



Introduction to Robotics

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- 1 -

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Grading

➤ Attendance

5%

Name (Original Name)	User Email	Join Time	Leave Time	Duration (Minutes)
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Bad ZOOM User Name (**Absent**)

- **Iphone** → Not your name
- **SiAko 202100001** → Wrong order
- **SiAko** → Name only
- **202100001** → ID Num only

ZOOM User Name (**Present**)

- University ID Num_Name
- 202100001 SiAko → GOOD (Present)

Name (Original Name)	User Email	Total Duration (Minutes)
		62
		63
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		62
		63
		62
		63





Student Responsibilities

- Download/Install **ZOOM** app for online lecture
 - Zoom profile must be your **OASIS ID+name** similar to OASIS
 - Ex.: **202061234 YourName**
 - *If you are asked, but no reply, then you'll be out of zoom & mark **absent***
- Regularly login, check **OLD IEILMS** for updates, notifications
 - <https://ieilmsold.jbnu.ac.kr>
 - Presentations & lecture videos will be uploaded after class
- Regularly check **Kakao Group Chat** for class
 - Everybody must have a Kakao talk account
 - Search & add account "**botjok**", introduce yourself and name of class ("**Robotics**"), then you will be added to the group chat




Intro To Robotics

FUZZY LOGIC CONTROL



Intro

- Control algorithms in Section 6
 - *Exact math computations determine signals to control robot behaviour*
 - *Recall On-off, P, PI, PID Controllers*
- Alternate approach is use of **fuzzy logic**
 - *A control algorithm based on rules*
- For **Ex.:** Cruise control system might have rules of the form
 - *If car in front is far away or car in back is near, set the speed to fast.*
 - *If car in front is near, set the speed to slow.*
- Logic is “**fuzzy**” since rules expressed in **linguistic variables**
 - *Like speed whose values has no precise mathematical definition*
 - *But only imprecise linguistic specifications such as **fast** and **slow***



Intro

(Expert)

- Fuzzy Logic controller has three phases run sequentially

1) Fuzzify

- Values of sensors *converted* into values of the linguistic variables
 - Such as far, closing, near, called **premises**
- Each premise specify certainty w/c is prob of our belief that variable is true

2) Apply Rules

- Set of rules *expresses* the control algorithm
- Given set of premises → a consequent is inferred
- Consequents also linguistic variables, ex: very fast, fast, cruise, slow, stop

3) Defuzzify

- Consequents *combined* so as to produce crisp output
 - A numerical value that controls robot aspects such as power to motor





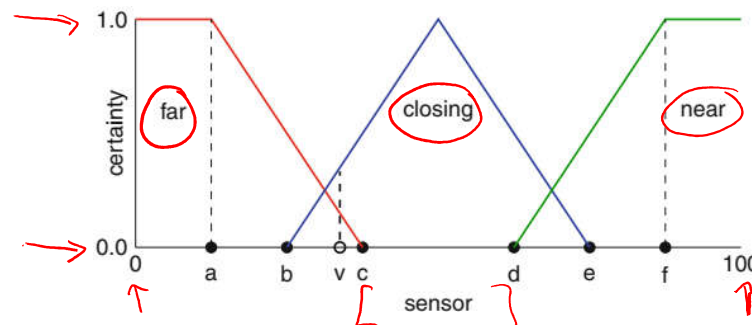
- Fuzzify
- Apply Rules
- Defuzzify



Fuzzify

Ex. Task : Robot approach an object & stop when very close to it

- When approaching an object
 - Value read by horizontal proximity sensor increase from 0 → 100
- Value returned by sensor is fuzzified
 - By converting it to a value of a linguistic variable
- Figure shows three graphs
 - Convert sensor values into certainties of linguistic variables



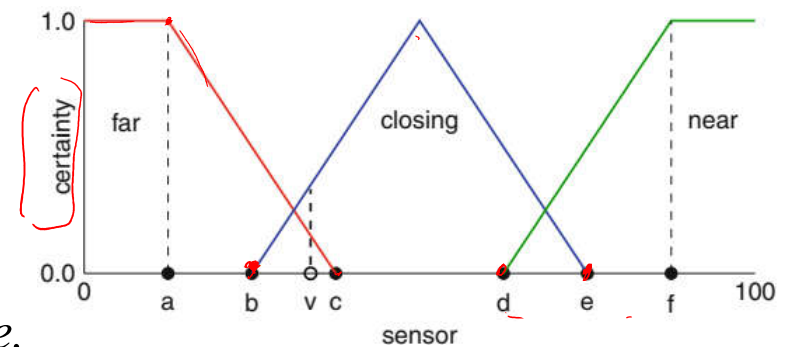
(a) Fuzzify the value of the horizontal proximity sensor



Fuzzify

Ex. Task : Robot approach an object & stop when very close to it

- Figure (a) shows three **graphs**
 - Convert sensor values into certainties of linguistic variables **far**, **closing** & **near**
 - X-axis** : Value returned by **sensor**
 - Y-axis** : Gives the **premise** for each variable, the certainty that the linguistic variable is true
- The points in x-axis refer to thresholds
 - (a) **far_low**, (b) **closing_low**, (c) **far_high**,
(d) **near_low**, (e) **closing_high** (f) **near_high**



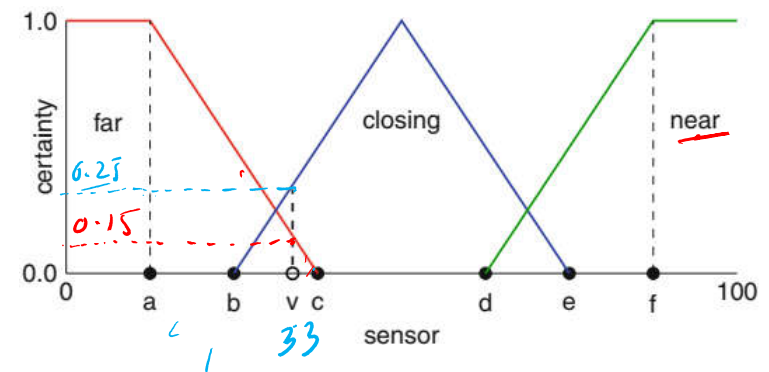
(a) Fuzzify the value of the horizontal proximity sensor



Fuzzify

Ex. Task : Robot approach an object & stop when very close to it

- The points in x-axis refer to thresholds
 - (a) far_low, (b) closing_low, (c) far_high, (d) near_low, (e) closing_high (f) near_high
 - If (*sensor value* < far_low) → completely certain object far away w/ certainty of 1
 - If (closing_low < *value* < far_high) → somewhat certain object is far away, but also somewhat certain that it is closing.
- Fuzziness results from the overlapping ranges
 - When value is *between* points (b) and (c) → *can't say* w/ complete certainty if object is far away or closing
 - Ex. $v = 33$ → far (certainty = 0.15) & closing (certainty = 0.25)



(a) Fuzzify the value of the horizontal proximity sensor



➤ Fuzzify

➤ Apply Rules

➤ Defuzzify



Apply Rules

- The three premises, certainties of far, closing & near
 - For computing five consequents using following rules

- 1) If far then very fast
- 2) If far and closing then fast -
- 3) If closing then cruise
- 4) If closing and near then slow -
- 5) If near then stop

- Certainties of consequents
 - Are same as certainties of corresponding premises
 - When resulting from Rules 1, 3, & 5
 - Are computed from the minimum of the certainties of the premises
 - Such as when there are two premises (Rules 2 & 4)
 - Since **both** premises *must apply* → We can't be **more certain** of the consequent than we are of the smaller of the premises



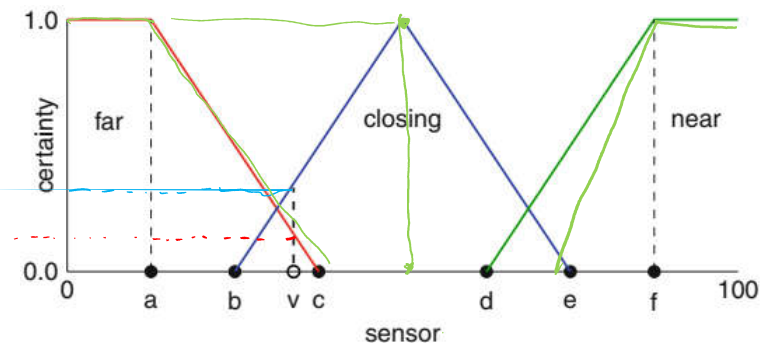
Apply Rules

- For **value v** in the figure
 - Ex. $v = 33 \rightarrow \text{far}$ (certainty = 0.15) & closing (certainty = 0.25)
 - Rule 2 applies \rightarrow hence certainty of consequent is $\min(0.15, 0.25) = 0.15$
- Another way of **combining** premises

- Is to take their joint probability:

$$p(A \cap B) = P(A) \cdot P(B)$$

- Ex. $v = 33 \rightarrow \text{far}$ (certainty = 0.15) & closing (certainty = 0.25)
- Hence, certainty of the consequent is $?????$,
much less than certainty obtained from the minimum function.



- 1) If **far** then **very fast**
- 2) If **far** and **closing** then **fast**
- 3) If **closing** then **cruise**
- 4) If **closing** and **near** then **slow**
- 5) If **near** then **stop**

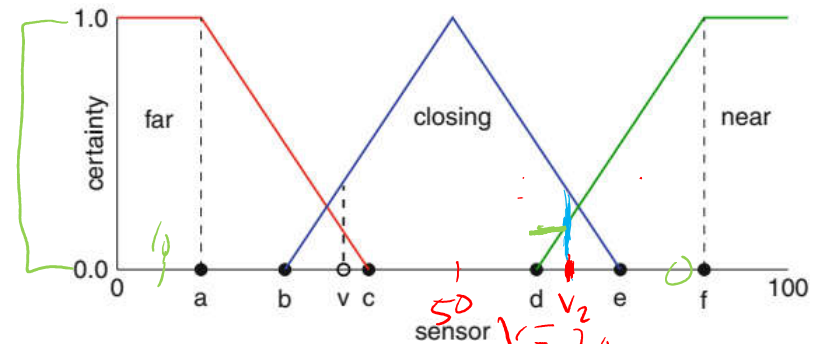


Apply Rules

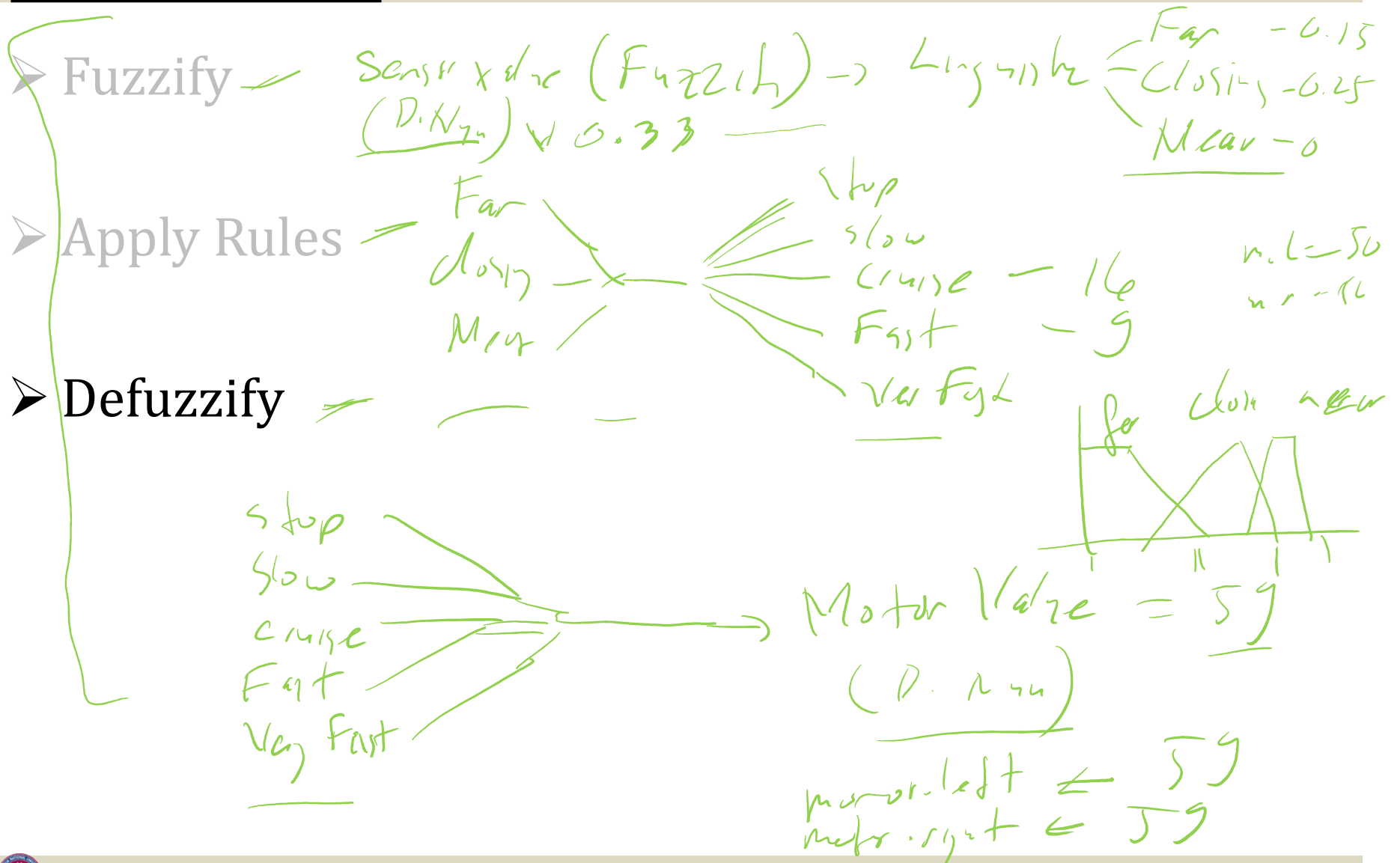
- For **value v** in the figure
 - Ex. $v = 33 \rightarrow \text{far}$ (certainty = 0.15) & closing (certainty = 0.25)
 - Rule 2 applies \rightarrow hence certainty of consequent is $\min(0.15, 0.25) = 0.15$
- Another way of **combining** premises
 - Is to take their joint probability:

$$p(A \cap B) = P(A) \cdot P(B)$$

- Ex. $v = 33 \rightarrow \text{far}$ (certainty = 0.15) & closing (certainty = 0.25)
- Hence, certainty of the consequent is $(0.15)(0.25) = 0.0375$,
much less than certainty obtained from the minimum function.



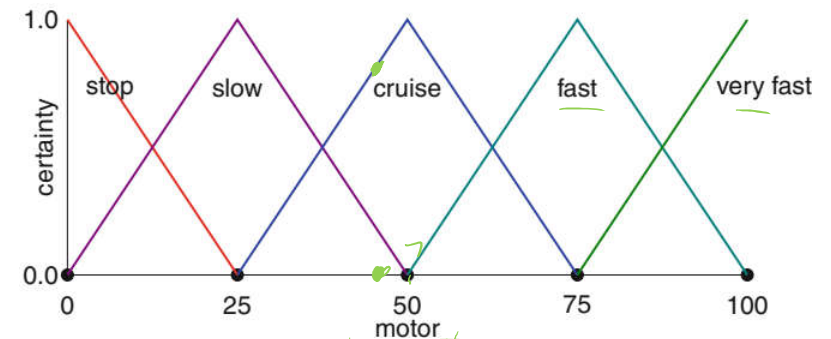
- 1) If **far** then **very fast**
- 2) If **far** and **closing** then **fast**
- 3) If **closing** then **cruise**
- 4) If **closing** and **near** then **slow**
- 5) If **near** then **stop**



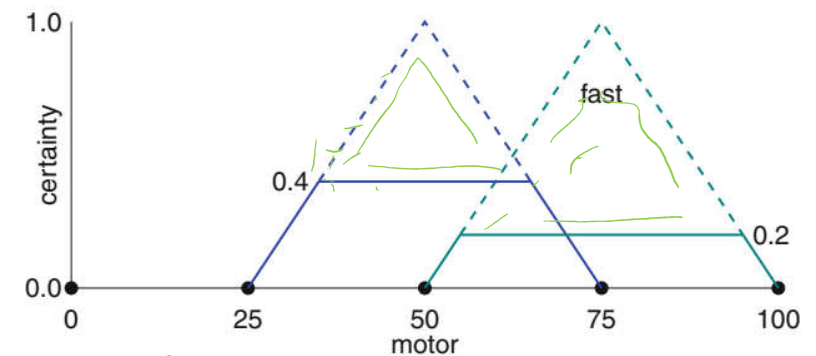


Defuzzify

- Next step combining the consequents
 - Taking into account their certainties
- Figure given in (a)
 - motor powers for each five consequents
 - Ex.: If *completely certain* output is **cruise**
→ motor power should be *set* to **50**;
If *less certain* → motor power should be *less or more*
- Suppose certainty of consequent of **cruise** computed as **0.4**
 - Center triangle in (a) no longer relevant
 - Since certainty can *never* be more than 0.4 displayed as a trapezoid in (b)



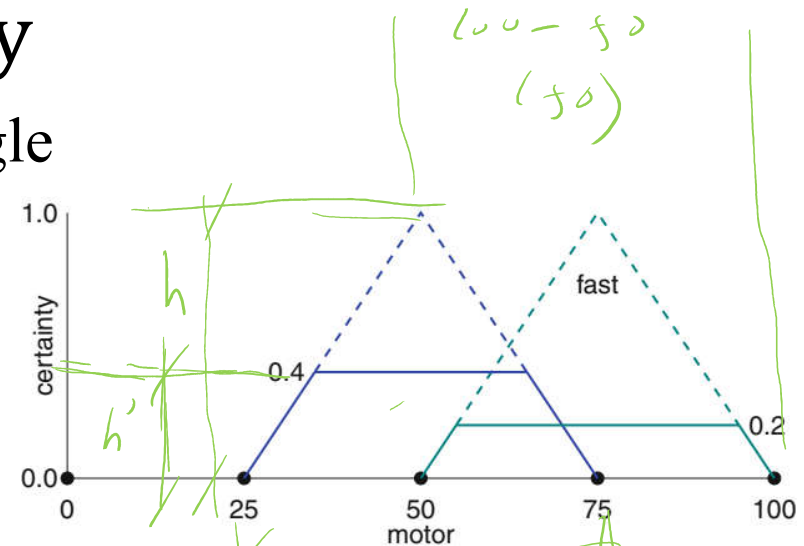
(a) Defuzzify to obtain
crisp motor setting



(b) Areas defined by certainties of
the consequents

Defuzzify

- Let w & h be width & height of triangle
 - The **area** of trapezoid bounded by line at height h' is: $wh' \left(1 - \frac{h'}{2h}\right)$
- Possible **more than one** consequent
 - Can have positive values
 - Trapezoids for consequent **cruise** (certainty=0.4) & **fast** (certainty=0.2) given in figure.
 - For $w = 50$, $h = 1$, $h'_c = 0.4$ (cruise), $h'_f = 0.2$ (fast), areas of the trapezoids a_c (cruise) and a_f (fast) are:



Areas defined by certainties of the consequents

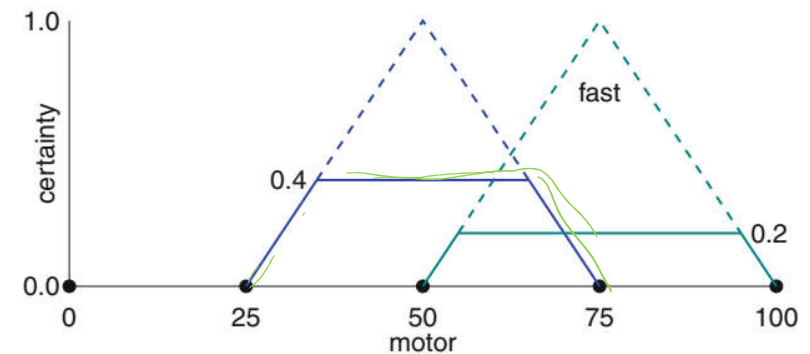
$$a_c = 50(0.4) \left(1 - \frac{0.4}{2(1)}\right) = 20(0.5) = 10$$

$$a_f = 50(0.2) \left(1 - \frac{0.2}{2}\right) = 10(0.5) = 5$$



Defuzzify

- Let w & h be width & height of triangle
 - The *area* of trapezoid bounded by line at height h' is:
$$wh' \left(1 - \frac{h'}{2h} \right)$$
- Possible **more than one** consequent
 - Can have positive values
 - Trapezoids for consequent **cruise** (certainty=0.4) & **fast** (certainty=0.2) given in figure.
 - For $w = 50$, $h = 1$, $h'_c = 0.4$ (cruise), $h'_f = 0.2$ (fast), areas of the trapezoids a_c (cruise) and a_f (fast) are:



Areas defined by certainties of
the consequents

$$a_c = (50)(0.4) \left(1 - \frac{0.4}{2} \right) = \underline{16}, \quad a_f = (50)(0.2) \left(1 - \frac{0.2}{2} \right) = \underline{9}$$

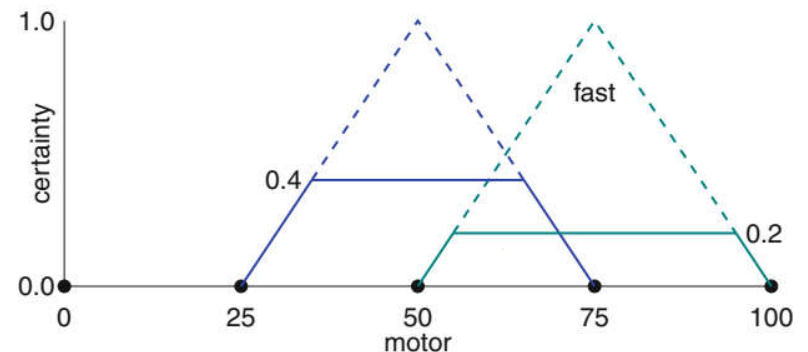


Defuzzify

- To obtain a crisp value
 - The center of gravity is computed
 - It is sum of the areas of the trapezoids, weighed by value at center of the base of each trapezoid, divided by sum of the areas. i.e.:

$$\frac{\bar{a}_c c_c + \bar{a}_f c_f}{a_c + a_f} = \text{?????}$$

- The value is closer to
 - Value associated with **cruise** rather than value associated with **fast**
 - Not surprising since the certainty of **cruise** is greater than the certainty of **fast**



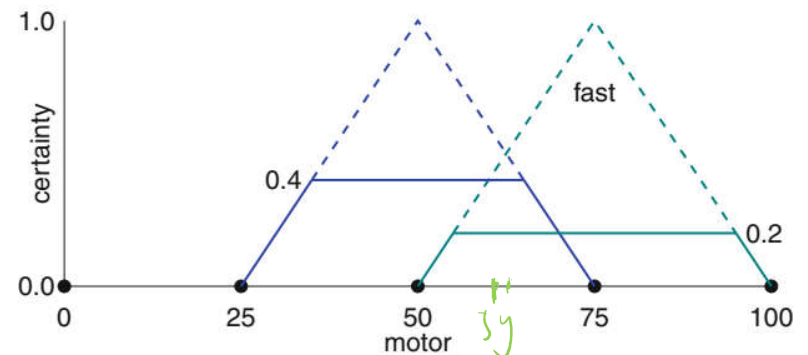


Defuzzify

- To obtain a **crisp value**
 - The **center of gravity** is computed
 - It is sum of the areas of the trapezoids, weighed by value at center of the base of each trapezoid, divided by sum of the areas. i.e.:

$$\frac{a_c c_c + a_f c_f}{a_c + a_f} = \frac{(16)(50) + (9)(75)}{16 + 9} = 59$$

- The value is closer to
 - Value associated with **cruise** rather than value associated with **fast**
 - Not surprising since the certainty of **cruise** is greater than the certainty of **fast**





Summary

➤ Fuzzy Logic Control

- ❖ *An alternative to classical control algorithms (On-Off, P, PI, PID)*

➤ Advantage

- ❖ Does not demand precise mathematical specifications of robot's behaviour
 - Which might be difficult to define

➤ Disadvantage

- ❖ *Behaviour of is not transparent as that of classical control algorithms*

➤ We studied an example for fuzzy definitions of speed

➤ Other examples can be

- ❖ color : *when does shade of range becomes orange*
- ❖ temperature : *when does a warm room become hot*



Thank you.

