SetCont  ::= (head:Types,tail:SetDef) .
1606   SetDef             ::= EmptySet + SetCont .
1607   aSet               ::= (SetDef) .
1608   ...
1609   //merge

```

```

1610 merge    ::= (st1: Binding, lVars: String, st2: Binding, rVars: String, stF:
1611             Binding).
1612 merge(bindL, setL, setR, bindR, bindRes) :- filter(bindL, setL, bindRes1),
1613             filter(bindR, setR, bindRes2),
1614             unionB(bindRes1, bindRes2, bindRes).
1615
1616 filter    ::= (b: Binding, vars: aSet, st2: Binding).
1617 filter(bind, set, bindR) :- bind = BBinding(SingleBind(vN, vVal), restB),
1618             set = aSet(vN, empty),
1619             bindR = BBinding(SingleBind(vN, vVal), nBind).
1620
1621 filter(bind, set, nBind) :- bind = BBinding(SingleBind(vN, vVal), restB),
1622             set = aSet(vN_, empty), vN != vN_.
1623
1624 filter(bind, set, bindR) :- set = aSet(vN, restS),
1625             filter(bind, aSet(vN, empty), bind1),
1626             filter(bind, restS, bind2),
1627             unionB(bind1, bind2, bindR).
1628
1629 unionB    ::= (bindX: Binding, bindY: Binding, bindZ: Binding).
1630 unionB(nBind, nBind, nBind).
1631 unionB(nBind, Sy, Sy) :- Sy is Binding(_,_,_).
1632 unionB(Sx, nBind, Sx) :- Sx is Binding(_,_,_).
1633 unionB(BBinding(SingleBind(varX, valX), S),
1634         BBinding(SingleBind(varY, valY), nBind),
1635         BBinding(SingleBind(varX, valX), S_)) :-
1636         BBinding(SingleBind(varX, valX), S_), varX != varY,
1637         union(S, BBinding(SingleBind(varY, valY), nBind), S_).
1638 unionB(BBinding(SingleBind(varX, valX), S),
1639         BBinding(SingleBind(varY, valX), nBind),
1640         BBinding(SingleBind(varX, valX), S_)) :-
1641         BBinding(SingleBind(varX, valX), S_), varX = varY
1642         S_ = S.
1643
1644 }
1645
1646 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1647     ...
1648     //the semantic parallelism
1649     primitive par    ::= (lSt: Binding, lProc: CMLProcess,
1650         SyncS : String, rSt: Binding, rProc: CMLProcess).
1651     //the syntactical parallelism
1652     primitive parll ::= (lProc : CMLProcess, lVars: String,
1653         SyncS : String, rVars: String, rProc : CMLProcess).
1654     lStVars        ::= (refName: String, vName: String).
1655     rStVars        ::= (refName: String, vName: String).
1656
1657     ...
1658 }
1659

```

Concerning the semantic rules, we have provided operations for merging bindings manipulated by the constituent processes of the parallelism. These are presented as follows.

```

1663 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1664     ...
1665     //the syntactical parallelism (par) originates the semantic one (parll)
1666     //and all necessary premises
1667     State(st, nP, P) :- State(st, nP, parll(P, lV, X, rV, Q)).

```

```

1668 State(st,nP,Q) :- State(st,nP,parll(P,lV,X,rV,Q)).
1669
1670 //parallelism begin
1671 State(st,nP,par(st,P,X,st,Q)),
1672 trans(iS,tau,State(st,nP,par(st,P,X,st,Q))):- iS is State(st,nP,parll(P,lV,X,rV,
1673 Q)).
1674
1675 //parallel independent
1676 trans(iS,ev, State(st,name,par(st_,P_,X,st_,Q))) :- iS is State(st,name,par(st,P
1677 ,X,st,Q)),
1678 trans(State(st,nP,P),ev,State(st_,nP,P_)),fail lieIn(ev, X).
1679
1680 trans(iS,ev, State(st,name,par(P,st_,X,st_,Q_))):- iS is State(st,name,par(st,P
1681 ,X,st,Q_)),
1682 trans(State(st,nQ,Q),ev,State(st_,nQ,Q_)),fail lieIn(ev, X).
1683
1684 //parallel synchronised
1685 trans(iS,ev,State(par(st_,P_,X,st_,Q_))):- iS is State(par(st,P,X,st,Q)),
1686 trans(State(st,nP,P),ev,State(st_,nP,P_)),
1687 trans(State(st,nQ,Q),ev,State(st_,nQ,Q_)), lieIn(ev, X).
1688
1689 //parallel end
1690 State(st,pN,Skip),
1691 trans(iS,tau,State(st,pN,Skip)) :- iS is State(st,pN,par(st,Skip,X,st,Skip)).
1692 ...
1693 }

```

1694 4.4.9 Hiding

1695 The hiding is almost the same as in CSP, where the process depends on facts that
1696 say if an event belongs to a specific set (lieIn facts). The translation of hiding
1697 is illustrated as follows.

```

1698 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1699 ...
1700 primitive hide ::= (proc : CMLProcess, hideS : String).
1701 ...
1702 }
1703
1704 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1705 ...
1706 //hiding general to create the premise
1707 State(st,pN,p) :- State(st,pN,hide(p,X)).
1708
1709 //hiding internal
1710 State(st_,pN,hide(P_,X)),
1711 trans(iS, tau, State(st_,pName,hide(P_, X))) :- iS is State(st,pN,hide(P,X)),
1712 trans(State(st,pName,P),ev,State(st_,pName,P_)), lieIn(ev, X).
1713
1714 // hiding visible
1715 State(st_,pN,hide(P_, X)),
1716 trans(State(st,pN,hide(P,X)),ev, State(st_,pN,hide(P_, X))) :-
1717 State(st,pN,hide(P,X)),
1718 trans(State(st,pN,P),ev,State(st_,pN,P_)), fail lieIn(ev, X).
1719 ...
1720 }

```

1721 The events `lieIn` depend on the events used in the process body. For example,
 1722 consider the following process

1723 `P = (a -> Skip) \{a}`

1724 Its translation to FORMULA results in a process and in a list of `lieIn` facts to
 1725 provide all premises for the firing rules of hiding.

```
1726 domain DependentDomain extends CML_PropertiesSpec {
1727   ...
1728   ProcDef("P", nopar, hide(Prefix(BasicEv("a"), Skip), "{a}")).
1729   lieIn(BasicEv("a"), {a}).
1730   ...
1731 }
```

1732 4.4.10 Recursion

1733 Implementation of CML recursion in FORMULA is similar to that for CSP. The
 1734 special constructor `proc` represents a process call that is replaced by the suitable
 1735 process body when necessary (via an internal transition). The FORMULA code
 1736 for recursion is presented as follows

```
1737 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1738   ...
1739   primitive proc ::= (name : String, p: Param).
1740   ...
1741 }
1742
1743 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1744   ...
1745   // Call reusing state
1746   trans(n, tau, State(st, P, PBody)) :- n is State(st, P, proc(P, pP)),
1747     State(st, P, PBody), ProcDef(P, pP, PBody).
1748
1749   //The body of a process is a call to another process
1750   State(st, name2, PBody),
1751   trans(n, tau, State(st, name2, PBody)) :- n is State(st, name1, proc(name2, pP)),
1752     ProcDef(name2, _, PBody).
1753   ...
1754 }
```

1755 Consider the following recursive process

1756 `P = a -> P`

1757 Its translation to FORMULA results in a process that calls itself.

```
1758 domain DependentDomain extends CML_PropertiesSpec {
1759   ...
1760   ProcDef("P", nopar, Prefix(BasicEv("a"), proc("P", nopar))).
1761   ...
1762 }
```

1763 4.4.11 Assignment and Operations

1764 Assignment are viewed as actions that change values of variables. In FORMULA,
 1765 assignments are represented by two constructs: one identifying the CML assign-
 1766 ment and another containing the variable change. The former is present in a
 1767 process fragment whereas the latter manipulates bindings to make the necessary
 1768 changes.

```
1769 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1770   ...
1771   primitive assign ::= (id: Natural).
1772   assignDef        ::= (id: Natural, st: Binding, st_: Binding).
1773   ...
1774   CMLProcess := ... + assign.
1775 }
```

1776 The constructor `assign` represents a process fragment and has an identifier. The
 1777 constructor `assignDef` is associated to its assignment fragment through the
 1778 identifier and contains two bindings: one before the assignment (`st`) and another
 1779 after the assignment (`st_`). Let's consider a simple CML process example, where
 1780 its main action declares a local variable, assigns a value to it and behaves like
 1781 `Skip`.

```
1782 process P =
1783 begin
1784   @(dcl x : int @(x := 4; Skip))
1785 end
```

1786 Its translation to FORMULA is given as follows

```
1787 domain DependentDomain includes CML_PropertiesSpec {
1788   ProcDef("P", nopar, seqC(assign(1), Skip)).
1789   assignDef(1, BBinding(SingleBind("x", valX), noBind), BBinding(SingleBind("x", Int
1790     (4)), noBind)).
1791   ...
1792 }
```

1793 As the process manipulates only one variable (`x`), the bindings contain only one
 1794 element. The process definition is a sequential composition whose first action
 1795 is an assignment and the second action is `Skip`. The corresponding assignment
 1796 definition has the same identifier and changes the old value (represented by `valX`)
 1797 with the intended value (`Int(4)` in FORMULA).

1798 The representation of the firing rule for assignments is given as follows:


```

1799 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1800   ...
1801   // Assignment
1802   trans(n,tau,State(st_,pN,Skip)) :- n is State(st,pN,assign(id)),assignDef(id,
1803     st,st_).
1804   ...
1805 }

```

The existence of an assignment and its corresponding definition enables the creation of an invisible transition from the assignment fragment to a state whose binding contains the effect of the assignment and the action is Skip.

Operations are also represented by more than one constructor: one for syntactical purposes, one for establishing operation's effect and two others to represent the enabling condition when it is valid or not. This approach to represent precondition evaluation in two ways has been used to avoid interpretation of operation's precondition.

```

1814 domain CML_SyntaxSpec includes AuxiliaryDefinitions {
1815   ...
1816   operation      ::= (name: String).
1817   operationDef    ::= (name: String, st: Binding, st_: Binding).
1818   preOpOk        ::= (name: String, st: Binding).
1819   preOpNok       ::= (name: String, st: Binding).
1820   ...
1821   CMLProcess := ... + assign + operation.
1822 }

```

The representation of the firing rule for assignments is given as follows:

```

1824 domain CML_SemanticsSpec extends CML_SyntaxSpec {
1825   ...
1826   State(st_, Q),
1827   trans(iS,tau,State(st_,Q)) :- preOpOk(name,st),iS is State(st, seqC(schema(name
1828     ),Q)),
1829                                     schemaDef(schN, st, st_).
1830   State(st, Chaos),
1831   trans(iS,tau,State(st,Chaos)) :- iS is State(st,seqC(schema(name), Q)),
1832                                     preOpNok(schN, st).
1833   ...
1834 }

```

4.4.12 VDM Types and Collections

In this section we present the embedding of the VDM types and collections in FORMULA. We present a hybrid embedding of the VDM types and collections of a CML specification in terms of FORMULA. The hybrid embedding is because some basic VDM types and operators can be directly available in FORMULA

Type name	VDM type	FORMULA type
Integers	int	NegInteger, PosInteger, Integer
Naturals	nat	Natural
Characters	char	String
Strings	seq of char	String
Reals	real	Real
Booleans	bool	Boolean
Basic	?	Basic
Any	?	Any
Tuples	tuple	constructors
Records	record	constructors
Sets	set of T	Interpreted
Sequences	seq of T	Interpreted
Mapping	map A to B	Interpreted

Table 1: Correspondence between VDM and FORMULA types

1840 whereas others need interpretation to become available. Table 1 shows a prelimi-
 1841 nary correspondence between VDM and FORMULA. The correspondence will be
 1842 given in terms of the operators supported by the respective types. This is because
 1843 FORMULA supports some types that are not supported by VDM and vice-versa,
 1844 and even for directly corresponding types, FORMULA does not support some
 1845 operators available in VDM.

1846 From Table 1 we can see that several types have a direct correspondence between
 1847 VDM and FORMULA. However, we need to further detail this correspondence
 1848 in terms of the available and corresponding operators. Table 2 has the correspon-
 1849 dence between VDM and FORMULA operators.

1850 For those VDM operators that do not have a corresponding FORMULA coun-
 1851 terpart, we have to provide an interpretation. Thus, for example, let's explain
 1852 how the absolute value (*abs*), directly available in VDM, can be obtained in FOR-
 1853 MULA. First, we have to recall that FORMULA works similarly to Prolog in the
 1854 sense that everything is made of facts that are instances of relations. So, the VDM
 1855 function

$$abs : real \rightarrow real$$

1856 becomes the FORMULA relation (construtor)

```

1857 abs      ::= (inp:Real, res:Real).
1858 abs(x, x) :- x is Real, x >= 0.
1859 abs(x, y) :- x is Real, x < 0, y = - x.
```

Operation name	VDM operator	FORMULA operator
The numeric types		
Unary minus	$-x$	$-x$
Sum	$x + y$	$x + y$
Difference	$x - y$	$x - y$
Product	$x * y$	$x * y$
Division	x / y	x / y
Less than	$x < y$	$x < y$
Greater than	$x > y$	$x > y$
Less or equal	$x \leq y$	$x \leq y$
Greater or equal	$x \geq y$	$x \geq y$
Equal	$x = y$	$x = y$
Not equal	$x \neq y$	$x \neq y$
	Character	String
Equal	$c1 = c2$	$c1 = c2$
Not equal	$c1 \neq c2$	$c1 \neq c2$
Record types		
Field select	$r.i$	$r.i$
Equality	$r1 = r2$	$r1 = r2$
Inequality	$r1 \neq r2$	$r1 \neq r2$
Is	$is_A(r1)$	$r1 = A(_)$
Union/optional types		
Equality	$t1 = t2$	$t1 = t2$
Inequality	$t1 \neq t2$	$t1 \neq t2$

Table 2: Correspondence between VDM and FORMULA basic operations

1860 In the first line we introduce the construtor `abs` with two real numbers, one named
 1861 `inp` (standing for input) and one named `res` (standing for result). The other two
 1862 lines capture the definition of the absolute value, where $|x| = x$ (when $x \geq 0$) and
 1863 $|x| = -x$ (when $x < 0$). To use the result of such a calculation, one has just to use
 1864 the field select operator `(.)` suffixed by the name `res`. So, from an `abs(x, y)`
 1865 one can use `y` directly or use `absN is abs(x, y)` and apply the field select
 1866 operator to `absN` (or `absN.res`).

1867 Similarly to the absolute value operator, we can encode the floor operation as

```
1868 | floor      ::= (inp:Real, res:Integer).
1869 | floor(x, y) :- x is Real, y is Integer, y <= x, x < y + 1.
```

1870 The remainder operation is obtained directly from its mathematical definition.

```
1871 | rem      ::= (inp1:Integer, inp2: Integer, res:Integer).
1872 | rem(x, y, z) :- x is Integer, y is Integer, y > 0, z = x - y * (x / y).
```

1873 Similarly to the remainder operation, the modulus operation is obtained directly
 1874 from its mathematical definition.

```
1875 | mod      ::= (inp1:Integer, inp2: Integer, res:Integer).
1876 | mod(x, y, z) :- x is Integer, y is Integer, y > 0, f = floor(x/y, r), z = x - y
1877 | * r.
```

1878 It is worth noting that `x rem y` and `x mod y` are the same if the signs of `x` and
 1879 `y` are the same, otherwise they differ and `rem` takes the sign of `x` and `mod` takes
 1880 the sign of `y`.

1881 **The Boolean type** VDM supports booleans through its **bool** primitive data type
 1882 with the traditional boolean operators. Let `a` and `b` be booleans: negation (**not** `b`),
 1883 conjunction (`a and b`), disjunction (`a or b`), implication (`a => b`), biimplication (`a`
 1884 `<=> b`), equality (`a = b`), and inequality (`a <> b`).

1885 In FORMULA, booleans only support directly negation, equality, inequality, con-
 1886 junction and disjunction. Booleans are treated differently in three distinct situa-
 1887 tions. The first is as the type (Boolean), one can only use the equality (`=`) and in-
 1888 equality (`!=`) operators. In rules (second situation), we have booleans as facts. As
 1889 facts, we have conjunction (as a comma). For example: for `a and b` we have

```
1890 | Rule :- a, b.
```

1891 That is, `Rule` only holds whether the facts `a` and `b` are present (hold) in the
 1892 database of facts. For disjunction (by splitting a rule). For example: for `a or b` we
 1893 have

```
1894 | Rule :- a.
1895 | Rule :- b.
```

Boolean operator	VDM expression	FORMULA query
Negation	not b	Query := !b.
Conjunction	b1 and b2	Query := b1 and b2.
Disjunction	b1 or b2	Query := b1 or b2.

Table 3: Correspondence between VDM and FORMULA booleans

1896 That is, `Rule` holds whether the fact `a` is present (holds) in the database of facts.
 1897 The same occurs in an independent statement concerning the fact `b`. This means
 1898 disjunction in FORMULA based on facts. For negation (`fail a`). For example:
 1899 for **not** `a` we have

1900 | `Rule :- fail a.`

1901 It is worth observing that the `fail` construct requires some prerequisites to be
 1902 used successfully. The most important of all is that the rule must be stratis-
 1903 fied [JSD⁺09]. In general terms this means that a fact $f(p_1, \dots, p_k)$ can only be
 1904 used with a `fail` construct whether none of its parameters p_1, \dots, p_k are found
 1905 in the head of the rule nor the fact $f(\cdot)$ itself cannot be created by another rule
 1906 creating a cycle between these rules. The CML model checker satisfies this re-
 1907 quirement easily, except for guards where we had to have a fact corresponding to
 1908 the positive evaluation of a guard and a complementary fact related to the negative
 1909 evaluation of the same guard.

1910 Finally we can have booleans inside queries (third situation). Now we are able to
 1911 use the FORMULA boolean operators `and` (conjunction), `or` (disjunction), and
 1912 `!` (negation), and thus we have a direct correspondence with VDM as illustrated
 1913 in Table 3.

1914 To be able to represent the state part of CML specifications more flexibly we
 1915 created a “super” type that is a disjoint union of all supported types (In what
 1916 follows we simply illustrate this).

```

1917 | primitive Int      ::= (v:Integer).
1918 | primitive Nat      ::= (v:Natural).
1919 | primitive Str      ::= (v:String).
1920 | primitive IR       ::= (v:Real).
1921 | Types              ::= Int + Nat + Str + IR.
```

1922 **Set types** VDM supports sets of any primitive or user-defined data type. Thus
 1923 we use **set of T** meaning “the set of elements of type T”.

1924 FORMULA does not support sets directly. Thus we need to give a deep embed-
 1925 ding (interpretation) of sets into FORMULA. To this end FORMULA provides us

with a recursive type that can be used to represent sets, sequences, and mapping.
For sets we have:

```

1928 |   NullSet      ::= { empty }.
1929 |   Powerset     ::= NullSet + aSet.
1930 |   primitive TS ::= (t:Types).
1931 |   aSet         ::= (anElement: TS, rSet: Powerset).

```

The constructor `NullSet` is a enumeration type that introduces the empty set (`empty`). This empty element is type independent and can be used for any set of a specific type `T`. A set is captured by the type `Powerset` that can contain two elements: an empty set or a set (`aSet`). The constructor `aSet` is the way we capture a single element (`anElement`) a given set of type `TS` (Recall that we have created a “super” type that can represent any FORMULA directly supported data type) and the rest of the set (by a recursive definition) is given by another `Powerset` element. It is worth observing that, from the “super” type we use inside a set, our sets can be heterogenous. That is, we can represent sets as: $\{1, \text{“vdm”}, \text{true}\}$. On the other hand, with such a definition we do not support sets of sets as well as set comprehensions (These can be done but have been left for future work).

Concerning set operations we present some encodings (An exhaustive encoding is straightforward and has been left for future work). The first set operation is membership that is available in VDM as “`e in set s`”, where `e` is an element of type `T` and `s` is a set of type `T`.

In FORMULA membership becomes the following constructor and rules:

```

1949 |   member      ::= (elem: TS, set: Powerset).
1950 |   member(x, aSet(x, S)) :- aSet(x, S).
1951 |   member(x, aSet(y, S)) :- aSet(y, S), x != y, member(x, S).

```

The constructor `member` can create facts relating single elements of type `TS` to set elements. The definition of `member` is given recursively by considering first the base case $x \in \{x, \dots\}$ and then the recursive situation $x \in \{y, \dots\} \equiv x \in \{\dots\}$ (if $x \neq y$). Note that to create `member` facts we need facts in the right-hand sides of the rules. In the base case, we need to find a set `aSet(x, S)` as a fact. In the recursive case, we need to find a set (`aSet(y, S)`) and a membership relation (`member(x, S)`) as well as facts to create the new fact (`member(x, aSet(y, S))`). The relation $x \neq y$ is trivially handled as long as the variables `x` and `y` are bound to facts.

The other important operation about sets is the union between two sets, possibly resulting in a new set. In VDM it is simply stated as “`s1 union s2`”, for sets `s1` and `s2`. In FORMULA, similarly to the previous case of the membership relation,

we have to create a new construct and corresponding rules to interpret the union of sets correctly.

```

1966      union                                ::= (setX: Powerset,
1967                                           setY: Powerset,
1968                                           setZ: Powerset).
1969
1969      union(empty, empty, empty).
1970      union(empty, S, S)                    :- S is aSet(_, _).
1971      union(S, empty, S)                    :- S is aSet(_, _).
1972      union(Sx, Sy, X)                      :- Sx is aSet(x, S), Sy is aSet(y, empty),
1973                                           y = x, X = aSet(x, S).
1974      union(Sx, Sy, X)                      :- Sx is aSet(x, S), Sy is aSet(y, empty),
1975                                           y.t.v < x.t.v, X = aSet(y, aSet(x, S)),
1976                                           fail member(y, S).
1977      union(Sx, Sy, X)                      :- Sx is aSet(x, S), Sy is aSet(y, empty),
1978                                           x.t.v < y.t.v, union(S, Sy, X_),
1979                                           X = aSet(x, X_).
1980      union(S, Sy, X_)                     :- T != empty, Sy is aSet(x, T),
1981                                           union(S, aSet(x, empty), X), union(X, T, X_).

```

The most trivial fact of all about set union is that $\emptyset \cup \emptyset = \emptyset$. A direct consequence of having a \emptyset is that it represents the zero property of union. Thus, we have that $\emptyset \cup S = S \cup \emptyset = S$. If the input sets are not empty then we have a number of situations to consider in FORMULA. But before to go on, it is worth pointing out that—to minimize the number of facts created towards set operations—we consider sets as ordered collections (partial orderings). Because of such an ordering, we need to consider the union with singleton sets to put the element in the right slot in the recursive structure. We have three situations: (i) the elements are equal. We do not create a new set ($y = x, X = aSet(x, S)$); (ii) the element in the singleton set (y) is less than ($y.t.v < x.t.v$) the current element (x) of the set being considered. We put the y before x in the set resulting set $X = aSet(y, aSet(x, S))$; and (iii) the element in the singleton set (y) is greater than ($x.t.v < y.t.v$) the current element (x) of the set being considered. We make a recursive call that puts y in the right place. Finally the general situation is based on the associativity of set union: $S \cup (\{x\} \cup T) = (S \cup \{x\}) \cup T$.

Complementing set union, we consider set intersection. In VDM it is simply stated as “ $s1$ **inter** $s2$ ”, for sets $s1$ and $s2$. In FORMULA, it is defined like union, requiring a new constructor and several rules.

```

2001      inter                                ::= (setX: Powerset,
2002                                           setY: Powerset,
2003                                           setZ: Powerset).
2004
2004      inter(empty, empty, empty).
2005      inter(empty, Sy, empty)               :- Sy is aSet(_, _).
2006      inter(Sx, empty, empty)               :- Sx is aSet(_, _).
2007      inter(Sx, Sy, Sy)                     :- Sx is aSet(x, S), Sy is aSet(x, empty).
2008      inter(Sx, Sy, empty)                  :- Sx is aSet(x, empty), Sy is aSet(y, empty),
2009                                           x != y.
2010      inter(Sx, Sy, X)                      :- S != empty, Sx is aSet(x, S),
2011                                           Sy is aSet(y, empty),

```

```

2012         inter(aSet(x, empty), aSet(y, empty), X1),
2013         inter(S, aSet(y, empty), X2),
2014         union(X1, X2, X).
2015     inter(S, Sy, X)      :- S != empty, T != empty, Sy is aSet(x, T),
2016                           inter(S, aSet(x, empty), X1),
2017                           inter(S, T, X2), union(X1, X2, X).

```

2018 Like set union, the intersection between empty sets is an empty set ($\emptyset \cap \emptyset = \emptyset$). Complementarily to set union, the intersection with an emptyset results in an empty set ($\emptyset \cap S = S \cap \emptyset = \emptyset$). As set intersection means possibly removing elements from the input sets (those that are different), we consider three situations:

2022 (i) the intersection between the set $\{x\} \cup S$ and the singleton set $\{x\}$ equals $\{x\} \cup S$

2023 (ii) the intersection of singleton sets results in an empty set when the elements are different ($\{x\} \cap \{y\} = \emptyset$, if $x \neq y$); (iii) the intersection $(\{x\} \cup S) \cap \{y\}$ equals $(\{x\} \cap \{y\}) \cup (S \cap \{y\})$ by the distributivity of \cap over \cup ; and finally (iv) $S \cap (\{x\} \cup T) = (S \cap \{x\}) \cup (S \cap T)$ by distributivity of \cap over \cup again.

2027 Another set operation we consider is set difference. In VDM it is simply stated as “ $s1 \setminus s2$ ”, for sets $s1$ and $s2$. In FORMULA, it is defined like the previous operations, requiring a new constructor and several rules.

```

2030     diff                                     ::= (setX: Powerset,
2031                                                setY: Powerset,
2032                                                setZ: Powerset).
2033     diff(empty, empty, empty).
2034     diff(empty, Sy, empty)      :- Sy is aSet(_, _).
2035     diff(Sx, empty, Sx)         :- Sx is aSet(_, _).
2036     diff(Sx, Sy, S)            :- Sx is aSet(x, S), Sy is aSet(x, empty).
2037     diff(Sx, Sy, aSet(x, X))    :- Sx is aSet(x, S), Sy is aSet(y, empty),
2038                                   x != y, diff(S, aSet(y, empty), X).
2039     diff(S, Sy, X)             :- S != empty, T != empty, Sy is aSet(x, T),
2040                                   diff(S, aSet(x, empty), X1), diff(S, T, X2),
2041                                   inter(X1, X2, X).

```

2042 The first rule is the trivial one: $\emptyset \setminus \emptyset = \emptyset$. The second rule comes from the fact set difference cannot remove elements from the empty set ($\emptyset \setminus S = \emptyset$). Complementarily, the empty set does not change the original set ($S \setminus \emptyset = S$). Before the last general rule, we have two rules that deal with singleton sets: (i) when the elements are equal and it is removed from the resulting set ($(\{x\} \cup S) \setminus \{x\} = S$); (ii) when the initial elements are different we recurse to consider the other elements as well ($(\{x\} \cup S) \setminus \{y\} = S \setminus \{y\}$, if $x \neq y$). The last rule states the general situation: $S \setminus (\{x\} \cup T) = (S \setminus \{x\}) \cap (S \setminus T)$.

2050 Our last set based operation is the subset relation. In VDM it is written as “ $s1$ subset $s2$ ”. In FORMULA we have:

```

2052     subs                                     ::= (setX: Powerset, setY: Powerset).
2053     subs(empty, empty).
2054     subs(empty, Sy)              :- Sy is aSet(_, _).
2055     subs(Sx, Sy)                 :- Sx is aSet(x, empty), Sy is aSet(x, S).
2056     subs(Sx, T)                  :- Sx is aSet(x, S), subs(aSet(x, empty), T),

```


2057 | `subs (S, T) .`

2058 The subset relation requires less rules to be captured in FORMULA. Again the
 2059 first one the most basic rule: $\emptyset \subseteq \emptyset$. A direct consequence is the next rule:
 2060 $\emptyset \subseteq S$ (for any set S). The third rule concerns the case of the singleton set:
 2061 $\{x\} \subseteq (\{x\} \cup S)$. And the last rule is the general case: $(\{x\} \cup S) \subseteq T = (\{x\} \subseteq$
 2062 $T) \wedge (S \subseteq T)$.

2063 Our last rules concerning sets are a bit curious because they are simply stated to
 2064 decompose compound set in terms of its internal elements. This is necessary to
 2065 allow the previous rules to work correctly.

2066 | `aSet (y, empty) ,`
 2067 | `aSet (x, S) :- aSet (y, aSet (x, S)) .`

2068 The previous rules simply state that from the set $\{y, x\} \cup S$ (as a fact) we may
 2069 decompose it as the sets $\{y\}$ and $\{x\} \cup S$ as new facts. Obviously that the new
 2070 created set $\{x\} \cup S$ can activate this rule again until the set S becomes empty.

2071 **Sequences type** Sequences are interpreted in FORMULA like sets because we
 2072 only have the recursive structure to capture these more elaborated data types. But
 2073 sequences, differently from sets, are more easily captured because they can repeat
 2074 internal elements and thus do not need a partial ordering to minimize its repre-
 2075 sentation. Unfortunately, sequences can become infinite very easily, contrary to
 2076 sets. In the case of a set S , the new element `Powerset` of S is only infinite
 2077 if S is. But for sequences, it suffices that the base set be nonempty. Our solution
 2078 is to consider a bound (`SBound`) in the number of elements that can constitute a
 2079 sequence.

2080 | `primitive SBound ::= (Natural) .`

2081 The recursive sequence representation follows directly from the recursive set rep-
 2082 resentation only differing the names of the constructors.

2083 | `NullSeq ::= { empty } .`
 2084 | `Seq ::= NullSeq + aSeq .`
 2085 | `aSeq ::= (anElement: TS, rSeq: Seq) .`

2086 In this document we describe four basic sequence operators: cardinality (**len** in
 2087 VDM), head (**hd** in VDM), tail (**tl** in VDM), and concatenation (**^** in VDM).

2088 We start with cardinality. It is very easily captured and similar to functional pro-
 2089 gramming.

2090 | `card ::= (seqX: Seq, c: Natural) .`
 2091 | `card(empty, 0) .`
 2092 | `card(Sx, n_) :- Sx is aSeq(x, S), card(S, n), n_ = n + 1,`
 2093 | `n_ <= L, SBound(L) .`

2094 The first rule corresponds to $\# \langle \rangle = 0$. The second rule corresponds to the tradi-
 2095 tional recursive definition $\#(\langle x \rangle^S) = 1 + \#S$, except for the bound.

2096 The head of a sequence is trivially defined. As long as the sequence has at least
 2097 one element we can obtain its head as the second element of the constructor `head`
 2098 ($\text{head}(\langle x \rangle^S) = x$).

```
2099 |   head      ::= (seqX: Seq, h: TS).
2100 |   head(Sx, x) :- Sx is aSeq(x, S).
```

2101 Similarly to the head of a sequence, its tail is easily obtained.

```
2102 |   tail      ::= (seqX: Seq, seqT: Seq).
2103 |   tail(empty, empty).
2104 |   tail(Sx, S)      :- Sx is aSeq(x, S).
```

2105 The first rule is the base case: $\text{tail} \langle \rangle = \langle \rangle$. And the general situation $\text{tail}(\langle x \rangle^S) = S$ is described by the last rule.

2107 Sequence concatenation is more complex than the previous operations because it
 2108 creates new sequences similarly to set union. The only exception is that we do
 2109 not need to worry about element repetition. another difference of the traditional
 2110 sequence concatenation is that we need to consider the cardinality of the resulting
 2111 sequence because it is bound.

```
2112 |   conc      ::= (seqX: Seq, seqR: Seq, seqT: Seq, c: Natural).
2113 |   conc(empty, empty, empty).
2114 |   conc(empty, Sx, Sx, n) :- Sx is aSeq(x, S), card(aSeq(x, S), n), n <= L,
2115 |                               SBound(L).
2116 |   conc(Sx, empty, Sx, n) :- Sx is aSeq(x, S), card(aSeq(x, S), n), n <= L,
2117 |                               SBound(L).
2118 |   aSeq(x, X),
2119 |   conc(Sx, Sy, X_, n_) :- Sx is aSeq(x, S), Sy is aSeq(y, T), card(X, n),
2120 |                               conc(S, aSeq(y, T), X, n), X_ = aSeq(x, X),
2121 |                               n_ = n + 1, n <= L, SBound(L).
```

2122 The first rule is the trivial situation $\langle \rangle^{\langle \rangle} = \langle \rangle$. The following two rules are a direct
 2123 consequence of the previous rule: $S^{\langle \rangle} = \langle \rangle^S = S$. The last rule is the general
 2124 case $(\langle x \rangle^S)^{\langle y \rangle^T} = \langle x \rangle^{(S^{\langle y \rangle^T})}$ which is based on sequence associativ-
 2125 ity.

2126 Like sets, our last rules concern sequence decomposition. This is necessary to
 2127 allow the previous rules to work correctly.

```
2128 |   aSeq(y, empty),
2129 |   aSeq(x, S)      :- aSeq(y, aSeq(x, S)).
```

2130 **4.4.13 VDM operations**

2131 Apart from the VDM Mathematical toolkit, the state part of CML also supports
 2132 functions and operations. As FORMULA only supports relations, we need to
 2133 show how to describe functions and operations as relations. This is somewhat
 2134 straightforward because relations are more general than functions and operations.

2135 **Functions** We start by considering functions. Let f be a VDM function from a
 2136 generic K -parameterized type $Tp1 * \dots * TpK$ —corresponding to the func-
 2137 tion’s input—to a resulting type TR , corresponding to the function’s result. Its
 2138 definition follows next and it is characterized by the token `==`. Thus assuming the
 2139 K input parameters $p1, \dots, pK$ and a certain function’s body definition `body`, we
 2140 have $f(p1, \dots, pK) == body$. Finally we can have a precondition, stat-
 2141 ing when the function can be applied safely. Let’s consider the predicate `Pred` as
 2142 the precondition of the function f . Thus the VDM definition looks like.

```
2143 f: Tp1 * ... * TpK -> $ TR
2144 f (p1, ..., pK) == body
2145 pre Pred
```

2146 The first thing to observe when transforming the previous VDM definition into
 2147 FORMULA is that the name of the function has to be defined as a new constructor
 2148 with the same name where all input parameters as well as the result of the function
 2149 are declared as fields of the constructor. Thus in FORMULA we have the construc-
 2150 tor $f ::= (p1: Tp1, \dots, pK: TpK, r: TR) ..$ The function’s body
 2151 is transformed in a FORMULA expression $T(body)$ that restricts the possi-
 2152 ble outputs by an equality operation. But as FORMULA requires expressions to
 2153 be bound, we need to add bound restrictions for all input parameters of the form
 2154 $p_i \text{ is } Tp_i(_)$ (for $i \in 1..K$). Thus we have in FORMULA the rule

```
2155 f(p1, ..., pK, r) :- p1 is Tp1(_), ..., pK is TpK(_), r = T(body).
```

2156 Finally, the precondition is simply appended to the right-hand side of the previ-
 2157 ous rule, obviously transformed (becoming $T(Pred)$) like the function’s body.
 2158 Therefore, we get in FORMULA the whole definition as.

```
2159 f ::= (p1: Tp1, ..., pK: TpK, r: TR).
2160 f(p1, ..., pK, r) :- p1 is Tp1(_), ..., pK is TpK(_), r = T(body), T(Pred).
```

2161 It is worth observing that, depending on the precondition `Pred`, the above rule
 2162 can be split in several rules as we pointed out previously when considering the
 2163 Boolean data type.

2164 Let’s consider a concrete example to illustrate how a VDM function is transformed
 2165 into a FORMULA constructor with defining rules.

```

2166 | id      : nat +> nat
2167 | id(n) == n

```

2168 This becomes

```

2169 | id      ::= (p1: Nat, r: Nat).
2170 | id(n, n) :- n is Nat(_).

```

2171 in FORMULA.

2172 Another example with a precondition.

```

2173 | divide   : real * real +> real
2174 | divide(x, y) == x / y
2175 | pre y <> 0

```

2176 This is transformed into FORMULA as.

```

2177 | divide      ::= (p1: Real, p2: Real, r: Real).
2178 | divide(x, y, r) :- x is Real(_), y is Real(_), r = x.v / y.v, y.v != 0.

```

2179 **Operations** Following deliverable D31.2, CML has two ways of defining operations: an implicit (more abstract and basically described in terms of pre and postconditions) and an explicit (more concrete and described in terms of an action possibly requiring some precondition) form. In this deliverable we focus on the implicit formulation.

2184 Operations are captured similarly to functions. The differences come from the fact that operations can change the system state. Thus we consider the initial and after state bindings as parameters of operations described in FORMULA (Indeed CML uses the `frame` keyword to explicitly indicate which state variables can be changed by an operation, following similar ideas of The Refinement Calculus of Morgan [Mor90]).

2190 Let Op be a CML operation with input parameters $p1: Tp1, \dots, pK: TpK$. Furthermore, consider its precondition given by the predicate $preC$ and its postcondition by the predicate $postC$. Thus we have.

```

2193 | Op (p1: Tp1, ..., pK: TpK)
2194 |   pre preC
2195 |   post postC;

```

2196 To transform the previous definition into FORMULA, we consider the name of the operation, and the current (`st`) and after (`st_`) system state bindings as new parameters (note that both bindings have type `SS` standing for system state) of a generic constructor named `operation`. The rule that defines how the operation Op may work is only given by the transformation of the postcondition $postC$ as a FORMULA right-hand side rule (That is, a conjunction of facts and propositions).

2202 Let's consider that $T(\text{postC})$ is the respective conjunction of facts. As result the
2203 operation in FORMULA becomes.

```
2204 | operation(`Op`, p1, ..., pK, st, st_, r) :- p1 is Tp1(_), ..., pK is TpK(_),  
2205 |                                     T(postC).
```

2206 Finally we need to take care of the precondition. From the SOS rules of CML,
2207 we need to test whether the precondition holds and otherwise; in this last case the
2208 resulting transition yields a Chaos process (see Section 11). Unfortunately due to
2209 the stratification restriction we need to have the transformation of the precondition
2210 preC in both (positive and negative) forms. That is, we need the FORMULA
2211 right-hand sides $T(\text{preC})$ and $T(\text{not preC})$. Finally we have the FORMULA
2212 constructors and rules.

```
2213 | preOper(`Op`, p1: Tp1, ..., pK: TpK, st: SS) :- T(preC).  
2214 | preNOper(`Op`, p1: Tp1, ..., pK: TpK, st: SS) :- T(not preC).  
2215 | operation(`Op`, p1, ..., pK, st, st_, r) :- p1 is Tp1(_), ..., pK is TpK(_),  
2216 |                                     T(postC).
```

2217 5 COMPASS Tool Model Checker Plugin

2218 The COMPASS tool platform was designed as a plugin-based architecture. The
2219 model checker functionality is added to the COMPASS IDE using such an ar-
2220 chitecture. The plugin connects to the COMPASS tool and the core functionality
2221 (CML parser and type checker) through the generated CML AST. This connection
2222 is defined through AST visitors. Further details are provided in [CML⁺13].

2223 The model checker plugin (or MCP for short) consists of two main parts: the
2224 `core` – containing modules to converting the AST of a CML model into FOR-
2225 MULA (using the AST visitors), to invoke FORMULA as an external application
2226 and to build the counterexample, the `ide` – establishing the extension points for
2227 Eclipse such as views, perspective, commands, handlers, etc., and the `feature`
2228 part, which simply creates a feature to be included in the entire compilation (gen-
2229 erating a COMPASS IDE tool with all plugins).

2230 5.1 Architecture

2231 The model checker plugin is a component in the COMPASS core analysis li-
2232 braries, and is bundled in the
2233 `eu.compassresearch.core.analysis.modelchecker.visitor`
2234 package. The plugin core is based on a collection of classes extending the Ques-
2235 tionAnswerCMLAdaptor. The visitor generates a single FORMULA (with exten-
2236 sion `.4ml`) file. To achieve this, it loads the basic embedding (also packaged as
2237 a resource in the model checker core part) and complements it by adding a new
2238 domain and a partial model corresponding to the processes to be analysed. As the
2239 basic embedding also allows extensions (for example, type extensions), the visitor
2240 also adds information to the basic content loaded.

2241 The visitor traverses the AST and, for each node, it generates a correspond-
2242 ing FORMULA code. This task involves the use of context objects (CMLMod-
2243 elcheckerContext) to keep information used by other nodes in such a way that
2244 dependencies between nodes are resolved using the context object.

2245 There are some utility classes (Utilities and FormulaIntegrationUtilities) that con-
2246 tain useful methods used by the core part of the model checker plugin.

2247 5.2 Model Checker Plugin Behaviour

2248 This section describes the usual flow of behaviour of the model checker plu-
2249 gin.

2250 **Plugin initialisation** The `MCHandler` class (the event handler of the model
2251 checker) captures the AST of the selected unit (a CML file), the property
2252 to be checked and instantiates the visitor.

2253 **Generate FORMULA script** The `generateFormulaScript` method of the
2254 `CMLModelcheckerVisitor` class takes a CML AST and the property
2255 to be checked. Then it initialises a new context object and calls the `apply`
2256 method for the top-level node. This method invokes the `apply` method in
2257 the children nodes and generates the corresponding FORMULA code (as a
2258 String object). This may also involve putting information on the context to
2259 be processed by other nodes.

2260 **Invoke FORMULA** After receiving the script from the visitor, the handler in-
2261 stantiates a `FormulaIntegrator`, whose method `analyseFile` in-
2262 vokes the FORMULA as an external application and keeps the result (a text
2263 containing the base of facts produced FORMULA and other extra informa-
2264 tion).

2265 **Build the counterexample** The FORMULA result is given to an instance of a
2266 `GraphBuilder` object that builds a graph description (written in DOT
2267 language with extension `.gv`) of the counterexample (only if the checked
2268 property is valid) and save it to a file. The counterexample construction
2269 naturally involves algorithms over graphs such as BFS, DFS, shortest paths
2270 and cycle detection.

2271 **Graph file generation and visualization** The `GraphViz` class receives the path
2272 of the generated DOT file and compile it to another file in the Scalable
2273 Vector Graphics (SVG) format. After a double click in the MC List View
2274 component the plugin opens the generated SVG file using the internal Web
2275 browser of Eclipse.

6 Lessons Learned from the Model Checker Implementation

This section contains an overall evaluation of the experiences acquired in the development of the CML model checker.

- Chosen framework:** When we started this project, we did an evaluation among certain implementation infrastructures to support the development. Several alternatives emerged from basic (object-oriented, functional or logic-based) programming languages, through contract-based languages (such as Perfect Developer [Cro03], which is able to create implementation code from contracts), reuse and extend other model checkers (FDR [For10] or PAT [SLDP09]), SMT solvers (such as Microsoft Research Z3 [DMB08] or Bremen SONOLAR [PVL11]), to abstract frameworks (like Microsoft Research FORMULA [JSD⁺09]). As we needed to develop the CML model checker conforming to its semantics while the CML language itself (both syntactically and semantically) was being designed, we chose Perfect Developer as our first alternative because it has a minimum desired high-level descriptive powerful infrastructure that seemed to meet our needs. But reasonably soon, we figured out that Perfect Developer would not be the best option. We spent a lot of effort (several months—from November, 2011 to March, 2012) just to create a basic model checker infrastructure (based on [Fre05]) similar to the future CML needs, assuming that the CML semantics would be closer to the Circus language [WCF05] (one of its baseline languages). This effort was huge even considering the helpful support from Escher Technologies to resolve our doubts about Perfect. So this alternative seemed to be too risky particularly because it would take too much time after the right CML syntax and semantics would be available to finish the model checker following such artifacts. Thus we decided to abandon this initiative and try to use FORMULA, whose risk was related to the next lesson learned item (**Framework support**). Although our CML model checker has serious performance problems (see Appendix C), we still think that Microsoft FORMULA was the right framework under the context that it was developed (its one-to-one relation with the semantics was fundamental to build a correct CML model checker within the schedule).
- Framework support:** Our first direct contact with Microsoft FORMULA occurred in the York University on March, 2012, during a COMPASS convergence meeting. At that time, we thought that FORMULA was like the logic programming language Prolog and thus very easy to learn and use, and full of available literature and users. However, after some initial exper-

iments with FORMULA we realised that it did not behave like Prolog. Our only hint at that time was some powerpoint presentations and conference papers where the author (FORMULA project's leader) said: "Prolog works top-down and FORMULA is bottom-up". As we did not have any kind of support from Microsoft Research, except the presentations and papers, we tried to apply some work available in the literature close to our needs but described in Prolog. We found the work of Leuschel [Leu01]. Our current solution is quite similar to [Leu01] but uses the FORMULA behavioural difference from Prolog. This difference created a serious initial difficulty to create the model checker because we started learning and experimenting with FORMULA on April, 2012 and only on December, 2012 we get a stable version of a CSP model checker. But we were happy with that choice because the time was not spent developing the model checker but mainly on learning how to use FORMULA to build the model checker. This was clear when we extended the CSP model checker to a preliminary Circus model checker in a few working hours. Therefore FORMULA was the right option to create a correct model checker for a formal language that was being developed simultaneously.

- Orthogonal development:** CML is a language that combines features from the process algebra CSP and the model-based language VDM, with some constructs from the language of Dijkstra [Dij76], in a similar way to Circus. Assuming the orthogonality of these aspects, we decided to create the model checker incrementally from CSP, through VDM until the full CML. This was a very successful decision in the sense that these aspects were really independent of each other (confirming one of the benefits of the Unifying Theories of Programming [HJ98] that was used to create CML). The current version of the model checker links the constituent aspects by pattern-matching, where the CSP constructs guide the activation of the SOS trigger rules. When a VDM syntactic element is found in the body of a process (like an operation call), it creates a CML state just mentioning such a call and containing certain holes to be filled by the interpretation of the VDM part. The syntactic operation call matches with a respective VDM semantic rule that defines the VDM operation itself. Upon activation of such an operation rule, the full CML state becomes available in the labelled transition system. This was also evident when we extended the CSP model checker version to a preliminary Circus version in a few hours.
- Semantics conformance:** Probably the easiest way to create a CML model checker would be to reuse FDR as we have done in [MS01, FMS04]. However, as the CML semantics has some subtle differences to the CSP semantics (possibly correctly implemented in FDR), we would have to resolve two

main difficulties to show that we could create a correct CML model checker by reusing FDR. First, we would need to show which subset of CML could be represented by CSP elements and prove the respective required proof obligations. Such an effort was accomplished in another COMPASS task (but using Circus instead of CML) and reported in this work [OSA⁺13]. Unfortunately, the model checker for a subset of Circus based on FDR following [OSA⁺13] also exhibited a poor performance, particularly because of the required CSP encoding to handle the semantics related to external choice and parallelism. This bottleneck is also present in the FORMULA model checker and thus indicates that the performance degradation is not purely associated to the use of the FORMULA technology. Second, and probably the most difficult aspect, CML is intended to support heterogeneous aspects such as time, probability, mobility, etc., that creates a big gap to existing model checkers, prohibiting possible reuses. Therefore we needed to create a model checker that followed the formal SOS semantics of CML independent of combined aspects. Once again FORMULA satisfied such a requirement (For instance, PAT is another model checker for CSP but it does not conform completely to the CSP semantics as FDR does, although in several situations it is faster than FDR due particularly to its on-the-fly model checking algorithm that is not based on a refinement theory [SLS⁺12]).

- Building versus searching in a model:** As we presented in the introduction of this deliverable as well as in other sections, most model checkers focus on the search part of the problem, abstracting almost completely the part concerned with building a model from the semantics of a formal language (This discussion is related to the previous item **Semantics conformance**). The FORMULA model checker performs both efforts because we are aiming at correctness about the whole model checking process. Thus it takes a time T_M —for building a model—and a time T_S —for searching for a certain problem in the model built. In our experiments we get that $T_M > T_S$ in general, particularly because the model construction is solely based on the successive application of FORMULA rules that are interpreted against the search procedure that is fully performed by the SMT solver Z3. Obviously if we create the model using another solution (or get a Kripke structure for free), like a programming language (Java, Python, Haskell, etc.), our FORMULA model checker becomes faster. We performed some experiments where we executed FORMULA to build an LTS of a problem as a collection of facts. Then we took this collection of facts as an input to an extremely simpler FORMULA abstraction (basically containing search related queries and nothing about LTS creation) and executed FORMULA

again. While FORMULA took minutes to build the LTS, it took seconds to solve the query. But we go back to the original problem of guaranteeing correctness. While a FORMULA abstraction is close to the SOS semantics of a language, a programming code in general is far distant.

- **On-the-fly model checking:** After we have created the CSP, Circus and CML model checkers using a combination between FORMULA rules (to build the LTS) and queries (to search for the desired properties), we tried another possibility: instead of creating the LTS, let's try to find only the counter-example trace if one exists. This alternative is a kind of combinatorial problem: given some open (not initially instantiated) transitions and the set of states containing all fragments of a process's body (the process that is being analysed), use FORMULA to try to fill the transitions using the given states in such a way that it cannot create invalid transitions and finds the counter-example. This is indeed possible and get such an alternative working. To do that we had to calculate the complement of every SOS trigger rule of a formal language (for instance, CSP). This is because FORMULA queries always answer existential questions and SOS trigger rules are stated using universal quantifiers. Thus, we used the logical equivalence $\neg \forall x : T \bullet P(x) \equiv \neg \exists x : T \bullet \neg P(x)$ and encoded the problem in this new way: (i) SOS rules are stated in its complementary form (the $\exists x : T \bullet \neg P(x)$ part) as a query `SOSComplRule`, and (ii) the goal becomes the negation of such a query (the \neg (i)) part) or `conforms := !SOSComplRule`.
- **Elaborate data types:** CML is not a simple language in this respect. By inheriting the power of VDM (its Mathematical toolkit), CML supports abstract and elaborate data types from sets to mappings. This is one of the reasons why we decided to opt for Microsoft Research FORMULA instead of using PAT, Microsoft Research Z3 or Bremen SONOLAR. It is well-known from the model checking literature that most model checkers have very restricted data types. An exception to this rule is FDR. FDR provides sets, tuples and enumerated data types, which can easily be used to create a VDM toolkit (as we have done for the Z toolkit [MS01]). By comparing PAT to Z3 or SONOLAR, we agree that one could create a model checker very easily [DSL13] as long as such a model checker does not demand elaborated data types. With respect to data types, PAT is similar to SONOLAR and Z3 would be a better choice. Z3 provides richer data types than the others. Finally, although FORMULA is based on Z3, it has a much more elegant language with recursive data types that allows one to create a VDM Mathematical toolkit as presented in Section 4.4.12. Unfortunately as we have to define all operations related to sets, sequences, and mappings, this creates a huge facts database that worsens the CML model checker perfor-

mance.

- **FORMULA monotonicity:** One of the most difficult and worst aspects of FORMULA is its facts database monotonicity. With FORMULA, you do not have temporal facts. After creation a fact will persist until the end of the computation. Concerning the CML model checker this creates a problem with respect to two main things: (i) several SOS trigger rules use auxiliary facts that are not used in the final LTS structure but they are necessary to create the facts that will belong to such a structure; (ii) all interpreted operations (for instance, the VDM toolkit) are defined by rules that create facts. Similarly to the auxiliary transitions necessary to build the final LTS, if a set is used then this set is a fact as well as all its subsets must become facts to allow set operations to be available, which by themselves become facts as well. Therefore, another difference between FORMULA and Prolog is that FORMULA does not have backtracking. All intermediate facts are never garbage collected.
- **FORMULA symbolic executor:** As we presented in Section 3, FORMULA uses a combination between a symbolic execution algorithm and the SMT solver Z3. In December, 2012 we thought that Z3 was called during the interpretation of each FORMULA rule. However, during the encoding the mini-mondex problem⁷ we realised that Z3 is only called after the symbolic algorithm finishes its job. And this creates a problem when using symbolic data (or an open primitive fact). If the CML process has a recursive call and before such a call, a VDM operation can change the system state, the symbolic algorithm does not stop creating symbolic variables and FORMULA diverges. In such a situation, as we cannot change FORMULA's internal implementation, we have to use a bound to control how many recursive calls a CML process can make. It is really curious because even though the CML process has a finite state space, the use of a symbolic input data creates an infinite symbolic state expansion. By using a bound we find another problem: which bound is appropriate for each problem? This is a similar problem that occurs to several bounded model checkers. An easy solution is to use the abstraction by counter-example approach reported in [CES86].
- **Concrete vs symbolic data:** This topic is related to the previous one. It is very important because although a model checker created by FORMULA exhibits a poor performance in general, it can beat the best model checker when heavy data types are used. In simple comparison tests between FDR

⁷Mini-mondex is a simpler and abstract CML specification version of the Mondex electronic purse specification.

2471 and our CSP model checker created in FORMULA, our model checker
2472 found problems in a CSP specification in less time than FDR when FDR
2473 had to expand the LTS in a huge structure due to sets of reasonable car-
2474 dinality used in channel declarations. This is because the time required to
2475 interpret a FORMULA specification to build a symbolic LTS and find a suit-
2476 able instance (by Z3) offset the effort of creating a fully interpreted LTS (as
2477 is done by FDR). Finding the right amount of data to exercise a model is an
2478 intrinsic model checking problem [CGP99]. The best solutions comes from
2479 abstract interpretation [CC92] and SMT solving [BMR12]. As FORMULA
2480 is based on SMT solving, we are already using an state-of-the-art solution to
2481 the problem. On the other hand, referring to FORMULA symbolic execu-
2482 tor, one has to find how to control the symbolic execution algorithm used
2483 by FORMULA to avoid symbolic state space explosion.

7 Related Work

Robby [RDH03], Dong [DSL13], and Duret-Lutz [DLP04] provide model checker frameworks whose idea is that we can create any model checker by simply extending the facilities these frameworks offer. From these, the most generic seems to be Bogor [RDH03] because it gives the power of a functional language to define new data types. However, none of them have facilities to guarantee that the SOS semantics of a given language is correctly implemented by the new model checker extension. K  zmi  rczak et al [KPg12] shows how to create a CTL model checker for Normative systems using Haskell. He uses Kripke structures and basically concentrates his implementation in an adaptation of traditional model checking algorithms (search only). The Kripke structure (the model of a given problem) is given directly without SOS rules. Data structures are trivial (integers). Still concerning the reuse of language and tools but concentrating on the model based language, we have the work reported in [DNS11] where the authors show how to encode a subset of the Z language into the SAL toolset (it includes a model checker and a simulator). In several points such an encoding is similar to ours as described in Section 4.4.12. The main difference is that in Z2SAL the authors focus only in Z instead of an integration between Z and a behavioural language. The resulting model checker seems to be fast but it must be observed that the proofs are related to discharging proof obligations instead of the analysis of a full LTS.

Banda [BG10] shows how to apply completely standard techniques for constructing abstract interpretations to the abstraction of a CTL semantic function, without restricting the kind of properties that can be verified. Furthermore we show that this leads directly to implementation of abstract model checking algorithms for abstract domains based on constraints, making use of an SMT solver. Her work is done in Prolog.

Palikereva [POR12] proposes a prototype called SymFDR, which implements a bounded model checker for CSP based on SAT-solvers. The authors compare with the FDR tool to show that SymFDR can deal with problems beyond FDR, such as combinatorial complex problems. Moreover, they found that FDR outperforms SymFDR when a counter-example does not exist. In our work we extend the capability of SymFDR by using SMT-solving and not depending on FDR to create the LTS. In this way we can handle infinite state systems while SymFDR can only deal with systems that FDR can, that is, finite state systems.

Leuschel [Leu01] proposes an implementation of the CSP language based on SIC-Stus Prolog (a variation of Prolog). His main goal is to provide a CSP interpreter and animator. According to Leuschel's work, with a little effort his solution could

2522 be combined with a CTL model checker (e.g. SPIN) and also provide verification
2523 of CTL properties. Part of the design of our model checker in FORMULA follows
2524 a similar declarative and logic representation as reported in [Leu01], but the main
2525 idea is to be able to reason about concurrent systems using a rich specification
2526 language like CSP. As our model checker can handle infinite state systems, we
2527 indeed concretise the future work of [Leu01] towards this subject.

2528 Meseguer [BM12] works with Maude but this time showing differences between
2529 dealing with Kripke structures (state info is relevant) and LTS (behaviour is rele-
2530 vant). The paper presents the need to use a formalism to specify state and another
2531 to specify properties, and analysis the consequence in “cooking” both the sys-
2532 tem and the property in both state-based and action-based tandems as a lack of
2533 expressiveness in both cases. It then considers a semantics extension of a CTL
2534 model checker written in Maude to a TLR (Temporal Logic of Rewriting) model
2535 checker.

2536 The idea of using an SMT-solver for model checking purpose is not new either.
2537 The advances of SMT solvers bring a new level of verification. Bjorner [BMR12]
2538 extend the SMT-LIB to describe rules and declare recursive predicates, which can
2539 be used by a symbolic model checking. The idea of property verification is sim-
2540 ilar to the reachability analysis. That is, the property verification can be rewrite
2541 as reachability questions [BMR12]. Alberti [ABG⁺12] proposes an SMT-based
2542 specification language to improve the verification of safety properties. We are
2543 interested in providing an efficient model checking for the CSP specification lan-
2544 guage. Ghilardi [GR10] proposes a SMT model checker to check safety proper-
2545 ties of infinite-state systems. Its capability of dealing with infiniteness is inherited
2546 from an SMT solver like in our case. This paper [GR10] shows the performance
2547 of the model checker for simple examples like ours and the result is quite similar.
2548 In our work we bring a new perspective for reasoning about infinite systems by
2549 using a high level specification language. Our work differs from them by using an
2550 SMT-solver to increase the expressiveness of the process algebra CSP to provide
2551 a powerful tool for verification and reasoning of programs.

8 Conclusions

In this deliverable we have shown how to build a semantics preserving model checker for a rich-state language in an iterative way, starting from a language as CSP and then dealing with the complexity of CML, where rich-state is described in VDM.

The main reason to work this way was that CML is a formal language based on (a combination of) other mature and formal languages such as VDM [ABH⁺95], CSP [Ros10], and Circus [WC02], whose syntax (reported in deliverable D23.1) and semantics (reported in deliverable D23.3) were being developed concurrently to the model checker. Furthermore, it is also expected that CML will evolve in the future to accomodate still more complex aspects such as mobility, probability, etc.

Apart from developing the model checker gradually, we also had to use an implementation framework that was trustworthy as well as easy to keep in pace with the evolution of the CML syntax and semantics. After some investigation related to possible alternatives (see Section 6), we chose Microsoft FORMULA as the best alternative to follow the CML semantics as close as possible while delivering a model checker of reasonable performance. In Sections 3 and 4 we present the details of the construction of the CML model checker in terms of FORMULA syntax, but in the Appendices A and B we also provide more formal material towards why FORMULA is a good candidate as implementation infrastructure to build a trustworthy CML model checker.

Our feasibility study has shown that although the CML model checker works reasonably well for creating a prototype tool, a number of improvements can be done to evolve such a model checker to a competitive scenario. We list some of them in what follows as possible future work.

- We have used FORMULA for two main things:

1. Create the labelled transition system of a CML specification: This requires FORMULA to process several rules corresponding to Structure Operational Semantics trigger rules;
2. Search the FORMULA knowledge base to ensure the satisfaction of desired properties: FORMULA knowledge base is a database or set of logical facts. Facts can be given as input (primitive facts) or generated by processing rules.

Step 1 takes a considerable time to execute while Step 2 is considerably fast. One solution to improve the performance of the CML model checker

is to create the LTS using another implementation medium, such as a functional programming language, like Haskell, or an object-oriented or mixed language, like Java or Python (This is more an engineer's problem);

- Still related to Step 1, one can try to simply rewrite the FORMULA rules in a more optimised way, following the correspondence between the FORMULA semantics and that of the Datalog language. As Datalog is maturer than FORMULA, the literature has some material related to Datalog rules optimisation [CGT89] (This is more an engineer's problem as well);
- A third option, aiming at optimising the CML model checker, is to see the FORMULA framework as a prototype generation medium that serves to create a correct by construction tool (a kind of implementable specification), whose optimal implementation is derived from it. Again from the literature of Datalog, we can use work in the literature towards a derivation of an imperative implementation code from a FORMULA abstraction (rules and queries). Although this can be classified as an engineer's effort, this also needs some research effort as well. It seems that a good candidate to follow this direction is to use the integration between Python and Z3, named Z3Py [dM13];
- As several SOS rules, particularly those related to external choice and parallelism, need to anticipate facts (what we call in Sections 3 and 4 of auxiliary facts) and the FORMULA knowledge base is monotonic (that is, once a fact is created it cannot be removed from the knowledge base), this creates a huge and heavy knowledge base to deal with. As future work one can avoid expanding such rules and acting on demand, following a similar solution that is implemented in the model checker FDR [For10];
- Although we provide the material in Appendices A and B, linking FORMULA code to First-Order Logic, the ideal situation is to create a refinement calculus to FORMULA in such a way that one can derive, following a stepwise refinement approach, a correct FORMULA abstraction from a formal description of a problem. This is indeed a hot topic for future research, particularly whether one can provide the semantics of FORMULA as well as a refinement calculus using The Unifying Theories of Programming [HJ98];
- The current CML model checker works similarly to several model checkers in the sense of it cannot cope with some infinite-state systems. It can handle some infinite-state systems, where the source of infinity comes from channel data, but it cannot reason about systems that have infinite internal states. As future work one can create a FORMULA abstraction suitable for inductive

2626

proofs;

A FORMULA Semantics

Microsoft FORMULA is a combination between Constraint Logic Programming (CLP) and Satisfiability Modulo Theories (SMT) [JSD⁺09]. Executing a FORMULA abstraction means determining whether a logic program can be extended by a finite set of (primitive) facts so that a goal is satisfied. This requires searching through (infinitely) many possible extensions using the state-of-the-art SMT solver Z3 [DMB08]. Consequently, FORMULA abstractions can include variables ranging over infinite domains and rich data types. Nonetheless, the method is constructive. That is, the algorithm behind FORMULA returns extensions of the program witnessing goal satisfaction.

First, let's introduce the concept of an interpretation. Let U be a (possibly infinite) set called a universe. Let r be an n -ary relation symbol and r^I a (finite) interpretation of r ; r^I is a (finite) subset of U^n . As shorthand, we use $r(\bar{t})$ meaning r applied to elements t_1, \dots, t_n of U .

Definition 1 (interpretation) *An interpretation is a triple $I = \langle D, \phi, \pi \rangle$, where*

- D is the domain (a nonempty set). Elements of D are individuals,
- ϕ is a mapping that assigns to each constant an element of D . Constant c denotes individual $\phi(c)$,
- π is a mapping that assigns to each n -ary predicate symbol a relation: a function from D^n into booleans ($\{true, false\}$).

followed by what means a truth in some interpretation.

Definition 2 (truth in an interpretation)

- A constant c denotes in I the individual $\phi(c)$.
- Ground (variable-free) atom $p(t_1, \dots, t_n)$ is
 - true in interpretation I if $\pi(p)(t'_1, \dots, t'_n)$, where t_i denotes t'_i in interpretation I and
 - false in interpretation I if $\neg\pi(p)(t'_1, \dots, t'_n)$.
- Ground clause $h \leftarrow b_1 \wedge \dots \wedge b_m$ is
 - false in interpretation I if h is false in I and each b_i is true in I , and
 - true in interpretation I , otherwise.
- A knowledge base, KB (or a least Herbrand universe $lm(\Pi)$, for a program Π), is true in interpretation I if and only if every clause in KB is true in I

2659 And variable assignment means.

2660 **Definition 3 (variable assignment)** *A variable assignment is a function from*
2661 *variables into the domain.*

2662 FORMULA has the concept of a model.

2663 **Definition 4 (model)** *A model of a set of clauses is an interpretation in which all*
2664 *the clauses are true.*

2665 and logical consequence.

2666 **Definition 5 (logical consequence)** *If KB is a set of clauses and g is a con-*
2667 *junction of atoms, g is a logical consequence of KB , written $KB \models g$ (or*
2668 *$lm(\Pi^*) \models \exists g$), if g is true in every model of KB .*

2669 Finally, we have the concept of CLP satisfiability.

2670 **Definition 6 (CLP Satisfiability).** *Given:*

- 2671 • *A program Π with relation symbols $R = \{r_1, \dots, r_n\}$,*
- 2672 • *$R_p \subseteq R$ a subset of the program relations, called the primitive relations.*
- 2673 • *A quantifier-free goal g over the program relations.*

Then find a finite interpretation R_p^I for primitive relations such that:

$$lm((\Pi \cup R_p^I)^*) \models \exists g$$

2674 *The program $\Pi \cup R_p^I$ is obtained by extending Π with a fact $r(\vec{t})$ whenever $R_p^I \models$*
2675 *$r(\vec{t})$.*

2676 *The program can only be extended by primitive relations R_p . The contents of R_p^I*
2677 *are the facts that, when added to the program, cause the goal to be satisfied.*

2678 FORMULA rules have a direct correspondence with First-Order Logic formulas.

2679 For instance,

2680 $q(X, Y) \text{ :- } p(X, Y) .$
2681 $q(X, Z) \text{ :- } q(X, Y) , \quad q(Y, Z) .$

2682 is equivalent to

$$\begin{aligned} &\forall X, Y \bullet (p(X, Y) \implies q(X, Y)) \wedge \\ &\forall X, Z \bullet \exists Y \bullet (q(X, Y) \wedge q(Y, Z) \implies q(X, Z)) \end{aligned}$$

2683 To avoid repetition of the right-hand side of a rule, one can write a comma between
2684 heads. For example.

2685 $q(X) , r(X) :- p(X) .$

2686 is equivalent to $\forall X \bullet p(X) \implies (q(X) \vee r(X))$. When the head is the same for
 2687 different bodies, one can use semicolon as in the following example.

2688 $q(X) :- r(X) ; p(X) .$

2689 is equivalent to $\forall X \bullet (r(X) \vee p(X)) \implies q(X)$.

2690 FORMULA queries, differently of rules, are existentially quantified. Thus, for
 2691 example

2692 $query1 := q(X, 2) , p(X, Y) .$

2693 is equivalent to

$$\exists X, Y \bullet q(X, 2) \wedge p(X, Y)$$

2694 and

2695 $query2 := q(X, _) , fail\ p(X, Y) .$

2696 is equivalent to

$$\exists X, Y, Z \bullet q(X, Z) \wedge \neg p(X, Y)$$

2697 **B Properties in FORMULA**

2698 In this section we show how the properties encoded in FORMULA were derived
 2699 following the correspondence between first-order logic formulas and constraint-
 2700 logic programs given by Clark completion, which is inherited in FORMULA [JSD⁺09].

2701 **B.1 Deadlock analysis**

2702 Formally, a deadlock occurs whether the formula

$$2703 \exists s : \mathcal{T}(P) \bullet ref(P/s) = \Sigma \cup \{\sqrt{\}\}$$

2704 holds. That is, if a process P evolves through a trace s and after that it cannot
 2705 engage (it refuses) in any visible event, including $\sqrt{\}$.

To find the equivalent FORMULA rules and queries that answer the above first-order logic formula, let's first rewrite that formula in some of its equivalent (simpler) logical formulas to become closer to a FORMULA corresponding logical solution.

$$\begin{aligned}
& \exists s : \mathcal{T}(P) \bullet \text{ref}(P/s) = \Sigma \cup \{\sqrt{}\} && \text{(by Definition)} \\
& \equiv \exists s : \mathcal{T}(P) \bullet \forall e : \Sigma \cup \{\tau, \sqrt{}\} \bullet e \in \text{ref}(P/s) \iff e \in \Sigma \cup \{\sqrt{}\} \text{ (=Def)} \\
& \equiv \exists s : \mathcal{T}(P) \bullet \forall e : \{\tau\} \cup (\Sigma \cup \{\sqrt{}\}) \bullet e \in \text{ref}(P/s) \iff e \in \Sigma \cup \{\sqrt{}\} \quad \text{(Set Th)} \\
& \equiv \exists s : \mathcal{T}(P) \bullet (\forall e : \{\tau\} \bullet e \in \text{ref}(P/s) \iff e \in \Sigma \cup \{\sqrt{}\}) \wedge (\forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in \text{ref}(P/s) \iff e \in \Sigma \cup \{\sqrt{}\}) && \text{(Range split)} \\
& \equiv \exists s : \mathcal{T}(P) \bullet \forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in \text{ref}(P/s) \iff e \in \Sigma \cup \{\sqrt{}\} \text{ (By conj)} \\
& \equiv \exists s : \mathcal{T}(P) \bullet \forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in \text{ref}(P/s) && \text{(By FOL)}
\end{aligned}$$

To find the equivalent FORMULA query to the previous first-order logic formula we have to introduce some definitions. Ideally we would like to define a fact concerning the after (/) operator as follows. Let $\langle e_1, \dots, e_k \rangle$ be a trace of P (that is, $\langle e_1, \dots, e_k \rangle \in \text{traces}(P)$), such that P is a process equation. Then $P/\langle e_1, \dots, e_k \rangle = S_k$, given by the following hypothetical fact.

$\text{Pafter}(\langle e_1, \dots, e_k \rangle, S_k)$

available in the FORMULA knowledge base as long as the following right-hand side of its rule

$$\begin{aligned}
& \text{trans}(\text{State}(\text{ProcDef}(P, -, P_{\text{body}})), \tau, \text{State}(P_{\text{body}})), \\
& \text{trans}(\text{State}(P_{\text{body}}), e_1, S_1), \dots, \text{trans}(S_{k-1}, e_k, S_k).
\end{aligned}$$

holds.

As FORMULA cannot have a variable-size rule body, we have to obtain it by transitivity (creating possibly several intermediary facts). Thus we have to define the previous general non-realizable rule by one or more new realizable rules in FORMULA.

First, it is worth noting that the trace s is not special. Any trace $(\exists s)$ is acceptable. So let's focus our solution in a reachability analysis viewpoint. That is, let's create the state P/s for any s .

Definition 7 Let s be a trace of P , such that P is the name of a process (that is, $P(p\text{Par}) = P_{\text{body}}$). If the fact $\text{reachable}(Q)$, given by the following rule.

$\text{reachable}(Q) :-$

2739 $GivenProc(P), ProcDef(P, pPar, P_{body}),$
2740 $trans(State(P_{body}), -, Q);$
2741 $reachable(R), trans(R, -, Q).$

2742 becomes available in the FORMULA knowledge base, then $Q = \exists s : \mathcal{T}(P) \bullet$
2743 $P/s.$

2744 Note that with Definition 7 we are computing P/s in FORMULA without record-
2745 ing the specific events of s .

2746 Refusals are defined following its logical formulation reported in [RBH84] as.

$$ref(P) = \{X \mid X \text{ finite} \wedge \exists Q. P \xrightarrow{\tau^*} Q \wedge X \cap \text{initials}(Q) = \emptyset\}$$

2747 where the notation τ^* means zero or more internal events can occur (and τ^+ means
2748 that at least one internal event occurs).

2749 **Definition 8** Let P and Q be states of an LTS. If $P \xrightarrow{\tau^+} Q$ then the $\text{tauPath}(P, Q)$
2750 is present in the FORMULA knowledge base, where tauPath is given by the fol-
2751 lowing rules.

2752 $\text{tauPath}(P, Q) :- trans(P, \text{tau}, Q).$
2753 $\text{tauPath}(P, Q) :- \text{tauPath}(P, S), \text{tauPath}(S, Q).$

2754 No we can define what means by an event e be refuted at state P (formally, $e \in$
2755 $ref(P)$).

2756 **Definition 9** Let e be a visible event. Then

2757 $e \in ref(P) \triangleq \text{fail trans}(P, e, _), e \neq \text{tau}; \text{tauPath}(P, Q), \text{fail trans}(Q, e, _), e$
2758 $\neq \text{tau}.$

2759 **proviso.** P is a process expression.

2760 To obtain the corresponding FORMULA script related to the formula $\exists s : \mathcal{T}(P) \bullet$
2761 $\forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in ref(P/s)$, we have to generalise the previous definition to
2762 any event. This is easy in FORMULA by using the “don’t care” ($_$) operator, as
2763 shown in the following lemma.

2764 **Lemma 1** $\forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in ref(P) \equiv \text{fail trans}(\text{State}(P), _, _).$

2765 *Proof.*

- 2766 1. $\forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in ref(P)$
- 2767 2. $e_1 \in ref(P) \wedge \dots \wedge e_k \in ref(P)$ (\forall -ext)

- 2768 3. **fail** $\text{trans}(P, e_1, _)$, $e_1 \neq \text{tau}$; $\text{tauPath}(P, Q)$, **fail** $\text{trans}(Q, e_1, _)$, $e_1 \neq$
 2769 tau, \dots , **fail** $\text{trans}(P, e_k, _)$, $e_k \neq \text{tau}$; $\text{tauPath}(P, Q)$, **fail** $\text{trans}(Q, e_k, _)$,
 2770 $e_k \neq \text{tau}$. (By Def. 9)
- 2771 4. **fail** $\text{trans}(P, _, _)$; $\text{tauPath}(P, Q)$, **fail** $\text{trans}(Q, _, _)$. ($_ - \text{Def.}$)

2772 Now we have to show what happens to a refusal check when the location (current
 2773 state of the labelled transition system) changes.

2774 **Theorem 1** Let s be a trace of P . If $\exists s : \mathcal{T}(P) \bullet \forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in \text{ref}(P/s)$
 2775 then $\text{reachable}(Q)$, **fail** $\text{trans}(Q, _, _)$; $\text{reachable}(Q)$,
 2776 $\text{tauPath}(Q, R)$, **fail** $\text{trans}(R, _, _)$.

2777 *Proof.*

- 2778 1. $\exists s : \mathcal{T}(P) \bullet \forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in \text{ref}(P/s)$ (By hyp.)
- 2779 2. $Q = \exists s : \mathcal{T}(P) \bullet P/s \wedge \forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in \text{ref}(Q)$ (By Pred. Calc.)
- 2780 3. $\text{reachable}(Q)$, **fail** $\text{trans}(Q, _, _)$; $\text{reachable}(Q)$,
 2781 $\text{tauPath}(Q, R)$, **fail** $\text{trans}(R, _, _)$. (By Def. 7 and
 2782 Lemma 1)

2783 Theorem 4 represents the corresponding FORMULA encoding (a query) of $\exists s :$
 2784 $\mathcal{T}(P) \bullet \forall e : \Sigma \cup \{\sqrt{}\} \bullet e \in \text{ref}(P/s)$. That is, a deadlock was found by following
 2785 some trace s . This encoding is enough for CML because CML does not use the
 2786 special event $\sqrt{}$ for representing SKIP. However, for CSP we have to consider
 2787 an extra clause because this encoding considers that a CSP process ending with
 2788 SKIP as a deadlock as well and this is not conceptually correct although the CSP
 2789 model checker FDR works this way. Therefore, to check deadlock in FORMULA
 2790 for CSP we have to add the condition $\text{last}(s) \neq \sqrt{}$. This is easily represented
 2791 in FORMULA as $\text{trans}(_, \text{tick}, _)$. Therefore for CSP, the final query
 2792 is

2793 $\text{reachable}(Q)$, **fail** $\text{trans}(_, \text{tick}, Q)$,
 2794 **fail** $\text{trans}(Q, _, _)$; $\text{reachable}(Q)$,
 2795 $\text{tauPath}(Q, R)$, **fail** $\text{trans}(R, _, _)$.

2796 and for CML it is

2797 $\text{reachable}(Q)$, **fail** $\text{trans}(Q, _, _)$; $\text{reachable}(Q)$,
 2798 $\text{tauPath}(Q, R)$, **fail** $\text{trans}(R, _, _)$.

2799 B.2 Livelock analysis

2800 Livelock analysis is similar to deadlock analysis in the sense of finding some
2801 initial trace, from which something happens. In the case of livelock, this means
2802 finding a loop of infinite invisible events.

2803 In logical terms, livelock is characterised as

$$2804 \exists s : \mathcal{T}(P); t : \mathcal{T}(P/s) \mid \mathbf{ran} \, t = \{\tau\} \bullet P/(s \frown t) = P/s$$

2805 Similarly to deadlock, let's first rearrange the previous logical formula in a more
2806 independent (orthogonal) description.

$$2807 \exists s : \mathcal{T}(P); t : \mathcal{T}(P/s) \mid \mathbf{ran} \, t = \{\tau\} \bullet P/(s \frown t) = P/s$$

$$2808 \equiv \exists s : \mathcal{T}(P); t : \mathcal{T}(P/s) \mid \mathbf{ran} \, t = \{\tau\} \bullet (P/s)/t = P/s \quad (I - \text{Def.})$$

$$2809 \equiv \exists s : \mathcal{T}(P); Q; t : \mathcal{T}(Q) \mid Q = P/s \wedge \mathbf{ran} \, t = \{\tau\} \bullet Q/t = Q \quad (\exists - \text{Def.})$$

$$2810 \equiv (Q = \exists s : \mathcal{T}(P) \bullet P/s) \wedge (\exists t : \mathcal{T}(Q) \mid \mathbf{ran} \, t = \{\tau\} \bullet Q/t = Q) \quad (\text{By} \\ 2811 \text{ FOL})$$

2812 From the previous formula, we already have the first part. That is, from Defini-
2813 tion 7 we know that $Q = \exists s : \mathcal{T}(P) \bullet P/s$ corresponds to

$$2814 \text{reachable}(Q)$$

2815 The other formula $(\exists t : \mathcal{T}(Q) \mid \mathbf{ran} \, t = \{\tau\} \bullet Q/t = Q)$ is similar to reachability
2816 in terms of transitivity and it was already introduced. We have only to find the fact
2817 $\text{tauPath}(Q, Q)$ in the FORMULA knowledge base to conclude that process
2818 Q has a infinite loop of invisible actions.

2819 Thus livelock analysis is simply the conjunction of the previous FORMULA en-
2820 codings, or

2821 **Theorem 2** *If $(Q = \exists s : \mathcal{T}(P) \bullet P/s) \wedge (\exists t : \mathcal{T}(Q) \mid \mathbf{ran} \, t = \{\tau\} \bullet Q/t = Q)$*
2822 *then $\text{reachable}(Q), \text{tauPath}(Q, Q)$.*

2823 *Proof.*

$$2824 1. (Q = \exists s : \mathcal{T}(P) \bullet P/s) \wedge (\exists t : \mathcal{T}(Q) \mid \mathbf{ran} \, t = \{\tau\} \bullet Q/t = Q) \quad (\text{By hyp.})$$

$$2825 2. \text{reachable}(Q), \text{tauPath}(Q, Q). \quad (\text{By Defs. 7 and 8})$$

2826 B.3 Nondeterminism analysis

2827 Roscoe [Ros10] defines determinism for a process P as

2828 $s \frown \langle a \rangle \in \mathcal{T}(P) \implies (s, \{a\}) \notin \mathcal{F}(P).$

2829 In order we can find a counter-example, we have to negate the previous definition.

2830 Thus we get

2831 $s \frown \langle a \rangle \in \mathcal{T}(P) \wedge (s, \{a\}) \in \mathcal{F}(P).$

2832 By a simple rewrite we obtain.

2833 $a \in \text{initials}(P/s) \wedge a \in \text{ref}(P/s).$

2834 The term $a \in \text{initials}(P)$ is trivially defined in FORMULA as follows.

2835 **Definition 10** Let P a state of an LTS. If $e \in \text{initials}(P)$ then the fact

2836 $\text{trans}(P, e, _)$ is present in the FORMULA knowledge base.

2837 **proviso** P is a process expression.

2838 Finally we can obtain nondeterminism in FORMULA as a result of the following
2839 theorem.

2840 **Theorem 3** Let P be a CML process. If $a \in \text{initials}(P/s) \wedge a \in \text{ref}(P/s)$ then
2841 the query

2842 $\text{reachable}(Q), \text{trans}(Q, a, _),$
2843 $\text{tauPath}(Q, R), \text{fail trans}(R, a, _)$

2844 holds in the FORMULA knowledge base.

2845 *Proof.*

2846 1. $a \in \text{initials}(P/s) \wedge a \in \text{ref}(P/s)$ (By hyp.)

2847 2. $\text{reachable}(Q), \text{trans}(Q, a, _),$
2848 $\text{tauPath}(Q, R), \text{fail trans}(R, a, _)$ (By Defs. 10 and 9)

2849 B.4 Traces refinement

2850 Our last property of interest in this deliverable is traces refinement. As said pre-
2851 viously, in FORMULA we indeed look for a violation of such a property. Thus
2852 in this section we show how to detect a counter-example in a traces refinement
2853 following its mathematical definition.

2854 The traces of a process (already in LTS form) are given by

$$\mathcal{T}(P) = \{s \mid P \xrightarrow{s} Q\}$$

2855 Traces refinement ($\sqsubseteq_{\mathcal{T}}$) is defined as follows.

$$P \sqsubseteq_{\mathcal{T}} Q \equiv \mathcal{T}(Q) \subseteq \mathcal{T}(P)$$

2856 which means (by FOL) that

$$\forall s \bullet s \in \mathcal{T}(Q) \implies s \in \mathcal{T}(P)$$

2857 As before, we have to negate the previous formula to get a counter-example (if
2858 one exists). Hence

$$\begin{aligned} \neg \forall s \bullet s \in \mathcal{T}(Q) &\implies s \in \mathcal{T}(P) \\ &\equiv \exists s \bullet s \in \mathcal{T}(Q) \wedge s \notin \mathcal{T}(P) \end{aligned}$$

2859 As the traces semantics is prefix closed and $\langle \rangle \in \mathcal{T}(P)$ for any process P , we can
2860 work with the above formula by a case analysis (induction).

2861 Suppose $s = \langle e \rangle$. Thus the formula

$$\langle e \rangle \in \mathcal{T}(Q) \wedge \langle e \rangle \notin \mathcal{T}(P)$$

2862 can be rewritten as

$$e \in \text{initials}(Q) \wedge e \notin \text{initials}(P)$$

2863 The other case is similar to this one, but more general. Consider now that $s =$
2864 $t \frown \langle e \rangle$. Thus

$$t \frown \langle e \rangle \in \mathcal{T}(Q) \wedge t \frown \langle e \rangle \notin \mathcal{T}(P)$$

2865 can be rewritten to

$$\langle e \rangle \in \mathcal{T}(Q/t) \wedge \langle e \rangle \notin \mathcal{T}(P/t)$$

2866 that is equivalent to

$$e \in \text{initials}(Q/t) \wedge e \notin \text{initials}(P/t)$$

2867 As result, we just have to find an after state for both processes P and Q for a
2868 prefixed trace t (which can be empty—the base case) and check the possibility
2869 and impossibility of a same event occurring in these processes.

$$\exists t \bullet e \in \text{initials}(Q/t) \wedge e \notin \text{initials}(P/t)$$

As FORMULA cannot handle traces of variable-size we had to capture the above logical formula by walking in both LTSs simultaneously. With respect to the previous formula to be reusable in FORMULA we need this rewritten.

$$\begin{aligned} \exists t \mid t = \langle e_0, \dots, e_k \rangle \bullet e_0 \in \text{initials}(Q) \wedge e_0 \in \text{initials}(P) \wedge \\ \vdots \\ e_k \in \text{initials}(Q/\langle e_0, \dots, e_k \rangle) \wedge e_k \in \text{initials}(P/\langle e_0, \dots, e_k \rangle) \wedge \\ e \in \text{initials}(Q/t) \wedge e \notin \text{initials}(P/t) \end{aligned}$$

We consider a relation C_Ex from states (of the specification and implementation) to states (of the specification and implementation) via an event from the implementation, given by a case analysis (or step-law).

Theorem 4 *Let P and Q be CML processes. If $\exists t \bullet e \in \text{initials}(Q/t) \wedge e \notin \text{initials}(P/t)$ then the fact $C_Ex(-, -, -, \Omega, \Omega)$ holds in the FORMULA knowledge base.*

Proof.

For the very first transition (process definitions) we have.

$$\begin{aligned} C_Ex(P_0, Q_0, \text{tau}, P_{body}, Q_{body}) :- \\ \text{Spec.GivenProc}(P), \text{Impl.GivenProc}(Q), \\ \text{ProcDef}(P, pP, PBody), \text{ProcDef}(Q, pQ, PBody). \end{aligned}$$

where

$$\begin{aligned} \bullet P_0 &= \text{Spec.State}(\text{proc}(P, pP)), \\ \bullet Q_0 &= \text{Impl.State}(\text{proc}(Q, pQ)), \\ \bullet P_{body} &= \text{Spec.State}(PBody), \\ \bullet Q_{body} &= \text{Impl.State}(PBody). \end{aligned}$$

It is worth pointing out that this fact will be present in the FORMULA knowledge base even if a counter-example cannot be found because, in logical terms, the fact $C_Ex(P_0, Q_0, \text{tau}, P_{body}, Q_{body})$ holds merely by the presence of the intent to check a trace refinement. We need it just to create a first case that satisfies the general rules to capture a traces refinement violation. Finally the prefixes Spec. and Impl. are needed by FORMULA due to a design decision (reuse of the domains related to syntax and semantics). In what follows we present in a more mathematical fashion to easy reading.

2901 As $\tau \notin \text{initials}(P)$ for any process P , the following rule jumps to another possi-
 2902 ble visible transition of the implementation LTS.

2903 $C_Ex(P, Q, ev, P', Q'') :-$
 2904 $Q' \xrightarrow{\tau} Q'', C_Ex(P, Q, ev, P', Q') .$

2905 To capture the traces prefix-closedness property in FORMULA we use the follow-
 2906 ing rule.

2907 $C_Ex(P, Q, ev, P', Q') :-$
 2908 $C_Ex(-, -, -, P, Q), Q \xrightarrow{ev} Q', P \xrightarrow{ev^*} P', ev \neq \tau .$
 2909

2910 where $P \xrightarrow{ev^*} P'$ means that we can have several invisible actions before ev can
 2911 occur. This special symbol is indeed equivalent to Definition 7 (Reachability),
 2912 although we had to write a new rule in FORMULA to deal specifically with the
 2913 specification process of a refinement relation. This rule is given by.

2914 $CEPath(P, ev, Q) :-$
 2915 $Spec.trans(P, ev, Q), ev \neq \tau ;$
 2916 $Spec.tauPath(P, S), Spec.trans(S, ev, Q), ev \neq \tau .$

2917 Finally the logical formula

$$\exists t \bullet e \in \text{initials}(Q/t) \wedge e \notin \text{initials}(P/t)$$

2918 is equivalent in FORMULA to the presence of the fact

2919 $C_Ex(-, -, -, \Omega, \Omega) .$

2920 in the FORMULA knowledge base, which is only possible whether the following
 2921 rule can be fired.

2922 $C_Ex(P, Q, ev, \Omega, \Omega) :-$
 2923 $C_Ex(-, -, -, P, Q), Q \xrightarrow{ev} Q', ev \neq \tau, P \not\xrightarrow{ev^*} P' .$

2924 C Key Examples

2925 This section contains key examples to emphasize strong and weak points of FOR-
 2926 MULA and FDR. We have observed that although FORMULA is able to deal
 2927 with infinite data types via SMT solving, its performance degrades with some
 2928 issues:

- 2929 • Size of the knowledge base: The more facts are in the knowledge base the
2930 more time the analysis takes to finish. The analysed examples show that this
2931 relation is exponential for some operators.
 - 2932 • Uninstantiated data: The more uninstantiated data is used, the more expen-
2933 sive is the analysis. This is because FORMULA calls Z3 to instantiate these
2934 data.
 - 2935 • Low coupling between rules: The generation of facts can be related in some
2936 way. The more precise is the specification of these relations, the more faster
2937 is the analysis. The language of FORMULA allows rules to be defined
2938 through constraints that can be sufficient (in the sense that they enable one
2939 rule but also enable others) or optimal (in the sense that they enable more
2940 than one rule).
- 2941 On the other hand, the capability of instantiating values that satisfy the constraints
2942 of a model is a strong feature of FORMULA that makes it more useful than FDR⁸.
2943 We show these differences through two simple examples.

2944 **Replicated constructs**

2945 Replicated constructs are a common source of degrading performance as they
2946 might combine executions in different ways (synchronous, asynchronous, etc.).
2947 For example, the following process replicates an action that gets a value x (a pa-
2948 rameter), communicates it on channel `choose` and terminates successfully.

```
2949 channels
2950 choose : int
2951
2952 process P =
2953 begin
2954 actions
2955 TEST = val x : int @ choose.x -> Skip
2956
2957 @ [] i in set {1,2} @ TEST
2958 end
```

2959 We consider the indexing variable i varying through the sets $\{1, 2\}$, $\{1, 2, 3\}$,
2960 $\{1, 2, 3, 4\}$ and $\{1, 2, 3, 4, 5\}$. The result is illustrated in Table 4.

⁸Under circumstances where automatic data abstraction is not available

Tool	$\{1, 2\}$	$\{1, 2, 3\}$	$\{1, 2, 3, 4\}$	$\{1, 2, 3, 4, 5\}$
FORMULA	3s and 44 facts	5s and 156 facts	21s and 556 facts	183s and 1946 facts
FDR	0.011s	0.012s	0.012s	0.013s

Table 4: FORMULA and FDR in replicated constructs

2961 Infinite Types Involved in Communications and Predicates

2962 Although the performance of FDR is superior to that of FORMULA, FDR can-
2963 not analyse specifications containing infinite data types in communications and
2964 in predicates. This is because FDR generates the set of events prior to the LTS
2965 construction. The following example shows a system that cannot be analysed by
2966 FDR whereas our model checker is able to handle it.

```
2967 channels  
2968 choose : int  
2969  
2970 process P =  
2971 begin  
2972 @ choose?x -> choose?y -> [x = y] @ Skip  
2973 end
```

2974 The events `choose?x` and `choose?y` are infinite as there are no constraint on
2975 the values of `x` and `y`. This is a typical situation not handled by FDR. However,
2976 our model checker is able to instantiate values suitable to falsify the guard and
2977 thus originate a deadlock.

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