

Although studies have implicated variants in active chromatin regions and eQTLs as contributing significantly to complex traits (2, 8, 10, 23), the importance of splicing remains unclear. We therefore wondered what role common sQTLs might play in complex diseases.

Owing to the extensive sharing of QTLs across cell types (2, 24), we reasoned that QTLs identified in LCLs should be informative about the relative contribution of different regulatory mechanisms to complex traits, in particular to immune-related diseases (8). We thus compiled genome-wide summary statistics for rheumatoid arthritis, multiple sclerosis, Alzheimer's disease, schizophrenia, height, and body mass index (16). Using two tests with different underlying statistical models, we searched for functional annotations that are associated with GWAS signals (16, 23).

As expected, eQTLs and haQTLs are predicted to contribute to rheumatoid arthritis, multiple sclerosis, and height according to one or both methods (Fig. 4). Consistent with the notion that disease SNPs in histone modification peaks are mediated through the SNPs' effect on chromatin, haQTLs are more enriched in risk loci than are variants that lie within H3K27ac peaks overall (Fig. 4C and fig. S14).

sQTLs appear to have effects of similar or even larger magnitude than eQTLs. For instance, there is an enrichment of sQTLs with low *P* values in the multiple sclerosis GWASs, even when compared to eQTLs (Fig. 4C and fig. S15). These enrichments are robust to the eQTL and sQTL detection cutoffs, suggesting that they are not simply due to the power of detection (fig. S16). We also found similar patterns when we compared the effect of sQTLs on multiple sclerosis to the effects of eQTLs identified in three purified immune cell types (fig. S17).

In conclusion, three main pathways mediate the impact of genetic variation on gene regulation with phenotypic and pathogenic consequences. Of these, our work uncovers an unexpectedly important role of RNA splicing in modulating phenotypic traits (Fig. 4D). These findings indicate that RNA splicing should be a focal point in future work on connecting genetic variation to complex disease.

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SUPPLEMENTARY MATERIALS

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BIOPHYSICS

Broken detailed balance at mesoscopic scales in active biological systems

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Systems in thermodynamic equilibrium are not only characterized by time-independent macroscopic properties, but also satisfy the principle of detailed balance in the transitions between microscopic configurations. Living systems function out of equilibrium and are characterized by directed fluxes through chemical states, which violate detailed balance at the molecular scale. Here we introduce a method to probe for broken detailed balance and demonstrate how such nonequilibrium dynamics are manifest at the mesoscopic scale. The periodic beating of an isolated flagellum from *Chlamydomonas reinhardtii* exhibits probability flux in the phase space of shapes. With a model, we show how the breaking of detailed balance can also be quantified in stationary, nonequilibrium stochastic systems in the absence of periodic motion. We further demonstrate such broken detailed balance in the nonperiodic fluctuations of primary cilia of epithelial cells. Our analysis provides a general tool to identify nonequilibrium dynamics in cells and tissues.

When a system reaches thermodynamic equilibrium, its properties become stationary in time, which requires a net balance between rates of transitions into and out of any particular microstate of

the system. Systems in thermodynamic equilibrium, however, are known to be balanced in an even stronger way. They obey detailed balance, in which transition rates between any two microstates are pairwise balanced (Fig. 1A). This means there can be no net flux of transitions anywhere in the phase space of system states. This principle was identified and used by Ludwig Boltzmann in his pioneering development of statistical mechanics, the microscopic basis for thermodynamics (1). In contrast, living systems operate far from equilibrium, and molecular-scale violations of detailed balance lie at the heart of their dynamics. For instance, metabolic and enzymatic processes drive closed-loop fluxes through the system's chemical states (Fig. 1B) (2).

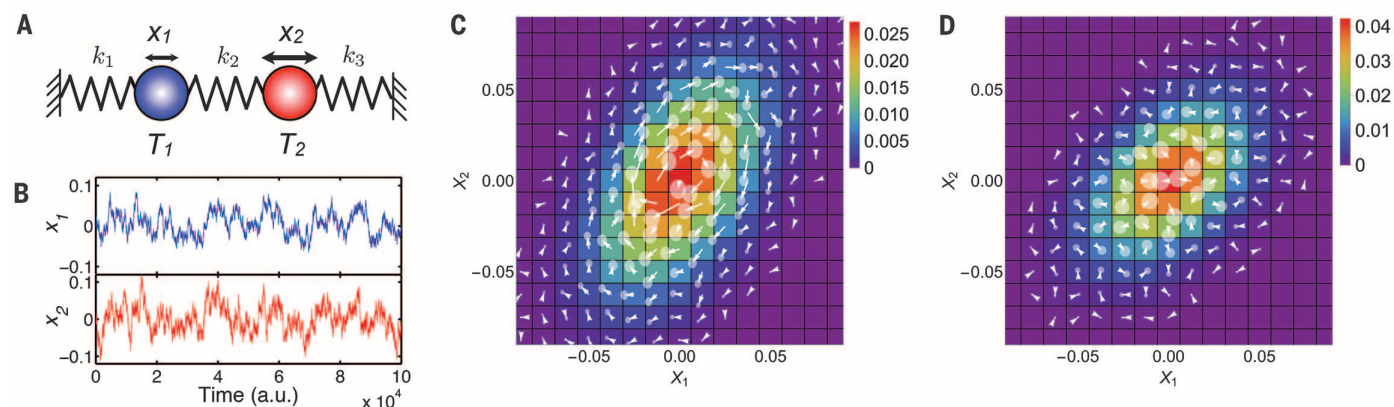
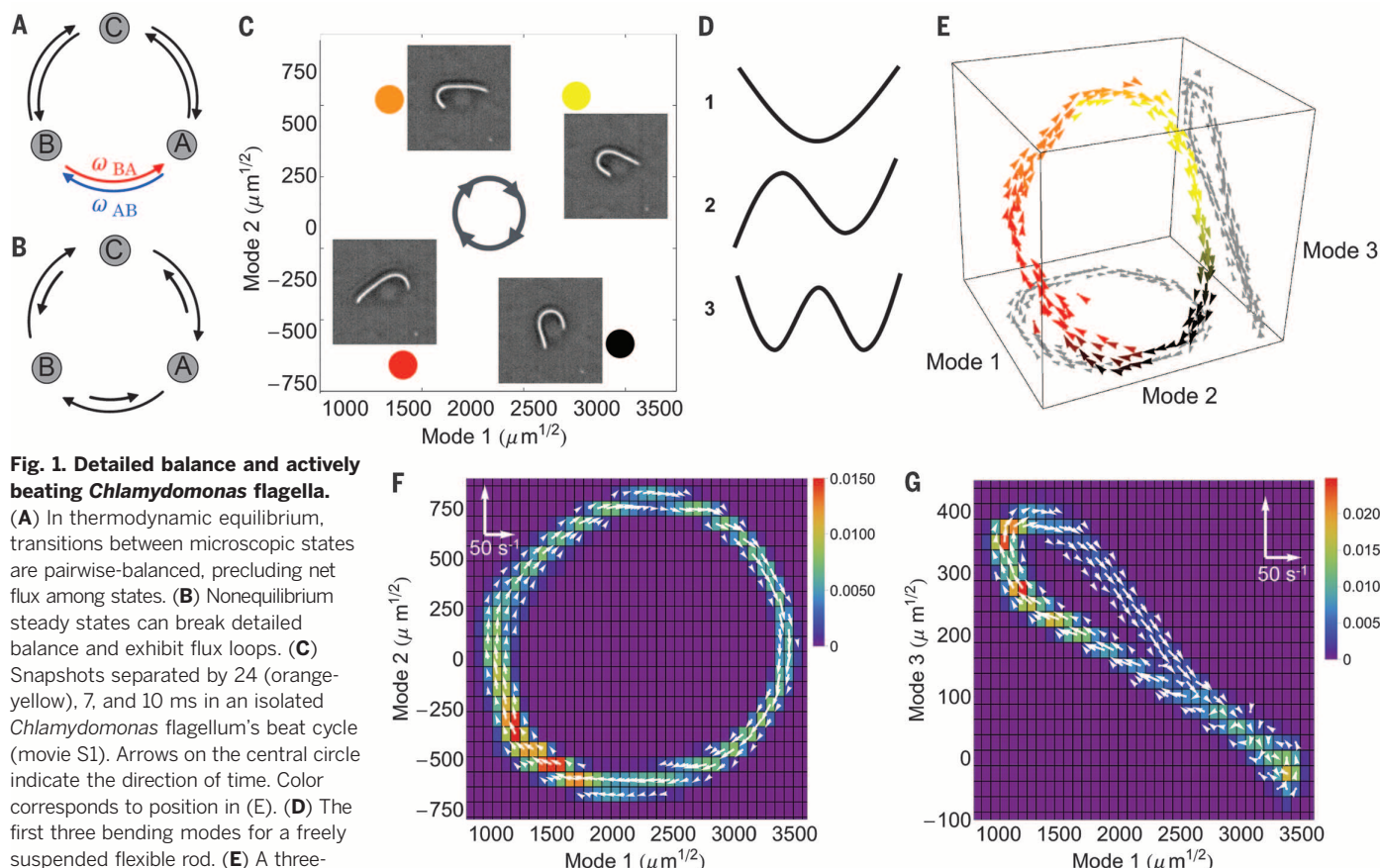
Nonequilibrium driving can boost intracellular transport (3–5), the fidelity of transcription (6), chemotaxis (7, 8), and the accuracy of sensory perception (9, 10). To understand cell

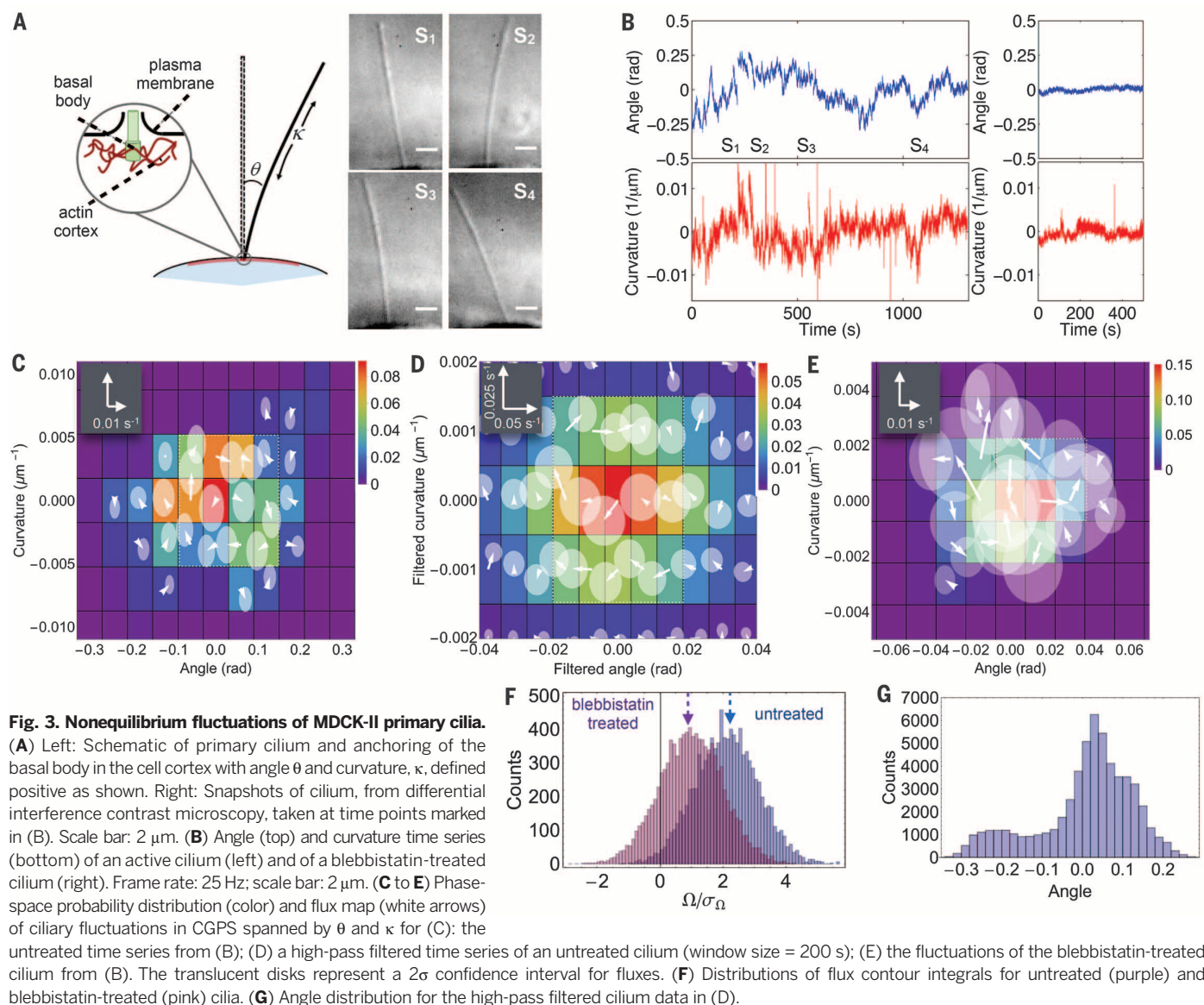
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function, it is thus important to determine whether particular cellular processes result from nonequilibrium activity, but this can be challenging. For instance, the stochastic nonequilibrium motion of tracer particles or fluorescently labeled proteins in cells is often

deceptively similar to that of thermally agitated Brownian particles (3–5, 11). It is unclear, however, to what extent the dynamics at such mesoscopic scales violate detailed balance, even if the system is out of equilibrium. Theoretically, detailed balance can reemerge at large scales

for nonequilibrium systems, which break detailed balance at small scales (12). To test for detailed balance and diagnose nonequilibrium dynamics at mesoscopic scales, we introduce a noninvasive approach based on quantifying flux loops (13) in configurational phase spaces of





strongly fluctuating stochastic steady-state systems. This should be contrasted with the deterministic dynamics of active swimmers, for which broken detailed balance is evident in the nonreciprocal nature of their motion (14). Moreover, our method is not limited to measuring conformational degrees of freedom, but can also include chemical variables, such as pH or ion concentrations.

We first illustrate this approach on a system displaying unmistakable nonequilibrium motion: a beating flagellum of *Chlamydomonas reinhardtii*. The main mechanical component of eukaryotic flagella is a conserved microtubule structure, the axoneme. Dynein motors drive relative axial sliding of the microtubules composing the axoneme, resulting in periodic beating (15, 16). We isolated and demembrated flagella from *C. reinhardtii* (17, 18) and reactivated the axonemes by addition of adenosine triphosphate (ATP). Figure 1C shows snapshots of the beat cycle

acquired by high-speed phase contrast microscopy (movie S1). We decomposed the axoneme shapes into the dynamic normal modes of a finite elastic filament freely suspended in a liquid (19), obtaining amplitudes $a_1(t)$, $a_2(t)$, $a_3(t)$ for the first three modes (Fig. 1D). From the time series of these amplitudes, we constructed a trajectory in the phase space spanned by the three modes. We discretized this space into a coarse-grained phase space (CGPS) (fig. S1) and determined the probabilities p_α to be in box α by temporal averaging (18). The steady-state dynamics are described by net transition rates $w_{\alpha,\beta} = (N_{\alpha,\beta} - N_{\beta,\alpha})/t_{\text{total}}$ determined by counting the number of transitions between adjacent states α and β in the time window t_{total} . These rates $w_{\alpha,\beta}$ determine the vector components of the flux \vec{j} from α to β (Fig. 1, F and G). In thermodynamic equilibrium, all these fluxes must vanish. By contrast, flux in closed loops is possible in a nonequilibrium steady state. The results of such a probability flux analysis (PFA)

for the beating cilium are shown in Fig. 1E, with vector fields indicating the fluxes for the first three modes. Figure 1, F and G, shows the $a_1 \times a_2$ and $a_1 \times a_3$ projections of CGPS probability and flux map. The clearly visible flux loops in phase space reflect the nonequilibrium, steady-state dynamics of the beating flagellum, and these fluxes are absent in the equilibrium dynamics of a microtubule (figs. S17 and S18).

The beating flagellum is an obvious nonequilibrium system, driven through its configurations at a defined frequency with relatively little stochasticity (20), resulting in a narrow band of populated states in phase space through which the trajectory cycles unidirectionally. To test our approach on a purely stochastic system, we numerically studied two overdamped, tethered beads at positions $x_1(t)$ and $x_2(t)$ coupled by a spring (Fig. 2A). This model system can be driven out of equilibrium by connecting the two beads to different heat baths at temperatures T_1 and T_2 ,

respectively, leading to heat flux from hot to cold. This minimal model is similar to a class of thermal ratchet models that have been studied, perhaps most famously by Feynman (21, 22). With $T_2 = 1.5T_1$ (Fig. 2B), the two simulated time series of random displacements were individually still indistinguishable from equilibrium dynamics. In particular, displacements maintained a Gaussian distribution, even in this nonequilibrium situation (fig. S6) (18). When we applied PFA, however, we found significant probability fluxes in the $x_1 \times x_2$ plane of CGPS (Fig. 2C). These flux loops demonstrate broken detailed balance, revealing the nonequilibrium nature of the system's dynamics. At equilibrium ($T_2 = T_1$), flux loops vanished (Fig. 2D).

The finite length of time trajectories creates a noise floor in the measured transition rates. To assess the statistical significance of the fluxes determined by PFA, we used trajectory bootstrapping (18, 23). Error estimates are shown as disks centered on flux arrowheads (fig. S2). The comparison with noise demonstrates the statistical significance of fluxes for the nonequilibrium system ($T_2 = 1.5T_1$, Fig. 2C), and their statistical insignificance in equilibrium ($T_2 = T_1$, Fig. 2D). The simulations thus demonstrate that even a purely stochastically driven system can be probed for nonequilibrium behavior by detecting broken detailed balance (figs. S4 and S5).

We next turned to a biological system that exhibits a stochastic steady state (18) (figs. S7 to S13). We imaged primary cilia of Madin-Darby canine kidney II (MDCK-II) epithelial cells grown in culture to a confluent layer (Fig. 3A). Primary cilia are hairlike organelles that project from many eukaryotic cells and can transduce mechanical and chemical stimuli into intracellular signals (24). Using invasive biochemical treatments, prior work (25) provided indirect evidence for nonequilibrium dynamics of these cilia. Flagella and primary cilia are structurally related, but the latter often lack the dynein machinery necessary for flagellar beating (26). Indeed, in marked contrast to the flagellum, we found that primary cilia of MDCK cells fluctuate in a way that appears random (Fig. 3B, movie S2, and figs. S14 and S15).

To analyze cilia dynamics, we characterized their state by the average deflection angle $\theta(t)$ from the normal and the average curvature $\kappa(t)$ (Fig. 3A) and calculated the probability flux map in the $\theta \times \kappa$ phase space (Fig. 3, C to E). From the time series $\theta(t)$ and $\kappa(t)$ in Fig. 3B (left), we found a clockwise circulation pattern (white box, Fig. 3C), indicative of broken detailed balance. To quantify the statistical robustness of this pattern, we calculated the contour integral along the flux loop (fig. S3) enclosed by the white box (Fig. 3C), $\Omega = \oint \vec{j} \cdot d\vec{\ell}$. We found $\mu_\Omega/\sigma_\Omega = 2.1$, where μ_Ω and σ_Ω are the bootstrapped mean and standard deviation of Ω (Fig. 3F) (18), indicating a statistically significant flux loop ($P = 0.018$, z -test). Long trajectories sometimes exhibited multimodal behavior in the angle distribution originating from a slow drift in the steady-state angle (Fig. 3G). In such cases, high-pass filtering

resulted in a statistically significant clockwise circulation pattern (Fig. 3D) (18). Actin-myosin dynamics underlie many types of cellular dynamics (4, 5, 27, 28), and the cilium basal body is embedded in the actin cortex (Fig. 3A, inset), providing a mechanism for the nonequilibrium motion of the cilium (25, 29, 30). To test whether detailed balance was restored when the main driving force was turned off, we treated MDCK-II cells with blebbistatin, a drug that inhibits non-muscle myosin II (Fig. 3E). This treatment suppressed the amplitude of angle and curvature fluctuations (Fig. 3B, right), as seen previously (25). The analysis of phase-space trajectories revealed that blebbistatin treatment (Fig. 3E) decreased phase space flux and rendered the residual fluxes statistically insignificant ($P = 0.16$) (Fig. 3F). As a further control, we observed that ATP depletion also suppressed, albeit not completely, cilia fluctuations and strongly decreased the flux pattern in phase space ($P = 0.16$) (fig. S16) (18). Finally, we verified the steady-state nature of cilia dynamics by the vanishing divergence of the fluxes in phase space (fig. S13). Taken together, these results demonstrate that the stochastic dynamics of the cilium can be clearly identified to be of nonequilibrium origin.

Steady-state fluctuations are common in living systems. It has, however, proved challenging to determine whether such stochastic dynamics result from nonequilibrium activity in given cases (3, 11). The PFA approach described here uses commonly observable conformational degrees of freedom to identify nonequilibrium dynamics in steady-state systems. This approach is broadly applicable to active biological systems, ranging from bacteria and the cell nucleus (11), all the way to tissues. Our method is intrinsically noninvasive, being based on imaging alone without requiring biochemical or mechanical manipulation. This is in contrast to other methods, where nonequilibrium fluctuations can be identified by the fluctuation-dissipation theorem or its nonequilibrium generalizations (27, 31). Furthermore, our method does not focus on rare events (32) or transitions between equilibrium states (33–35), nor does it rely on Markovian dynamics (33). It is interesting to consider possible extensions of our method to quantify energy dissipation or entropy production (36).

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SUPPLEMENTARY MATERIALS

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Broken detailed balance at mesoscopic scales in active biological systems

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Identifying nonequilibrium dynamics

Living systems clearly operate out of thermodynamic equilibrium at the molecular scale. How these activities are manifest at the cellular scale, however, has been unclear. Battle *et al.* use video microscopy together with statistical thermodynamics to unambiguously identify which random fluctuations at the cellular scale are out of equilibrium (see the Perspective by Rupperecht and Prost). Transitions between states obey a detailed balance in equilibrium, whereas imbalanced transitions point to nonequilibrium dynamics. For instance, nonequilibrium dynamics can be identified in the periodic beating of a flagellum and in the nonperiodic fluctuations of primary cilia.

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