### 🔹 Shortest Path (Bellman equation – min-cost form)

### 🔹 General Bellman Equation (max-reward form)

Lemma 1 proof: